Modeling and Simulation of Attacks on Cyber-physical Systems

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Abstract: This paper presents a methodology for the formal modeling of security attacks on cyber-physical systems, and the analysis of their effects on the system using logic theories. We consider attacks only on sensors and actuators. A simulated attack can be triggered internally by the simulation algorithm or interactively by the user, and the effect of the attack is a set of assignments to the variables. The effects of the attacks are studied by injecting attacks in the system model and simulating them. The overall system, including the attacks, the system dynamics and the control part, is co-simulated. The INTO-CPS framework has been used for co-simulation, and the methodology is applied to the Line follower robot case study of the INTO-CPS project.

1 INTRODUCTION

Model-based design of cyber-physical systems (CPS) allows to analyze the system behavior before a physical prototype of the system is built. Simulation is one of the techniques that are usually applied together with testing in the analysis of systems behaviors. In the case of cyber-physical systems, simulation often takes place in the form of co-simulation, which allows sub-systems, each modeled with its most appropriate languages and tools, to be composed together. The main advantage of co-simulation is modeling flexibility, because it does not require a single modeling language for all system parts (e.g., discrete and continuous parts). The Functional Mockup Interface (FMI) (Blochwitz et al., 2012) is an emerging standard for co-simulation of cyber-physical systems.

Moreover, model-based design based on formal methods reduces development costs and enables proofs of correctness for the system. Formal methods have been used intensively in the past in the development of safety-critical systems, and they are also assuming a fundamental role in the security field. The main advantage of formal methods in the field of security is that they are the only technique that can be used to formally prove resilience to attacks. For example, (Meadows, 2003) reports on the history of application of formal methods to cryptographic protocol analysis, and in (Avvenuti et al., 2012) abstract interpretation was applied to certify programs for secure information flow.

A recent survey by Humayed et al. (Humayed et al., 2017) reports on a large number of publications from the literature on CPS security and proposes a classification framework based on three orthogonal criteria: security, with the categories of threats, vulnerabilities, attacks, and controls; components, with the categories of cyber, physical, and cyber-physical components; and systems, with categories related to general system characteristics, such as architecture or application field.

Burmester et al. (Burmester et al., 2012) describe a formal model for CPS security based on hybrid timed automata and the Byzantine fault model, using an international natural gas distribution grid as an example.

The notion of impact metric for cyber-physical attacks is introduced by Lanotte et al. (Lanotte et al., 2018), who establish a theoretical framework built on weak bisimulation metrics.

Ferrante et al. (Ferrante et al., 2014) approach the issue of security requirements specification for embedded systems by defining a UML profile and developing an automatic process to generate system requirements from user requirements.

Formal method have already been applied for fault injection and simulation of the system after the occurrence of faults (Butler et al., 2009; Bernardeschi et al.,...
In this paper, we propose a similar approach for the analysis of system security. The PVS tool, a specification, verification, and simulation environment based on higher-order logic, is used for the specification of the control part of CPSs. Then the INTO-CPS co-simulation framework (Larsen et al., 2016) is used to generate simulation traces of the overall system. Preliminary results on a case study (a simple robot vehicle) are presented.

The paper is organized as follows: Section 2 briefly describes the PVS framework, and the co-simulation framework; Section 3 describes our methodology to formally model an attack; Section 4 shows an application of the method, using a Line Follower robot as a case study (the theory of the line follower robot, the theories of the modeled attacks and results of the co-simulation are presented); Section 5 concludes the paper.

2 BACKGROUND

2.1 The PVS Environment

The Prototype Verification System (PVS) (Ovre et al., 1992) is an interactive theorem-proving environment whose users can define theories in a higher-order logic language and prove theorems with respect to them. The language of PVS is a purely declarative language, but its PVSio extension (Muñoz, 2003) can translate PVS function definitions into Lisp code, so that a PVS expression denoting a function application with fully instantiated arguments can be interpreted as an imperative function call. The PVSio extension includes input/output functions allowing the system prototype to interact with the user and the computing environment. Moreover, MisraC code can be automatically generated from PVS theories for automata (Masci et al., 2014; Mauro et al., 2017), using the PVSio-web toolset (Oladimeji et al., 2013).

The PVS specification language provides basic types, such as Booleans, naturals, integers, reals, and others, and type constructors to define more complex types. The mathematical properties of each type are defined axiomatically in a set of fundamental theories, called the prelude. Among the complex types, the ones used in this work are record types and predicate subtypes.

A record is a tuple whose elements are referred to by their respective field name. For example, given the declarations:

```
axle: wheels = [# left := 1.0, right := 2.0 #]
```

axle is an instance of type wheels and the expressions `left(axle)` and `right(axle)` denote the speeds of the left and right wheels of axle, respectively. Equivalent notations are `axle\'left` and `axle\'right`.

The overriding operator `:=` in a WITH expression redefines record fields. With the declarations above, the expression

```
axle WITH { left := -1.0 }
```

denotes the record value `(#-1.0, 2.0#).

An example of predicate subtype is the following:

```
LightSensorReading: TYPE = { x: nonneg_real | x <= 255 }
```

which represents the real numbers in the `}[0,255]` interval.

The PVS syntax includes the well-known logical connectives and quantifiers, besides some constructs similar to the conditional statements of imperative languages. These constructs are the IF ... ENDIF expression and the COND ..., ENDCOND expression. The latter is a many-way switch composed of clauses of the form `condition \rightarrow expression` where all conditions must be mutually exclusive and cover all possible combinations of their truth values (an ELSE clause provides a catch-all). The PVS type checker ensures that these constraints are satisfied.

Definitions within a given theory may refer to definitions from other theories. This makes it possible to build complex system specifications in a modular and incremental way. Theory control_th below imports robot_th and defines functions for controlling the robot.

```
robot_th: THEORY
BEGIN
  id: posnat
  State: TYPE [# ... #]
  ....
END robot_th
```

```
control_th: THEORY
BEGIN IMPORTING robot_th
  ACC_STEP: Speed = 0.1
  accelerate(st: State): State
  BRAKE_STEP: Speed = 0.05
  brake(st: State): State
  ....
END control_th
```

The PVS environment includes the NASALIB theory libraries (Dutertre, 1996) providing axioms and theorems addressing many topics in mathematics, including real number analysis, and it can be applied to model both the discrete and the continuous part of the system (Bernardeschi and Domenici, 2016).
2.2 The Co-simulation Framework

Co-simulation is the joint simulation of independent sub-models each representing a component or subsystem of the overall system.

In the FMI standard (Blochwitz et al., 2012), co-simulation is performed by a number of Functional Mockup Units (FMUs), each responsible for simulating a single model in the native formalism with the tool used to create the model. The FMI architecture is shown in Figure 1.

An FMI-compliant environment provides a Co-Simulation Engine (COE) that communicates with FMUs, in a master-slave configuration to exchange data.

The COE and the FMU exchange commands and data using buffers in the FMU. The COE invokes (i) fmi2Set() for updating the values of the input variables in the buffers of the FMU; (ii) fmi2DoStep() for the execution of a co-simulation step. This function copies the values of the input variables from the FMU buffers to the PVS state: invokes the simulator and copies the values of the output variables from the PVS state to the buffers; (iii) fmi2Get() to get the new values of the output variables from the buffers of the FMU.

INTO-CPS (Bagnato et al., 2015; Larsen et al., 2016) is a co-simulation environment that integrates tools for the engineering of cyber-physical systems, covering both modeling of discrete and continuous behaviors and formal proofs.

Examples of tools available in INTO-CPS for modeling and analysis are Modelio (modelio, 2018), Overture (Larsen et al., 2010), and 20-sim (Broenink, 1999).

In (Palmieri et al., 2017), the authors extended the INTO-CPS co-simulation framework with FMUs that allow user interaction in the co-simulation. Such FMUs are based on the PVS tool and implement the interface using PVSio-web (Oladimeji et al., 2013).

3 MODELING ATTACKS

The behavior of a cyber-physical system consists of a control loop, finalized at controlling the physical part according to control laws. At each cycle of the loop,
sensors in the plant send data to the controller, which acts on the plant sending commands to the actuators.

In the FMI framework, the Controller and the Plant are FMUs, and the COE links outputs of the Plant FMU with inputs of the Controller, and vice-versa.

We assume the Controller FMU is formally described in the PVS language. The specification consists of two basic elements: the state of the sub-system (State), and the function \( \text{tick(State)} : \text{State} \), which given a state, according to control laws, computes the output to be forwarded to other sub-systems.

In particular, data read from sensors in the Plant FMU are put into the input variables of the state of the Controller. Data computed by the Controller for the actuators are stored into the output variables of the state of the Controller.

In this work, we consider the following types of attacks:

- **Attack to sensors.** The effect of such an attack is the corruption of data read from sensors. At the beginning of each co-simulation step, such data are stored into the input variables of the Controller’s state.

- **Attack to actuators.** The effect of such an attack is the corruption of data sent to actuators. At the end of each co-simulation step, such data are stored into the output variables of the Controller’s state.

The FMU of the Control part is modified as follows:

- For each attack, the time of the occurrence of the attack must be specified, distinguishing between permanent attacks, or temporary attacks, and, in that case, distinguishing between sporadic attacks or attacks executed only once.

- An attack can be simulated in two ways: (i) It can be generated internally by the simulation algorithm, or (ii) it can be activated interactively by the user (i.e., the developer in charge of performing the simulation).

In particular, an attack \( A \) is formally specified by a set of state variables, a set of clocks and a set of guarded statements:

\[
A = (\text{Var}_A, \text{Clk}_A \cup \{ \text{stepCounter} \}, \text{Com}_A)
\]

- **State variables.** \( \text{Var}_A \) is the set of variables of the state of the controller that are accessed by the attacker.

- **Clocks.** Two types of clocks are used: a set \( \text{Clk}_A \) of attacker clocks and a global clock \( \text{stepCounter} \), which is initialized to 0 when a co-simulation run starts; and it is incremented for each co-simulation step. The attacker cannot modify this global clock.

- **Guarded statements.** \( \text{Com}_A \) is a set of guarded statements. A guarded statement has the form:

\[
\text{fun_attack(st: ext_State): ext_State =}
\]

\[
\begin{cases}
\text{IF condition}\text{ THEN st WITH } x_1 := v_1, \ldots, x_n := v_n \text{ ELSE st ENDIF}
\end{cases}
\]

Some possible attacks could be:

- every 20 simulation steps, increment by 3 the value read from a sensor;
- every 100 simulation steps, lock at zero the value sent to an actuator for 20 steps;
A local clock is used to count the number of steps between two attacks; and two local clocks are used to model the lock-at-zero attack, one to count the duration of the attack and another to count the steps between two attacks.

Probabilistic behaviors can be encoded in attacks using the function NRANDOM(n: posnat): below(n), which is available in the PVS framework and that implements a uniform pseudo-random number generator that returns a natural number in the interval [0..n]. Using the language of PVS, more sophisticated attacks could also be implemented.

3.1 Attacks Generated Internally by the Simulation Algorithm

Let Sensor_attack be a function modeling an attack to sensors. The behavior of the system under attack is specified as the result of the function tick() on the extended state of the system after the attack to sensors:

\[
\text{system\_under\_attack(st: ext\_State) : ext\_State =}
\]

\[
\begin{align*}
\text{LET } st1 &= \text{Sensor\_attack(st),} \\
\text{IN } \text{tick}\,(st1)
\end{align*}
\]

We assume that ext State is the state of the system with the addition of a variable for each clock defined in the model of the attacks, and tick() is the function applied by the controller. The LET ... IN ... construct introduces a definition to be used in the expression following IN.

Let Actuator_attack be a function modeling an attack to actuators, the behavior of the system under attack is specified as the result of the function Actuator_attack on the state of the system generated by the function tick().

\[
\text{system\_under\_attack(st: ext\_State) : ext\_State =}
\]

\[
\begin{align*}
\text{LET } st1 &= \text{tick(st)} \\
\text{IN } \text{Actuator\_attack(st1)}
\end{align*}
\]

Finally, the two attacks could be combined. Since attacks to sensors affect the inputs to the controller and attacks to actuators affect its outputs, system_under_attack first passes the current state to the function modeling sensor attacks, then the resulting state is passed to the controller, which computes another state that is further transformed by the function modeling actuator attacks, as shown in the following code.

\[
\text{system\_under\_attack(st: ext\_State) : ext\_State =}
\]

\[
\begin{align*}
\text{LET } st1 &= \text{Sensor\_attack(st),} \\
&\quad \text{st2 = tick(st1)} \\
&\quad \text{IN } \text{Actuator\_attack(st2)}
\end{align*}
\]

3.2 Attacks Activated Interactively by the User

Another approach to activate attacks in the co-simulation is through the creation of an HTML page that is able to connect with the FMU and to invoke different functions. When the HTML page is open on a web-browser, the function that represents the attack is invoked at each co-simulation step. This implementation uses the PVSio-web (Oladimeji et al., 2013) tool, which allows us to create the graphical interface of a device and to link interface elements with functions describing how the device responds to user actions. When an action is executed (e.g. user clicks a button or a timer expires), a JavaScript module sends the appropriate command to the PVS FMU that executes the action in the co-simulation step. In our case, the command is “execute fun_attack() before tick()” or “execute fun_attack() after tick()” depending on the type of attack (i.e., attack to sensors or attack to actuators). When an attack is activated interactively, it is independent of the current co-simulation timestep, and the attack is only active when the HTML page is open. When the HTML page is closed the simulated system is no longer under attack. As a consequence, it is possible to change the number and the duration of the attacks during a co-simulation run.

4 A CASE STUDY

The system considered in this work is the Line Follower robot case study of the INTO-CPS project (http://projects.au.dk/into-cps/), see Figure 2 in Section 2. The robot has two drive wheels each propelled by its own independent motor, and two optical sensors, symmetrical with respect to the longitudinal axis, that measure the reflected light intensity of the floor immediately ahead of the robot. The robot starts astride the black line, so that both sensors see the white floor. The robot keeps heading forward as long as both sensors detect a white color. When the path curves, one sensor intercepts the black line while the other still sees the white floor. The robot controller then steers the vehicle by slowing down the internal wheel (on the side of the sensor detecting the line) with respect to the external one.

In addition to the automatic mode of operation, it is possible for a human to override the automatic control and drive the robot with a remote dashboard,
in our implementation a joystick console is used (see Figure 3 in Section 2).

4.1 Robot Theory

In the following, we show the main parts of a PVS theory describing the above system.

First, some type definitions provide the types of data needed for the model: CruiseControl to distinguish the two modes of operation, LightSensorReading to specify the values from the sensors, LightSensors to access the left and right sensor readings, Speed to specify the angular speed range for the wheels, MotorSpeed to access or control the two wheel motors, and Gear to distinguish the three modes of the gear train. Positive and negative speed values represent clockwise and counterclockwise rotation, respectively.

robotUI: THEORY
BEGIN
CruiseControl: TYPE = { AUTO, MANUAL }

LightSensorReading: TYPE = { x: nonneg_real | x <= 255 }
LightSensors: TYPE = [#
    left: LightSensorReading,
    right: LightSensorReading#
]

Speed: TYPE =
    { x: real | x >= -1 AND x <= 1 }
MotorSpeed: TYPE = [#
    left: Speed,
    right: Speed#
]

%-- gears
Gear: TYPE = { DRIVE, REVERSE, NEUTRAL }

Data of the above types compose the system state, plus a real value representing time:

State: TYPE = [#
    lightSensors: LightSensors,
    motorSpeed: MotorSpeed,
    gear: Gear,
    time: real,
    cc: CruiseControl #]

The control algorithm is specified by functions that update the system state by setting the motor speed depending on the sensor readings. In the two following functions, a reading of 150 units is chosen as the threshold between a light (white) and a dark (black) light intensity. Note that for each combination of readings, the two motors have opposite speed values, due to the mechanical arrangement.

update_left_motor_speed(st: State): Speed =
    LET ls = lightSensors(st) IN
    COND ls'right < 150 AND ls'left < 150->0.4,
        ls'right > 150 AND ls'left < 150->0.5,
        ls'right < 150 AND ls'left > 150->0.1,
        ELSE -> motorSpeed(st)'left
    ENDCOND

update_right_motor_speed(st: State): Speed =
    LET ls = lightSensors(st) IN
    COND ls'right < 150 AND ls'left < 150->-0.4,
        ls'right > 150 AND ls'left < 150->-0.1,
        ls'right < 150 AND ls'left > 150->-0.5,
        ELSE -> motorSpeed(st)'right
    ENDCOND

The simulation is driven by a tick() function that is called at each simulation step to update the motor speeds and increment time:

tick(st: State): State =
    IF cc(st) = AUTO
    THEN st WITH [motorSpeed := (#
        left := update_left_motor_speed(st),
        right := update_right_motor_speed(st))],
        time := time(st)+0.01 ]
    ELSE st WITH [time := time(st)+0.01] ENDIF

Finally, the theory defines functions (not shown) called from the user interface to switch between automatic and manual control, and in the latter case to execute user requests, such as accelerating, decelerating, or steering.

Figure 3 in Section 2 shows the results of the co-simulation when the system is co-simulated for 20 s, assuming a co-simulation step of 0.01.

4.2 Attack Theories

An attack is injected into the system by executing the controller together with the functions modeling attacks. In order to model attacks, the robot state is extended with fields characterizing the different types of attacks. In the present example, two types of attack are considered: (i) Attack to sensors, occurring once and acting indefinitely and (ii) Attack to actuators, occurring sporadically with a duration of one simulation step.

**Attack to Sensors.** The following function implements an attack that forces to white the value read by the left sensor indefinitely starting from a co-simulation step chosen randomly. Function NRANDOM in the initial state is invoked with an upper bound of 500.

Variable lightSensors is modified (140 is the constant for white color); Clock clk1 specifies the co-simulation step at which the attack starts.

\[
\text{VarSensor:attack} = \{\text{lightSensors}\}
\]
\[ \text{Clock}_{\text{Sensor attack}} = \{\text{clk1}, \text{stepCounter}\} \]

\[ \text{Com}_{\text{Sensor attack}} \] is the body of the following function.

\[
\text{Sensor attack}(st: \text{ext State}): \\
\text{ext State} = \\
\begin{align*}
\text{IF} \ & \text{stepCounter}(st) \geq \text{clk1}(st) \\
& \text{THEN} \ & \text{st} \\
& \quad \text{WITH} \ \left[ \text{lightSensors} := (\# \leftarrow 140, \ \ightleftharpoons \rightleftharpoons \left\lfloor \text{st}'\text{lightSensors}'\text{right} \right) \right] \\
& \text{ELSE} \ & \text{st} \\
\end{align*}
\]

\[ \text{ELSE} \ & \text{st} \]

\[ \text{ENDIF} \]

\textbf{Attack to Actuators.} The following function implements an attack that sporadically switches off the power of each motor for one co-simulation step. The co-simulation step, at which the power of each motor is switched off, is chosen randomly. Function \text{NRANDOM} in the initial state is invoked with \(500\). Then, function \text{NRANDOM} is invoked with an upper bound of \(20\).

Clock \text{clk2} specifies the co-simulation step at which the next occurrence of the attack starts; Clock \text{clk3} counts the number of co-simulation steps since the last attack. Clock \text{clk3} is reset at zero when the attack is executed.

\[ \text{Var}_{\text{Actuator attack}} = \{\text{motorSpeed}\} \]

\[ \text{Clock}_{\text{Actuator attack}} = \{\text{clk2, clk3, stepCounter}\} \]

\[ \text{Com}_{\text{Actuator attack}} \] is the body of the following function.

\[
\text{Actuator attack}(st: \text{ext State}): \\
\text{ext State} = \\
\begin{align*}
\text{IF} \ & \text{clk2}(st) = \text{clk3}(st) \text{ THEN} \\
& \text{st} \quad \text{WITH} \ \left[ \text{motorSpeed} := (\# \leftarrow 0, \ \ightleftharpoons \rightleftharpoons \left\lfloor \text{st}'\text{motorSpeed}'\right) \right] \\
& \quad \text{ELSE} \ & \text{st} \\
\end{align*}
\]

\[ \text{ELSE} \ & \text{st} \quad \text{WITH} \ \left[ \text{clk3} := \text{clk3} + 1 \right] \]

\[ \text{ENDIF} \]

The new state (and the initial state) of the line follower robot under attack is the following:

\[ \text{ext State: TYPE} = \]

\[
\begin{align*}
\text{[# // robot state} \\
& \quad // ... omitted \\
& \quad // \text{global clock} \\
& \quad \text{stepCounter:int,} \\
& \quad // \text{attack to sensors} \\
& \quad \text{clk1: int,} \\
\end{align*}
\]

// attack to actuators
\text{clk2: int,}
\text{clk3: int} #]

In the initial state, the step at which the attacks start is initialized with a random value:

\[ \text{init state: State} = \]

\[
\begin{align*}
\text{[# // robot state} \\
& \quad // ... omitted \\
& \quad // \text{global clock} \\
& \quad \text{stepCounter := 0;} \\
& \quad // \text{attack to sensors} \\
& \quad \text{clk1 = \text{NRANDOM}(500),} \\
& \quad // \text{attack to actuators} \\
& \quad \text{clk2: \text{NRANDOM}(500),} \\
& \quad \text{clk3: 0} \\
\end{align*}
\]

Function \text{tick()} implements the controller as previously shown, except that it is redefined on the extended state, and contains the update of the global clock (\text{stepCounter}).

\[
\text{tick}(st: \text{ext State}): \text{ext State} = \\
\begin{align*}
\text{IF} \ & \text{cc}(st) = \text{AUTO} \text{ THEN} \\
& \text{... omitted} \\
& \quad \text{stepCounter := stepCounter +1;} \\
& \quad \text{ELSE} \\
& \quad \text{... omitted} \\
& \quad \text{stepCounter := stepCounter +1;} \\
\end{align*}
\]

\[ \text{ENDIF} \]

\[ \begin{align*}
\text{4.3 Execution Traces} \\
\end{align*} \]

Figures 5 and 6 show two sample trajectories for two special cases, i.e., when only actuator attacks occur (Figure 5) and when only sensor attacks occur (Figure 6). In the first case, the robot follows the nominal path, but the execution traces, reporting the simulated time at each simulation step, show that the robot is retarded. This is expected, since the attack consists in stopping both motors for a short time. Since the motors stop at the same time, the robot heading at each instant is unchanged. The slowing down effect can be observed while looking at the displayed trajectory as the simulation progresses. In the second case, the left sensor is stuck at a fixed value, so that the robot starts turning at the onset of the attack, ending up in a closed trajectory.

\[ \begin{align*}
\text{5 CONCLUSIONS} \\
\end{align*} \]

This paper shows our preliminary work in defining a methodology for modeling attacks and analyzing the
effects of security attacks in cyber-physical systems using a co-simulation framework. More complex attacks than those shown in the paper can be modeled. In particular, models of attacks could be extended to timed automata (Alur and Dill, 1994), using the translation from networks of timed automata to PVS theories defined in (Bernardeschi et al., 2018). Moreover, verification is not addressed in this paper. Following an approach similar to that in (Fitzgerald et al., 2017), where it has been formally proved that, in case of automatic control, the path followed by the robot corresponds to the line on the ground, properties of the system under attack that are satisfied for all co-simulation runs could be analyzed. This will be objective of further work.

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