Abstract: This study proposes a new method of fitting a glottal model to the glottal flow estimate using system identification (SI) algorithms. Each period of the glottal estimate is split into open and closed phases and each phase is modelled as the output of a linear filter. This approach allows the parametric model fitting task to be cast as a system identification problem and sidesteps issues encountered with standard glottal parametrisation algorithms. The study compares the performance of two SI methods: Steiglitz-McBride and Prony. The tests were performed on synthetic glottal signals (n=121) and real speech (n=50 healthy, n=23 pathological). The effectiveness of the techniques is quantified by calculating the Normalised Root Mean Squared Error (NRMSE) between the estimated glottal fit and the glottal estimate. Tests on synthetic glottal signals show that the average performance of the Steiglitz-McBride method (97.25%) was better than the Prony method (70.41%). Real speech tests produced results of 64.29% and 51.57% for healthy and pathological speech respectively. The results show that system identification techniques can produce robust parametric model estimates of the glottal waveform and that the Steiglitz-McBride method is superior to the Prony method for this task.

1 INTRODUCTION

The glottal waveform represents the activity of the vocal folds and can provide vital information about the vocal folds and their behaviour. The glottal waveform can be estimated from the speech signal and is utilised in many speech processing applications, including speech coding, synthesis and speech disorder diagnosis (Klatt, 1990). Parametric models of the glottal waveform are often employed and despite the success of the glottal signal in applications, challenges remain in accurately and robustly estimating the parameters of these models. This is the case for healthy speech but is particularly notable for pathological speech. This study aims to present a new model of the glottal waveform and test methods to estimate the parameters of this model. This is partly motivated by the need to develop a method that can accurately and robustly estimate the glottal parameters of pathological speech.

Parameterisation of the glottal signal consists of two steps: (1) glottal waveform estimation and (2) fitting a parametric model to the estimated glottal waveform. Glottal waveform estimation is achieved by removing the effect of the vocal tract from the speech waveform, often by estimating a vocal tract filter and inverse filtering the speech signal with this filter to remove the vocal tract component. The resulting glottal estimate will have the parametric model fitted by applying an appropriate optimisation procedure. This is typically a nonlinear optimisation problem, depending on the particular glottal model and how the problem is cast. This is the case for the Liljencrants-Fant (LF) model, which is currently the most widely adopted glottal waveform model. Both of these steps have a number of known difficulties as reported in (Li et al, 2011, 2012) (Fu, Murphy, 2006). It is often impossible to fully remove the vocal tract component from the speech waveform. This can result in distortion of the glottal waveform often presenting as ripples in the glottal waveform (Fant, Lin 1987). This can also cause problems with correct estimation of glottal opening and closing instants (GOI and GCI respectively) and in turn, inaccurate glottal parameter estimation. In fitting the parametric model to the estimated glottal waveform, due to the necessity to employ nonlinear optimisation methods, the accuracy of the final glottal parameters depends critically on the initial estimates used to initialise the optimisation procedure (Strik, 1993). Bad initial estimates will result in suboptimal estimation of the parameters (Li et al, 2012). This problem becomes
particularly challenging for pathological speech, when the glottal parameters may be outside the typical range expected for healthy speech.

This paper proposes a new way to model the glottal waveform, which in turn allows the application of new algorithms to estimate the glottal parameters. The model being proposed considers the open and closed phase of the glottal signal individually and models the glottal signal within each phase as the impulse response of a linear filter. This allows fitting of the parametric model to the glottal estimate to be cast as a system identification problem. In this case the input is modelled as an impulse, the output is either the open or closed phase of the glottal estimate and the problem is to estimate the filter that can best approximate the output for the given input signal. Many system identification algorithms exist that could be used for this task (Ljung, 1999), including algorithms that have been developed to be robust to noise in the output signal. This is particularly beneficial for glottal signals with high levels of aspiration noise, which is often the case for pathological speech.

The remainder of this paper is arranged as follows. Section 2 presents some background on existing glottal models before presenting the details of the new approach being proposed in this paper. Section 3 describes how the model and associated algorithms are tested. Section 4 presents the results with discussion and Section 5 presents the conclusions.

2 MODELING THE GLOTTAL WAVEFORM

Many signal models of the glottal waveform have been proposed in the literature. These include the Rosenberg model (Rosenberg, 1971), the KLGLOT88 (Klatt, 1990), the R++ model (Veldhuis, 1998), the CALM model (Doval et al., 2003) and the LF model, among others. Signal models of the glottal flow generally focus on the differentiated glottal flow. Typically, a separate mathematical function is used to model the open and return phases of the differentiated glottal signal, such that they join at the GCI. An example model signal of the differentiated glottal flow waveform generated with the LF model is depicted in Figure 1. Most models have a similar approach, in that they have a separate mathematical function for modelling the open and return phases of the signal. The primary difference between many of these models is the functions employed to model each phase.

Currently the most widely adopted glottal model is the LF model, equation 1. The model consists of two parts, representing the open and return phases of the glottal signal. The LF model is a five-parameter model. The entire model can be defined using the timing parameters $T_a$, $T_p$ and $T_e$, the pitch period $T$ and the amplitude of the glottal closure instant (GCI) $E_c$. $T_a$ and $T_p$ are times relative to the start of the pitch period as depicted in Figure 1. $T_a$ is the time constant of the exponential in the return phase. The time parameter $T_e$ marks the instant of the glottal closure and $E_c$ is the corresponding amplitude. Despite having several more parameters, the LF model is constrained by the five primary parameters and the remaining parameters can be estimated from the primary parameters.

\[
x(t) = \begin{cases} 
E \cdot e^{at} \sin(\omega_0 t), & 0 \leq t \leq T_e \\
E_b \cdot e^{-\beta(t-T_e)}(e^{-\beta(t-T_a)} - e^{-\beta(t-T_p)}), & T_e \leq t \leq T_p \\
0, & \text{elsewhere}
\end{cases}
\]  

Fu and Murphy (2006) proposed a new glottal source estimation method based on a joint source-filter separation technique using the LF model. Their proposed technique estimates the parameters based on the Rosenberg model and then converts them to the LF parameters. They perform tests on synthetic speech covering six phonation types and real healthy speech files to verify the performance of their method on ‘real-world’ data. They report a high accuracy of the synthetic speech results and robustness against additive glottal noise, stating that this allows their new method to be applied to a wide range of voice types. Tests on real speech report performance comparable with that of the synthetic speech and state that their model provides rather reliable estimation in the case of natural utterances.

Li et al. (2011) proposed a new approach for LF model based glottal source parameter estimation by
extended Kalman filtering and use synthetic speech to conduct tests. They quantify the results by calculating the error rates of the estimated shape controlling parameters and report the model to be effective for a wide range of LF parameters and overall, perform better than the standard time-domain LF-model fitting algorithm when tested on synthetic speech.

Work of Muthukumar et al. (2013) proposes estimating the LF model parameters using a gradient descent optimization algorithm. The accuracy of their approach inherently depends on the accuracy of the initial parameters. They iteratively fit a LF model to the inverse filtered glottal signal and then optimise it to minimize the RMS error. As a way of quantifying the performance of their approach, they conducted a listening test, comparing their model with a baseline system described in (Yoshimura et al, 2001). The majority of the listeners chose the proposed system as more natural sounding and the results were deemed statistically significant.

Previous studies on glottal fitting report difficulties with the standard model fitting approach and aim to overcome them in different ways. A major problem is with estimating the vocal tract filter without the glottal flow having an effect on the output speech. This issue was already reported by Fant and Lin back in (1987).

The glottal waveform estimation step can be impacted by source-tract interaction and the performance limitations inherent in some inverse filtering algorithms (Quatieri, 2006). In the IAIF method (Alku, 1991), the vocal tract filter is estimated using an adaptive filter algorithm and subsequently applied to estimate the glottal signal. A more recent Quasi Closed Phase (QCP) method described in (Airaksinen et al, 2014) eliminates the source effect using weighted linear prediction (WLP) and focuses on the samples located in the closed phase. Recent work of Sahoo and Routray (2016) implements system identification methods in a novel glottal inverse filtering method. They report that when compared to the most widely used IAIF and the more recent QCP methods, their model using system identification techniques produced results indicating their model outperforms IAIF and QCP, however, at the cost of computational speed.

### 2.1 Proposed Glottal Model

This study proposes modelling the open and return phases of the glottal signal as the impulse response of two linear filters. The input impulse occurs at the GCI and the resulting filter outputs produce the open and return phases of the glottal signal. For practical purposes in processing the glottal signal the open phase will be reversed in time and treated as a causal, stable impulse response.

In the method proposed by Doval et al (2003), the differentiated glottal flow signal is modelled as the response of a linear filter. The model is referred to as the causal-anticausal linear model (CALM), as the glottal signal is modelled as having both causal and anticausal components. The return phase corresponds with the causal component and the open phase corresponds with the anticausal component. The method proposed in this study adopts a similar approach, by modelling the glottal signal as the output of linear filters. However, our approach treats the two phases as outputs of two independent linear filters as opposed to one a causal-anticausal linear filter model considered by CALM, and models those filters using SI methods.

The transfer functions requirements for the glottal modelling filters are determined by matching them to the LF model. The LF equation for the return phase is a decaying exponential which corresponds with the impulse response of a continuous time first order filter. The open phase, when time reversed, corresponds with a damped sinusoid or equivalently the impulse response of a continuous time stable second order filter. The corresponding transfer functions in the Z transform domain are given in equation 2 for the open phase transfer function, \( G_{op}(z) \), and equation 3 for the return phase transfer function, \( G_{rp}(z) \). The meeting point of the open and return phases represents the GCI, \( T_c \), with amplitude value of \( E_c \). The input impulse for each filter is set to an amplitude of 1. For the open phase the input impulse is applied at the sample corresponding with the GCI. For the closed phase the impulse is applied at the sample adjacent to the GCI within the closed phase.

\[
G_{op}(z) = \frac{b_1 + b_2z^{-1}}{a_1 + a_2z^{-1} + a_3z^{-2}} \tag{2}
\]

\[
G_{rp}(z) = \frac{b_1}{a_1 + a_2z^{-1}} \tag{3}
\]

This model establishes the framework for estimating the parameters of the glottal waveform as a system identification problem allowing us to bypass the problems posed by the issues encountered with standard glottal parameterisation algorithms. The input and output signals for open and closed phases are known and a method to estimate the system that can produce the corresponding response is required to estimate the glottal parameters.
2.2 Parameter Estimation

Numerous algorithms exist that could be used to solve the system identification problem to estimate the glottal parameters for the proposed models (Ljung, 1999). For this study Prony’s method (Hayes, 2009) and the Steiglitz McBride method (Steiglitz, McBride, 1965) where selected to estimate the parameters of the transfer function models of the open and return phases of the glottal signal.

Prony’s method was selected as it has a relatively low computational complexity only requiring the solution of a set of linear equations, to provide the parameters of a given model. A disadvantage of Prony’s method is that it is known to have poor performance when presented with a noisy output signal (Kumaresan et al, 1984).

The Steiglitz-McBride algorithm is an iterative technique of linear system identification. It works by minimising the mean-square error between the output of the system and the estimated model output and improving the estimate at each iteration. The first iteration of the Steiglitz-McBride algorithm requires a means to make an initial estimate of the model parameters to initialise the algorithm. This is often achieved by applying Prony’s method. The Steiglitz-McBride algorithm was selected for this study as it is known to be robust to noise in the output signal and can provide optimal estimates in the case of white noise in the output signal (Steiglitz, McBride, 1965 and Stoica, Soderstrom, 1981). This study employs Prony’s method to initialise the Steiglitz-McBride algorithm.

3 THE EXPERIMENT

The aim of this study is to test a new model of the glottal waveform that utilises SI algorithms to parametrise the glottal signal. Two SI algorithms are considered, the Prony method and the Steiglitz McBride algorithm, as described in section 2.2. The experiment is designed to (1) quantify the performance of the SI algorithm in terms of the accuracy of the glottal fit, (2) to determine their robustness to noise in the glottal estimate and (3) to identify the performance of the algorithms in real speech and identify differences in performance of each algorithm between healthy and pathological speech.

Tests are performed to fit the proposed glottal model to glottal waveform estimates using each of the two SI algorithms considered. These tests are performed on both synthetic glottal pulses and on glottal estimates from real speech, including pathological speech. To quantify the quality of the glottal fit to a glottal pulse the Normalised Root Mean Square Error (NRMSE) is employed. The NRMSE will be displayed in the form of a percentage in which an NRMSE of 100% represents a perfect fit of the model to the glottal estimate and 0% represents a performance level corresponding with that of a best line fit to the glottal waveform estimate. Testing is performed on both synthetic glottal signals and glottal estimates from real speech.

3.1 Synthetic Glottal Waveforms

The first part of this study tests the algorithms on synthetic glottal signals. Synthetic glottal signals allow the comparison between the glottal fit with the true glottal signal, unlike for real speech in which the true glottal signal is not known and only an estimate is available. Glottal signal estimates from real speech are likely to have unquantifiable sources of variation introduced by errors in the inverse filtering algorithm used to estimate the glottal signal. This typically introduces features into the glottal signal that are not accounted for by the glottal model and can impact the results. Using synthetic glottal signals bypasses these issues and allows the test set to cover a broad range of glottal parameters and noise levels in a controlled manner.

The tests with synthetic glottal signals consist of 3 parts:

- Test 1 - The first part consists of testing 100 synthetic glottal pulses with no noise over a range of voice types. This test determines the accuracy of the proposed model and accompanying SI algorithms across a range of voice types with no noise present.
- Test 2 - The second part of the test is similar to test 1, but with noise added. This test determines the accuracy of the proposed model and accompanying SI algorithms across a range of voice types when noise is present in the glottal signal.
- Test 3 - The third part of the test is to determine the accuracy of the fit as the noise level is varied. The parameters of the glottal pulse are held constant. This test indicates the robustness of the methods to noise in the glottal signal.

All synthetic glottal pulses were created using the LF model equations as given in equation (1). The parameters were varied to simulate the variations in real human speech.

For test 1 the 100 pulses are split into 2 groups of 50 pulses, representative of male and female speech.
Table 1: Artificial speech timing parameters.

<table>
<thead>
<tr>
<th>Voice type</th>
<th>Tp(%)</th>
<th>Te(%)</th>
<th>Ta(%)</th>
<th>Tc(%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Modal</td>
<td>41.0</td>
<td>55.0</td>
<td>0.9</td>
<td>58.0</td>
</tr>
<tr>
<td>Fry</td>
<td>48.0</td>
<td>59.0</td>
<td>2.7</td>
<td>72.0</td>
</tr>
<tr>
<td>Breathy</td>
<td>46.0</td>
<td>66.0</td>
<td>2.7</td>
<td>77.0</td>
</tr>
<tr>
<td>Falsetto</td>
<td>50.0</td>
<td>80.0</td>
<td>8.0</td>
<td>100.0</td>
</tr>
<tr>
<td>Harsh</td>
<td>25.0</td>
<td>30.0</td>
<td>1.0</td>
<td>50.0</td>
</tr>
</tbody>
</table>

The 50 pulses representing male speech contain 100 samples per pitch period, this corresponds with a pitch of 100 Hz and sampling frequency of 10000 Hz. The 50 pulses representing female speech contain 41 samples per pitch period, this corresponds with a pitch of 244 Hz and sampling frequency of 10000 Hz. Within each set of 50 pulses the glottal parameters are selected to have 10 pulses each of the voice types; modal, fry, breathy, falsetto and harsh. The timing parameters used to create these voice types are given in Table 1 (Ghosh, Narayanan, 2011). To create 10 samples of each voice type, the timing parameters were randomly varied in the range of 5% about the values in Table 1.

For test 2, the signal to noise ratio (SNR) of the glottal signals was set to 40 dB. This was achieved by adding white noise to each of the glottal pulses in the test set for test 1. The value of 40dB was chosen as it is the typical SNR value reported for modal speech (Ghosh, Narayanan, 2011). For test 3, 21 glottal pulses were generated with SNR levels varying between 0 and 100 dB, increasing in 5 dB increments. The glottal pulses each contained 100 samples per pitch period and had the timing parameters of modal speech. Only the SNR value varied between the 21 glottal pulses.

3.2 Real Speech

Tests on synthetic glottal signals provide insight on the effectiveness of the methods, but does not present as challenging a task as real speech. The real speech tests show how the method performs on samples with levels of signal complexity not represented in the synthetic glottal signals. It also indicates how the performance is impacted when the methods being tested are combined with non-ideal glottal estimation algorithms. The real speech tests consist of two parts, the first part investigates real healthy speech and the second part investigates real pathological speech. The real speech files have been accessed from the Speech Synthesis book by D.G. Childers (Childers, 1999). The study uses healthy and pathological speech samples from patients 20 to 80 years old consisting of /a/ and /i/ vowel utterances. The signals were sampled at 10 kHz and recorded using a Bruel & Kjaer microphone. The speech database assembled for this study is as follows:

- Healthy speech – 50 utterances of the vowel /a/, 25 male and 25 female.
- Pathological speech - 23 utterances of the vowel /i/, 8 male and 15 female.

The files were inverse filtered to extract the glottal flow derivatives using the IAIF method described in (Alku, 1991). The GCI locations were determined using the SEDREAMS algorithm reported in (Drugman, 2012). Using the GCI locations of the inverse filtered signals, each glottal estimate signal was divided into sections of individual pitch periods. The glottal model fitting algorithms were then applied to each pitch period. The NRMSE values were calculated between each glottal signal and its glottal model fit and the average NRMSE value for each speech file was recorded.

4 RESULTS AND DISCUSSION

The following section presents the test results in two subsections, first section documents the synthetic glottal signal results and the second presents the results from real speech tests.

4.1 Tests Using Synthetic Glottal Signals

The performance of the algorithms is compared by investigating the NRMSE values between the estimated fit and the original glottal signal. The results for synthetic glottal signals are presented in Table 2.

- Test 1 – For the 50 pulses simulating a 100 Hz male speech, the NRMSE values for Steiglitz-McBride and Prony methods are 97.99% and 97.93% respectively. Tests on the set of 50 pulses created to simulate a 240 Hz speech signal sampled at 10000 Hz produced the following results: The mean NRMSE value for the Prony algorithm was 98.24% and 98.86% for the Steiglitz-McBride method. These result shows that the performance of the two methods was approximately equal for these tests.
- Test 2 – The NRMSE values for the Prony and Steiglitz-McBride algorithms tested on the 50 pulses with added noise for male samples are 29.20% and 96.23% respectively. For female samples, the results are 55.66 % and 96.55% for Prony and Steiglitz-
A notable drop in performance occurs in the results for the Prony method when noise is introduced, consistent with reports that the Prony algorithm does not perform well in noisy environments (Kumaresan et al., 1984). The Steiglitz McBride results are comparable with the results recorded when no noise was present in the glottal signal.

- **Test 3** – The results of this test are illustrated in Figure 2. The NRMSE values are plotted against the corresponding SNR values. This indicates the decline in performance as noise levels increase for each algorithm. It can be noted from Figure 2 that between SNR of 100 and 70 dB, both algorithms perform similarly. As the noise level increases, the performance of the Prony method begins to deteriorate noticeably more than the performance of the Steiglitz-McBride algorithm. Taking the 90% NRMSE value as a reference point, it can be seen that the performance of the Prony method drops below this level at SNR at approximately 60 dB while the Steiglitz-McBride algorithm provides a 90%+ fit to approximately 30 dB SNR level. This indicates that the Steiglitz-McBride method performs more robustly than the Prony method for noisy glottal signals.

A statistical analysis test was carried out to verify whether the results provide any statistical significance. The results of Steiglitz-McBride and Prony algorithms were compared using the student t-test. The null hypothesis states that the samples from the two datasets have the same mean at the 5% significance level. In all cases, the null hypothesis is rejected indicating the difference in the means is statistically significant.

### 4.2 Tests Using Real Speech

The second part of the study consisted of performing tests on real speech, including both healthy and pathological speech. The results are presented in Table 3. For healthy speech the mean NRMSE value for the Prony method was 29.23% and for the Steiglitz-McBride method was 64.29%. For the pathological speech results, the Prony methods mean NRMSE value was 25.66% while the mean NRMSE value of the Steiglitz-McBride method is 51.57%.

The Steiglitz-McBride method demonstrated better accuracy at fitting the glottal model to the estimated glottal waveform for both healthy and pathological speech. The results for real speech are notably lower than those reported for synthetic glottal signals.

To verify the statistical significance of the results for real speech, we again used the student t-test, with the same null hypothesis and levels of significance. For both, healthy and pathological results, the test rejected the null hypothesis indicating the difference in the means is statistically significant, when comparing Steiglitz-McBride and Prony algorithms.

### 4.3 Sample Fits

This section presents sample fits of the glottal model to the inverse filtered estimate for both healthy and pathological speech using the Steiglitz-McBride algorithm. The example glottal fit in Figure 3 is for a healthy glottal pulse and has a match of 75.57%. The fit in Figure 4 illustrates the Steiglitz-McBride method applied to the glottal waveform of a pathological speech sample and has an NRMSE of 54.17%.

![Figure 2: Graph comparing NRMSE values with their respective SNR values for Prony and Steiglitz-McBride methods.](image)
Many factors can influence the quality of the glottal fit and the NRMSE value, including the complexity of the signal, the presence of noise in the glottal signal, the number of samples available for parameter estimation in each pitch period and the accuracy of the GCI locations. The presence of noise in the glottal signal causes the NRMSE values to decrease, even when a good fit is achieved. The fit in Figure 3 is a representative example of this.

Pathological speech typically contains more aspiration noise than healthy speech and may have features not modelled by existing glottal models. The accuracy of the glottal fitting depends on the accuracy of the glottal estimation algorithms. If the inverse filtering method is not accurate, it can lead to artefacts in the glottal estimate. All these factors can affect the performance of the model fitting algorithms and in turn the accuracy of the fit. This is notably evident in Figure 4, in which the glottal pulse contains features that cannot be captured by the model, which is reflected in the NRMSE value.

5 CONCLUSION

Accurate glottal model parametrisation for real speech proves to be challenging problem, most notably for pathological speech. The purpose of this study was to investigate if this challenge can be overcome by using a different approach.

The results of this study show that it is possible to reliably fit and parametrise the glottal model of the speech signal using system identification algorithms applied through the newly proposed approach. The method created accurate fits for artificial speech samples and fit the glottal models with the average accuracy of 64.29% for healthy and 51.57% for pathological speech using the Steiglitz-McBride method. The method demonstrates the effectiveness of the proposed approach for a wide range of voice qualities and different levels of noise in the glottal signal.

The study also found that out of the two methods used, the Steiglitz-McBride algorithm performs the operation more robustly in both, synthetic and real speech. The synthetic speech test results for samples without additive noise show that both algorithms have similar performance, however, results from samples containing noise show superior performance of the Steiglitz-McBride method. The Prony method was found to perform poorly in noisy environments. Results from real speech tests show that the Steiglitz-McBride method outperforms the Prony method in all cases.

This study shows promising results of the proposed approach and indicate that it could be an effective tool in estimating glottal models for healthy speech and for the more challenging case of pathological speech. Further research is required to more comprehensively evaluate the method, on larger real speech datasets and with a broader range of performance metrics, to identify the strengths and weaknesses of the method and compare it with existing glottal model fitting methods.

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