Design and Control of an Autonomous Photovoltaic System with Battery Charge Regulator using the MPPT Control Followed by PI Correctors

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Abstract: An autonomous photovoltaic (PV) system requires a battery charger to store energy for consumption during the night and during days with low irradiation. This paper presents the design of the PV charger system modulator and controller implemented with the asymmetric primary inductance converter (SEPIC). The designed SEPIC is controlled by the MPPT (Pando) command to extract the maximum power of the PV generator. To the used MPPT control, a PI control regulator has been added to manage the charge loop of the battery. Subsequently, a BOOST converter has been associated with the system to adapt the output voltage of the battery to the load. The modeling of the state space is done to determine the transfer function of the converters (SEPIC and BOOST). The values of the PI correctors (Kp and Ki) are obtained using the method of Ziegler Nichols. Finally, we simulated and analyzed the performance of a 250W stand-alone photovoltaic power system on MATLAB- Simulink.

1 INTRODUCTION

With the depletion of fossil fuel reserves, economic crises due to soaring oil prices, accidents at nuclear power plants such as Three Mile Island (USA, 1979) and Chernobyl (USSR, 1986), as well as Fukushima (Japan 2011), public interest in renewable energies continues to grow. Of the various sources of renewable energy, photovoltaic occupies a prominent place (S. Gueye, 2014). In stand-alone photovoltaic systems, batteries are widely used to power loads in the absence of sunshine or in the event of a failure of the solar energy system. These batteries are sensitive to overload, deep discharge and temperature current drift. It is then necessary to associate them with a regulator to ensure their protection. The importance of a charge controller in an autonomous photovoltaic system is obvious. However, it must be well designed to meet the requirements of cost, simplicity, and reliability (S. Gueye, 2014) (S. J. Chiang, 2009).

The objective of this work is the study of an autonomous photovoltaic system with a battery charger for energy storage, controlled by an MPPT command with two PI correctors, one intended for the control of the state of charge battery discharge and the other to adapt the output voltage of the battery to the load. The article is structured as follows: we start with the presentation of the operation of the autonomous photovoltaic system, then the modeling of the state space of the converters (SEPIC and BOOST), after the method of Ziegler and Nichols is presented to determine the values of PI correctors, later we present the system control algorithm and finally the results and the discussion.
2 AUTONOMOUS PHOTOVOLTAIC SYSTEM

An autonomous photovoltaic system is one that produces electricity through the sun, but operates independently of the electricity grid. In the majority of cases, this system is used in isolated sites where it would be much too expensive to connect the house or the room that you want to supply with electricity. The major difference with a standard photovoltaic installation (connected to the grid) is the presence of batteries. An autonomous photovoltaic system must be able to provide energy, even when there is no more sun (at night or in bad weather). It is therefore necessary that a part of the daily production of the photovoltaic modules is stored. Below is the synoptic diagram of our autonomous photovoltaic system that consists of a GPV with a SEPIC type converter to charge the battery and a BOOST converter to power our load (S. J. Chiang, 2009)(D. S. Karanjkar, S. Chatterji, S. L. Shimi, and A. Kumar, 2014).

The PV module directly converts sunlight into direct current. Here, the chosen PV module is of American Solar Wholesale type ASW-250P of following characteristics:

<table>
<thead>
<tr>
<th>Characteristic</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Maximum power(W)</td>
<td>249.92</td>
</tr>
<tr>
<td>Open circuit volatgeVoc(V)</td>
<td>43.22</td>
</tr>
<tr>
<td>Short-circuitcurantls (A)</td>
<td>7.76</td>
</tr>
<tr>
<td>Voltage at maximum power point Vmp(V)</td>
<td>35.2</td>
</tr>
<tr>
<td>Current at maximum power point Imp(A)</td>
<td>7.1</td>
</tr>
<tr>
<td>Shunt resistance Rsh(ohms)</td>
<td>111.87</td>
</tr>
<tr>
<td>Series resistance Rsh(ohms)</td>
<td>0.42</td>
</tr>
</tbody>
</table>

Figure 1: Synoptic diagram of the photovoltaic system

Figure 2: Ppv=f(Vpv) for influence of temperature

Figure 3: Ppv=f(Vpv) for influence of temperature

Figure 4: Ppv=f(Vpv) for influence of Illumination

Figure 5: Ppv=f(Vpv) for influence of Illumination

3 MODELING THE CONVERTER

3.1 SEPIC Converter

A SEPIC is a type of DC-DC converter allowing the electrical potential (voltage) at its output to be lower, greater or equal to that at its input.
The use of the SEPIC converter (which can play the role of a boost converter if $\alpha > 0.5$ or step down if $\alpha < 0.5$) is explained by the fact that the voltage delivered by the panel is greater than the voltage of the battery which is 24 V and has the advantage of having a non-inverted output (S. J. Chiang, 2009).

Figure 6: Circuit diagram of the SEPIC converter

For a SEPIC converter operating in continuous conduction mode (CCM), the duty cycle is given by (B. Paranthagan, 2015):

$$\alpha = \frac{V_s + V_d}{V_s + VPV + V_d} \text{ with } 0 < \alpha < 1 \quad (1)$$

The PI regulator is used to monitor the state of charge-discharge of the battery and to size these parameters Ziegler and Nichols have proposed a method that requires the recording of the index response in open loop, just record the answer index of the process alone (i.e. without the regulator), then draw the tangent to the point of inflection of the curve. To do this the determination of the transfer function of the converter is mandatory.

The state space model (Chun T. Rim, Gyu B. Joung, and Gyu H. Cho, 1991) is used to determine this function. For our study we apply the values of Table 2 obtained after sizing of our converter or I determine the constants of the model (6).

So if the transistor is in ON state:

$$\begin{bmatrix}
\frac{dl_{L1}}{dt}
\frac{dl_{L2}}{dt}
\frac{dv_{CS}}{dt}
\frac{dv_{OUT}}{dt}
\end{bmatrix} =
\begin{bmatrix}
0 & 0 & 1 & 0
0 & 0 & 0 & 1
0 & -\frac{1}{C_{s}} & 0 & 0
0 & 0 & 0 & -\frac{1}{RC_{OUT}}
\end{bmatrix}
\begin{bmatrix}
l_{L1}
l_{L2}
v_{CS}
v_{OUT}
\end{bmatrix}
+ \begin{bmatrix}
\frac{1}{l_{L1}}
0
0
\end{bmatrix}
[V_{IN}] \quad (2)$$

And if the transistor is in OFF state:

$$\begin{bmatrix}
\frac{dl_{L1}}{dt}
\frac{dl_{L2}}{dt}
\frac{dv_{CS}}{dt}
\frac{dv_{OUT}}{dt}
\end{bmatrix} =
\begin{bmatrix}
0 & 0 & 0 & 1
0 & 0 & 0 & 1
0 & 0 & 0 & 0
0 & 0 & 0 & 0
\end{bmatrix}
\begin{bmatrix}
l_{L1}
l_{L2}
v_{CS}
v_{OUT}
\end{bmatrix}
+ \begin{bmatrix}
\frac{1}{l_{L1}}
0
0
\end{bmatrix}
[V_{IN}] \quad (3)$$

In the case of a linear system, the state representation is in the form:

$$\dot{x} = Ax + Bu \quad y = Cx \quad (4)$$

The variables:
- $x (t)$: State Vector
- $u (t)$: Vector of the entries
- $y (t)$: Vector of the outputs
- $A$: state matrix
- $B$: input matrix
- $C$: output matrix

The transfer function can be written in this way by applying the Laplace transform (Marie Chantal, Niyomansibutimbiri, 2016):

$$\frac{Y(s)}{U(s)} = C(Sl - A)^{-1}B \quad (5)$$

$$\frac{V_{OUT}}{V_{IN}} = \frac{A_{1}S^{3} + A_{2}S^{2} + A_{3}S + A_{4}}{A_{5}S^{4} + A_{6}S^{3} + A_{7}S^{2} + A_{8}S + A_{9}} \quad (6)$$

Avec:
- $A_{1} = L_{1}C_{S}L_{2}$
- $A_{2} = L_{1}C_{S}R$
- $A_{3} = -\alpha^{2}L_{1}$
- $A_{4} = \alpha^{2}R$
- $A_{5} = (1 - \alpha)^{2}L_{1}C_{S}L_{2}C_{OUT}R$
- $A_{6} = (1 - \alpha)^{2}L_{1}C_{S}$
- $A_{7} = (1 - \alpha)^{2}R(L_{1}C_{S}(1 - \alpha)^{2} + L_{1}C_{OUT}(1 - \alpha)^{2} + C_{S}L_{2}(1 - \alpha)^{2} + L_{1}C_{OUT}R^{2})$
- $A_{8} = (1 - \alpha)^{2}(L_{2}(1 - \alpha)^{2}L_{2}\alpha^{2})$
- $A_{9} = (1 - \alpha)^{4}R$

For our study we apply the values of Table 2 obtained after sizing of our converter or I determine the constants of the model (6).
The values of the inductances are calculated as follows:

\[ L_1 = L_2 = \frac{V_{pv}}{\Delta L \times f_{sw}} \]  \hfill (8)

The values of the output and coupling capacitors are calculated as follows:

\[ C_s \geq \frac{I_s}{V_{Cs \text{ ripple}} \times 0.5 \times f_{sw}} \times \alpha \] \hfill (9)

\[ C_c = \frac{I_c \alpha}{\Delta u_{Cc} \times f_{sw}} \] \hfill (10)

Table 2: Dimensioning of the SEPIC converter.

<table>
<thead>
<tr>
<th>SEPIC converter parameters</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cyclic duty ( \alpha )</td>
<td>0.41</td>
</tr>
<tr>
<td>Cutting frequency</td>
<td>100KHz</td>
</tr>
<tr>
<td>Value of inductance ( L_1 \text{ et } L_2 )</td>
<td>200( \mu )H</td>
</tr>
<tr>
<td>Output capacitor</td>
<td>1000( \mu )F</td>
</tr>
<tr>
<td>Coupling capacitor</td>
<td>47( \mu )F</td>
</tr>
<tr>
<td>Input voltage ( V_{pv} )</td>
<td>35.2V</td>
</tr>
<tr>
<td>Output voltage ( V_{out} )</td>
<td>24V</td>
</tr>
<tr>
<td>Power ( P_{pv} )</td>
<td>250W</td>
</tr>
</tbody>
</table>

The following figure illustrates the open-loop step response of the SEPIC converter.

![Open Loop Step Response](image)

Figure 7: Open loop index response of the SEPIC converter

From the index response, the two constants namely the delay time \( L = 0.0007 \)s and the time constant \( T = 0.0025s \) are obtained.

The transfer function of the PI controller is written in general form:

\[ \frac{U(s)}{E(s)} = k_p + \frac{k_i}{s} = k_p \left(1 + \frac{1}{T_p s}\right) \] \hfill (11)

Using the Ziegler and Nichols settings, we obtain the values of our PI controller (Smitha K, 2012) (Mitulkumar R, 2012):

\[ K_p = \frac{0.9 T}{L} = 3.21 \] \hfill (12)

\[ T_i = \frac{L}{0.3} = 0.0023 \text{ s} \] \hfill (13)

### 3.2 Modelling of the BOOST Converter

With this type, the average output voltage \( V_2 \) is greater than that of the input \( V_1 \). The use of the BOOST converter is for the sake of adapting the output voltage of the battery to the load (S.S.Shinde, 2016).

![Circuit Diagram of the Boost Converter](image)

Figure 8: Circuit diagram of the Boost converter

The duty cycle in CCM mode is given by:

\[ \alpha = \frac{V_1 - V_2}{V_2} \text{ avec } 0 < \alpha < 1 \] \hfill (14)

To adapt the output voltage of the battery to the load the PI regulator is used, these parameters are obtained by the use of Ziegler and Nichols method.

To make this study the determination of the transfer function of the converter is mandatory. Following the same procedure of the SEPIC converter we have (Smitha K, 2012):

\[ \begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} 0 & 0 \\ 0 & -1/RC \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 1 \\ \sum \end{bmatrix} V_{pv} \] \hfill (15)

If the transistor is in the ON state:

If the transistor is in the OFF state:
By application of the Laplace transform (Marie Chantal, Niymonazi Sebutimbiri, 2016), the transfer function is written as:

\[
\frac{V_s}{V_{pv}} = \frac{\alpha}{RC(1-\alpha)^2} \times \frac{\frac{R(1-\alpha)^2}{L} - \frac{S}{L}}{S^2 + \frac{S}{RC} + \frac{(1-\alpha)^2}{LC}}
\]  

The values of Table 3 are obtained after sizing of our converter where I determine the constants of the model (17).

The value of the inductance is calculated as follows:

\[L = \frac{\alpha \times V_{bat}}{f_{sw} \times \Delta I}\]  

The value of the output capacitor is calculated as follows:

\[C_s = \frac{I_p \alpha}{f_{sw} \Delta V_{cs}}\]  

Table 3: Dimensioning of the BOOST converter.

<table>
<thead>
<tr>
<th>BOOST converter parameters</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cyclic duty ( \alpha )</td>
<td>0.5</td>
</tr>
<tr>
<td>Cutting frequency</td>
<td>100KHz</td>
</tr>
<tr>
<td>Value of inductance ( L1 )</td>
<td>200µH</td>
</tr>
<tr>
<td>Output capacitor</td>
<td>47µF</td>
</tr>
<tr>
<td>Input voltage ( V_{bat} )</td>
<td>24V</td>
</tr>
<tr>
<td>Output voltage ( V_s )</td>
<td>48V</td>
</tr>
<tr>
<td>Charge R</td>
<td>10Ω</td>
</tr>
</tbody>
</table>

From the step response, the two constants namely the delay time \( L = 0.0005s \) and the time constant \( T = 0.005s \) are obtained.

The following figure illustrates the open-loop step response of the BOOST converter.

The transfer function of the PI controller is written in general form:

\[ \frac{U(s)}{E(s)} = k_p + \frac{k_i}{s} = k_p(1 + \frac{1}{T_1s}) \]  

Using the Ziegler and Nichols settings, we obtain the values of our PI controller (Smitha K, 2012) (Mitulkumar R, 2012):

\[ k_p = 0.9T \]

\[ T_1 = \frac{L}{0.3} = 0.0016 \text{ s} \]  

4 DIMENSIONING BATTERY VOLTAGE

We recall that a battery consists of several electrochemical conversion elements. Each element is considered as a voltage generator of 2V. By stacking these elements, one obtains batteries of 6V, 12V, 24V or 48V.

In order to determine the appropriate voltage of the battery, it is appropriate to be placed in the most unfavorable configuration, that is to say when the batteries completely power the electrical equipment (without any contribution of the photovoltaic field) (S.S.Shinde,2016) (C. de Manuel, J. Cubas, and S. Pindado,2014).

The mathematical formula for determining the battery voltage is shown below:

\[ (23) \]
\[ V_{\text{bat}} = \sqrt{\frac{\rho \times 2 \times L \times P}{S \times \varepsilon}} \]

Avec:
- \( \rho \): resistivity of the conductive material (copper or aluminum) under operating temperature conditions, expressed in \( \Omega \text{mm}^2 \text{/m} \). We can consider that \( \rho = 1.25 \times \rho_0 \) where \( \rho_0 \) is the resistivity of the conductor at 20 °C.
- \( L \): Length of the cables connecting the battery to the distribution board, expressed in m. The factor 2 makes it possible to take into account the distances to and from the cable.
- \( P \): is the electrical power, expressed in W.
- \( S \): Cable cross-section between the battery and the distribution board, in mm².
- \( \varepsilon \): Voltage drop tolerated between the battery and the distribution board.

4.2 Determination of Charging Time

The charging time \( T \) is the time required for recharging a battery can be estimated by calculation

\[ T = \frac{Q}{I} \]  \hspace{1cm} (26)

- \( Q \): the maximum electric charge of a battery announced in amperes-hours (Ah)
- \( I \): The rated load current

For our case we use a battery with an energy capacity of 7 Ah with a nominal load of 1A so:

\[ T = \frac{7}{1} = 7h \] \hspace{1cm} (27)

5 MAXIMUM POWER POINT TRACKING (MPPT)

The MPPT command, "Maximum Power Point Tracking", is an essential control for optimal operation of the photovoltaic system. The principle of this control is based on the automatic variation of the duty cycle by bringing it to the optimum value in order to maximize the power delivered by the PV panel. For this reason, we will present and study the PandO algorithm (M.R. Sourov, U.T. Ahmed and M.G. Rabbani, 2012) (M. Azab, 2009).

5.1 Algorithm of the PandOCommand

The perturb and observe control (PandO) is used to extract the maximum power of the PV generator whatever the variation of the irradiation and the temperature (D. S. Karanjkar, S. Chatterji, S. L. Shimi, and A. Kumar, 2014).

In our case we used a voltage battery:

\[ V_{\text{bat}} = 24V \] \hspace{1cm} (24)

4.1 Calculation of the Nominal Capacity of the Battery

The nominal capacity of the battery, noted \( C_{10} \) (C10), makes it possible to quantify the autonomy of the battery vis-à-vis the electrical consumption of the equipment.

\[ C_{10} = \frac{\text{Autonomie} \times \text{Energie journalièr}}{1 - \alpha_t} \] \hspace{1cm} (25)

With:
- \( \alpha_t \): Desired end state of charge
5.2 PI Controller

In this way the systems are intended to ensure equality (or at least the smallest error) between the set point and the output.

The controller P will reduce the rise time and reduce the static error, without eliminating it completely. An I controller will eliminate the static error, but can make the transient response worse. The D controller will increase the stability of a system, reduce overshoot and can improve the transient response (Mitulkumar R, 2012).

The goal of using the PI controllers is to monitor the state of charge and discharge of the battery and to adapt the output voltage of the battery to the load (Smitha K, 2012).

And the parameters of the PI controllers used are grouped in the table below:

<table>
<thead>
<tr>
<th>Parameters of PI controller</th>
<th>Kp</th>
<th>Ti</th>
</tr>
</thead>
<tbody>
<tr>
<td>Parameters of PI controller for SEPIC converter</td>
<td>3.21</td>
<td>0.0023</td>
</tr>
<tr>
<td>Parameters of PI controller for BOOST converter</td>
<td>9</td>
<td>0.0016</td>
</tr>
</tbody>
</table>

6 SIMULATION RESULTS

The simulation results presented in this section are developed using Matlab/SIMULINK. The battery voltage used has a nominal voltage of 24V. A resistive load of 10 Ω is used for the simulation.
The simulation results have shown that the charge-discharge regulator of the battery has good regulating capacity by the use of the SEPIC converter, the voltage $V_{bat}$ is of the order of 23.86 V with a response time of 0.08 s and a ripple rate of 1%. The current $I_{bat}$ with charge is stabilized at 10.34 A, that is to say with a power of 246.71 W and a yield of 98.6%.

For the boost converter model “Figure 16” shows the output voltage response of the BOOST converter for an input voltage of 24 V with an output load of 10 Ω. The controller PI stabilizes the output voltage $V_s$ compared with the reference voltage 48 V. According to the simulation, after 0.1 s, the output voltage is restored to its reference value with a ripple rate of 1% in the steady state. The efficiency of the converter is of the order of 98%, that is to say an output power of 244.7 W for a load of 10 Ω.

The following table summarizes the main specifications of the PV and previously studied MPPT algorithms.

### Table 5: PV performance based on luminal radiation.

<table>
<thead>
<tr>
<th>PV</th>
<th>$P_{pvmax}$</th>
<th>$I_{cc}$</th>
<th>$V_{co}$</th>
<th>$N_s$</th>
<th>$N_p$</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 kW/m²</td>
<td>250 W</td>
<td>7.76 A</td>
<td>43.2 V</td>
<td>10</td>
<td>6</td>
</tr>
</tbody>
</table>
Table 6: Analysis the performance of PV system.

<table>
<thead>
<tr>
<th>Parameters PV System</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Maximum power extracted</td>
<td>244.7W</td>
</tr>
<tr>
<td>Voltage at the battery terminal Vbat(V)</td>
<td>24V</td>
</tr>
<tr>
<td>Output voltage Vout(V)</td>
<td>48.21V</td>
</tr>
<tr>
<td>Response time Vbat</td>
<td>0.1s</td>
</tr>
<tr>
<td>Response time Vs</td>
<td>0.1s</td>
</tr>
<tr>
<td>% of Overshoot Vbat</td>
<td>1%</td>
</tr>
<tr>
<td>% of Overshoot Vs</td>
<td>1%</td>
</tr>
<tr>
<td>Efficiency%</td>
<td>98%</td>
</tr>
<tr>
<td>Observation</td>
<td>GOOD in response and power transmitted</td>
</tr>
</tbody>
</table>

8 CONCLUSION

In this article we have described the main elements of the autonomous PV system. Then, we dimensioned the parameters of the PI correctors by the use of the state space method to define the transfer function of the following converters: SEPIC and BOOST and after the use of the Ziegler and Nichols method to define the values of Kp and Ki. Finally, we finished with a simulation of the autonomous PV system. The results of the simulations show that the system has an efficiency of 97% with a ripple rate of 1% and a response time of 0.1s. The use of the SEPIC converter with the MPPT command followed by the PI controllers shows that the system has good regulation capacity, the voltage Vbat is of the order of 23.86 V with a response time of 0.08 s and a ripple rate of 1%. The current Ibat is stabilized at 10.34A that is to say the power is of the order of 246.7124 and the efficiency is equal to 98.6%. The BOOST converter is used to adapt the output voltage of converter SEPIC At the voltage demand by the load, the result shows that the converter has good performance: an efficiency of the order of 97% that is to say an output power of 242W for a load of 10Ω.

REFERENCES


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