Regression for Trend-Seasonal Longitudinal Data Pattern: Linear and Fourier Series Estimator

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Abstract: Longitudinal data is a pattern that consists of time series and cross section data pattern. In a research with longitudinal and panel data often be used combination between trend and seasonal pattern, for example the relationship between profit and demand for seasonal commodities, in education insurance, meteorology case and many more for many subjects. Recently, we develop Fourier series estimator to approach curve regression for longitudinal data. Fourier series which usual be used in Mathematics, but also linear function. In this research we compare performance of new estimator with linear estimator that often be used in panel data regression or parametric regression for longitudinal data. The trend-seasonal data that be used in this analysis is gotten from simulation process based on Box et.al., (1976). The Fourier series estimator gives better result with goodness indicator smaller Mean Square Error (MSE) and greater determination coefficient than linear estimator.

1 INTRODUCTION

Recently, longitudinal data analysis develops for some Statistical method. Longitudinal data is a pattern that consists of more than one subject. Each subject is observed more than one time. Therefore, in longitudinal data structure, consist of time series and cross section data pattern (Weiss, 2005).

In regression analysis, one of statistical method that be used to model the relationship between responses and predictors, longitudinal data analysis often be used. Panel data regression is one of the linear regressions for longitudinal data. The differences between longitudinal and panel data, panel data is longitudinal data with the number of observations and periods are same for every subject (Baltagi, 2005).

Regression analysis that be developed is not only regression with linear estimator, but also nonparametric regression. Nonparametric regression is a Statistical modeling that be used to overcome the relationship between responses and predictors which have unknown pattern. Nonparametric regression is an alternative method that be used when the result of regression analysis with certain function, such as linear regression, cannot suitable with goodness criteria of regression analysis (Takezawa, 2006). The advantage of nonparametric regression is having high flexibility. Flexibility means that the pattern of data that presented on the scatter plot can determine the shape of regression curve based on estimators in the nonparametric regression (Budiantara et.al., 2015). Based on plot, we can identify the pattern of data, the pattern of pairs data, a response versus a predictor variable data, have trend, oscillation, uncertain pattern, and combination pattern.

The pattern of data that often be found is combination between trend and seasonal or trend-seasonal data pattern. In research with longitudinal and panel data this pattern often be encountered. Some example like, the relationship between profit and demand for seasonal commodities, in education insurance, meteorology case and many more for many subjects.

Trend – seasonal data pattern popular in time series data analysis. This pattern will pass some procedure when time series analysis be used, be-cause there are some assumptions must be satisfied. Time series – regression approach is an...
alternative to forecast time series data (Bloomfield, 2000). Based on that concept, trend – seasonal data pattern analysis is applied to longitudinal data, that consist of time series and cross section data pattern.

Regression for longitudinal data pattern that be discussed in this study based on linear and Fourier series estimator. Linear estimator represents trend pattern, and Fourier series represents seasonal pattern. Bilodeau (1992) proposed combination linear function and Fourier cosine series in his paper to get smooth estimator for the relationship of a response and predictors. In longitudinal analysis, linear estimator often be used, especially in regression, the most popular method is panel data regression. However, that method is not suitable when the variation of oscillation is large. So, we propose new method based on the development of Bilodeau (1992). The method is longitudinal data regression based on Fourier series estimator that consist of linear function, cosine and sine function. Visually and mathematically, that estimator accommodates trend-seasonal pattern that be presented in scatter plot and time series plot for longitudinal data.

In this paper, second part discuss about linear estimator for longitudinal data regression. The third part discuss about Fourier series estimator for longitudinal data regression. Fourier series that be used based on Fourier series estimator that consist of linear function, cosine and sine function. Using simulation data, we make comparison based on MSE and determination coefficient value to make conclusion which regression method that suitable to be used for trend – seasonal longitudinal data pattern. In the end of this part, given longitudinal data structure in Table 1 as follows:

Table 1: The structure of longitudinal data that be used.

<table>
<thead>
<tr>
<th>Subject</th>
<th>Response</th>
<th>Predictors</th>
</tr>
</thead>
<tbody>
<tr>
<td>y_{ij}</td>
<td>x_{i1j}</td>
<td>x_{i2j} ... x_{ipj}</td>
</tr>
<tr>
<td>1\textsuperscript{st} Subject</td>
<td>y_{11}, y_{12}, \ldots, y_{1n}</td>
<td>x_{111}, x_{112}, \ldots, x_{11p}, x_{121}, x_{122}, \ldots, x_{12p}, \ldots, x_{1n1}, x_{1n2}, \ldots, x_{1np}</td>
</tr>
<tr>
<td>2\textsuperscript{nd} Subject</td>
<td>y_{21}, y_{22}, \ldots, y_{2n}</td>
<td>x_{211}, x_{212}, \ldots, x_{22p}, \ldots, x_{2n1}, x_{2n2}, \ldots, x_{2np}</td>
</tr>
<tr>
<td>\vdots</td>
<td>\vdots</td>
<td>\vdots</td>
</tr>
<tr>
<td>n\textsuperscript{th} Subject</td>
<td>y_{n1}, y_{n2}, \ldots, y_{nn}</td>
<td>x_{n11}, x_{n12}, \ldots, x_{np}, x_{n21}, x_{n22}, \ldots, x_{nn1}, x_{nn2}, \ldots, x_{nnp}</td>
</tr>
</tbody>
</table>

\[ y_{ij} = \beta_0 + \sum_{k=1}^{p} \beta_k x_{ijk} + \epsilon_{ij}; \epsilon_{ij} \sim i.i.d. N(0, \sigma^2) \] (1)

with $\beta_0$ is an intercept parameter for $i\textsuperscript{th}$ subject, $\beta_k$ is parameter for $k\textsuperscript{th}$ predictor and $i\textsuperscript{th}$ subject. Random error for $i\textsuperscript{th}$ subject and $j\textsuperscript{th}$ observation denoted by $\epsilon_{ij}$ that independent and identically normal distributed with mean equals to 0 and variance equals to $\sigma^2$. An estimator for parameter which be formed as vector for equation (1) can be determined based on Weighted Least Square (WLS) optimization (Weiss, 2005). The WLS optimization result given as follows:

\[ \hat{\beta} = (X'WX)^{-1}X'Wy \] (2)

In this case $y = (y_1, y_2, \ldots, y_n)^T$, that have $\sum_{i=1}^{n} n_i \times 1$ or $N \times 1$ with vector components that correspond are $y_i = (y_{i1}, y_{i2}, \ldots, y_{in})^T$ that have $n_i \times 1$. $X$ is a matrix that has $N \times (p + 1)$ or $\sum_{i=1}^{n} n_i \times (p + 1)$, and parameter vector defined by

\[ X = \begin{bmatrix} 1 & x_{111} & x_{112} & \cdots & x_{11p} \\ 1 & x_{121} & x_{122} & \cdots & x_{12p} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 1 & x_{n11} & x_{n12} & \cdots & x_{n1p} \\ 1 & x_{n21} & x_{n22} & \cdots & x_{n2p} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 1 & x_{nn1} & x_{nn2} & \cdots & x_{nnp} \end{bmatrix} \]
\[ \beta = (\beta_0, \beta_1, \beta_2, \ldots, \beta_p)^T \] that has \((p + 1) \times 1\). In addition, there is \(W = V^{-1}\) as a weight matrix with structure as follows:

\[
V = \begin{bmatrix}
V_1 & 0 & \cdots & 0 \\
0 & V_2 & \cdots & 0 \\
\vdots & \vdots & \ddots & \vdots \\
0 & 0 & \cdots & V_n
\end{bmatrix}
\]

where

\[
V_i = \begin{bmatrix}
u_{1i} & v_{12} & \cdots & v_{1n} \\
v_{21} & v_{22} & \cdots & v_{2n} \\
\vdots & \vdots & \ddots & \vdots \\
v_{ni} & v_{n2} & \cdots & v_{nn}
\end{bmatrix}
\]

with variance matrix \(v_{ab} = v_{ba}\) where \(a \neq b\). The estimator for curve regression can be determined as follows:

\[
y_{ij} = \hat{\beta}_0 + \sum_{k=1}^{p} \hat{\beta}_k x_{ijk}. \tag{3}
\]

In regression for longitudinal data based on linear estimator, inference Statistics for significant test has been provided. There are unit root test using Augmented Dickey Fuller (ADF), simultaneous and partial significance test (Baltagi, 2005), heteroscedasticity test for error using Lagrange Multiplier (Greene, 2012) and normality test using Jarque Bera test (Baltagi, 2005). The good estimator is estimator with small MSE value, and big determination coefficient value.

3. FOURIER SERIES ESTIMATOR FOR LONGITUDINAL DATA REGRESSION

Consider a longitudinal data structure that be presented in Table 1. Based on Table 1, there are pairs of data with form \((x_{ijk}, y_{ij})\). \(x_{ijk}\) denotes \(k^{th}\) predictor variable for \(j^{th}\) observation in \(i^{th}\) subject. Here, \(i = 1, 2, \ldots, n\) denote the number of subjects, \(j = 1, 2, \ldots, n_i\) denote the number of observations for each subject, and \(k = 1, 2, \ldots, p\) represents the number of predictors. Response variable for \(j^{th}\) observation in \(i^{th}\) subject is denoted by \(y_{ij}\). The pairs of data that be presented in Table 1, follows nonparametric regression equation for longitudinal data as follows:

\[
y_{ij} = \sum_{k=1}^{p} f_k(x_{ijk}) + \epsilon_{ij}; \epsilon_{ij} \sim N(0, \sigma^2), \tag{4}
\]

where \(f_k(x_{ijk})\) represents a regression curve. Random error for \(j^{th}\) observation in \(i^{th}\) subject is denoted by \(\epsilon_{ij}\) that independent, identically normal distributed with mean 0, and variance \(\sigma^2\). In this case, \(f_k(x_{ijk})\) approached by Fourier series as follows:

\[
f_k(x_{ijk}) = \frac{a_{0k}}{2} + \sum_{r=1}^{p} \left(\alpha_{r,k} \cos r x_{ijk} + \beta_{r,k} \sin r x_{ijk}\right) \tag{5}
\]

Equation (5) is substituted to equation (4), the result is a nonparametric regression equation for longitudinal data that be approached by Fourier series. Based on equation 5, \(y_{ijk}\) is a component that accommodates trend pattern, \(\gamma_{ijk}\) denotes parameter that be estimated for \(k^{th}\) predictor and \(i^{th}\) subject. The other component accommodates seasonal pattern, \(\frac{a_{0k}}{2}\) is an intercept parameter for \(k^{th}\) predictor and \(i^{th}\) subject, \(\alpha_{r,k}\) is the parameter of cosine basis for \(k^{th}\) predictor, \(i^{th}\) subject, and oscillation parameter \(r = 1, 2, \ldots, R\) that be inputted, \(\beta_{r,k}\) is the parameter of sine basis for \(k^{th}\) predictor, \(i^{th}\) subject, and oscillation parameter \(r = 1, 2, \ldots, R\) that be inputted.

An estimator for parameter which be formed as vector for nonparametric regression equation with longitudinal data that be approached by Fourier series can be determined based on Weighted Least Square (WLS) optimization. The WLS optimization result given as follows:

\[
\hat{\beta} = \left(X^T [R]W_X[R]\right)^{-1}X^T [K]W_Y
\]

The structure of \(y\) vector is same with linear estimator for longitudinal data regression in second part. The matrix structure of \(X[R]\) is given as follows:

\[
X[R] = \begin{bmatrix}
X_1[R] & 0 & \cdots & 0 \\
0 & X_2[R] & \cdots & 0 \\
\vdots & \vdots & \ddots & \vdots \\
0 & 0 & \cdots & X_n[R]
\end{bmatrix}
\]

where \(X_i[R]\) equals as follows:

\[
\begin{bmatrix}
x_{11} & \cos x_{11} & \cdots & \cos R x_{11} & \sin x_{11} & \cdots & \sin R x_{11} \\
x_{21} & \cos x_{21} & \cdots & \cos R x_{21} & \sin x_{21} & \cdots & \sin R x_{21} \\
x_{n1} & \cos x_{n1} & \cdots & \cos R x_{n1} & \sin x_{n1} & \cdots & \sin R x_{n1}
\end{bmatrix}
\]

Vectors that include regression parameters denoted by \(\beta = [\beta_1, \beta_2, \ldots, \beta_n]^T\), where
\[ \beta_i = \left( \frac{\alpha_{0_i}}{2}, \gamma_i, \alpha_{1_i}, \ldots, \alpha_{R_i}, \beta_{1_i}, \ldots, \beta_{R_i}, \ldots \right)^T. \]

In addition, there is \( W = V^{-1} \) as a weight matrix. In this study, two kinds of weight are used based on Wu and Zhang (2006). There are uniform, and variance weighted. The structure of \( V \) based on uniform weight denoted as follows:

\[ V = \frac{1}{N} \begin{bmatrix} I_1 & 0 & \cdots & 0 \\ 0 & I_2 & \cdots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \cdots & I_n \end{bmatrix}, \tag{6} \]

where \( N \) denotes the total of the observations number for all subjects. An identity matrix for \( i^{th} \) subject is denoted by \( I_i \). The structure of \( V \) based on uniform weight denoted as follows:

\[ V = \begin{bmatrix} S_{11} & S_{12} & \cdots & S_{1n} \\ S_{21} & S_{22} & \cdots & S_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ S_{n1} & S_{n2} & \cdots & S_{nn} \end{bmatrix}, \tag{7} \]

with variance matrix \( S_{ab} = S_{ba} \) where \( a \neq b \). The estimator for curve regression can be determined as follows:

\[ \hat{y}_{ij} = \sum_{k=1}^{T} \hat{f}_k(x_{ijk}), \tag{8} \]

with

\[ \hat{f}_k(x_{ijk}) = \frac{2u_k}{\pi} + \hat{p}_k x_{ijk} + \sum_{r} (d_{rk} \cos r x_{ijk} + \beta_{rk} \sin r x_{ijk}). \tag{9} \]

In regression for longitudinal data based on Fourier series estimator, the good estimator is estimator with optimal oscillation parameter, small MSE value, and big determination coefficient value. An optimal parameter oscillation can be determined based on the smallest Generalized Cross Validation (GCV) value that given as follows:

\[ GCV(R) = \frac{\text{MSE}(R)}{(N^{-1} \text{trace}(I-A(R)))^{2}}, \tag{10} \]

where

\[ \text{MSE}(R) = N^{-1}y^T(I - A(R))^TW(I - A(R))y, \]

and hat matrix is defined with \( A(R) = X[R]X^T[R]W \) (Tripena and Budiantara, 2006).

### 4 DISCUSSIONS

In this part we concentrate to application of either linear or Fourier series estimator for longitudinal data regression. There are four sub sections in this part. The first sub section we discuss about the simulation data. The second sub section we discuss about application for linear estimator. The third sub section we discuss about application for Fourier series estimator. The last sub section we compare the goodness of estimator result based on linear and Fourier series estimator for longitudinal data.

#### 4.1 About the Data

Consider simulation data that consist of one response and two predictors. The response data used represent monthly wind velocity data in 10 cities, whereas the predictor data used represents the monthly average temperature in 10 cities, and the observation period. In this case study there are 10 cities each observed for 12 months. Based on the scatter plot between response and predictors, there are trend – seasonal pattern.

Simulation processes have been constructed based on the characteristics from equation (5) where the function included of linear and trigonometric parts. For this simulation, we concern to modified data based on Box et al. (1976) with take 2R + 2 parameters. Two parameters represent trend components and 2R parameters represent seasonal components that be related to trigonometric function. This simulation based on an analogue from the data that be presented on Box et al. (1976).

Figure 1 presents plot of data sample from equation (5). Simulation process based on equation (7) have been constructed with \( \beta_i \) as follows:

\[ \hat{y}_{ij} = -4.1801 + 0.3124x_{ij1} + 0.0113x_{ij2}. \]
The summary from the series of hypothesis test for the first estimation is presented in Table 2.

Table 2: The summary from the series of hypothesis test for the first estimation.

<table>
<thead>
<tr>
<th>Test</th>
<th>Result</th>
</tr>
</thead>
<tbody>
<tr>
<td>Augmented Dickey Fuller</td>
<td>Time series component stationer</td>
</tr>
<tr>
<td>Simultaneous</td>
<td>Parameter that be estimated affect to response variable simultaneously.</td>
</tr>
<tr>
<td>Partial</td>
<td>For second predictor (observation period) does not significant</td>
</tr>
<tr>
<td>Lagrange Multiplier</td>
<td>Heteroscedasticity is happened.</td>
</tr>
<tr>
<td>Jarque Bera</td>
<td>Error distribution is normal</td>
</tr>
</tbody>
</table>

Because of second predictor, observation period, does not significant based on hypothesis test, so we eliminate that predictor, and we use a predictor variable, the first predictor, to estimate a response variable. The result of the second linear regression estimation for longitudinal data is as follows:

\[ \hat{y}_{ij} = -4.1136 + 0.3126x_{ij1}. \]

The second regression model has a determination coefficient value equals to 0.87241, which means that the predictor can explain the response of 87.241%. The MSE value equals to 0.1106. The determination coefficient value is big, and the MSE value is small, so it can satisfy the indicator of goodness estimator. However, the weakness of the linear estimator for longitudinal data regression in this study, the wind speed estimation does not involve period variable, and there are cases of heteroscedasticity in the error. The resulting MSE value can be smaller, and the resulting determination coefficient value can be greater if using other approaches such as nonparametric regression for longitudinal data.

4.3 Fourier Series Estimator Result

Furthermore, using the same data, applied to nonparametric regression for longitudinal data based on Fourier series estimator. The weighting types that be used are uniform weighting and variance based on Wu and Zhang (2006). The criterion of goodness that be used is the small MSE value, and the large of determination coefficient value. The optimal oscillation parameter is determined based on minimum GCV value. The Fourier series estimator for nonparametric regression of longitudinal data is determined based on equation (8). The GCV value is calculated based on equation (10). The GCV values based on uniform weighting for each oscillation parameter are presented in Table 4. The GCV values based on uniform weighting for each oscillation parameter are presented in Table 5.
Table 4: GCV value based on uniform weighting for each oscillation parameters.

<table>
<thead>
<tr>
<th>Oscillation Parameter</th>
<th>GCV Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>164,001.8</td>
</tr>
<tr>
<td>2</td>
<td>145,905.457</td>
</tr>
<tr>
<td>3</td>
<td>116,867.687</td>
</tr>
<tr>
<td>4</td>
<td>103,764.306</td>
</tr>
<tr>
<td>···</td>
<td>···</td>
</tr>
</tbody>
</table>

Table 5: GCV value based on variance weighting for each oscillation parameters.

<table>
<thead>
<tr>
<th>Oscillation Parameter</th>
<th>GCV Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>19,680.216</td>
</tr>
<tr>
<td>2</td>
<td>17,508.654.9</td>
</tr>
<tr>
<td>3</td>
<td>14,024.122.4</td>
</tr>
<tr>
<td>4</td>
<td>12,451.716.7</td>
</tr>
<tr>
<td>5</td>
<td>10,386.213.6</td>
</tr>
<tr>
<td>···</td>
<td>···</td>
</tr>
</tbody>
</table>

It can be seen from Table 4, based on uniform weighting obtained the minimum GCV is 5,880,609. That value is achieved by the Fourier series estimator with an oscillation parameter of 35. Table 5 shows the result that the minimum GCV value is 708,797.7 based on the variance weighting. That value is achieved by the Fourier series estimator with an oscillation parameter of 36. However, based on the comparison of GCV values that be generated in Table 4 and Table 5, it is seen that the GCV values for uniform weighting is always smaller than the GCV values for variance weighting in each oscillation parameter. In this case, it can be concluded that the uniform weighting is more optimal than the variance weighting. However, this study does not guarantee uniform weighting is always better than variance weighting.

The selected of Fourier series estimator for longitudinal data nonparametric regression approach based on uniform weighting. The estimator has a small MSE value of 0.00214. The estimator has a high determination coefficient value of 0.99766 which means that predictors can explain the response of 99.766%.

4.4 A Comparison

In this sub section we make comparison about the result of regression for trend-seasonal data pattern using linear estimator, the second estimator, and Fourier series estimator, based on uniform weighting. The comparison is presented on Table 6.

Based on Table 6, it should be noted that in the goodness indicator of estimator, the Fourier series estimator is better than the linear estimator for regression that be used in case of trend – seasonal longitudinal data pattern. The MSE for Fourier series estimator is smaller than linear estimator. The determination coefficient for Fourier series is greater than linear estimator. In addition, the information that be obtained based on the Fourier series estimator is more complete than the linear estimator, since the predictor that be contained in the model for the Fourier series estimator are more complete. Table 7 presents estimation result for both of estimator for first subject. Based on Table 7 can be inferred that estimator value for Fourier series is not much different from the original data and linear estimator. The result is supported by plot that be presented on Figure 2. It can be concluded that Fourier series estimator can become an alternative for regression, in this case for longitudinal data.

Table 6: The comparison between linear and Fourier series estimator in regression for trend-seasonal longitudinal data pattern.

<table>
<thead>
<tr>
<th>Linear estimator</th>
<th>Fourier series estimator</th>
</tr>
</thead>
<tbody>
<tr>
<td>Consist of a predictor</td>
<td>Consist of two predictors</td>
</tr>
<tr>
<td>Does not fulfill the assumption of homogeneity</td>
<td>It does not test the assumption of homogeneity, because there has been no relevant inference study.</td>
</tr>
<tr>
<td>MSE value equals to 0.1106</td>
<td>MSE value equals to 0.00214</td>
</tr>
<tr>
<td>Determination coefficient value equals to 87.241%</td>
<td>Determination coefficient value equals to 99.766%</td>
</tr>
<tr>
<td>Estimator form is parsimony</td>
<td>Estimator form is more complex</td>
</tr>
</tbody>
</table>

Figure 2: Plot of the comparison result based on estimator value from linear and Fourier series estimator and original data for first subject.
Table 7: The comparison based on estimator value from linear and Fourier series estimator and original data for first subject.

<table>
<thead>
<tr>
<th>obs.</th>
<th>y data</th>
<th>y linear</th>
<th>y Fourier series</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>2.9</td>
<td>2.90543</td>
<td>2.910106</td>
</tr>
<tr>
<td>2</td>
<td>3</td>
<td>2.97832</td>
<td>2.964548</td>
</tr>
<tr>
<td>3</td>
<td>3.1</td>
<td>3.13808</td>
<td>3.132132</td>
</tr>
<tr>
<td>4</td>
<td>3.1</td>
<td>3.08934</td>
<td>3.090152</td>
</tr>
<tr>
<td>5</td>
<td>3</td>
<td>3.02323</td>
<td>3.027406</td>
</tr>
<tr>
<td>6</td>
<td>3.2</td>
<td>3.16562</td>
<td>3.170019</td>
</tr>
<tr>
<td>7</td>
<td>3.3</td>
<td>3.308</td>
<td>3.302801</td>
</tr>
<tr>
<td>8</td>
<td>3.3</td>
<td>3.31139</td>
<td>3.303712</td>
</tr>
<tr>
<td>9</td>
<td>3.2</td>
<td>3.19316</td>
<td>3.189406</td>
</tr>
<tr>
<td>10</td>
<td>3</td>
<td>3.0228</td>
<td>3.014211</td>
</tr>
</tbody>
</table>

5 CONCLUSIONS

In modelling longitudinal data with trend - seasonal pattern with regression analysis, not only linear estimators are used, but also the Fourier series estimator can become an alternative. Based on the discussion, the Fourier series estimator has better value for the indicator of goodness estimator than the linear estimator. The MSE for Fourier series estimator is smaller than linear estimator. The determination coefficient for Fourier series is greater than linear estimator. Nevertheless, inference for the Fourier series estimator still needs to be developed.

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