

# Continual Representation Learning for Images with Variational Continual Auto-Encoder

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**Keywords:** Continual Learning, Generative Models, Representation Learning, Variational Autoencoders.

**Abstract:** We propose a novel architecture for the continual representation learning for images, called variational continual auto-encoder (VCAE). Our approach builds a time-variant parametric model that generates images close to the observation by using optimized approximate inference over time. When the dataset is sequentially observed, the model efficiently learns underlying representations without forgetting previously acquired knowledge. Through experiments, we evaluate the development of test log-likelihood over time, which shows resistance to the catastrophic forgetting. The results show that VCAE has stronger immunity against catastrophic forgetting in comparison to the benchmark while VCAE requires much less time for training.

## 1 INTRODUCTION

Artificial intelligence(AI) should be capable of learning the knowledge over time-varying domain as biological agents do in nature (Hassabis et al., 2017). Continual learning (also called lifelong learning, incremental learning) is to learn task-independent knowledge under the environment that contains a multitude of learning tasks over the agent's entire lifetime (Thrun and Mitchell, 1995). The main obstacle of continual learning in artificial intelligence is so-called catastrophic forgetting (McCloskey and Cohen, 1989; French, 1999), which is the phenomenon that the knowledge of previous tasks that have learned be degenerated as the model learn new tasks. This evolves as time goes by with the shift of network parameters toward new Optima for new tasks while the covariate and data shift happen. Recent researches have found evidence on how the biological agents carry out continual learning tasks (Fagot and Cook, 2006; Cichon and Gan, 2015). Since the connection between artificial intelligence and continual learning is inspiring over the fields, the solution of catastrophic forgetting with elegant mathematics has been a challenge.

Shared representations are helpful to handle multi-task learning that tasks might arrive over time, or to apply acquired knowledge to tasks for which few or no examples are observed but the representation

of tasks exist. Understanding underlying representation would make application of machine learning, ultimately artificial intelligence, easier to understand the world. In other words, the key for common sense in the real world that required for AI would be representation learning. Popular type of modern representation learning is the Auto-Encoders (AEs) (Hinton and Zemel, 1994). These models explicitly define a feature extractor called encoder parametrized closed form. Encoder tries to find latent code or representation from origin data. Then it defines another closed form parametrized function called the decoder, that maps latent code to origin space. By minimizing reconstruction loss, it finds the optimal latent representation of the data. The most popular methods to unsupervised representation learning are Variational Auto-Encoders (VAEs) (Kingma and Welling, 2013). VAEs are built on top of standard neural net-based AEs. By using approximations, it operates efficient inference and stable learning in directed probabilistic models for continuous latent variables from intractable posterior distributions and large datasets.

The problem of catastrophic forgetting has been discussed in different ways entailing each overhead. The dropout technique (Srivastava et al., 2014) that regularizes the network parameters shows the effect of avoiding catastrophic forgetting, including extra regularization (e.g. L2) helps reduce perturbation during adopting new knowledge (Goodfellow et al., 2013). A neuroscience-inspired AI algorithm called Elastic weight consolidation (EWC)

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slows down learning in a subset of network parameters considered as important to previous knowledge, thereby anchoring these parameters to the former configurations. It allows the networks to be tuned for multiple tasks without adjusting network capacity (Kirkpatrick et al., 2017). Recent research introduces a method called Learning without Forgetting (LrF) that only uses new task data to train the network while preserving the capacity (Li and Hoiem, 2018).

While online Bayesian inference is a natural way to perform learning by considering prior knowledge for posterior knowledge (Ghahramani and Attias, 2000), a simple and general framework for continual learning that exploits variational inference is proposed, which is called variational continual learning (VCL) (Nguyen et al., 2018). VCL retains a distribution over model parameters of previous knowledge. When new data arrives, it reconfigures the setting of parameters with the previous posterior and the likelihood of current data. Through Bayesian inference, it concocts new posterior while regularizing the sense of previous knowledge not to be seriously perturbed. For now, VCL is the closest state of the art technique since it shows outperforms or be on par with the most recent techniques such as EWC (Kirkpatrick et al., 2017), SI (Zenke et al., 2017).

Convolutional neural networks (CNNs) are the processes inspired by the animal’s visual cortex in that neuronal connection pattern. Each cortical neurons is only activated in the related visual field known as the receptive field (Hubel and Wiesel, 1968; LeCun et al., 1998). AI systems using CNN have already shown competitive capabilities to human’s performances in tasks that require coping with images (He et al., 2016; Szegedy et al., 2017). However, VCL does not employ convolutional networks structure despite it treats images.

In this paper, we construct a novel framework that is resistant and stable against catastrophic forgetting in continual task, which is an essential advantage for AI. The major contributions of this work can be summarized as follows.

1. This paper proposes a generative model architecture with convolution that performs continual learning, which is referred to as Variational Continual Auto-Encoder (VCAE).
2. It is shown that VCAE outperforms the generative model of VCL in terms of training time, optimization and resistance against catastrophic forgetting in large gaps.

## 2 TECHNICAL BACKGROUND

This section provides background knowledge that is required to develop our method. We adopt the variational auto-encoder to learn the representation of each dataset under the framework of the variational continual learning, which is a general type of online learning using Bayes’s Rule.

### 2.1 Variational Auto Encoder

Let  $x$  be the observed data,  $z$  latent codes, and  $p(x, z)$  be the joint distribution of them. The prior over latent codes  $p(z)$  is assumed to be Gaussian. We want to approximate posterior inference  $p(z|x)$  parameterized by  $\theta$  and the marginal likelihood of the data  $x$  with prior. Given a dataset  $X = x^{(1)}, \dots, x^{(n)}$ , we want to use maximum likelihood to approximate parameters  $\theta$  that allows the hidden process to generate artificial data alike the real data. But both the marginal likelihood  $p_\theta(x) = \int p_\theta(z)p_\theta(x|z)dz$  and the true posterior  $p_\theta(z|x) = p_\theta(x|z)p_\theta(z)/p_\theta(x)$  are intractable.

A solution is to introduce an amortized inference model  $q_\phi(z|x)$  defined by a neural network, named encoder, to approximate the posterior  $p_\theta(z|x)$ . VAEs jointly train encoder with the probabilistic generative model, called decoder  $p_\theta(x|z)$ . Then the marginal likelihood is composed of a sum over the marginal likelihoods of each data point:

$$\log p_\theta(x^{(1)}, \dots, x^{(n)}) = \sum_{i=1}^n \log p_\theta(x^{(i)}), \quad (1)$$

which can be rewritten as:

$$\begin{aligned} \log p_\theta(x^{(i)}) &= \mathbb{E}_{q_\phi(z|x^{(i)})} [\log p_\theta(x^{(i)}, z) - \log q_\phi(z|x^{(i)})] \\ &\quad + D_{KL}(q_\phi(z|x^{(i)}) || p_\theta(z|x^{(i)})) \end{aligned} \quad (2)$$

Since the KL divergence term  $D_{KL}$  has non-negative value, the first term is called the variational lower bound on the marginal likelihood of each data point  $i$ . So the loss function of VAE is defined as:

$$\begin{aligned} L(\theta, \phi; x^{(i)}) &= \mathbb{E}_{q_\phi(z|x^{(i)})} [\log p_\theta(x^{(i)}, z) - \log q_\phi(z|x^{(i)})] \\ &= \mathbb{E}_{q_\phi(z|x^{(i)})} [\log p_\theta(x^{(i)}|z) - D_{KL}(q_\phi(z|x^{(i)}) || p_\theta(z))] \\ &\leq \log p_\theta(x^{(i)}) \end{aligned} \quad (3)$$

The loss function, termed as ELBO, comprises of the expectation of negative reconstruction error and the KL divergence term as regularization that matches the posterior  $q_\phi(z|x)$  to the prior  $p(z)$ .

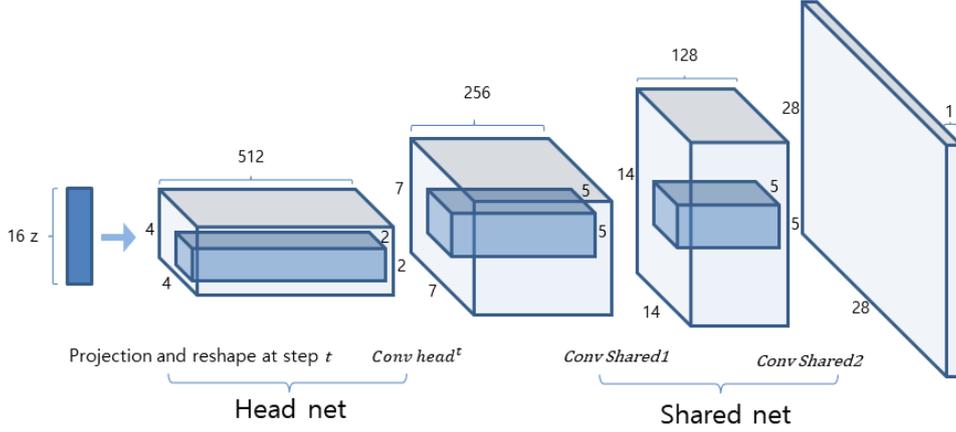


Figure 1: VCAE decoder used for experiments in this paper. For 28x28-sized dataset, 16-dimensional latent variables  $z$  is used as input. As it projected into convolutional decoder, feature maps are employed to sample possible data. The encoder has same but reverse structure except it does not distinguish head and shared net.

## 2.2 Variational Continual Learning

From the concept of continual learning, the goal of VCL is to learn the parameters of the model from sequentially arriving datasets  $X_t = \{x_t^{(n)}\}_{n=1}^{N_t}$  where each consisting of  $N_t$  i.i.d. samples and the input domain might differ over the turns in the sequence of  $t = 1 : T$ . In the perspective of Bayesian, the posterior distribution is updated by the prior distribution  $p(\theta)$  after seeing  $T$ -th datasets:

$$p(\theta|X_{1:T}) \propto p(\theta) \prod_{t=1}^T \prod_{n=1}^{N_t} p(x_t^{(n)}|\theta) \quad (4)$$

$$= p(\theta) \prod_{t=1}^T p(X_t|\theta) \propto p(\theta|X_{1:T-1})p(X_T|\theta).$$

Thus, the posterior after seeing the  $(T-1)$ -th dataset and likelihood of  $T$ -th dataset are utilized to update the posterior after seeing  $T$ -th dataset. This is a very general form of online learning emerged naturally from Bayes' rule.

## 2.3 VCL in Deep Generative Models

Let us consider VAEs as a generative model  $p(x_t|z_t)$  at the step  $t$ , where  $x_t$  is some continuous or discrete variable and  $z_t$  is an unobserved continuous random variable. To overcome catastrophic forgetting, VCL divides decoder into two subnetworks: the head net and the shared net. The head net is replaced with a new head net as task changes. Hence, this is called multi-head structure. The latent variables  $z_t$  pass through head net first then shared net. The loss function of VAEs is ELBO stated above (2) that a lower bound of marginal likelihood consisting of reconstruction error and a regularizer. This was because

the second RHS term at (1) is intractable but negligible by the numerical properties. However, in the continual learning setting, we can render it to return parameter uncertainty estimates for weighting the old parameter's distribution. Thus, the VCL in generative models approximates full marginal inference of the variable  $x$ .

Loss function of VCL:

$$L_{VCL}^t(q_t(\theta), \phi) = \mathbb{E}_{q_t(\theta)} [L_{VAE}^t(\theta, \phi; X_t) - D_{KL}(q_t(\theta) || q_{t-1}(\theta))] \quad (5)$$

From (3), the loss function of VAE at step  $t$  is defined as:

$$L_{VAE}^t(\theta, \phi; X_t) = \sum_{n=1}^{N_t} L_{VAE}^t(\theta, \phi; x_t^{(n)})$$

$$= \sum_{n=1}^{N_t} \mathbb{E}_{q_\phi(z_t^{(n)}|x_t^{(n)})} \left[ \frac{\log p(x_t^{(n)}|z_t^{(n)}, \theta) p(z_t^{(n)})}{q_\phi(z_t^{(n)}|x_t^{(n)})} \right] \quad (6)$$

where  $q_t(\theta) \approx p(\theta|D_{1:t})$ , after observing the  $t$ -th dataset. The approximate posterior  $q_t$  is derived from the complete form of marginal likelihood optimized with Maximum Likelihood parameterized by  $\theta$  and  $\phi$ .  $\phi$  is task-specific parameters of encoder at task  $t$ . The head net's parameters are used to calculate  $q_{t-1}(\theta)$  as part of  $\theta$  but these are re-initialized at every task  $t$ . For a choice of parameters  $\theta$ , the whole decoder and encoder are used.

## 3 VARIATIONAL CONTINUAL AUTO-ENCODER

CNNs are designed to understand visual scenes by replicating biological process and have been success-

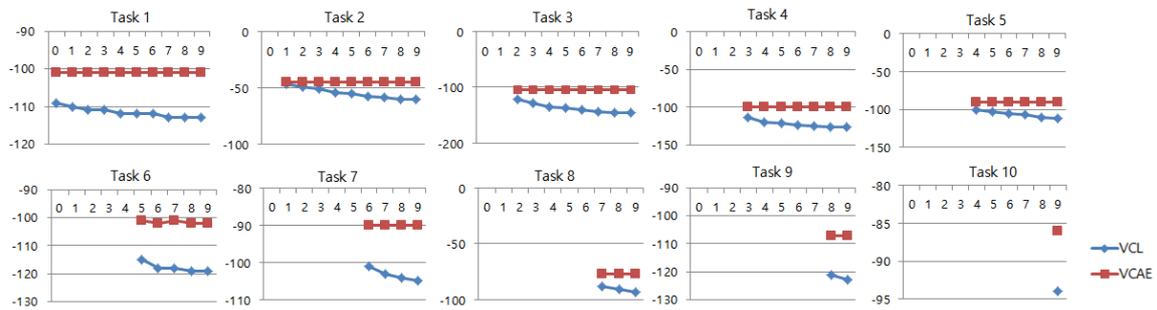


Figure 2: Development of changes of test log-likelihood passing different tasks. The x-axis is task sequence, the y-axis is the value of the log-likelihood, the higher the better. The generative model of VCL still has resistance for catastrophic forgetting, but the log-likelihood goes lower as model learn the new task. Meanwhile, VCAE shows almost perfect consistency in overall tasks.

ful in AI. So, we adopt the convolutional structure to the VCL and develop a novel framework named VCAE that memorize sequentially arriving visual knowledge.

At each stage of learning, convolutional encoder inference latent variable  $z$  concerning visual information of the current task. Shared-net in convolutional decoder stores visual knowledge to generate upcoming task while preserving previously acquired knowledge. And Head-net in convolutional decoder supports estimating upcoming distribution with respect to visual information.

After exploration, we found that VCAE shows better performance in terms of optimization and less forgetting of the previous task and also stable, faster training than the generative model of VCL. The structure is inspired by DCGAN generator (Radford et al., 2015).

Our approach uses two recent techniques in CNN architectures. First, global average pooling (GAP) (Lin et al., 2013) is deployed for the stable training instead of fully connected layers at the end of encoders. The fully connected layer has two main downsides than GAP: the larger number of parameter and losing locational information. Hence, it is not necessary to follow the classic CNN structures that use the FC layer.

Second, all convolutional net structure (Springenberg et al., 2014) replace deterministic spatial pooling (e.g. max pooling) with stridden convolutions. Max pooling is sufficient when we train classification model because the dominant features learned by max pooling are enough clues to classify labels. However, in terms of reconstruction or generation, information loss incurred by max pooling is disadvantageous. In addition, since only selected elements would be optimized with backpropagation, bias can be incurred during optimization. By using all convolutional structure, we can stably keep whole locational information

in maximum.

For the classification models, selective linear functions (e.g. ReLU) are fine to abuse over the whole structure. But in generative models, the bounded function can make the training stable since it adjusts the distribution of output. Consequently, we used the sigmoid function at the end of the shared network in the decoder, and Tanh function before the GAP in the encoder.

## 4 EXPERIMENTS

These experiments compare VCAE to the generative model of VCL. For the sake of time efficiency, MNIST dataset is employed as a benchmark. In VCAE, encoders use Leaky ReLU activation function except for tanh function before GAP, decoder mainly utilize ReLU over the head net and the shared net excluding sigmoid function at the output of shared net. All the strides are 2. The VCAE decoder is shown in Figure 1. All the weights of convolutional filters in encoder were initialized to the normal distribution with zero mean and standard deviation of 0.02. VCL employs linear function at the end of encoders and sigmoid for the shared part of the decoder. The generative model in VCL used for comparison consists of 4 intermediate hidden layers each 500 hidden unit deployed with the latent variable  $z$  of 50 nodes. In decoder of VCAE and all VCL weights, mean of the weights are initialized with Xavier method (Glorot and Bengio, 2010) and the log standard deviation is set to  $10^{-6}$ . The minibatch size is fixed to 64. Training epoch and learning rate set to same as 20 iterations for each task with learning rate 0.001, which was enough to learn generation of MNIST for both VCL and VCAE. Environmental setup is described in Appendix A.

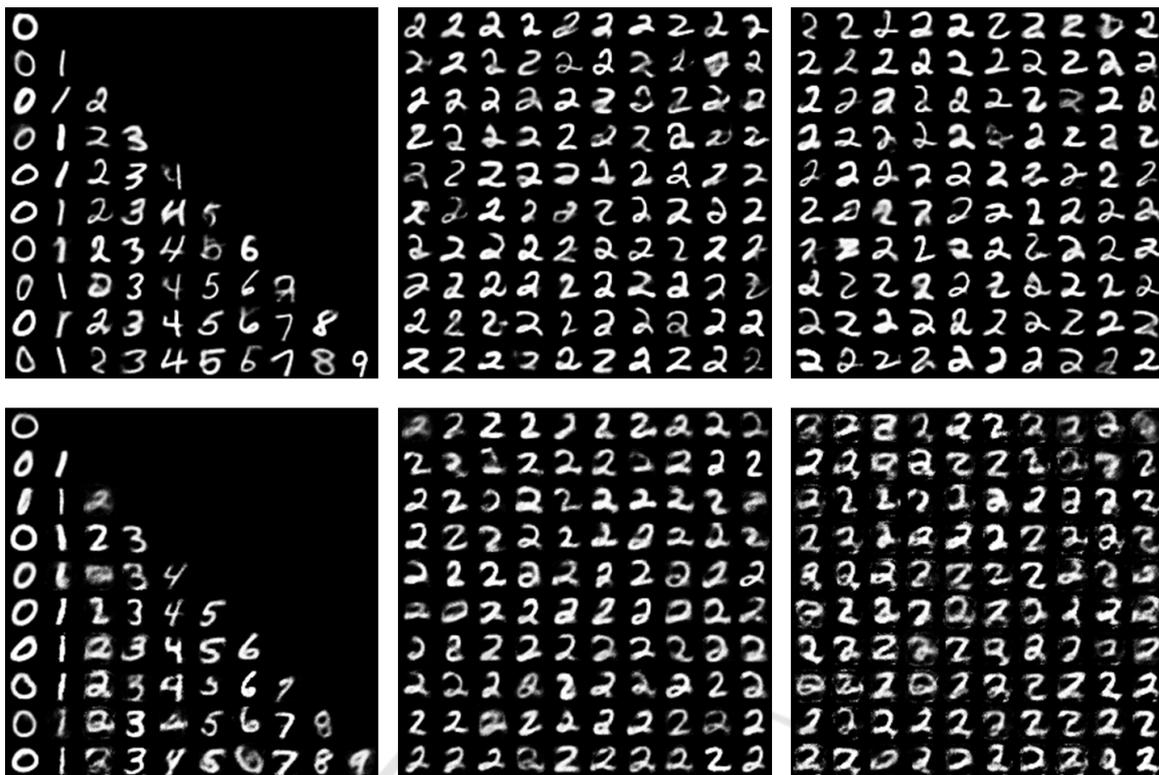


Figure 3: The first row is samples of VCAE, the second row is from VCL. Development of changes in image generation passing different tasks (left). 100 generated samples of digit 2 right after the model trained for it as task 3 (middle). 100 generated samples of digit 2 after trained all 10 digit tasks. (right). Middle columns show the samples generated right after it trained are not different in quality. But as the model learn other tasks, VCL start to make image blurry, while VCAE keeps a solid memory.

### 4.1 Evaluation

The generative model of VCL and VCAE are quantitatively evaluated using two factors: training time and sampling estimate of the log-likelihood. Naturally, the likelihood goes less as the model learns new tasks. If this effect is critical, we call it as the catastrophic forgetting.

Figure 2 shows how VCAE is stable over the growth of knowledge the model learns. Test log-likelihood refers to estimated log marginal likelihood after training is finished. Since VCL and VCAE are both strong frameworks against catastrophic forgetting, they show no critical memory degeneration. But VCL model still shows degeneration of likelihood while VCAE constantly retains it. The initial performance of VCAE itself is better than VCL model as well, but also VCAE is far stronger in holding memory against vaporization of knowledge. Suffice to say, no catastrophic forgetting is shown.

Generated samples in Figure 3 are consistent with the numerical result shown in Figure 2. Generated samples after the stage in learning of task 3, that is

digit 2 in MNIST, show both generative models are well trained. But after the models are trained with all 10 digits, generated samples from VCL become vague while ones generated from VCAE are showing equivalent quality. Moreover, the elapsed time for training has significant gaps between VCL and VCAE.

Training time comparison is shown in Figure 4. While VCL take more and more time as it learns new tasks, VCAE only requires extremely short time constantly over tasks.

## 5 CONCLUSIONS

We propose a strategy for continual learning dealing with visual tasks. By using twofold variational inference and the convolutions, VCAE can perform continual learning that memorizes image representation of independent tasks over time. VCL framework is extended to VCAE in which experimental results show VCAE improves the performances with respect to immunity to catastrophic forgetting and sta-

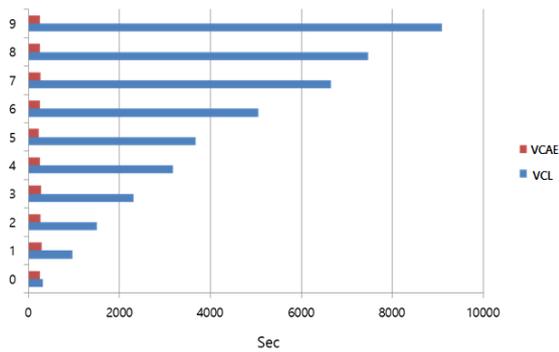


Figure 4: Training time for each task from 0 to 9. Note that it is not cumulative time. As going for next task, the generative model of VCL took much more time while VCAE is only taking less than 300 sec for every task.

ble training. This allows multiple tasks to be learned without increasing network capacity nor introducing new parameters to the networks.

Future works should extend this framework for high dimensional random variables. Also, VCAE can be adopted to deep reinforcement learning tasks to support continual learning at large scale so that agents can learn new knowledge by itself in real-time.

## ACKNOWLEDGEMENTS

This research was supported by the MSIT(Ministry of Science, ICT), Korea, under the ITRC(Information Technology Research Center) support program(IITP-2018-2014-1-00639) supervised by the IITP(Institute for Information & communications Technology Promotion)

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## EXPERIMENTAL ENVIRONMENT

Experiments are progressed with NVIDIA Geforce GTX 1080 GPU, Intel® Core i7-3370 CPU @ 3.40GHz x8, Ubuntu 18.04.1 LTS, Tensorflow-GPU.

