Virtual Flattening of a Clothing Surface by Integrating Geodesic Distances from Different Three-dimensional Views

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Abstract: We propose a method of virtually flattening a largely deformed surface using three-dimensional images taken from different directions. In a previous paper (Kita and Kita, 2016), we proposed a method of virtually flattening a surface from a 3D depth image according to the calculation of geodesic lines, which are the shortest paths between two points on an arbitrary curved surface. Although the work showed the promise of the proposed approach, only gently curved surfaces can be flattened owing to the limit of the observation being made from one direction. To apply the method to a wider range of surfaces, including sharply curved surfaces, we extended the method to three-dimensional depth images taken from different directions integratively. This was done by combining equations obtained from each observation through the surface points observed commonly in different observations and by solving all the equations simultaneously. Experiments using actual clothing items demonstrated the effect of the integration.

1 INTRODUCTION

Robots need to act more flexibly according to circumstance when their activities are extended from factories to the daily lives of people. To that end, computer vision plays an important role in recognizing various objects. Especially, the recognition of deformable daily objects presents difficulties that are different from those presented by rigid objects that have long been studied in factory automation. The recognition of clothing items for the automatic handling of clothing is a typical example.

The complex self-occlusion that accompanies the large deformation of clothing items makes the task of recognizing the items challenging. Figure 1 shows a clothing item being handled by a robot. It is not easy to determine the clothing type (e.g., trousers) or to detect the best position to grasp next (e.g., the corner of the waist) from such deformed shapes. Therefore, many studies on clothing recognition aimed at automatic handling have tried to first spread the clothing item to reduce the level of self-occlusion (F. Osawa and Kamiya, 2007) (Hu and Kita, 2015) (D. Triantafyllou and Aspragathos, 2016) (A. Doumanoglou, 2014). However, selecting proper positions to grasp for good spreading is another difficult recognition problem.

Meanwhile, a person can often imagine the flattened shape from a three-dimensionally deformed shape. Our aim is to realize this virtual flattening function by transforming the three-dimensional (3D) surface into a two-dimensional (2D) shape as shown in Fig. 1. Hereafter, we refer to the shape after virtual flattening as the flattened view. In a previous paper (Kita and Kita, 2016), we proposed a method of virtually flattening a clothing surface on a 2D plane from a 3D depth image of the surface. The method formulates the flattening of the observed 3D surface as a problem of solving simultaneous equations given by
sets of the geodesic distance, which is the length of the shortest path between two points on an arbitrary curved surface. However, because only one depth image is considered as the input in that paper, the target is limited to the case that the whole surface can be observed from one direction. In reality, most clothing items can be seen only partially when they are held in the air by one hand and do not satisfy this condition. The present paper extends the method to virtually flatten a sharply curved surface by integrating views taken from different directions.

Section 2 introduces the basic method of flattening proposed in the previous paper. Section 3 explains a method of integrating partial observations of a deformed surface to flatten the whole surface. Experimental results using actual clothing items are presented in Section 4. Finally, the results and future topics are discussed in Section 5.

2 BASIC FLATTENING METHOD

2.1 Calculation of the Geodesic Distance

Many methods of calculating the geodesic lines use finite element meshes (P. Bose, 2011) (Zhong and Xu, 2006) or a voxel representation (R. Grossmann and Kimme, 2002). However, both mesh-based and voxel-based methods assume uniformly dense 3D data of objects, which is not always the case for observation data in the real world. To calculate a geodesic line directly from 3D point clouds obtained by a range sensor or stereo cameras, we adopt an approach proposed by Kawashima et al. (T. Kawashima, 1999) that calculates geodesic lines in a mesh-free way.

To calculate the geodesic line between two points on a surface, \( P_i \) and \( P_e \), we set M nodes on the surface to represent the line \( P_i P_e = p_1 p_2 ... p_M \), where \( p_1 = P_i \), \( p_M = P_e \) and \( p_i = (x_i, y_i, z_i) \) as shown in Fig. 2. The problem of obtaining the geodesic distance of \( P_i P_e \) can be set as minimizing \( L_{total} \):

\[
L_{total} = \sum_{i=1}^{M-1} L_i, \tag{1}
\]

\[
L_i = \sqrt{(x_{i+1} - x_i)^2 + (y_{i+1} - y_i)^2 + (z_{i+1} - z_i)^2}. \tag{2}
\]

We here represent the surface as \( z(x) \), \( x = (x, y) \). To solve this minimization problem, \( z(x) \) at any place on the surface should be continuously determined from discontinuous observed 3D points of the surface. For this purpose, the surface around the position \( x = (x, y) \) is approximated by the local surface function with continuous partial derivatives using the element-free Galerkin method (T. Belytschko and Gu, 1994). Specifically, \( z(x) \) is approximated by a polynomial function:

\[
z(x) = p^T(x) a(x), \tag{3}
\]

where \( w(r) \) is a weight function defined by the distance between the target point, \( x \), and observed points \( x_i = (x, y, z) \) within a fixed distance, \( r_0 \). A fourth-order spline function is used as the weight function in this paper.

The depth and normal at \( x \) are calculated using the resultant \( a(x) \):

\[
z(x) = a_1(x) + a_2(x)x + a_3(x)y, \tag{4}
\]

\[
n(x) = (a_2(x)/D, a_3(x)/D, 1/D), \tag{5}
\]

\[
D = \sqrt{a_2(x)^2 + a_3(x)^2 + 1}. \tag{6}
\]

Figure 2 shows an example of synthetic observed points sampled from the surface of \( z = \sqrt{25 - (x - 3)^2} \) (red crosses). The green points in Fig. 2 show an example of surface interpolation along the line \( y = -x + 10 \).

Because \( L_{total} \) includes the term \( z(x) \) determined using Eq. (2), it is a complicated function of \( x \). To stably minimize this function, we make the zero-length spring analogy. Specifically, we assume that each segment \( p_ip_{i+1} \) is a spring connecting two nodes, \( p_i \) and \( p_{i+1} \), with a basis length (i.e., the length at neutral time) of zero and a spring constant \( k \). The total length of all springs, \( L_{total} \), is a minimum when the spring system is at equilibrium.
Because each node is constrained to move on the surface, when a force $F$ is exerted on a node, $p_i$, only the component of $F$ along the surface, $\tilde{F}$, affects the movement of $p_i$:

$$\tilde{F} = F - (F \cdot n_i)n_i,$$  \hspace{1cm} (6)

where $n_i = (n_{i_x}, n_{i_y}, n_{i_z})$ is a unit vector in the normal direction at $p_i$. The blue points in Fig. 2 show the geodesic line obtained after the convergence of the successive approximation, using the green line as the initial position.

### 2.2 Calculation of the Flattened View

We assume that a clothing surface can be flattened onto a 2D plane, $(u, v)$. If we then consider $N$ points on the clothing surface, $P_i(x_i, y_i, z_i), i = 1, \cdots, N$, the flattening can be formulated as the problem of calculating the 2D coordinates of $P_i$ when the surface is flattened on the plane, $(u_i, v_i)$.

The geodesic distance between $P_i$ and $P_j$, $G_{ij}$, is invariant regardless of the surface deformation and equals the Euclidean distance between $(u_i, v_i)$ and $(u_j, v_j)$ on the flattened 2D surface.

$$\sqrt{(u_i - u_j)^2 + (v_i - v_j)^2} = G_{ij},$$  \hspace{1cm} (7)

Although the number of equations of the form of Eq. (7) is $N^2C_2$ if we consider all combinations of $N$ points, not all equations are required if the number of equations related to one point is more than two, which is the number of unknowns for the point. By representing the use/disuse of $G_{ij}$ as $B(i,j) = \{1,0\}$, the flattening becomes the minimization problem of the equation

$$H(u, v) = \sum_{i=1}^{N-1} \sum_{j=i+1}^{N} B(i,j) (\sqrt{(u_i - u_j)^2 + (v_i - v_j)^2} - G_{ij})^2.$$  \hspace{1cm} (8)

The solution is then obtained by solving $2N$ simultaneous equations, where the two equations for each $P_i$ are

$$\frac{\partial H(u, v)}{\partial u_i} = 0, \quad \frac{\partial H(u, v)}{\partial v_i} = 0.$$  \hspace{1cm} (9)

### 3 INTEGRATION OF MULTIPLE OBSERVATIONS

We assume that an item is held in the air by a robot hand and can be observed from different directions. Although we plan to integrate several views in the future, in this paper, we deal with the integration of two views taken from largely different directions (separated by about 90 to 120 degrees) as a first step. We assume that the views are selected so that they cover occluded parts of each other. Figure 3(a) shows an example of a pair of such views.

The surface points commonly observed in the two 3D images are used to combine two sets of simultaneous equations of $(u, v)$ that are obtained from each observation. Although we plan to automatically detect such point correspondences using 2D/3D char-
acteristic points, we currently give the correspondences manually. The steps described below are the concrete procedure of combining two observations, which cover one whole side of a clothing item by complementing each other.

1. Point Setting

Figure 3(b) shows an example of 3D observation data, where the observed 3D points are illustrated with grey dots. Basically, we choose points from the boundary of the observed clothing region, \( P_i(x_i, y_i, z_i), i = 1, \cdots, N_b \), as shown by blue points in the left figure of Fig. 3(c). Then, from the region observed in both observation images, characteristics points that correspond to the two images are selected and replaced as shown by green points on the right of Fig. 3(c). Figure 3(d) shows an example of selected surface points for the observation of Fig. 3(a) with the letters indicating the correspondence between images.

2. Calculation of Geodesic Lines

Geodesic lines are calculated in each observation. Pairs of two points for calculating geodesic distances are selected such that the two points have similar height. This is because folds on the surface occur mainly in the vertical direction owing to the effect of gravity. Figure 4 shows an example of the calculation of a geodesic line. An initial line, \( p_{1} \) through the uniform sampling of \((x, y)\) from the line between \((x_i, y_i)\) and \((x_j, y_j)\) and calculating \( z(x, y) \) as described in Section 2.1. The blue line in Fig. 4 shows an example of the initial line. By minimizing Eq. (1), the geodesic line between \( P_i \) and \( P_j \) is calculated as shown by the red line.

The geodesic distance between \( P_i^m \) and \( P_j^m \) of observation \( m \) (in this paper, \( m = 1, 2 \)) is stored in the array \( G^m[P_i^m][P_j^m] \), where \( G^m[P_i^m][P_j^m] = G^m[P_j^m][P_i^m] \). Besides the geodesic distance, to maintain the local shape, the Euclidean distance between the pair of neighboring points, \( P_i^m \) and \( P_m^m \), is recorded in \( G^m[P_i^m][P_j^m + 1](2) \).

3. Integration of Geodesic Distances

After all \( G^m \) are calculated, the arrays are integrated to one array, \( G[i][j] \), by merging the points observed in common among the observations. During this process, the \( x^m \) and \( y^m \) coordinates of each \( P_i^m \) are respectively set as initial values of \( u \) and \( v \), where \( u_0 \) and \( v_0 \). At this time, the \( x^m \) and \( y^m \) coordinates of \( m \geq 2 \) observations are two-dimensionally translated and rotated on the \( x \) \( y \) plane so that the average coordinates and direction of the corresponding points coincide with those of another observation. Figure 5 shows an example, where three points (\( A, B \), and \( C \)) on the fold are selected as the corresponding points of the two observations. In Fig. 5(b), points from observation \( m = 2 \) are set using the original \( x^m \) and \( y^m \). Figure 5(c) shows their position after the 2D transformation.

4. Calculation of the Flattened View

The flattened view represented by \( (u, v) \) is calculated via the minimization of

\[
H'(u, v) = \sum_{i=1}^{N} B(i, j)(\sqrt{(u_i - u_j)^2 + (v_i - v_j)^2} - G[i][j])^2,
\]

where \( B(i, j) = \{1, 0\} \) represents the use/disuse of the pair of \( i \) and \( j \). We solve this minimization using a spring analogy by setting a spring between the pairs of \( B(i, j) = 1 \) with a basis length of \( G[i][j] \).

4 EXPERIMENTS

Experiments were conducted using two long-sleeve shirts and two pairs of trousers. So that the situation was similar to practical applications, the items were hung by a robot hand, after the robot had picked them up from a desk and had grasped their least part. The target item was recorded by a trinocular stereo vision system (Ueshiba, 2006) while the robot rotated the item along the vertical axis through the holding position. Two different views were manually selected from the sequence of 3D data recorded during the rotation. Three to five corresponding points between the different views were manually given.

Figure 6 shows the result for the long-sleeve shirt (LS1) in Fig. 3. The red lines in Fig. 6(a) show geodesic lines calculated from 3D observation data. Figure 6(b) and (c) shows the initial state set at \( (u_0, v_0) \) obtained as described in Section 3 and the resultant flattened view. Although there are small
Figure 6: Experimental results of the virtual flattening of a long-sleeve shirt (LS1): (a) geodesic lines; (b) initial state of \((u,v)\); (c) final state of \((u,v)\).

zigzags owing to the inaccuracy of 3D observation data along the region boundary, the shape of the long-sleeve shirt when flattened on a table was globally well estimated by the virtual flattening process.

Figure 7 shows the results for the other three sets, LS2, TR1 and TR2. By combining two complementary views, the flattened views of the whole items were roughly but well obtained. Especially in the case of trousers, the acute fold of one leg can be unfolded by this virtual flattening. In the case of TR2 (Fig. 7(c)), one leg was flattened in the wrong direction with a shorter length. This resulted from large deep creases marked by orange circles in Fig. 7(c), where some hidden parts were not measured in both observations. The parts hidden by such deep creases would be difficult to observe from any direction, until some kind of action removes the creases.

The virtual flattened view can be directly matched with the canonical shape of clothing items. This is a great advantage for the analysis of largely deformable objects. To examine this merit, we conducted a preliminary experiment of category classification. Figure 8(a) shows clothing model images, \(I\), calculated from one of the typical shapes of each category, where higher values represent a higher possibility of the contour of each category. When comparing the virtual flattened view with the model images, the size of the flattened view is normalized so that the longest lengths of the view and the model typical shape become the same. The matching criterion \(R\) is then calculated as

\[
R = \frac{\sum_{n=1}^{N_c} I(i_n, j_n)}{N_c},
\]

where \(N_c\) is the number of contour points of the flattened view and \((i_n, j_n)(n = 1, \ldots, N_c)\) denotes the coordinates of the contour point on the image. While rotating the contour after placing it on the model image so that the centroid of the contour coincides with the center of the image, the highest \(R\) is selected as the matching score of the category. The resultant matching score is summarized in Table 1, where the values of the larger class are indicated in boldface. All views are stably classified into the correct category. Figure 8(b) shows the matching results, where each view is superposed on the model image with higher \(R\).

To examine the accuracy of the virtual flattening, we manually measured the width (W) and length (L) of the resultant flattened views as marked by thin orange lines in Fig. 6 and Fig. 7. The comparison of those lengths with the actual length (GT: ground truth) is summarized in Table 2. The errors are about 1–2 cm, or about 5%, except for the length error of TR2 (Fig. 7(c)) owing to the flattening error as noted. Combining the categorization result, the system can describe the item such that “the observed item is a long-sleeve shirt with width of about 35 cm and body length of about 34 cm” for the case of Fig. 6.

<table>
<thead>
<tr>
<th>Data</th>
<th>W (cm)</th>
<th>Error (%)</th>
<th>L (cm)</th>
<th>Error (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>LS1 (Fig. 6)</td>
<td>35.6</td>
<td>1.1</td>
<td>36.2</td>
<td>35</td>
</tr>
<tr>
<td>LS2 (Fig. 7a)</td>
<td>35.6</td>
<td>8.7</td>
<td>38.1</td>
<td>40</td>
</tr>
<tr>
<td>TR1 (Fig. 7b)</td>
<td>25.7</td>
<td>2.8</td>
<td>64.2</td>
<td>62</td>
</tr>
<tr>
<td>TR2 (Fig. 7c)</td>
<td>26.0</td>
<td>3.7</td>
<td>55.8</td>
<td>67</td>
</tr>
</tbody>
</table>

Table 1: Matching score with the canonical model images of each category.

<table>
<thead>
<tr>
<th>Category</th>
<th>LS1</th>
<th>LS2</th>
<th>TR1</th>
<th>TR2</th>
</tr>
</thead>
<tbody>
<tr>
<td>Long-sleeve shirts (LS)</td>
<td>0.65</td>
<td>0.78</td>
<td>0.43</td>
<td>0.47</td>
</tr>
<tr>
<td>Trousers (TR)</td>
<td>0.56</td>
<td>0.53</td>
<td>0.57</td>
<td>0.57</td>
</tr>
</tbody>
</table>
Figure 7: Experimental results of the virtual flattening of long-sleeve shirts and trousers: (a) LS2; (b) TR1; (c) TR2.

5 CONCLUSION

We proposed a method of virtually flattening a clothing surface onto a 2D plane from 3D depth images of the surface taken from different directions. On the basis that geodesic distances between surface points equal 2D distances of the points on the flattened plane, the method realizes flattening by solving simultaneous equations of the geodesic distances among the surface points. Through points observed in common in different observations, the equations derived from the observations are integrated and simultaneously solved to flatten the whole surface.

Experimental results for actual clothing items show that the proposed method well estimates the shape of a clothing surface when the clothing is flattened on a table from two 3D observations of the deformed surface. The recognition of clothing items having such shape is much easier than that for an arbitrary shape. Accordingly, this allows a robot to rec-
Figure 8: Category classification using the flattened views:
(a) model images; (b) selected model.

... benefits the automatic handling of clothing items. Category classification using the resultant views demonstrated the good prospects of using the virtual flattened view as a mediator between canonical models and deformed items.

Although the corresponding points between different observations are manually given at present, automatic point correspondence should be possible using characteristic points of color (or intensity) features and/or the particular 3D shape. As future work, we plan to extend the method to integrate more observations, which will allow us to use more reliable 3D data for all parts of the surface.

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