

Actual Impact of GAN Augmentation on CNN Classification Performance

Thomas Pinetz, Johannes Ruisz and Daniel Soukup

Center for Vision, Automation & Control, AIT Austrian Institute of Technology GmbH, Giefinggasse 4, 1210 Vienna, Austria

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Abstract: In industrial inspection settings, it is common that data is either hard or expensive to acquire. Generative modeling offers a way to reduce those costs by filling out scarce training data sets automatically. Generative Adversarial Networks (GANs) have shown incredible results in the field of artificial image data generation, but until recently were not ready for industrial applications, because of unclear performance metrics and instabilities. However, with the introduction of Wasserstein GAN, which comprises an interpretable loss metric and general stability, it is promising to try using those algorithms for industrial classification tasks. Therefore, we present a case study on a single digit image classification task of banknote serial numbers, where we simulate use cases with missing data. For those selected situations, different data generation algorithms were implemented incorporating GANs in various ways to augment scarce training data sets. As a measure of plausibility of those artificially generated data, we used the classification performance of a CNN trained on them. We analyzed the gains in classification accuracy when augmenting the training samples with GAN images and compare them to results with either more classically generated, rendered artificial data and near perfect training data situations, respectively.

1 INTRODUCTION

Sufficient amounts of relevant training data for real world machine learning tasks are hard to obtain. Especially, edge classes, such as certain error classes, are often underrepresented. Machine learning algorithms tend to have problems with correctly classifying unbalanced datasets (More, 2016). In order to overcome such deficiencies, usually training data are augmented with plausible, artificially generated example images to enrich the amount of variation in the training data sets. This has advantageous regularizing effects on the training procedure, e.g. mitigate overfitting. Although, there are a number of methods to fight overfitting within the deep learning model (Srivastava et al., 2014), carefully fostering ones training data should not be underestimated as a primary requirement. Particularly in real world applications, one wants to be sure that predictions are made on the basis of as adequate as possible training data.

In the past, this was often accomplished by simply including randomly slightly shifted and/or rotated versions of available training examples, which already provides a significant amount of classification accuracy (He et al., 2016). For certain types of data,

it is also possible to generate yet more variations of artificial training data by means of 3D or text rendering algorithms. However, a solution to such problems is offered by generative modeling. In generative modeling, approximations of the actually underlying probability distributions of the available real data sets are learned, which are used to generate realistically looking new samples to fill out an underrepresented data class (Goodfellow et al., 2014). Generative Adversarial Networks (GANs) currently form the state-of-the-art in generative modeling (Karras et al., 2017) and have been applied with state-of-the-art results in domains such as data generation (Arjovsky et al., 2017), few shot learning (Antoniou et al., 2017), and data refinement (Pinetz et al.,).

GANs consist of two Neural Networks (NN), which are trained adversarial. The first network (*generator*) learns to construct artificial images to fool the second network (*critic*), while the critic tries to distinguish artificially generated from real data. Since the original inception of GANs by Goodfellow et al. (Goodfellow et al., 2014), GANs have been notorious for being unstable and dependent on the weight initialization of the networks (Salimans et al., 2016). Substantial amounts of research have gone into mak-

ing GANs more stable (Arjovsky and Bottou, 2017; Arjovsky et al., 2017; Salimans et al., 2016; Gulrajani et al., 2017; Yadav et al., 2017), produce higher resolution or better quality images (Karras et al., 2017), or to better model the actual variations inherent in the real data (Antoniou et al., 2017; Pinetz et al.,). GAN algorithms learn to smartly interpolate/extrapolate in high dimensional spaces (Karras et al., 2017). Therefore, if only a subset of the clusters of a real data sample is available, even a GAN algorithm will not magically generate vastly different plausible data clusters or completely missing classes of data.

An open research field is the quality evaluation of GAN generated data, as it is still unclear which metric to use (Theis et al., 2015). One metric in use is the inception score, which has been shown to correlate well with human perception (Salimans et al., 2016). However, the inception score has also been shown to be misleading (Barratt and Sharma, 2018). For Wasserstein GANs, the estimated Wasserstein Distance is used as a quality metric. While there were attempts to compare various GAN algorithms, the results were inconclusive and showed, that GANs are strongly dependent on their hyper parameters and random seeds (Lucic et al., 2017).

This work aims to investigate possible advantages of data augmentation with GAN algorithms over a classical augmentation approach such as digit rendering, both w.r.t. perfect training data situations. Therefore, a relatively simple industrial task is considered, namely 10-class single digit image classification of banknote serial numbers, where nearly 100% classification accuracy can be achieved given enough training data (Fig. 1 column a.). The simplicity of the selected task itself and the knowledge that it is virtually perfectly solvable allows to isolate the actual influences of augmentation strategies. The availability of sufficient data enables the simulation of situations with different amounts of available training data from none up to a quasi perfect training set. Certain use cases are simulated, such that only $\{0, 1, 10, 20, 50, 100, 200\}$ example images of one selected underrepresented digit class existed. Classical and GAN data augmentation strategies are used to compensate those lacks of data and classification CNNs were trained for all simulated training set scenarios. The quality of augmented training samples was compared and evaluated by means of testing those CNNs on a shared test set of real BN number digits.

In this context our contributions are as follows:

- A showcase on how reliable GAN augmentation in fact works for an actual realistic classification task.

- In terms of applicability of augmentation algorithms for image classification:
 - Confrontation of image rendering algorithm with GAN augmentation.
 - Comparison of different GAN augmentation strategies.

The remaining paper is organized as follows. In Section 2, the augmentation algorithms - classical rendering and GAN - are explained in detail. Section 3 contains descriptions of used data, experiment scenarios, and a presentation of results. Finally, a summary and conclusions are presented in Section 4.

2 DESCRIPTION OF DATA GENERATION ALGORITHMS

2.1 Digit Image Generation by Text Rendering

The chosen use case of banknote serial number single digit image classification offers the possibility of rendering additional digit image data with a text renderer in order to compensate for a lack of training data. We used Matlab's text renderer (MATLAB, 2016). The rendering script generated a huge number of simulated sample images for each digit class, whereas the corresponding fonts were randomly drawn from all fonts that were installed on the computer. Fonts used on banknotes are special, such that the rendered fonts do not exactly correspond to them. The large variation of fonts in the rendering procedure on the other hand should avoid that the classification CNN focuses too much on special font features.

The images were rendered on higher resolution and down-sampled to the target resolution of 24×16 by interpolation, according to the resolution of the real banknote serial number digit images. Font color was black, background white. Banknotes in general contain patterns of high frequency and high contrast drawings. Those also appear in the backgrounds of serial numbers, which might cause the classification CNN to cling to them, especially when only a small sample of real images is at hand. Thus, we blended a random salt-and-pepper noise pattern multiplicatively onto the synthetic images, which made the background of simulated data noisy instead of plain white. This measure added another regularizing effect, which obviates that the classification CNN gets distracted by background features rather than analyzing pure digit strokes.

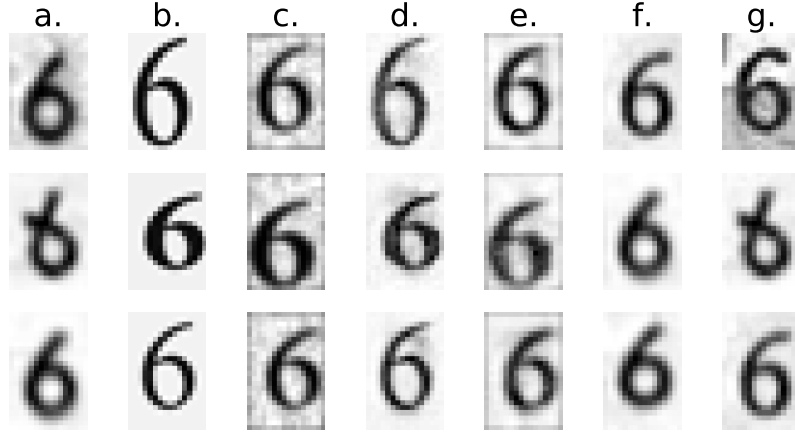


Figure 1: Example images for digit class '6' used for training the classification CNNs (3 examples per type): original real banknote serial number digits (a.), Rendered blank (b.), Rendered noise (c.), RGAN blank (d.), RGAN noise (e.), DGAN (f.), and DAGAN (g.).

For experiments (see Section 3), we randomly sampled images from those synthetically generated data in order to fill out small real data samples.

2.2 Data Augmentation using GAN Methods

Generative Adversarial Networks (GANs) (Goodfellow et al., 2014) are the prevalent way to generate new data points of a sample based dataset (Lucic et al., 2017). The objective of GANs is to learn a probability distribution \mathbb{P}_r . This is done by approximating said distribution with a parametric distribution referred to as \mathbb{P}_θ . Samples from \mathbb{P}_θ are used to augment an existing dataset with artificially generated yet plausible new examples, and use those for training to improve classification performance.

The GAN principle relies on two neural networks (NN). The first NN, named *generator*, transforms a noise distribution in a latent space, e.g. Gaussian ($z \sim \mathcal{N}(\mathbf{0}, \mathbb{I})$), into examples from a parametric distribution ($g_\theta(z) \sim \mathbb{P}_\theta$). The second NN, denoted as *critic* (Arjovsky et al., 2017) is used to distinguish generated data from real data. Using the classical log-loss for the critic yields following saddle point problem:

$$\min_{\theta} \max_D L(\theta, D) = \mathbb{E}_{x \sim \mathbb{P}_r} [\log(D(x))] + \mathbb{E}_{z \sim \mathcal{N}(\mathbf{0}, \mathbb{I})} [\log(1 - D(g_\theta(z)))] \quad (1)$$

It is well known, that optimizing Eq. (1) minimizes the Jensen-Shannon Divergence between \mathbb{P}_r and \mathbb{P}_θ (Goodfellow et al., 2014). The solution to

such a problem is called a Nash equilibrium, where the generator produces data, which follows the same distribution as the real data, i.e. $\mathbb{P}_\theta = \mathbb{P}_r$. The common procedure to achieve those saddle point solutions is to alternately perform gradient ascent for the critic parameters and gradient descent for the generator parameters (Yadav et al., 2017). Eventually, trained generator NNs produce artificial new training images, which are used to augment scarce real training samples in an actual deep learning task.

However, two distributions on low dimensional manifolds in high dimensional spaces are unlikely to comprise large enough overlap for the Jensen-Shannon Divergence to be defined (Arjovsky and Bottou, 2017). Using noise on the real data to smooth out the distributions (Arjovsky and Bottou, 2017) resulted in blurry generated images. A better solution is to change the distance metric between the distributions, namely using the *Wasserstein distance* (Arjovsky et al., 2017), which yields following GAN formulation:

$$L = \min_{\theta} \max_{Lip(f) \leq 1} \mathbb{E}_{x \sim \mathbb{P}_r} [f(x)] - \mathbb{E}_{z \sim \mathcal{N}(\mathbf{0}, \mathbb{I})} [f(g_\theta(z))]. \quad (2)$$

Wasserstein distance is well defined even if there is no overlap between two distributions. Moreover, using this GAN formulation produces an interpretable critic output, which alleviates balancing the Wasserstein loss term with additional regularizing loss terms (Antoniou et al., 2017). Such might be a required regularizer penalizing deviations from the Lipschitz constraint ($Lip(f) \leq 1$). A number of them have been proposed (Arjovsky et al., 2017; Gulrajani et al., 2017; Wei et al., 2018). Due to consistent good performance in comparison experiments, we chose *Gradient Penalty* (Gulrajani et al., 2017). Therefore, loss

functions for generator and critic are modified as follows:

$$L_g(\theta_g) = -\mathbb{E}_{z \sim p_{noise}} [f(g_{\theta_g}(z))] \quad (3)$$

$$L_d(\theta_c) = \mathbb{E}_{x \sim p_{data}} [f_{\theta_c}(x)] - \mathbb{E}_{z \sim p_{noise}} [f_{\theta_c}(g(z))] + \mathbb{E}_{\bar{x} \sim p_{\bar{x}}} \lambda \|\nabla_{\bar{x}} f_{\theta_c}(\bar{x}) - 1\|^2, \quad (4)$$

where $p_{\bar{x}}$ is defined as a linearly interpolated distribution between the generated distribution and the real distribution. In all of our experiments, we set $\lambda = 10$, which was reported to perform well across various datasets and architectures (Gulrajani et al., 2017).

There are multiple ways the GAN principle can be utilized for data augmentation based on real data at hand. We investigated following methods:

- **DGAN** Direct GAN: Generating plausibly looking, artificial images for an underrepresented object class based on a few given real examples of that class.
- **RGAN** Refinement GAN (Pinetz et al.,): On the basis of rendered simulated images and real images (not necessarily of the underrepresented class) learn to transform the rendered images to look more realistically in terms of image appearance rather than object structure, e.g. digit strokes.
- **DAGAN** Data Augmentation GAN (Antoniou et al., 2017): A realistic object distortion function is learned from real images that mimics inherent real distortions within real image distributions.

In all those GAN methods, the critic function is modeled as a CNN, whereas they all utilize the same CNN architecture, which is inspired by DCGAN (Radford et al., 2015). We use 3 strided convolution layers with 3×3 filter kernels and $\{32, 64, 128\}$ feature maps, followed by leaky ReLU activation. A fully connected layer with 1 output unit yields the distribution distance measure. Gradient penalty was added to the critic loss during GAN training. All weights were initialized with Glorot's initialization scheme (Glorot and Bengio, 2010).

2.2.1 DGAN

In DGAN, only the actual available real images of an underrepresented image class are used. In our simulation experiments (Section 3), we decided to use digit class '6' to play that role. Based on those images, during the GAN training procedure, the generator eventually learns to generate artificial images mimicking the corresponding appearances of those real examples of the according class without simply reproducing them exactly.

The generator is modeled as a NN, whose architecture is a DCGAN variant visualized in Fig. 2. 5×5 convolution kernels were implemented together with ReLU activations. In the training procedure, the proposed hyper parameter setting by Gulrajani et al (Gulrajani et al., 2017) was used.

2.2.2 RGAN

Unlike DGAN, RGAN not only requires real examples, but also synthetically generated data, e.g. by a renderer. In RGAN, instead of learning to generate plausibly looking images from an underlying real image distribution \mathbb{P}_r , a refinement function is learned, which transforms synthetic images into more realistically looking versions. In order that it mimics the typical statistics of the image acquisition systems of real images without changing the depicted object structures. While one requires synthetic data to perform the task, one is not restricted to a scarce sample of an underrepresented object class during GAN training. Those image appearance statistics can also be learned from the other classes. Incorporating RGAN refined images into training sets in different learning tasks like fingerprint minutia detection or gaze estimation showed notable performance improvements (Pinetz et al., ; Shrivastava et al., 2016), respectively.

In order to ensure that the actual object structures in the synthetic input images are preserved by the generator NN, an additional regularization term in the generator loss L_g is required, penalizing excessive structural deviations of the output w.r.t. the input images:

$$L_g = \mathbb{E}_{z \sim p_{synthetic}} [(f(g_{\theta}(z))) + \omega \|g_{\theta}(z) - z\|^2] \quad (5)$$

During training RGANs, the balance of loss terms by the regularization parameter ω is critical in order to achieve good results (Salimans et al., 2016). As an RGAN generator produces images from other (synthetic) images rather than from random vectors in some latent space, a U-shaped CNN architecture is utilized to model the corresponding generator NN (Ronneberger et al., 2015). Similarly to an auto-encoder NN, a U-shaped CNN has a coder and decoder part, connected by a bottleneck layer (see Fig. 3). The generator's input consists only of an image and no additional noise component, why the RGAN generator is fully deterministic. Consequently, each input image results in one and only one refined output image.

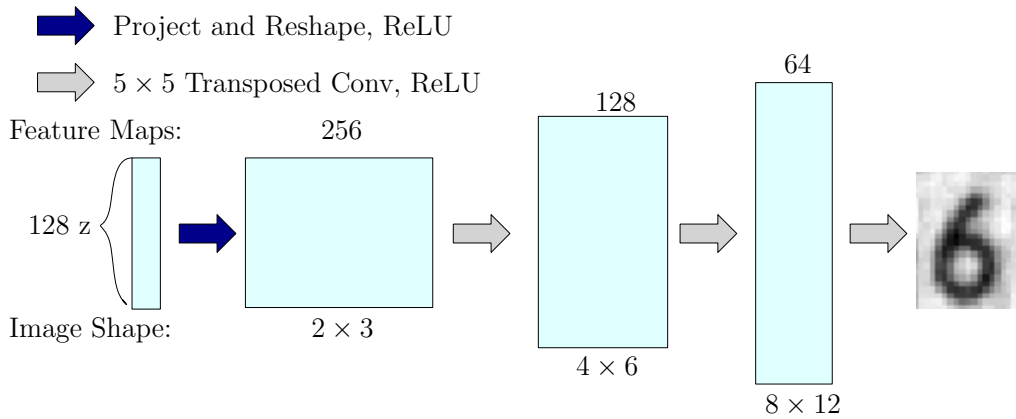


Figure 2: Generator used for the DGAN approach, inspired by the DCGAN architecture.

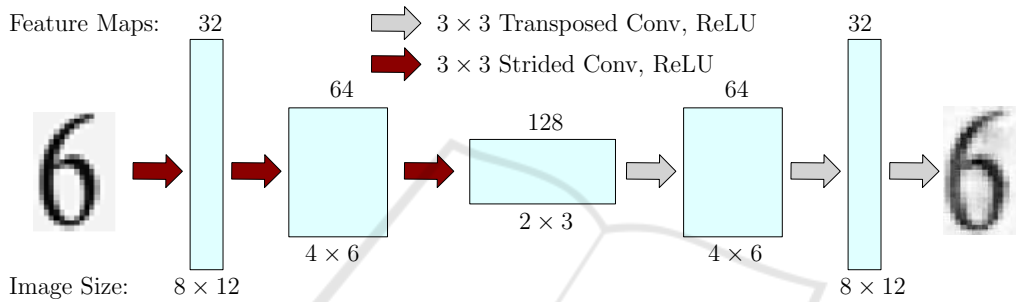


Figure 3: Generator used for the RGAN approach, inspired by the U-Shaped NN architecture (Ronneberger et al., 2015).

2.2.3 DAGAN

The aim of this GAN variation is to learn realistic distribution manifolds of the real object classes along which plausible inner-class distortions take place, i.e. learn to realistically distort given real images rather locally. The generator NN is trained to construct randomly slightly and - w.r.t. the real image sample - consistently distorted versions of real input images. Randomness is introduced by adding a random vector in the latent space (NN bottleneck layer) of the U-shaped generator NN (Fig. 4). Concurrently, the critic NN learns to distinguish pairs of real/real images from pairs of real/generated images. The DAGAN training procedure is considered converged as soon as the critic is unable to discern that generated images are involved in those image pairs.

Similarly to the RGAN method, the generator in DAGAN is trained to modify input images in such a way that the output images comprise appearances consistent with the real training data set. While in RGAN the aim is to induce statistics of the real image acquisition systems to synthetic images, in DAGAN, the generator learns distortion models of real object classes in order to increase variation of the available real data sample appropriately. Moreover, the DAGAN method comprises a random component enab-

ing the generation of arbitrarily many variations of each input image. DAGAN can be trained on basis of images of all object classes, so that one is not restricted only to real examples of the certain underrepresented object class.

DAGAN only makes sense though, if the images across different classes share similar distortion models (Antoniou et al., 2017). That assumption is commonly accepted for fine-grained classification tasks such as the one covered in this work.

The generator NN's architecture is similar to RGAN's, except for an additional injection of the already mentioned random noise vector, which is concatenated to the latent representation in the bottleneck layer (Fig. 4). The input to the critic NN is a pair of input images:

- an original real image AND the generator's output w.r.t. to that real image, OR
- an original real image AND another real image of the same object class.

The critic measures deviations between distributions of real/generated image pairs and real/real image pairs. This is similar to comparing different distributions of images, only that pairs of images are considered as twice as high dimensional images, e.g. stacked along the color dimension.

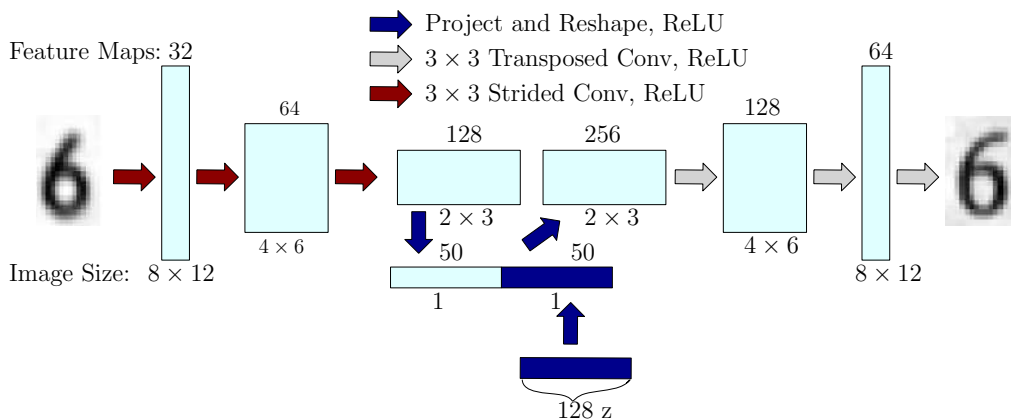


Figure 4: Generator used for the DAGAN approach, inspired by the U-Shaped NN architecture (Ronneberger et al., 2015). Notice the additional noise component added to the latent representation.

3 EXPERIMENTS

We chose a simple 10-class classification problem of printed digits '0' to '9' for our experiments. Those digit images were extracted from serial numbers of banknote images with different background patterns, fonts, and sizes. NN achieve near perfect performance on this task, given enough training data. Therefore this task allows to investigate the influences of various situations of insufficient training data and according methods to overcome them.

Digit class '6' was selected to play the role of an underrepresented class, i.e. a class with too little available training images to varying degrees, from none to sufficiently many. To each of those situations, the augmentation methods mentioned in Section 2 were applied to compensate the simulated missing data situations for digit class '6'. The other classes were represented with sufficient training images in all setups, i.e. 300 digit images for each class '0', '1', '2', '3', '4', '5', '7', '8', and '9'.

In order to solve the classification task, we trained CNNs with six convolution layers, where three layers were configured with stride 2 for pooling. The output is a one-hot encoded layer of 10 values with a softmax applied to it. The network architecture was held constant for all conducted experiments.

The outcome of those experiments shall show if there is a preferred method of data generation for the particular problem, in order to compensate lacks of training data.

3.1 Missing Data Scenarios and Corresponding Data Augmentation

For all classes except for digit class '6', we used the same training data for each run, i.e. 300 example im-

ages per class consisting of 24×16 gray scale images depicting banknote serial number digits. A lack of training data for digit class '6' was simulated by only using 0, 1, 10, 20, 30, 40, 50, 100, 200 original digit '6' images. In each of those 10 settings, we added artificially generated class-6 data by means of the data generation algorithms described in Section 2, such that we always filled up the data lack and obtained 300 training images for class '6' as well.

On each of those data configurations, a digit classification CNN was trained and its according performance was measured on a shared test set of 350 original digit '6' images that were never used for training.

Naturally, for each setting, we additionally trained the CNN without using artificially generated images for augmentation. Those performances were taken as references from which to improve by augmentation. In the worst case, where no images of digit '6' were contained in the training set, neither original nor artificial, digit '6' test images were never classified correctly by a fully trained CNN.

3.1.1 Rendered Images

As described above, we utilized Matlab's text renderer (MATLAB, 2016) to generate synthetic digit images comprising various fonts and variations (see Fig. 1). We generated two versions of that data set:

- *Rendered blank*: digit image set with blank white image background.
- *Rendered noise*: digit image set with a blended random noise pattern in the image background.

As we argued earlier that the noise pattern might be advantageous due to a regularizing effect, conducting experiments on both versions allows to evaluate that argumentation.

3.1.2 Direct GAN (DGAN)

For DGAN training, only those images of class '6' considered to be at our disposal in each setting were used. Since DGANs learn the underlying data distribution of given data, that procedure only makes sense for more than 1 original image example, so that DGANs were only applied to those situations supposing 10, 20, 30, 40, 50, 100, 200, 300 available real examples.

3.1.3 Refinement GAN (RGAN)

The RGAN critic was trained with all the available original data, i.e. real examples from all classes were used, plus those few class-6 images considered to be at our disposal in each setting. The input to the RGAN generator consists of rendered synthetic digit images, for which we utilized the already rendered data sets. Due to the usage of synthetic data, the RGAN algorithm is also suited for test cases, where not a single real image was used for training. Based on the used two rendered datasets, RGANs also yielded two different augmentation data sets (see Fig. 1 columns d. and e.):

- *RGAN blank*: Refinement of rendered images with blank background.
- *RGAN noise*: Refinement of rendered images with random noise background.

3.1.4 Data Augmentation GAN (DAGAN)

In DAGAN, images of all digit classes are used to train the DAGAN augmentation generator. However, the classes have to be carefully balanced, so that for DAGAN, only as many images per class can be used as are available for the considered underrepresented digit class '6'.

From the real example images of digit '6' and random vectors from the latent space, the fully trained generator eventually generated the necessary amount of random augmentation image variations of class '6', such that the scarce training sets could be augmented appropriately (see Fig. 1 columns g.).

3.2 Results

Fig. 5 shows the performance plots of 10-fold cross-validated classification accuracies for each setting (0, 1, 10, 20, 30, 40, 50, 100, 200, and 300 original digit '6' images in training set) and the corresponding *Rendered blank*, *Rendered noise*, *RGAN blank*, *RGAN noise*, *DGAN*, and *DAGAN* generated training sets. Naturally, for DGAN and DAGAN only settings with

more than 1 real digit '6' image were considered. For each setting and algorithm, the corresponding classification CNN was trained with 10-fold cross-validation and the classification accuracies on a shared test set of 350 original class '6' images were averaged. Note, that we only present test performances for class '6' due to presentational reasons.

The following observations are apparent from the performance plots:

- More original data improves classification in general.
- If there are quasi no training images of digit class '6' at hand, augmentation with rendered data make training possible, whereas RGAN based on those data already yields really good classification results (Fig. 5 left).
- The introduced noise pattern in the background of rendered images ensures better performance, which also elevates performance of RGAN based on those images.
- RGAN improves quality of rendered images w.r.t. to achievable classification accuracies in both cases, blank and noisy image background, respectively. That is an indicator that RGAN drags the rendered image distributions more towards the underrepresented real image distributions.
- DGAN augmentation, which is the classical setup in terms of GAN strategies, improves classification, but lies behind performances with rendered images with noisy background and significantly behind RGAN based on those (Fig. 5 right).
- DAGAN augmentations contribute to classification improvements, but not in a consistent manner, which makes it difficult to make reliable predictions of their impact (Fig. 5 right).

4 CONCLUSION

The goal of the work was to investigate the actual impact of image augmentation strategies on the CNN classification performance in a real industrial scenario. We utilized a relatively simple 10-class classification problem of digit images extracted from banknote serial numbers. While the task is quasi perfectly solvable with the sufficient image sample at hand, it allowed to simulate various scenarios of too little training images for one certain digit class that we considered to be underrepresented to varying degrees.

We augmented the supposedly underrepresented training sample by means of different methods, classical digit rendering and various GAN oriented proce-

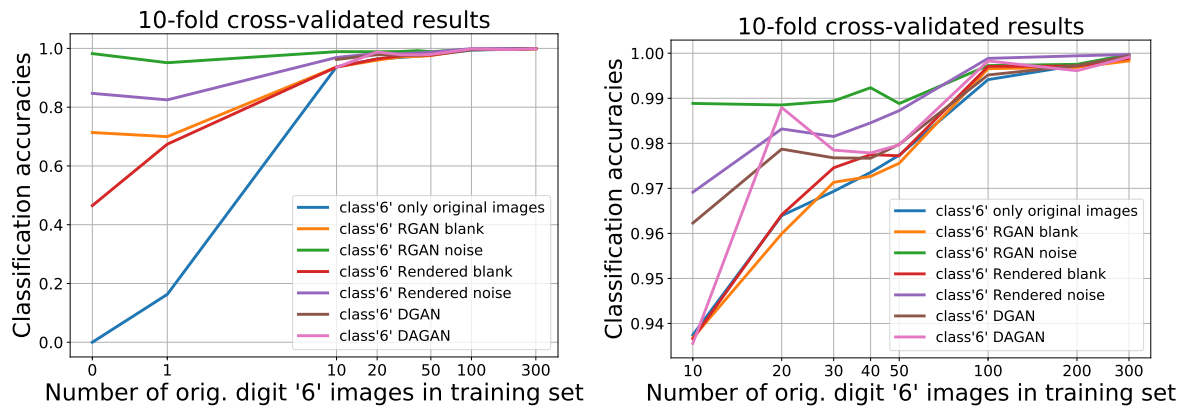


Figure 5: Left: 10-fold cross-validated CNN classification results for digit class '6' based on different original training data sample sizes for digit '6' and augmented with various data generation strategies. Right: Zoom into left plot for class '6's training data sample sizes 10 to 300 and corresponding classification accuracies ≥ 0.9 . Note the scale of y-axes.

dures, respectively. The analysis of classification performance of each scenario was carried out on a shared real test sample of digit images. Results showed that classical digit rendering contributes a lot to improvements already for very scarce training samples. However, GAN refined versions of those data yet still elevated performances significantly. Moreover, it pays off investing into the rendering model, e.g. by background modeling. GAN augmentation strategies based only on available real training images do have a positive impact on classification, but to a much lesser extent and not necessarily reliably.

Finally, our results revealed the simple truth that the more possibly realistic information is put into an augmentation strategy the better will be the final classification outcome. While GANs are often reported of yielding astonishing results, their performances are only as good as the underlying data they operate on. However, combined with image rendering, they clearly showed the capability of overcoming significant missing training data scenarios.

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