

Transfer and Extraction of the Style of Handwritten Letters using Deep Learning

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Abstract: How can we learn, transfer and extract handwriting styles using deep neural networks? This paper explores these questions using a *deep conditioned autoencoder* on the IRON-OFF handwriting data-set. We perform three experiments that systematically explore the quality of our style extraction procedure. First, We compare our model to handwriting benchmarks using multidimensional performance metrics. Second, we explore the quality of style transfer, i.e. how the model performs on new, unseen writers. In both experiments, we improve the metrics of state of the art methods by a large margin. Lastly, we analyze the latent space of our model, and we show that it separates consistently writing styles.

1 INTRODUCTION

One aspect of a successful human-machine interface (e.g. human-robot interaction, chatbots, speech, handwriting, etc.) is the ability to have a personalized interaction. This affects the overall human experience, and allow for a more fluent interaction. At the moment, there is a lot of work that uses machine learning in order to model for such interactions. However, most of these models do not address the issue of personalized behavior: they try to average over the different examples from different people in the training set. Identifying the human styles during the training and inference time opens the possibility of biasing the model's output to take into account human preferences. In this paper, we focus on the problem of extracting styles in the context of handwriting.

Defining and extracting handwriting styles is a challenging problem, since there is no formal definition for these styles (i.e. it is an ill-posed problem). A style is both social – depends on writer's training, especially at middle school – and idiosyncratic – depends on the writer's shaping (letter roundness, sharpness, size, slope, etc.) and force distribution across time. To add to the problem, till recently, there were no metrics to assess the quality of handwriting generation.

Therefore, there are two questions: how can we disentangle tasks and styles? and what is the style used to achieve a given task?. In handwriting, the task space is well defined (i.e. which letter to write), thus,

allowing us to focus on the second question, extracting styles for achieving this task.

In this paper, we address the problem of style extraction by using a conditioned-temporal deep autoencoder model. The conditioning is performed on the letter identity (i.e., the task). The reason we use an autoencoder is that there is no explicit way to evaluate the quality of the handwriting styles other than using them to generate handwriting, and evaluate this generation. In previous work (Mohammed et al., 2018), we introduced benchmarks and evaluation metrics in order to assess the quality of generating handwritten letters. In comparison to this work, we achieve higher performance, while extracting a meaningful latent space.

We also hypothesize that the latent space of styles is generic, i.e. that it will generalize over unseen writers, thus achieving a "transfer of style". To test this hypothesis, we assess our model on 30 new writers. We compare the tracings generated by this model to a benchmark model already proposed for online handwriting generation.

In addition, we explore the latent space of our model for each letter separately. This revealed that there is a limited number of 'unique' categorical styles per letter. We report our analysis for some of the letters, since a full analysis is out of the scope for this paper.

The contributions of this paper are the following:

- We test and compare our deep conditioned autoencoder with the state of the art benchmarks. We

show that this model greatly improves the generation performance over a state of the art benchmark model.

- We experiment on performing style transfer on new writers using this model achieves, and we show that it achieves much better results than the benchmark model.
- Finally, and maybe most interestingly, we further analyze the extracted the latent space from our model to show that there is a limited number of styles for each letter and that the style manifold is not a continuous space.

2 RELATED WORK

2.1 Generative Models

Recent advances in deep learning (Goodfellow et al., 2016) architectures and optimization methods led to remarkable results in the area of generative models. For static data, like images, the mainstream research builds on the advances in *Variational Autoencoders* (Kingma and Welling, 2013) and *Generative Adversarial Networks* (Goodfellow et al., 2014).

For generating sequences, the problem is more difficult: the model generates one frame at a time, and the final result must be coherent over long sequences. Recent recurrent neural networks architectures, like *Long-Short Term Memory* (LSTM) (Hochreiter and Schmidhuber, 1997) and *Gated Recurrent Units* (GRU) (Chung et al., 2014), achieve unprecedented performance in handling long sequences.

These architectures has been used in many applications, like learning language models (Sutskever et al., 2014), image captioning (Vinyals et al., 2015), music generation (Briot and Pachet, 2017) and speech synthesis (Oord et al., 2016).

We use these powerful tools to extract meaningful latent spaces for styles. Our work is strongly inspired by the seminal work performed by (Ha and Eck, 2017). They investigated the problem of sketch drawing (Google, 2017) using a Variational Autoencoder. The latent space that emerged from training encoded meaningful semantic information about these drawings. We use here a similar architecture, without the variational part, showing a similar behaviour.

2.2 Data Representation

For handwriting, a continuous coordinate representation (e.g. continuous X, Y) seems the natural option. However, generating continuous data is not straightforward. Traditionally, in neural networks, when we

want to output a continuous value, a simple linear or *Tanh* activation function is used in the output layer of the neural network.

However, Bishop (Bishop, 1994) studied the limitations of these functions and showed that they can not model rich distributions. In particular, when the input can have multiple outputs (one-to-many), these functions will average over all the outputs. He proposed the use of *Gaussian Mixture Model* (GMM) as the final activation function of a neural network. The alliance of neural networks and GMMs is called *Mixture Density Network* (MDN). The training consists in optimizing the GMM parameters (mean, standard deviation, covariance). The inference is done by sampling from the GMM distribution.

To simplify the process, and focus our study on investigating of styles, we extract two features for the tracings: directions and speed (explained in section 3), and we quantize these features. Thus, we model each point in the letter tracings as two categorical distributions, and use two *SoftMax* functions (one for each feature) as the outputs of the network, which is much simpler than MDN. This was inspired by the studies done in (Oord et al., 2016), where they report impressive results on originally continuous data, using suitable quantization policy. Categorical distributions are more flexible and generic than continuous ones.

2.3 Evaluation Metrics

The objective evaluation of a generative model performance is a challenging task, since there is no consensus for objective evaluation metrics. In many cases, a subjective evaluation is performed to overcome this problem. For handwriting of Chinese letters, (Chang et al., 2018) proposed two metrics: *Content accuracy* and *Style discrepancy*. In the first metric, a classifier is trained to determine the type of the letter on the reference letters, then it is used to evaluate the generated letters. However, it is not clear how to reliably use the classifier trained on one distribution (reference letters) to evaluate new distribution (the generated letters). The second metric is not applicable to our case, since it assumes the use of *Convolution Neural Network* (CNN) on the image of the letter, while we use the pen sequence of drawing the letter (i.e., temporal data) with RNNs.

We use the same metrics like in (Mohammed et al., 2018) to evaluate the quality of handwriting generation: the *BLEU score* (Papineni et al., 2002) – a metric widely used in text translation and image captioning – and the *End of Sequence* (EoS) analysis (both metrics are explained in section 5).

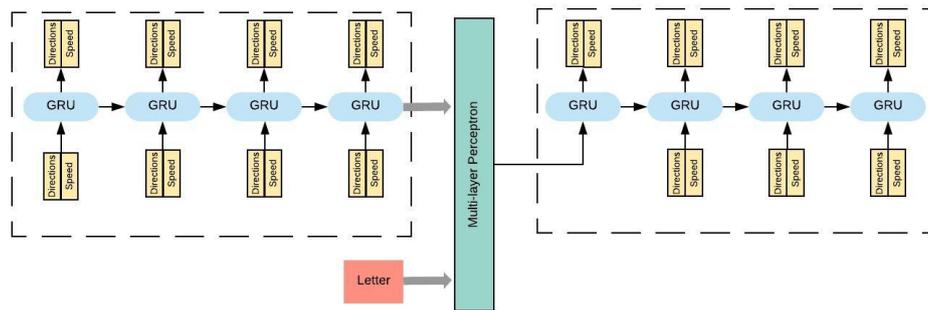


Figure 1: Schematic diagram of the model we used. Both the encoder and the decoder have 2 layers, with size of 128. A dropout of 0.2 is used for the decoder. Learning rate selected is 0.001. During the training time, the input to the model is always the ground truth. During the inference time however, the input to the decoder (generator) part at each time step is its own predication in the previous time step.

3 DATASET

In this study, we use the *IRON-OFF* Cursive Handwriting Dataset (Viard-Gaudin et al., 1999), which contains isolated handwritten letters. To summarize this dataset:

- 412 writers who have written isolated letters.
- 10,685 isolated lower case letters, 10,679 isolated upper case letters, 4,086 isolated digits and 410 euro signs.
- gender, handedness (left or right handed), age and nationality of the writers.
- letter image and timed pen tracings, comprising continuous X, Y and pen pressure, and also discrete pen state.

We focused on the uppercase letters only, and we did not use the pen state or the pen pressure. The idea was to limit the number of possible style factors, so that we can better study them. 90% of the data is used for training, and 10% for validation.

One challenging issue with this dataset is that we have only one example for each writer-letter combination. This makes the task more difficult, because it is hard to extract a writer style using very few items (the 26 letters/writer in this case).

We represent each letter tracing by two features: directions and speed of the pen between each two consecutive points. Each feature is quantized into 16 levels and represented as a one-hot encoded vector. Freeman coding (Freeman, 1961) is used to encode the direction feature.

4 MODEL ARCHITECTURE

The model architecture is shown in figure 1. The trace of the letter is first fed to the encoder module. The

final hidden state of that module summarizes the letter. In order to allow this module to focus on learning the style embedding, we complement this last hidden state with the one-hot encoding of the letter identity, and combine them as the input bias of the generator. Thus, we decouple the *task space* – the letter – from the *style space*: the encoder is freed from the need to learn the letter identity, and can focus on capturing additional information that enables the generator to better approximate the ground truth tracings.

In the decoder, we follow the framework proposed by (Vinyals et al., 2015) in order to bias the model: we create an extra time step at the beginning, which has the information we want to bias the model with. In this case, this time step is the projection of the encoder last hidden state and the letter identity. This has a much lower dimension than encoder hidden state, which further encourage the model to only learn necessary style information, as suggested by (Skerry-Ryan et al., 2018).

4.1 Hyper-parameter Tuning

We ran random hyper-parameter search for a wide range of parameters (learning rate, size and the number of layers for the encoder and the decoder, dropout percentage, etc). GRU layers (Chung et al., 2014) are used in our work (we did not experiment with other architectures, like LSTM). We used *Adam* optimizer (Kingma and Ba, 2014). In order to allow for faster exploration of different hyper-parameters, we used the following early stopping: if no significant improvement is observed after 20 epochs on the validation data, the training is stopped.

4.2 Training

The encoder and the decoder parts aim at modeling the

next time frame in the sequence, x_{t+1} , given the previous time frames, or in other words, $P(x_{t+1}|x_1, x_2, \dots, x_t)$, where x_t is the tracing point at time t . To achieve this, we used teacher forcing: the model is given with the ground truth input of points x_1, x_2, \dots, x_{T-1} and is asked to output the sequence x_2, x_3, \dots, x_T , where T is the length of the input sequence

The model is trained to minimize the negative log likelihood loss of the correct point at each time step. For each feature (speed and freeman codes), it is calculated as in equation 1. The final loss is the average loss of the two features, as in equation 2.

$$\begin{aligned} Loss &= -\log \prod_{t=1}^T p(x_t|x_1, x_2, \dots, x_{t-1}) \\ &= -\sum_{t=1}^T \log p(x_t|x_1, x_2, \dots, x_{t-1}) \end{aligned} \quad (1)$$

$$TotalLoss = (Loss_{speed} + Loss_{freeman})/2.0 \quad (2)$$

During the training, the output of the model at each time step is :

$$x_{t+1}^g = \operatorname{argmax}_x p(x|x_t, h_t) \quad (3)$$

where x_{t+1}^g is the generated/predicted next time frame by the model, x_t is the ground truth input at the current time frame t , and h_t is the hidden state of the GRU at the current time frame. To sample from the model, we used the *Temperature Sampling* strategy from the *Softmax* output.

5 EVALUATION METRICS

Evaluation is a challenging problem when using generative models. We want metrics to capture the distance between the generated and the ground truth distributions. Similar to the work done in (Mohammed et al., 2018), we use the same two evaluation metrics in our model:

- **BLEU score** (Papineni et al., 2002) It is a well-known metric to evaluate text generation applications, like image captioning (Vinyals et al., 2015) and machine translation (Sutskever et al., 2014). Since we discretized the letter drawings, this nicely fits to our work. The general intuition is the following: if we take a segment from the generated letter, did this segment happen in the ground truth letter? We keep doing this for segments of increasing length (the length of the segment here is the number of grams used in the BLEU score). For our work, we report the results on segments from 1

to 3 time steps. Each part of the letter has two parallel segments: freeman codes and speed, thus, we report the BLEU score for both of them. The equation to compute the BLEU score for each feature is the following:

$$BLEU_N = \frac{\sum_{C \in G} \sum_{N \in C} Count_{Clipped}(N)}{\sum_{C \in G} \sum_{N \in C} Count(N)} \quad (4)$$

$$Score_N = \min(0, 1 - \frac{L_R}{L_G}) \prod_{n=1}^N BLEU_n \quad (5)$$

where: G is all the generated sequences, N is the total number of N-grams we want to consider. $Count_{Clipped}$ is the clipped N-grams count (if the number of N-grams in the generate sequence is larger than the number in the reference sequence only), L_R is the length of the reference sequence, L_G is the length of the generated sequence. The term $\min(0, 1 - \frac{L_R}{L_G})$ is added in order to penalize short generated sequences (shorter than the reference sequence), which would deceptively achieve high scores.

- **End of Sequence (EoS)** The letter length is another aspect of the style. The distribution of length in the generated examples should follow the ground truth examples. In order to perform this analysis, we compute *Pearson Correlation Coefficient* between the lengths of the generated sequences and whose of the ground truth data.

6 EXPERIMENTS AND RESULTS

In these experiments, we compare our model with the baseline used in (Mohammed et al., 2018). In that baseline, the model is biased by the letter and writer identities only. Our model, as explained earlier, is biased by the letter identity and the style features extracted from the letter tracings.

6.1 Letter Generation with Style Preservation

The objective here to compare the quality of the generated letters to the state-of-the-art benchmarks. As mentioned earlier, we compare the model's output using the BLEU score and the EoS distribution. The BLEU score results can be seen in table 1, and the results for EoS analysis results are in table 3. We can see that the BLEU-3 (i.e., using 3, 2 and segments) score results of our model achieves 32.3% accuracy in speed feature and 38.7% accuracy in freeman feature,

compared to 25.1% and 28.3% accuracy using the benchmark model on both features respectively.

The same goes for the EoS analysis. In comparing the Person Coefficient, our model achieves 0.99 score compared to 0.55 for the benchmark model (the highest score is 1.0). This is a support that our model capture the style of handwriting better than the benchmark.

Examples for the generated letters can be found in figure 11.

6.2 Style Transfer across Writers

One of the hypotheses we want to test is whether there is a limited number of styles that can generalize over new writers. To achieve this, the learned representation for styles should extract generic information about the styles. In order to test this hypothesis, we expose our model to 30 writers that have not been seen before. We compare our model's performance on these writers with the benchmark model.

The BLEU scores can be seen in table 2. Our model achieves on BLEU-3 score 32.2% and 42.1% accuracy on the Speed and Freeman code features, compared to 25.3% and 27.7% on the benchmark model for the same features respectively. The EoS analysis can be seen in table 4. Our model achieves a coefficient value of 0.93, compared to 0.50 for the benchmark. Thus, the new model clearly outperform the current benchmarks on the transfer task, on both BLEU score and EoS analysis.

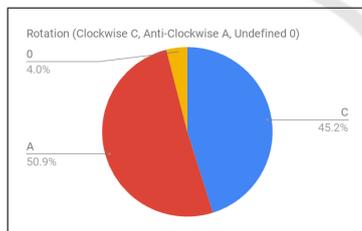


Figure 2: Results of the manual annotation for the rotation of letter X drawings over the whole dataset. Almost half the writers draw X clockwise, the other half counterclockwise. The remaining writers often perform the drawing using two strokes: one clockwise, the other counterclockwise.

6.3 Styles per Letters

One of the nice consequences of using our model is that we can have a closer look at the styles. We explore the latent space for multiple letters, and see that we can uncover interesting writing styles per letter. A full scale analysis is beyond the scope of this paper. We project the latent space using *Principal Components Analysis* (PCA) (Jolliffe, 2011) and t-SNE (Maaten and Hinton, 2008).

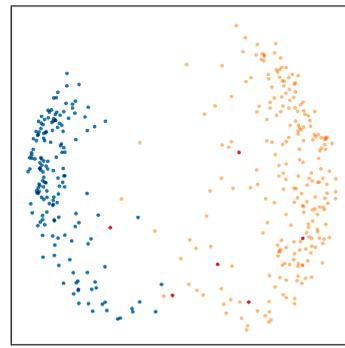


Figure 3: Projection for latent space for letter X using PCA. The colors show the ground truth of the X rotation: blue is counter clockwise, orange is clockwise, and the few red points are undefined.

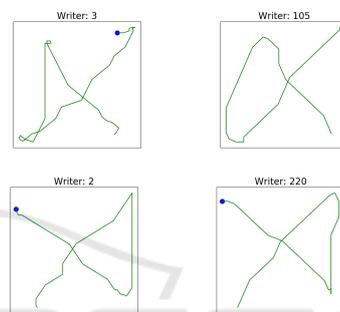


Figure 4: Examples of writing of letter X. Starting point is marked with the blue mark. Each row is randomly sampled from each cluster in the bottleneck. The clusters shows that almost half the writers draw the letter clockwise (first row, first cluster), and the other half draw it anti-clockwise (second row, second cluster).

Firstly, we take a look at letter X. Beforehand, we identified a style feature in letter X: some writers draw X clockwise while others draw it anti-clockwise. We manually annotated the whole dataset for this feature; the result can be seen in figure 2. Almost half of the writers draw the letter X clockwise, and the other half draw it anti-clockwise. If our assumption is correct, our model should be able to capture this feature. We project the latent of the model using PCA on all the letter X, which can be seen in figure 3. The model latent space clusters almost perfectly the two rotation sets. Examples for letters from both clusters are in figure 4.

Encouraged by the results on letter X, we explored more letters. For letter C, we can see the latent space project in figure 5. It can be seen that there are at least two main clusters. Examples from the cluster circled by a red ellipse are in figure 6, first row. It features the Edwardian handwriting style. The rest of the writers (in the big cluster) have a very similar style (this is expected, since the drawing of the letter C is quite simple).

Table 1: BLEU scores for different models for known writers.

Aspect/Feature	Speed			Freeman		
Model / B-score	B-1	B-2	B-3	B-1	B-2	B-3
Letter + Writer bias	51.5	41.4	25.1	56.7	39.4	28.3
Style Extractor	71.0	51.7	32.3	65.6	51.5	38.7

Table 2: BLEU scores for different models for style extraction for 30 new writers (style transfer).

Aspect/Feature	Speed			Freeman		
Model / B-score	B-1	B-2	B-3	B-1	B-2	B-3
Letter + Writer bias	55.4	39.6	25.3	50.2	38.6	27.7
Style Extractor	72.4	52.4	32.2	70.4	55.6	42.1

Table 3: Pearson correlation coefficients for the End-Of-Sequence (EoS) distributions for the different models on the normal generation scenario.

Models	Pearson coefficient
Letter + Writer bias	0.55
Style Extractor	0.99

Table 4: Pearson correlation coefficients for the End-Of-Sequence (EoS) distributions for the different models on 30 new writers (style transfer).

Models	Pearson coefficient
Letter + Writer bias	0.50
Style Extractor	0.93

For letter A, our model latent space create two main clusters, figure 7. We give examples from those two groups in figure 8, where we can see clear differences in the styles. Some people start drawing the letter from down-left whole others start from the top-left, move down and then continue the letter drawing as previously. This is similar to results reported in (Sraphin Thibon et al., 2018), which analyzed the handwriting of uppercase letters.

Another example is for letter S bottleneck, figure 9. There are three resulting clusters which we investigated. The cluster circled in red is clearly different from the other two clusters (not indicated). Examples can be seen in figure 10. This cluster is again for writers with Edwardian handwriting style. We did not find a clear difference between the other two clusters though, but this is an expected outcome of using t-SNE (since it does not have the clear objective of clustering styles).

7 CONCLUSIONS AND FUTURE WORK

In this paper, we explored handwriting styles, using a deep neural network paradigm. We have approached the problem systematically. First, we compared our

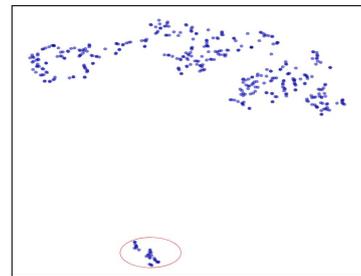


Figure 5: Projection for latent space for letter C using t-SNE. The cluster surrounded by the red circle has a clear interpretation, where writers have a cursive style.

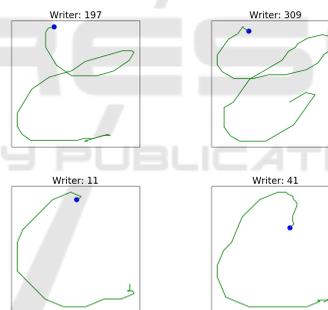


Figure 6: Examples for writing of letter C from the selected cluster (first row) versus the rest of the letter drawings (second row). Starting point is marked with the blue mark. The drawings from the selected cluster show people with Edwardian style of handwriting.

generation results to the benchmark reported in the state-of-the-art on this problem, and we show that our model outperforms the benchmark. Second, we explore the ability to perform style transfer, by testing the model’s performance on 30 new writers. We hypothesize that there is a limited number of style components that describe handwriting, and a good style extraction model should generalize well to new writers. Last, we analyze the latent space of our model for multiple letters, and show that the model separate the different styles in different clusters. We are interested in further investigating the concept of style transfer. In this work, we fixed the task (the uppercase letters),

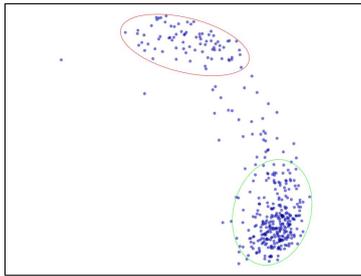


Figure 7: Projection for latent space for letter A using PCA.

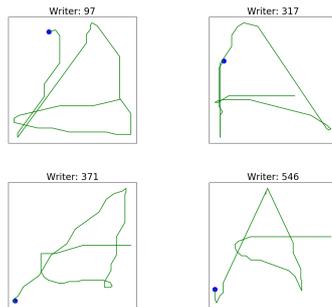


Figure 8: Examples for writing of letter A from the selected clusters. Starting point is marked with the blue mark. Each row is from one cluster. The first row show people who start drawing the letter from the top, going down, and then continue the drawing of the letter. The second row show people who start drawing from down direction.



Figure 9: Same as figure 5 but for letter S. We identify the circled cluster as the Edwardian style. The other two clusters (not indicated) did not show clear differences.

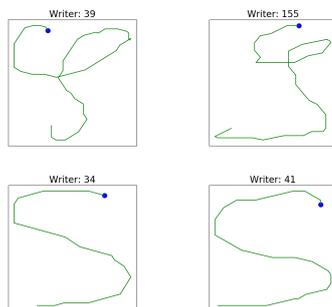


Figure 10: Examples for writing of letter S from the selected cluster (first row) versus the other two clusters (second row). Starting point is marked with the blue mark. The drawings from the selected cluster is always Edwardian style.

and performed transfer of style across writers. Our plan is to investigate style transfer while changing the task (e.g., learn style on uppercase letters, and transfer them to the lowercase writers).

Based on the results of the latent space analysis, it is interesting to investigate a latent space structure and objective function that can disentangle the style manifold. So far, we used multiple projection techniques in order to explore the style information in the latent space. The objective in this case is to encourage the styles to emerge on its own in the latent space.

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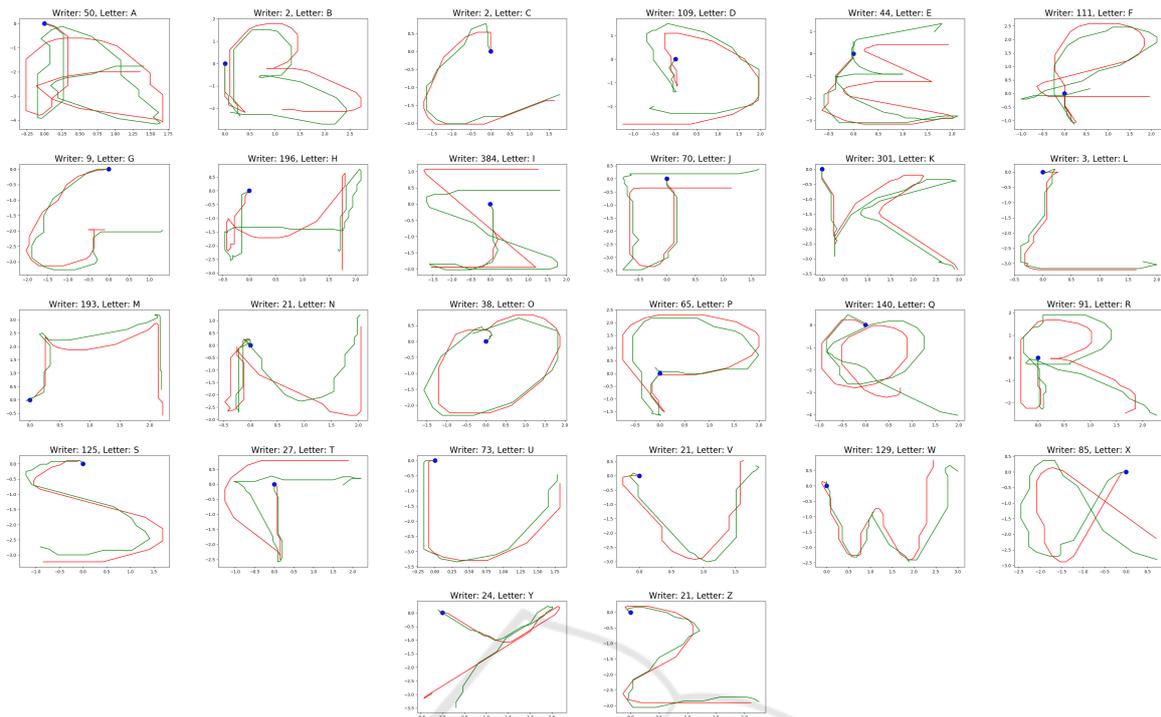


Figure 11: Examples of generated letters. The blue mark is the starting point. The traces in green is the ground truth, and the red is the generated ones by our model.

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