Simulation of Temperature Field of Sponge Titanium Prepared by Magnesium Thermal Reduction Process

N W Wang* and J X Zou
School of Vanadium and Titanium, Panzhihua University, 617000 Panzhihua, People’s Republic of China

Corresponding author and e-mail: N W Wang, wnw_2008@163.com

Abstract. In this paper, based on the analysis of the current production process of titanium sponge, the temperature field model was built by using the assumption of the model and the temperature field of different models were simulated by using the FLUENT software. The characteristics of temperature field was obtained in the process of sponge titanium prepared by magnesium thermal reduction process under different process ways, by which a feasible scheme was provided for the actual production.

1. Introduction
At present, sponge titanium production enterprises mainly produce titanium sponge by magnesium thermal process (Kroll process). The main process is that sponge titanium is prepared by magnesium reduction TiCl4, including reduction process and distillation process, and the reduction process is the key link. The reaction of magnesium reduction to TiCl4 is a strong exothermic reaction. If the residual heat in the reactor is not discharged in time, the temperature in the reactor will rise sharply[1-5]. In this experiment, the temperature field is simulated in the reactor produced by Kroll process using FLUENT software, the influence rule of process parameters are explored on the temperature field distribution, and the direction of technological improvement is researched[6-8].

2. Establishment of model
2.1. Model assumes
The following conditions are assumed to hold for the process of the calculation.

(1) The liquid part in the reactor is a continuous medium, and the property parameters are consistent at all parts.

(2) It is a complex process for magnesium reduction TiCl4. Not only can it obtain a single titanium, but also it can generate three valence titanium and two valence titanium[9-10]. In order to simplify the model, the reactor interior reduction reaction is referred to formula (1).

\[ \text{TiCl}_4 + 2\text{Mg} = \text{Ti} + 2\text{MgCl}_2 \]  \hspace{1cm} (1)

(3) TiCl4 added at the space above the liquid surface is completely vaporized. The reduction reaction occurs only with the gas liquid reaction, and the reaction is evenly distributed across the surface on the liquid. The reaction liquid is used as a reservoir in the reduction process.
2.2. Mathematical equations

The energy equation is referred to formula (2) by using fluent software[11].

\[
\frac{\partial}{\partial t}(\rho E) + \nabla \cdot \left[ \left( \rho \mathbf{v} E + \rho \frac{\partial E}{\partial t} \right) \right] = \nabla \cdot \left[ \lambda_{\text{eff}} \nabla T - \sum \mathbf{h}_j \frac{\partial}{\partial t} (\mathbf{J}_j \cdot \mathbf{v}) \right] + S_h
\]  

(2)

In the formula: \( t \) is time, s; \( \rho \) is density, kg/m\(^3\); \( E \) is energy, J; \( \mathbf{v} \) is fluid velocity, m/s; \( P \) is pressure, Pa; \( \lambda_{\text{eff}} \) is the effective thermal conductivity coefficient, W/(m\( \cdot \)K); \( T \) is temperature, K; \( \mathbf{h}_j \) is the enthalpy of component \( j \), J; \( \mathbf{J}_j \) is the diffusion flux is \( j \), mol/(m\(^2\)\( \cdot \)s), the effective viscous dissipation coefficient, and the stress tension, Pa. The right side of the equation represents the energy transfer caused by heat conduction, component diffusion and viscous dissipation. \( S_h \) contains the chemical reaction (absorption) heat and other forms of defined volume heat sources. In this experiment for cylindrical reactor, the axisymmetric physical parameters according to \( t \) he center, so can choose 2 d cylindrical coordinate to establish mathematical model of the reactor, the heat in the form of differential equations can be written which referred to formula (3).

\[
\rho c \left( \frac{\partial t}{\partial \tau} + \mathbf{u} \cdot \frac{\partial t}{\partial \mathbf{x}} + \mathbf{v} \cdot \frac{\partial t}{\partial \mathbf{y}} \right) = \lambda \left( \frac{\partial^2 t}{\partial x^2} + \frac{\partial^2 t}{\partial y^2} \right) + S_h
\]  

(3)

In the formula: \( \rho \) is density, kg/m\(^3\); \( c \) is the specific heat capacity, J·kg/K; \( T \) is temperature, K; \( \tau \) is \( t \)ime, s; \( \mathbf{x} \) and \( \mathbf{y} \) are two directions of two dimensional space; \( \mathbf{u} \) is moving in the \( x \) direction, m/s; \( \mathbf{v} \) is the velocity of the material in the \( y \) direction, m/s; \( \lambda \) is the thermal conductivity, W/(m\( \cdot \)K); \( S_h \) is the heat source generated by the chemical reaction. In this paper, the position of the heat source is the liquid surface, and its energy is characterized by the heat flux density generated by the chemical reaction.

2.3. Basic physical parameters

In this experiment, the basic physical parameters of mixed liquid in the reactor are simplified[12]. Density and viscosity are calculated by simple rule of mixtures, this is shown in the following formula (4).

\[
\rho = \sum_{i=1}^{n} m_i \rho_i; \mu = \sum_{i=1}^{n} m_i \mu_i
\]  

(4)

In the formula: \( m_i \) is the mass fraction of the liquid of each component, \( \rho_i \) is the density of Components of the i, and \( \rho \) is the density of mixing liquid, kg /m3; \( \mu_i \) is the viscosity of component I, \( \mu \) is the viscosity of the mixed liquid, Pa\( \cdot \)s.

In the reduction reactor, the main component of liquid is the raw material of liquid magnesium, magnesium chloride and titanium particles produced by the reduction reaction, under the condition of high temperature, the thermal conductivity of magnesium chloride (5W/(m\( \cdot \)K)) and the thermal conductivity of the titanium particles(8W/(m\( \cdot \)K)) are obviously lower than the thermal conductivity of the liquid magnesium(97.33W/(m\( \cdot \)K)). Therefore, the thermal conductivity of liquid magnesium is used to represent the thermal conductivity of the liquid in the reactor.

3. Setting of heat source

3.1. Heat dissipation mechanism

Reactor cooling is mainly through the wall of the gas convection and radiation heat dissipation of the reaction exhaust[13]. Therefore, the unit wall heat dissipation unit time is the sum of convective heat transfer and radiation heat transfer power, the relationship is referred to formula (5).
In the formula: \( q \) is the sum of convection heat transfer power and radiation heat transfer power, W; \( \varepsilon \) is the emissivity, W/(m\(^2\)•K\(^4\)); \( A \) is the heat dissipation area, m\(^2\); \( T_w \) is the wall temperature, K; \( T_g \) is the air room temperature, K; \( U \) is the convection coefficient, W/(m\(^2\)•K).

3.2. Setting

Reduction process[14], the reactor heat mainly comes from magnesium reduction reaction heat produced by the TiCl\(_4\), its main chemical reactions are gasification TiCl\(_4\) react with magnesium liquid in the liquid level, main equation is referred to formula (6).

\[
\text{TiCl}_4 + 2\text{Mg} = \text{Ti} + 2\text{MgCl}_2 - 519 \text{kJ/mol}
\]

Continuously for the reduction in the process of the reaction and assumes that the reaction liquid level as the heat source location, depending on the feed rate, set different heat flux, feeding rate of 260, 300, 350, 400 kg/h, set the heat flux density of 63 270 W/m\(^2\), 72 306 W/m\(^2\), 84357 W/m\(^2\), 96 408 W/m\(^2\).

4. Analysis and discuss

4.1. Iterative analysis

Analysis according to the requirement of feeding rate of 260 kg/h, 300 kg/h, 350 kg/h, 400 kg/h when temperature field of iterative graph, as shown in figure 1.

![Figure 1. Iterative diagram of temperature field at different feeding speeds.](image-url)  
(a) 260kg/h (b) 300kg/h (c)350kg/h (d) 400kg/h
4.2. Analysis of temperature field in adiabatic condition
Assumption of all gasification of TiCl4, the distribution of temperature field in the reactor is shown in figure 2, specific data are shown in Table 1. The simulation results are the distribution of temperature field after the initial reaction of 1 h. From Table 4.1, with the increase of feed speed, temperature rise in the post 1h reactor. When the feeding speed is 400 kg /h, the temperature in the reactor is 100 degrees centigrade higher than the feed rate of 260 kg /h. It will be seen from this that, if a long reaction will lead to a sharp increase in the temperature in the reactor, causing temperature excursion. To control the temperature in the reactor, expelled heat from the reaction process, it is necessary to heat the reactor.

![Figure 2](image)

**Figure 2.** Temperature distribution at different feeding speeds under adiabatic conditions.
(a) 260kg/h  (b) 300kg/h  (c)350kg/h  (d) 400kg/h

**Table 1.** Central temperature corresponding to different feeding velocities under adiabatic conditions.

<table>
<thead>
<tr>
<th>feeding velocities /kg·h⁻¹</th>
<th>260</th>
<th>300</th>
<th>350</th>
<th>400</th>
</tr>
</thead>
<tbody>
<tr>
<td>Central temperature /K</td>
<td>1200</td>
<td>1240</td>
<td>1280</td>
<td>1320</td>
</tr>
</tbody>
</table>

4.3. Analysis of the temperature field under natural air cooling condition
Through sampling the model, the physical parameters and setting of the boundary conditions. The temperature field distribution in the designed reactor of 5.1 m × 1.8 m (reaction medium feed rate of 260 kg /h) was simulated. It can be seen from the simulation results that the reactor center temperature is 1200K at the feeding rate of 260 kg/h, and the reactor wall temperature is about
1020K, which is similar to the known temperature (1 010 ~ 1 039 K). As shown in Figure 3, it can be seen that the model is feasible.

The model was used to simulate the distribution of temperature field inside the reactor, and under different conditions of natural air cooling and different feed rates. It can be seen, with the increase of feed rate, the center temperature and wall temperature showed an up, the wall temperature doesn’t increase. However, as the feed rate increases, the temperature in the center of the reactor increases from 1180K to 1300K. So increasing the feed rate, the center temperature rose sharply and it can easily cause the reactor temperature over-temperature. In order to obtain better sponge titanium quality and higher genuine rate, we need to increase the cooling capacity of the reactor. Generally forced air cooling can be used.

![Simulation results of temperature Field in reactor when feeding speed is 260kg /h.](image)

4.4. Analysis of temperature Field under forced Air cooling

In this condition of forced air cooling, the temperature distribution of feeding velocity of 300 kg/h, 350kg /h and 400 kg/h is shown in Figure 4, referred to Figure 4 (a), (b) and (c).

As can be seen from the graph, when the feeding speed has been increased, the temperature of the reactor is close to the temperature field of which feeding speed is 260 kg/h and in the condition of natural ventilation, and the temperature of the reactor decreases obviously.

It can be seen that forced air cooling has been used to dissipate heat which can effectively control the temperature field in the reactor. Namely, the temperature of the reactor center is also close to the temperature of low speed 260 kg/h when the feed rate of TiCl4 is significantly increased.

Simulation results of the temperature field in the reactor at different feeding speeds in forced air cooling, referred to Figure 4.

In addition, related studies have shown that the relationship between feeding speeds and forced air-cooled ventilation can be represented in the following form if the feed rate is more than 260 kg/h, reference equation is listed by formula 7.

$$Y = 180 \times (X - 260) + 1570$$  \hspace{1cm} (7)

In the equation, $Y$, ventilation, $m^3$/h; $X$, feeding speed, kg/h.

By calculation, when the feeding speed is 260 kg/h, 300 kg/h, 350kg /h and 400 kg/h, the ventilation is 1 570$m^3$/h, 8 881$m^3$/h, 17 876$m^3$/h, 26 888$m^3$/h respectively. With the increase of feeding speed, the ventilation rate increases.
Figure 4. Simulation results of temperature field in reactor at different feeding speeds for forced air cooling. (a) 300kg/h (b) 350kg/h (c) 400kg/h.

Acknowledgements

This work is financially supported by Science and Technology Project of Panzhihua City. The title of the project is Optimization of Thermal Reduction Process and Equipment for Sponge Titanium magnesium, the project number is 2013CY-G-11.

5. Conclusions

(1) With the speed of feeding in raw material increases, the temperature of reactor rises on condition that thermal is isolated. When the speed is 400kg/h, its central temperature is 1320 K, and 260kg/h, 1200K. Compared to the temperature at speed of 400kg/h, that at 260kg/h decreases by 120K.

(2) If the reactor is air cooling, its central temperature will rise with the speed of feeding increases. When the speed is 260kg/h or 400kg/h, their respective temperature is 1180K and 1300K. In contrast with the two speeds, the temperature differs in 120K.

(3) Adding artificial winds, the temperature dispersion at speed of 300kg/h, 350kg/h, 400kg/h is similar with that at speed of 260kg/h and air cooling. When ventilation quantity is 26888 m³/h and its categorical wind speed is as 17.2 times as air, the speed of feeding TiCl₄ can be increased to 400kg/h, and its central temperature is 907°C, the same as on condition that the speed is 260kg/h with air cooling.
References


[9] Xiao Z Q and Zhu M Y 2006 Application of numerical simulation analysis technology in metallurgical process. *M. Metallurgical Industry Press*


