Understanding Sprinting Motion Skills using Unsupervised Learning for Stepwise Skill Improvements of Running Motion

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Abstract: To improve running performances, each runner’s skill, such as characteristics and habits, needs to be known, and feedback on the performance should be outputted according to the runner’s skill level. In this paper, we propose a new coaching system for detecting the skill of a runner and a method of giving feedback using a sprint motion dataset. Our proposed method calculates an extracted feature to detect the skill using an autoencoder whose middle layer is an LSTM layer; we analyse the feature using hierarchical clustering, and we analyse the human joints that affect the skill. As a result of experiments, five clusters are obtained using hierarchical clustering. This paper clarifies how to detect the skill and to output feedback to achieve a level of performance one step higher than the current level.

1 INTRODUCTION

Receiving appropriate guidance based on objectively evaluated performance in rehabilitation and sports practice is important for learners to improve their skill. In particular, it is essential for a guidance system to output feedback on their improvement so that learners can efficiently improve their skill. Traditionally, such feedback has relied on the professional experience of medical and sports experts. Nowadays, emerging technologies such as deep learning (DL) and image processing have made it possible to use computerized coaching systems that are able to obtain information from sensors and analyze it to give objective feedback. The advantage of a computerized coaching system is not only the ability to objectively evaluate the learner’s performance but also to help the learner to improve their skill. Implementing such a coaching system may be helpful for human performers.

In this paper, we propose a coaching system that addresses the problem of enhancing sprinting performance effectively by offering feedback in a step-by-step manner. Section 2 describes work related to objectively evaluating performance. In Section 3, we explain the requirements for the coaching system, as described above, and our proposed methods. Then, experiments on exercise behaviour and experimental results are presented in Section 4. We discuss the experimental results in Section 5 and conclude the paper in Section 6.

2 RELATED WORK

Many systems that automatically evaluate exercise motion using sensors and output a score based on the performance level have been presented in the literature. As an example in the field of sports, Pirsiavash et al. proposed a system that can automatically evaluate performance in diving and figure skating. They used performances from videos recorded during Olympic games. Their method predicts the score given by referees from the movement of the performer’s joints, and also outputs feedback for the joint positions that need to be improved in case of a performance with a low score. They used a discrete cosine transformation (DCT) matrix to extract features from the movement of the performer’s joints. In other work, Venkataraman et al. used Cross Approximate Entropy (XApEn) instead of DCT and applied supervised learning to Pirsiavash et al.’s dataset. Venkataraman et al. claim that XApEn extracts better features than DCT.

In the healthcare field, Parmar et al. presented a method for evaluating exercises for physical therapy: for example, the Blastoff exercise. Here, the practitioner’s performance is indicated by a “good” or
“bad” outcome using a support vector machine (SVM). In the medical field, Zia et al. introduced a system for assessing surgical skill using robot kinematics data in Robot-Assisted Minimally Invasive Surgery (RMIS) training, to address the problem of enhancing surgical skill. Their method involves not only predicting scores for surgical skill, but also classifying the skill into three levels: novice, intermediate, and expert. In general, the above methods cannot handle features that are involved in determining the performer’s skill, such as a habit. Therefore, we use unsupervised learning because this approach can classify each performer’s skill without the necessity of knowledge about the performance.

3 PROPOSED METHOD

3.1 Basic Idea and Strategy

The skill of a person performing an exercise motion cannot be represented by a one-dimensional evaluation axis, such as the quality of the performer. We believe that it could be represented by multi-dimensional evaluation axes composed of many abilities, such as body flexibility, agility of action, etc. Additionally, an ideal exercise motion is not composed of only one pattern, but has multiple patterns. From this viewpoint, target skills could be represented by peaks (local optimal solutions) when it is evaluated with multi-dimensional evaluation axes. For example, in case of a sprinter’s running form, the peak changes to fit the various aspects of different running forms, such as step frequency type or stride length type during sprinting. In particular, the peak is decided according to each person’s skill, such as the individual’s talent, characteristics and habits. With the systems in the related work described above, it can be difficult to improve the performance because these systems output an improvement which is not possible to fit each person’s skill; therefore, we consider that, to improve performance, it is necessary to know each person’s skill. We believe that the performers should improve their skill by following a plan that leads to a higher level of skill than the current level. The reason is that this plan is easier and more efficient for them than a plan that involves directly improving their skill so as to achieve a peak. Therefore, the coaching system we aim to develop should be improved step-by-step in accordance with the performance achieved after each performer have understood their skill, rather than to improve the performance so as to simply indicate a difference in skill after analysing the difference between bad performers and good performers.

Second, we think that the feedback given to improve a performance should not include all of the joints that must be improved, as opposed to Pirsiavash et al.’s method, because this is generally difficult. The method of Parmar et al. could only evaluate whether a performance was right or wrong. Also, the method of Zia et al. could evaluate a performer’s skill, such as a low or high level, because they could use the result of evaluating scores to judge the level of skill in surgical techniques. However, these two studies did not propose how to improve the skill of unskilled performers. In general, we assume that the above systems that objectively evaluate performance could not understand the performer’s skill and could not improve it step-by-step by considering the performer’s skill level.

In outline, our approach for improving performance step-by-step to a peak is quite different from the approaches in the related work described above for directly improving performance to an optimal solution. Against this background, we propose a new coaching system based on the following approach: 1) Extract features of exercise behavior of performers and recognize the skill of the performers using these features; 2) Determine a peak that fits their skill in order to improve the performance; and 3) Output advice for stepwisely improving the skill level to achieve the peak. In this paper, we focus on how to get the features of skill and to understand it.

Our system uses unsupervised learning because we hypothesize that similar skill levels in performances form clusters, and those clusters lead to an understanding of the character of the performances As a prerequisite, using unsupervised learning is more accurate and results in higher reproducibility than classifying the performances based on an expert’s experience. Therefore, our coaching system uses unsupervised learning.
In Section 3.2, we explain a method of detecting human joints in a video of running motion. In Section 3.3, we describe a method of learning an autoencoder, which is one kind of unsupervised learning. In Section 3.4, we clarify Cluster Analysis to use the features calculated by the autoencoder. Finally, we verify the feature of the clusters calculated after cluster analysis. Figure 1 shows outline of our proposed methods.

3.2 Human Detection and Joint Detection in a Video

To detect a human in a video of a human performance, it is possible to use higher object detection’s methods. We chose YOLOv3 (Redmon et al., 2018) because it is ideal for use in detecting running motion while maintaining high accuracy and achieving real-time processing speed.

As the method of human joint detection, we chose the network of Chu et al. There are several reasons for this. First, the method of Newell et al. has the same problem that occurs in false detection, namely, that the right and left joints of the lower limbs are swapped, and this works as noise, which leads to unsuccessful results using a training dataset. Last, the method of Yang et al. is much more accurate than that of Chu et al. using the MPII dataset (Andriluka et al., 2014), but Chu et al.’s network gives more false detections than Yang et al.’s network with our data. Therefore, we used Yang et al.’s network in order to stabilize the detection of human joints.

3.3 Feature Extraction

Given a video, we propose a method of unsupervised learning for extracting generic features of running motion based on the detected joints using Yang et al.’s network.

Feature Extraction of Human Pose: Let \( \mathbf{p}(i)(t) \) and \( \mathbf{p}(0)(t) \) be the x component of the j-th joint and head position in the t-th frame of the video, respectively. We normalize the vector given by subtracting the head position from the j-th joint position:

\[
\mathbf{q}(j)(t) = \frac{\mathbf{p}(i)(t) - \mathbf{p}(0)(t)}{\mathbf{p}(i)(t) - \mathbf{p}(0)(t)}
\]

Eq. (1) is similar to Pirsiavash et al.’s method, but our method can calculate similar features in the performance of each person even if they have different physical constitutions, such as their height.

Network Structure: Our network is based on an autoencoder structure, which was used as the LSTM layer in the middle layer, such as ERD (Fragkiadaki et al., 2015). Those networks have traditionally been used to generate and predict human motions.

We use the network with the structure in Fig. 2(b) and Fig. 2(c). As shown in Fig. 2(b), the input layer and output layer have 30 dimensions, and the inner product layer has 100 dimensions in the part of the Encoder layer and the Decoder layer. The middle layer has 50 dimensions. We use Euclidean distance for the loss function on the features using Eq. (1) between the output data and the input data. We train our model with stochastic gradient descent (SGD), using the Caffe (Jia et al., 2014) package. Second, we change the middle layer to an LSTM layer, as shown in Fig. 2(c), and we do transfer learning to use the model in Fig. 2(b) and use same loss function using Fig. 2(b). We train our model with SGD and backpropagation through time with momentum and the gradient clipping set at 60. After the network has learned, we perform hierarchical clustering for the features obtained from the Encoder layer and the LSTM layer to verify classification by unsupervised learning, as shown in Fig. 2(d).
3.4 Algorithm for Analysing Learned Network

To analyze how the input affects the output in DL, it is important to verify which element of the input is related to the output of the learned network. In this paper, the degree of influence of the input on the output in DL is called the contribution degree of input values (CDIV).

The methods of Zhou et al. and Selvaraju et al. both involve calculating the CDIV. Both methods visualize the degree of influence of a pixel of the input image on the output using a heatmap for the model of supervised learning of image classification by DL. Their CDIV can help for analysing features which is obtained by supervised learning to understand what inputs have an influence in the features. We suppose that they do not use only the features obtained by supervised learning, but also we suppose those methods use the feature obtained by unsupervised learning. In fact, we used the CDIV to verify each cluster in the cluster analysis described later Fig. 3(c), and our proposed method is simpler to calculate it than the methods of Zhou et al. and Selvaraju et al. This can help to verify the skill of an individual, which is obtained by unsupervised learning, in exercise behavior in each cluster after the cluster analysis in Fig. 2(d).

To calculate the CDIV, we propose a simpler method than the conventional methods using the weight of the last layer (j-th layer in Fig. 3) in the network and the gradient of the learned model in the network. First, as shown in Fig. 3 (a), we find a node in (j-1)-th layer that has the most influence on the j-th layer. Second, we give 1 point to the most influential node in the (j-1)-th layer, and we give 0 points to the other nodes. This operation is performed on all nodes in the (j-1)-th layer. After scoring all nodes in the (j-1)-th layer, we exclude the nodes that have 0 points or that were not activated in the (j-1)-th layer, as shown in Fig. 3(a). For the remaining nodes, we perform operations similar to those performed on the (j-1)-th layer in the (j-2)-th layer. Third, we repeat the same operations as shown in Fig. 3(b) until it reaches the input layer. Last, we can calculate the node of the input contribution in the network, as shown in Fig. 3(c). Our method has the advantage that the principal input for the output can be found easily by tracing the nodes. In our case, the CDIV leads to knowing not only the joints contributing to the performance for each person but also the direction in which the joints contribute.

Figure 4 visualizes the input contribution in human joints using the calculated CDIV result in Fig. 3(c). This can help to verify skill of an individual in exercise behavior in each cluster after the cluster analysis in Fig. 2(d).

Figure 3: Outline of the CDIV in our method: The method can calculate the principal input for the output which can be found easily by tracing the nodes.

Figure 4: Visualization of CDIV in human joints: We visualize the CDIV of human joints in order to understand the skill of a human performance. Blue color's node is expressed as not contributing to the motion. Green one is expressed as contributing to the motion in the x-axis direction. Red one is expressed as contributing to the motion in the y-axis direction. Yellow one is expressed as contributing to the motion in the x-axis and y-axis direction.

Figure 5: Sprint Dataset: (a) experimental conditions for creating our dataset; (b) sample frames in our dataset.

4 EXPERIMENTS

In this section, we introduce the dataset used in the experiments and present the experimental results obtained using the method in Section 3.
Table 1: Observational motion evaluation items concerning running motion in sprinting: These evaluation items can be evaluated for performers by keeping scores.

<table>
<thead>
<tr>
<th>Body Part</th>
<th>Evaluation Point</th>
<th>20</th>
<th>10</th>
<th>0</th>
</tr>
</thead>
<tbody>
<tr>
<td>Upper Limb</td>
<td>Putting the elbow forward</td>
<td>The elbow moves forward by a large amount before the body side.</td>
<td>The elbow moves slightly forward before the body.</td>
<td>The elbow does not go forward before the body.</td>
</tr>
<tr>
<td></td>
<td>Bending the elbow</td>
<td>Hold the elbow bent while swinging.</td>
<td>Hold the elbow bent and stretched while swinging.</td>
<td>Bend the elbow to hook arm in front of body.</td>
</tr>
<tr>
<td></td>
<td>Size of lower limb movement</td>
<td>It can be seen that the knee of the swinging leg moves forward by large amount, and the leg swings back just below the body.</td>
<td>The swinging leg is swings weakly in running motion.</td>
<td>The forward swinging of the swinging leg and the extending of the knee are very small, and flight duration is extremely short.</td>
</tr>
<tr>
<td>Lower Limb</td>
<td>Switching of legs</td>
<td>The swinging leg overtakes the supporting leg almost at the same.</td>
<td>The swinging leg over-takes the supporting foot immediately after touching the ground.</td>
<td>The swing leg slowly overtakes the supporting leg by touching the ground.</td>
</tr>
<tr>
<td></td>
<td>Foot on the ground</td>
<td>Ground of the thenar part.</td>
<td>Ground of the sole of the foot.</td>
<td>Ground of the heel.</td>
</tr>
</tbody>
</table>

4.1 Running Motion Dataset

It is difficult to evaluate our proposed system for datasets such as that used by Pirsivash et al., which cannot be evaluated without professional skills, but our system needs a dataset in order to be used by persons even without professional skills. From this viewpoint, the running motion in sprinting was applied to our system; this was optimal also in that it was easy to determine the individual’s characteristics and habits during running. Therefore, we chose running motion as our target.

Our dataset consists of mostly subjects who had no experience of athletics. The reason for this is that we judged that this is essential for the introduction of our study to verify how a performer’s skill could lead to stepwise improvements in a performance that is evaluated as imperfect. For example, if we used the data of top sprinters, we would not be able to discover imperfect performances, because it would not be possible to evaluate top sprinters using only the joint motion we propose, and we would have to use the joint motion and other information, such as information from myoelectric sensors, if we want to evaluate their performance. Therefore, such an approach is not suitable for ascertaining the advantages of our system, so we gathered data mostly from test subjects having no experience of athletics.

We collected data from 14 healthy subjects (13 male and 1 female, aged 23-31 years old) by measuring running motion when they ran 30 m at full speed. As the experimental conditions, the video camera was placed at the position shown in Fig. 5(a) so that the range from 0 m to 15 m appeared in the videos. The reason for taking the video in this range is that the...
starting motion makes a large contribution to the total running time. Thus, we focused on improving the starting motion, which is considered to lead to improving skill. On the other hand, we used a video camera capable of capturing video at 60 frames per second when the subject was running. At the same time, we measured the time taken to run 30 m. Each subject was asked to run 4 to 6 times, and we captured 71 videos. We used the videos to detect human joints using the method described in Section 3.1, as shown Fig. 5(b), and to analyze the detected joints using the methods described in Section 3.2 and Section 3.3.

In addition, as for the scoring related to the running motion, a person having experience of springing in athletics was asked to keep scores for the subjects using the evaluation items shown in Table 1. Here, one-cycle is defined as the period from when the supporting leg leaves the ground until the opposite foot reaches the ground. In preparing these evaluation items, we referred to the work Suzuki et al. Their evaluation items were targeted at elementary school students in Japan, but we considered that there would be no problem even if we used them to evaluate adults because they referred to many studies on sprinting by athletes and non-athletes in the creation of these items.

4.2 Result of Cluster Analysis

We show the visualization of the features in the running motion using the method of Section 3.4 based on Principal Component analysis (PCA). As a result of performing hierarchical clustering on this feature, we found that there are roughly 5 clusters, as shown in Fig. 6. In particular, Cluster 1, which has the largest number of subjects among the 5 clusters, was divided into another three clusters (sub-clusters), as shown in Fig. 6. We discuss the feature of each cluster in Section 5.

5 DISCUSSION

5.1 Discussion of Results of Cluster Analysis

We verified the validity of the 5 clusters obtained in Section 4 by comparing the CDIV described in Section 3.4 with the evaluation method in Table 1. Figure 7(a) shows the joint ids in the MPII dataset (Andriluka et al., 2014), and Fig. 7(b)-(f) show the CDIV in each cluster. At this time, the contributed x-axis direction of the CDIV is the forward moving direction of the subject, and the contributed y-axis direction of the CDIV is the upward direction of the subject. Table 2 shows the average of the scores and the standard deviation of the score for each cluster by scoring the running motion using Table 1.

According to Fig. 7(b), the subjects in Cluster 0 had all joints contributing to the motion in the x-axis direction for the upper limbs and left lower limbs, and it is considered that the thrust during running was higher than the subjects in the other clusters. In fact, Table 2 shows that the average value of the scores was higher than those of the other clusters. As seen in Fig. 6, overwhelmingly most of subjects belonged to Cluster 1, and the standard deviation of Cluster 1 was also large. Figure 7(c) shows a visualization of the top 15 joints that contribute most to the running motion in Cluster 1. Since the features of these 3 clusters are more efficient running motion in which the lower limb moves more in the upward and downward directions compared with the other clusters. Actually, the average value of the score for Cluster 2 was small, as shown in Table 2, and this was due to the lower scores for the items related to lower limbs in Table 1. Cluster 3 was occupied by one subject.
According to Fig. 7(e), the CDIV of this subject was contributed to by the right hip joint in the x-axis direction and the left hip joint in the y-axis direction. We can only evaluate usual running based on Table 1. As we checked the running record of the subject in our experiment, the features were calculated when the subject in Cluster 3 started to run prematurely. Therefore, it can be presumed that this cluster indicated the characteristics of the premature start. Cluster 4 was occupied by one subject too.

According to Fig. 7(f), the CDIV of this subject was contributed to by the part from the hip joint to the upper limb. It is thought that there is a tendency for inefficient running motion, like Cluster 2, but this running motion was evaluated based on usual running as specified in Table 1. However, we know that the running time for the subject in Cluster 4 was the slowest in his running times that he ran in the experiments. We consider that something that cannot be measured using the evaluation items in Table 1 can be detected by unsupervised learning, and the cause could be identified by analysing the CDIV of the learned network.

Figure 8: Visualization of the CDIV of human joints in each cluster in Cluster 1: (a) CDIV of Cluster 1-0. (b) CDIV of Cluster 1-1. (c) CDIV of Cluster 1-2.

Table 2: The basic information in each cluster: the number of people, number of frames, mean score, and standard deviation of score in each cluster.

<table>
<thead>
<tr>
<th>Cluster</th>
<th>Number of People</th>
<th>Number of Frames</th>
<th>Mean Score</th>
<th>Standard deviation of Score</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>2</td>
<td>323</td>
<td>58.08</td>
<td>16.95</td>
</tr>
<tr>
<td>1</td>
<td>66</td>
<td>10810</td>
<td>49.60</td>
<td>15.68</td>
</tr>
<tr>
<td>2</td>
<td>6</td>
<td>1099</td>
<td>47.24</td>
<td>10.12</td>
</tr>
<tr>
<td>3</td>
<td>1</td>
<td>165</td>
<td>54.79</td>
<td>10.13</td>
</tr>
<tr>
<td>4</td>
<td>1</td>
<td>157</td>
<td>47.58</td>
<td>11.08</td>
</tr>
<tr>
<td>Total</td>
<td>76</td>
<td>12464</td>
<td>49.56</td>
<td>22.57</td>
</tr>
</tbody>
</table>

Next, we discuss the three clusters in Cluster 1. Figure 7 shows the CDIV of human joints in each cluster. Table 3 shows the average of the scores and the standard deviation of the score for each cluster, obtained by scoring the running motion using Table 1. According to Fig. 8(a), Cluster 1-0 has a larger number of joints contributing to motion in the x-axis direction. From this, it is thought that the thrust during running is higher than the other clusters. In fact, groups with slightly higher scores are included in Cluster 1-0, as shown in Table 3. According to Fig. 8(b), Cluster 1-1 has a small number of joints contributing to motion in the x-axis direction compared with Cluster 1-0. In Table 3, this is considered to be a normal level for running motion since the scores are distributed around the score of 51.35. According to Fig. 8(c), Cluster 1-2 is considered to be inefficient running motion in that it has a larger number of joints contributing to motion in the y-axis direction, as shown in Cluster 2. Actually, the score in Table 1 also has the lowest average value in the other clusters, as shown in Table 3. As a whole, it can be ascertained from Fig. 8 that Cluster 1 tends to have a higher number of joints contributing to motion in the y-axis direction, leading to a lower score, and a higher number of joints contributing to motion in the x-axis direction, leading to a higher score.

From the above, it is considered that the clusters obtained by unsupervised learning had validity in that they can be understood from the evaluation items in Table 1. In addition, it can be considered that, for achieving skill in running motion, a feature that analyses the skill of running motion using the CDIV and the evaluation items in Table 1 could be detected by cluster analysis.

Table 3: The basic information in each sub-cluster in Cluster 1: number of people, number of frames, mean score, and standard deviation of score in each cluster.

<table>
<thead>
<tr>
<th>Cluster</th>
<th>Number of People</th>
<th>Number of Frames</th>
<th>Mean Score</th>
<th>Standard deviation of Score</th>
</tr>
</thead>
<tbody>
<tr>
<td>1-0</td>
<td>6</td>
<td>981</td>
<td>59.88</td>
<td>15.57</td>
</tr>
<tr>
<td>1-1</td>
<td>29</td>
<td>4686</td>
<td>51.35</td>
<td>14.65</td>
</tr>
<tr>
<td>1-2</td>
<td>31</td>
<td>5143</td>
<td>46.04</td>
<td>15.47</td>
</tr>
</tbody>
</table>

5.2 Method of Feedback

As the method of feedback, we focus on the fact that each cluster in Cluster 1 is divided into the step-by-step clusters in Table 3. We believe that the subjects can improve their skill by aiming at other skills which are higher than the skill they possess. For example, a subject in Cluster 1-2 aims to achieve the CDIV of Cluster 1-1, which is one step higher, and the subject in Cluster 1-1 aims to achieve the CDIV of Cluster 1-0, which is one step higher too. Therefore, with the
improved skill, it may be possible to achieve a skill that is one step higher than the current skill. However, this method is not perfect because we cannot confirm it. For this reason, we would like to conduct other experiments in order to verify our method using the results obtained in this paper.

5.3 Remaining Issues

It is difficult to find a peak of each cluster, which is aimed at improving running motion, because the peak is not clear using our dataset alone. In other words, we do not know which direction is the peak for the subjects to improve the skill of their running motion. We believe that this problem can be solved to improve the running motion by not only subjects who have no experience of athletics but also subjects who have experience of athletics. The reason is that, using our method, the running motion of experienced people may be a peak that is a few steps higher than that of non-experienced people, and their motion may be the peak for the motion of non-experienced people in the same cluster.

Second, in this paper, we evaluate the running motion using the evaluation items in Table 1, but it will be necessary to automatically output a score for running motion in the future. For this reason, it is possible to find the score for a performance one step higher than the current one in the same cluster. In particular, the evaluation items in Table 1 focus only on the upper limbs and lower limbs, yet other items are needed, such as a forward-bent posture, which is important in running motion. We plan to expand these items by using a method such as dynamically analysing each cluster’s features obtained as described in Section 3.3.

6 CONCLUSIONS

This paper has proposed a system that can let the viewer understand the skill of a performer and can output feedback for achieving one step higher performance aimed at by the performer. Among them, we proposed CDIV as a method for analysing the input component of the features obtained by an autoencoder in which the middle layer is replaced with an LSTM layer. From the CDIV, the validity of the running skill, in which five clusters were obtained by hierarchical clustering, was confirmed by comparing with the evaluation items in Table 1. In addition, we showed the possibility of detecting skill involving aspects such as the individual’s characteristics. Then, we demonstrated the possibility of a method of feedback for improving the performance to a level one step higher than the current one using the CDIV of each cluster in Cluster 1.

As the future work, we will further clarify the skill of running motion by adding the running motions of experienced athletes. Also, we will improve the evaluation items by dynamically analysing the running motion in each cluster. Moreover, we would like to conduct other experiments in order to verify our method.

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