

# Statistical and Combinatorial Analysis of the TOR Routing Protocol

## *Structural Weaknesses Identified in the TOR Network*

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Abstract: In this paper, we present the results of a deep analysis of TOR routing protocol from a statistical and combinatorial point of view. We have modeled all possible routes of this famous anonymity network exhaustively while taking different parameters into account with the data provided by the TOR foundation only. We have then confronted our theoretical model with the reality on the ground. To do this, we have generated thousands of roads on the TOR network and compared the results obtained with those predicted by the theory. A last step of combinatorial analysis has enabled us to identify critical subsets of Onion routers (ORs) which 33%, 50%, 66% and 75% of the TOR traffic respectively depends on. We have also managed to extract most of the TOR relay bridges which are non public nodes managed by the TOR foundation. The same results as for the ORs have been observed.

## 1 INTRODUCTION

The various computer networks such as the Internet today allow everyone to have many means of communication. However, this access is only possible if the user has an IP address. This condition therefore allows entities that have access to the network flows, to analyze it and thus to retrieve information about particular users.

When communicating in a secure and anonymous manner, it is necessary to protect not only the confidentiality of information (NATO's COMSEC) but also to protect the communication channel (NATO's TRANSEC) in order to reduce the risk of a targeted attack (Defense\_Science\_Board, 2015).

Communities have been formed to defend the anonymity of each other and have developed networks whose purported purpose is to enable people to navigate without anyone being able to identify the origin and destination of the communication. These networks therefore seem to be an ideal tool for criminals and terrorists of all kinds, as they can carry out their actions with little trace.

The purpose of this article is therefore to study a particular network of anonymization, both for clients and services: *The Onion Router* (TOR for short). Its purpose is to protect the confidentiality, integrity and availability of exchanges within its organization. This

network relies on a community that uses a particular network protocol. The open source code is documented, but many aspects such as route construction are only briefly documented. This is contrary to the principles of security, since TOR's security of this network is based on a considerable amount of obscurity and secrecy. Therefore, would it be possible for an attacker who controls a limited number of routers to be able to control and impact a significant part of the traffic and hence more or less would be able to damage TOR's security?

Our study of the architecture and functioning of this network has focused on TOR's routing protocol. We have established a theoretical statistical model of this network, based solely on information provided by the Tor Foundation (TOR\_Foundation, 2014b) and the deep analysis of the TOR source code. We have shown that the statistical law governing the route generation is a power law and not a normal or uniform law, the latter laws being more compatible with the level of security claimed for such a network. The analysis of a large number of routes via the Tor network has confirmed the validity of our model. In a second part, the analysis of this problem from the point of view of graph theory and sub-problems of optimal paths and vertex cover has made it possible to identify particular reduced subsets of nodes on which a large proportion of the TOR traffic depends. Taking control of these

nodes by an attacker could significantly damage the security of the TOR network.

The paper is organized as follows. Section 2 shortly presents what the TOR network is and how it works. Then Section 3 presents our statistical analysis of the TOR routing protocol. Section 4 refines our results through a combinatorial analysis. Before concluding in Section 6, we discuss in Section 5 how our results may impact the TOR general security. All data related to this study are publicly available on (Filiol et al., 2017).

## 2 DESCRIPTION OF THE TOR PROTOCOL

The TOR project is a complex architecture and due to lack of space we will only give a brief description of its structure and how it works, for the paper to be self-contained. The interested reader will find detailed information in (TOR\_Foundation, 2014b; TOR\_Foundation, 2014d; TOR\_Foundation, 2014a).

The *Tor Project Inc.* is a non-profit foundation located in Massachusetts. It was founded in December 2006 by seven computer scientists, including Roger Dingledine and Nick Mathewson. It is primarily responsible for software maintenance — including the Tor Browser and Tail — for the Tor anonymous network.

The Tor protocol is directly derived from a project developed within the *United States Naval Research Laboratory* in which Paul Syverson participated (Goldschlag et al., 1996; Syverson et al., 1997). Its purpose was to provide the armed forces with a network that provided TRANSEC and COMSEC. The Tor project was born in 2004 thanks to this laboratory which opened the source code and provided the necessary funding. Today the organization is funded by donors and government agencies, including the *US Department of State Bureau of Democracy* and the *German Federal Foreign Office* (see (Delong et al., 2018) for a deep OSINT analysis of the Tor project and foundation).

### 2.1 TOR Architecture

The Tor network consists of about 12,000 routers divided into two families, relays and bridges. The Tor Foundation publishes almost all the information in the first category, and quite nothing for the second category in order to prevent a state from denying access to the network because it does not have the IP addresses of these hidden nodes.

The Tor network is organized into several levels where routers have multiple roles. These depend on the trust placed in them by the network, which is particularly dependent on the time of activity. The different roles by level are:

- Four Authority levels are identified:
  - Nine *Directory authorities* and *Bridge authorities*. They list all the routers — relays or bridges — in the network, analyze the bandwidth, assign them a particular weight — depending on age, bandwidth and stability. They also assign specific roles to routers and establish, sign and publish a document called *consensus file*. The IP addresses of these servers are listed directly in the source code of TOR.
  - *Directory caches* that download authorities' data to cache them for distribution to customers who request them.
  - *Fallback directory mirrors* which are cache servers whose IP addresses are also written in the code. They allow clients to download the consensus file during initialization connection.
  - *HSDir* which are servers equivalent to the Internet DNS servers. They hold the information to contact a hidden service such as the addresses of the *introduction points*, defined below.
- For the TOR routers:
  - the *Exit* node is the third router of a circuit intended to transmit the network stream to the Internet.
  - the *Non exit* node is a router that only processes incoming or internal flows in TOR.
  - the *Entry* node is the first router to which a client addresses itself to go through TOR.
  - the *Guard* node is an input router to the TOR network. It also has the role of *non exit* router and can therefore process internal network flows.
  - the *Bridge* node (TOR\_Foundation, 2014d) is a router whose information is only partially published and whose purpose is to allow customers to bypass censorship. Currently, they are acting as *entry* routers. As for this particular class, we have developed an automatic extraction procedure which is non public. At the present time, a first list of more than 2,500 bridges (on a total number of 3,000-3,500) have been extracted (Filiol et al., 2017) as well as many information about the way bridges are managed behind the scene. Recently the Tor foundation has increased the number of bridges but this does not change anything with respect to our extraction procedure.

- To provide services within the network:
  - The *hidden service* is a server that will only accept incoming connections through a particular protocol. The initiators of the connection will not be able to learn the IP address of the service in order to preserve its anonymity.
  - The *introduction point* is a router (*relay* type) connected to a service hidden by a particular circuit and which allows a client to submit an appointment request for establishing a connection.
  - The *rendezvous Point* is a router (*relay* type) that connects two independently built circuits, one by a client and the other by a hidden service to allow end-to-end exchanges.

## 2.2 TOR Protocol Description

The TOR protocol manages two types of communications, either to the Internet network (external circuits, three routers) or to its internal network (internal circuits, six routers) through which an end-to-end flow will be exchanged between a client and a server.

To build TOR routes (or circuits), clients and servers of the TOR network build routes consisting of three second level routers. A route consists of an *entry* router, a *relay non-exit* router and a *relay* specific router depending on the type of communication.

From the client, the connection to the third server is either to an *exit relay* (connection to the Internet) or any *relay* (connection with a *hidden service*). In this latter case, a special protocol is used to establish the junction between two independently constructed circuits that meet at a point called *rendezvous point* (or RP).

## 3 STATISTICAL ANALYSIS OF THE TOR ROUTING PROTOCOL

We essentially focus on the public routers in the rest of the papers (external circuits). As far as bridges are concerned, it is sufficient to say that we have obtained similar results (6-node circuits) as for public routers. Other information are not public.

### 3.1 Consensus and Details Files

The Tor routing protocol relies on the consensus file which contains all the available TOR routers<sup>1</sup>. It is

<sup>1</sup>The file can be downloaded on <https://metrics.torproject.org/collector.html>

renewed every hour. It is downloaded by the Tor protocol during each first communication and then every two hours. This file is created, signed and published by the *authority* routers. It is also possible to retrieve enriched information, including probabilities by router type, by downloading the *details* file<sup>2</sup>. Essential information we need is:

- the router name and its fingerprint (in fact the SHA-1 value of its public key).
- IP address with useful ports.
- Router role and type.
- A weight called *consensus weight* which is voted by the *authority* servers and depends in particular on the bandwidth.
- Probabilities of choosing this type of router (*guard*, *middle*, *exit*) when establishing a route.
- An exit policy when the router belongs to the *exit* type as well as the ownership family, i. e. all the routers that belong to the same owner. This is provided by the latter if he wishes.
- A published bandwidth.

A very first analysis (see Figure 1) clearly shows that the distribution of routers is far from being uniform and exhibits a wide dispersion. In the minds of the



Figure 1: *middle* router probability distribution.

general public, the choice of each router is made randomly. This popular belief is false insofar as it implies that each node has the same probability of being chosen.

It remains to determine how the Tor protocol uses the weight assigned to a router when selecting a node of a circuit (TOR.Foundation, 2014c). First, it will use a random value (use of the OpenSSL library) and is considered to be of quality.

Building a circuit requires the choice of three separate routers. In the case of an external route, the protocol will have to choose a *guard*, a *middle* and a *exit* node. To make this choice, the protocol groups routers by type. If necessary, it eliminates routers that

<sup>2</sup><https://metrics.torproject.org/onionoo.html>

are not specification-compliant. Then, it computes the different sums of the weights and chooses a random value  $r$  between 0 and this sum. Finally, it scrolls through the list of the type considered by summing weights up to  $i$ -th rank such as  $\sum_{j=0}^{i-1} \text{weight}_j < r$  and  $\sum_{j=0}^i \text{weight}_j > r$ .

This choice is not *a priori* questionable since it weighs certain routers according to their stability, duration of network activity and available bandwidth. However, this weighting is already partly undermining the supposed equiprobability. After this first observation, it is important to study the extent to which this particular weight influences possible choices. Indeed, if it is possible to favor certain routers, it is therefore possible for the Tor foundation to restrict the choice of routers to particular subsets.

### 3.2 Theoretical Statistical Model

Since the open source code of Tor is very large and complex, we first implement the automatic extraction of all relevant data the writing of routers given by the *details* file and to analyze them. It has then been possible to find the links between probabilities and weights. Indeed, if we sort the routers by type *guard*, *middle*, *exit*, it appears that we have a constant ratio:

$$\frac{\text{consensus\_weight}_{\text{router}}}{\text{probability}_{\text{router}}} = C_{\text{router\_type}}$$

The constant value  $C_{\text{router\_type}}$  depends on the router type as follows:

- *guard* nodes:

$$C_{\text{guard}} = \sum_{i \in \text{guards}} \text{consensus\_weight}_i;$$

- *middle* nodes with *guard* flag set:

$$C_{\text{middle\_guard}} = \frac{C_{\text{guard}} \times C_{\text{middle\_guard}}}{C_{\text{guard}} - C_{\text{middle\_guard}}}$$

- *middle* nodes without any flag set:

$$C_{\text{middle\_seul}} = \frac{1}{2} \sum_{i \in \text{middles}} \text{consensus\_weight}_i;$$

- *exit* nodes:

$$C_{\text{exit}} = \sum_{i \in \text{exits}} \text{consensus\_weight}_i;$$

Moreover, we established other relationships between those values:

$$C_{\text{guard}} \approx \frac{C_{\text{middle\_guard}} + C_{\text{middle\_seul}}}{2}$$

$$C_{\text{middle\_guard}} \approx C_{\text{middle\_seul}} \times (1 + \sqrt{2})$$

All these relationships have been used to calculate the probability of choosing the next router knowing the choice of the precedent ones. Indeed, the specifications of the Tor network require that two routers on the same circuit do not belong to the same  $x.y.z.w/16$  subnetwork (class B) as well as to the same (Johnson et al., 2013) family. Finally, the Tor network seeks to optimize its own workload. This is why the *consensus* files are established every hour in order to change these weights by router. This has the effect of influencing client choices. Let us precise that a highly multi-threaded implementation enables to process any new version of the consensus file in less than 5 minutes (around 10 billions of possible routes).

In order to synthetize all these information and build our model, we used the following procedure:

1. Get the *details* file.
2. Count the router numbers (relay and bridges).
3. For the relay family, sort routers according to their type (*guard*, *middle*, *exit*) with respect to their weight.
4. For bridge routers as well as for nodes in the third position of an internal circuit, calculate an empirical probability and then sort all the routers in each category with respect to it.
5. Calculate the sum of weights or probabilities on parts of each type.

The results obtained show that the impact of weight is not negligible. Indeed, in the case of *middle* and *exit* routers, the probability of choice follows a power law that favors a minority since about 80% of the total weight is given to 20% of the nodes. The detailed mathematical results are given in Appendix.

It is therefore possible, with a good probability, to restrict the study of Tor routes to a part of them by considering only sub-sets of each type (Table 1).

After having determined the predominant parameter in the choice of routers and knowing the constraints imposed in the construction of a circuit, it is possible to generate all the routes and to accumulate for each router the conditional probabilities of being chosen given the circuit. By noting  $K$  the routers of a type which is compatible with the previous nodes,  $W_k$  the weight of router  $k$  and  $C_K$  the constant of the type considered, the probability  $P_i$  of the router  $i \in K$  is computed as follows:

$$P_i = \frac{W_i}{C_K}$$

The cumulation of these probabilities gives an occurrence for each of the roles for each router. The results of these occurrences for approximately 1 billion and 10 billion generated external circuits are presented in

Table 1: Fraction of ORs involved in different percentage of the Tor routes/traffic.

Proba	Guard fraction	Middle fraction	Exit fraction	Number of routes			
50%	1/2	81,6%	1/4	78,1%	1/4	78%	308 millions
66%	1/2	81,6%	1/3	85,5%	1/2	95,5%	823 millions
75%	2/3	91,0%	1/3	85,5%	1/2	95,5%	1,1 billion
100%	All	100%	All	100%	All	100%	9,9 billions

Appendix. A second important parameter is the number of routes to which a router may belong. Indeed, some routers may belong to fewer circuits than others but this difference is compensated by the weight. Conversely, some nodes may belong to all roads but are downgraded because of their low weight.

### 3.3 Testing of the Statistical Model

Our theoretical model must now be compared with what is observed within the TOR network in order to validate it or not. In order to have a representative sample with a margin of error of 1% and a confidence level of 99%, we must consider at least 16,500 TOR routes. We wrote a python script, using the *Stem* library developed by the Tor foundation. We have then extracted more than 60,000 routes considering a change of the router of entry or not <sup>3</sup>.

The comparison between the results obtained from the data extracted and processed by the algorithm and all generated routes validates our model. Figure 2 represents the occurrences obtained for the different types of routers when generating routes and shows that, according to the established model, they follow a power law. Therefore, the weight assigned to each router is the parameter that influences the choice made by the protocol (see Table 2). It is also important to look at the case of internal circuits (used to access to hidden services). In this case, the probability of the third router on the circuit cannot be established directly from the data provided by the Tor foundation. It was therefore necessary to identify the proportions of each type of router (*guard*, *middle*, *exit*) positioned in third position. Thus, it became possible to determine the constants necessary for calculating probabilities similarly to what was found for an external circuit since the probabilities of the third routers verify the equation:

$$\sum_{i \in \text{guard}} \frac{\text{poids}_i}{C_{\text{guard}}} + \sum_{i \in \text{middle}} \frac{\text{poids}_i}{C_{\text{middle}}} + \sum_{i \in \text{exit}} \frac{\text{poids}_i}{C_{\text{exit}}} = 1$$

The statistical analysis of the 60,000 routes revealed the following fractions for router types: about  $\frac{4}{7}$  are

<sup>3</sup>By default, the configuration freezes the entry router during connection initialization for a period of two to nine months

of *Guard* type, about  $\frac{5}{28}$  are *Middle* routers and about  $\frac{1}{4}$  are *Exit* nodes. These results are empirical but they identify the significant proportions of *relay* routers to be considered in the calculation of routes in the case of a study of internal circuits. Similar to external circuits, the study of routes can be restricted to subsets of nodes (see Table 3). It is important to note the ratio — in the order of 30 — that exists between the total number of routes and the number that we can study while considering 50% of the traffic. Finally, we have compared the observed and theoretical rankings of each router type according to the number of occurrences. The theoretical and observed results are not exactly identical but are very close. In other words, each ranking shows the same list for the most used routers in a slightly different order. This may be due to the fact that theoretical computation are made from the *details* file while the route generation took about two days. As a result, the weighting of each router may have slightly evolved during the votes in order to homogenize flows within the network. In addition, the study was conducted on a small but representative sample size but it is acceptable that on a large number of simulations, the results would converge to the theory.

## 4 COMBINATORIAL ANALYSIS OF THE TOR ROUTING PROTOCOL

The statistical approach has enabled the development of a model that has highlighted subsets of important routers within the Tor network through which a significant portion of traffic transits. However, it is possible to refine these subset if the network is modeled differently. Indeed, the previous study of routes has focused only on routers and not on the links between nodes. The purpose of this section is therefore to analyze how these links can favor some routes over others. This will also reveal that significant fractions of the flow are managed by a particular subset of nodes. Without loss of generality, this new model deals with at external circuits only and when the input router is

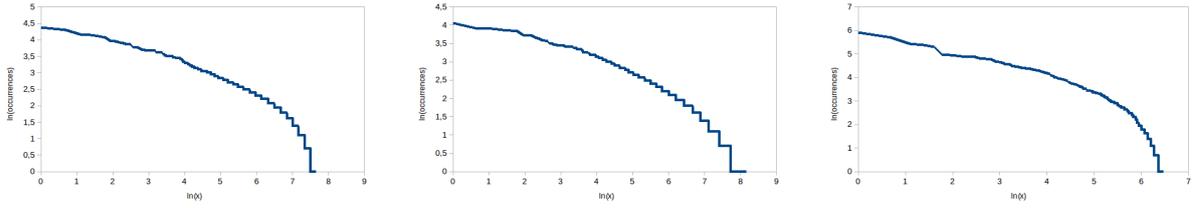


Figure 2: Observed frequencies of router types (*guard* on the left, *middle* in the center and *exit* on the right) with a log-log scale.

Table 2: Comparison of the theoretical model and the TOR reality.

Ratio	Guard		Middle		Exit	
	Theoretical	Virtually	Theoretical	Virtually	Theoretical	Virtually
1/4	58,16%	56,44%	78,1%	78,36%	78,01%	77,82%
1/3	67,40%	68,82%	85,49%	85,24%	86,22%	87,09%
1/2	81,59%	81,68%	94,05%	94,47%	95,53%	96,14%
2/3	91,02%	90,51%	98,44%	98,90%	98,98%	99,13%
3/4	94,29%	93,70%	99,35%	99,64%	99,66%	99,64%

Table 3: Fraction of ORs involved in different percentage of the Tor routes/traffic for internal circuits.

Proba	Guard fraction		Middle fraction		Relay fraction		Number of routes
50%	1/2	81,6%	1/4	78,1%	1/4	81,1%	2,7 billion
66%	1/2	81,6%	1/3	85,5%	1/2	95,5%	7,2 billion
75%	2/3	91,0%	1/3	85,5%	1/2	95,5%	9,6 billion
100%	All	100%	All	100%	All	100%	86,6 billion

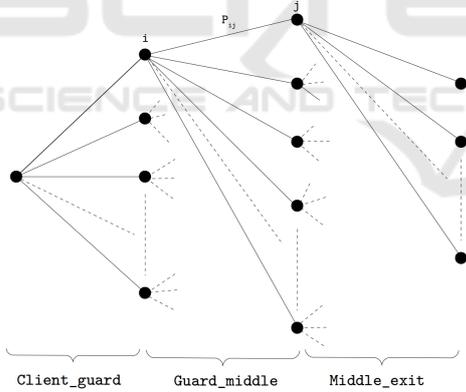


Figure 3: Graph model for the Tor routing protocol.

a *guard*. Additional results can be obtained by contacted the first author.

We modeled the network as a graph (Figure 3) to analyze the problem from a combinatorial perspective. Initially, the vision in *vertex cover* seemed to be the right solution, but given the weightings that cannot be taken into account effectively in this type of problems, we opted for an optimal path search. The purpose of graph modeling is to try to determine a relationship between the links *guard-middle* and *middle-exit*. Thus, routers are represented by vertices and the links by edges, the latter being characterized by a weight.

The calculation of these weights was a real difficulty, since it had to reflect the previous results obtained while being sufficiently discriminating to extract a particular relationship between the *guard-middle* and *middle-exit* links. The weight considered here is therefore a function of the number of routes that use this link as well as the weight of the destination routers. Indeed, previous calculations have shown that these two factors are predominant.

Let us note  $N$  the number of routes using edge  $i \rightarrow j$  (Figure 3),  $K$  the set of all destination routers which are compatible with the source router  $i$  and  $p_k$  the weight of the router  $k$ . The the weight  $P_{ij}$  of the edge  $i \rightarrow j$  is computed as follows:

$$P_{ij} = \frac{1}{N} \sum_{n=1}^{n=N} \frac{p_j}{\sum_{k \in K} p_k}$$

Since each  $i \rightarrow j$  edge has its own weight of  $P_{ij}$ , we calculate the ratio between the total sum of the weights of the links *guard-middle* and the total sum of the links *middle-exit*. This ratio is taken as a reference to calculate the proportions of each type of routers. In this case, the ratio is about three.

Therefore, in order to determine a subset of *exit* routers, it will be necessary to determine a subset of *middle* routers and then calculate the total weight of the links *guard-middle* considered (the determination

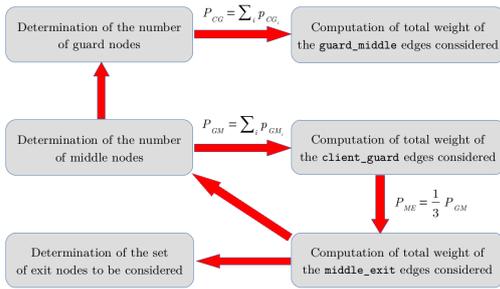


Figure 4: Algorithm description for router links analysis.

of the *middle* nodes leads to the determination of the *guard* nodes). In our case, we consider the strongest links. Then, to determine the totality of the *exit* routers, the total weight of *middle-exit* links is deducted from the one obtained above and, considering the most favorable links, the weights of the latter are summed until they obtain a value approaching that calculated (Figure 4).

This modeling has enabled to refine the number and identity of routers of each type that manage a significant proportion of the Tor traffic (Table 4) These

Table 4: Number of top-significant routers per percentage Tor traffic.

Fraction	Guard	Middle	Exit	Total
33%	755	899	166	1065
50%	1030	1217	246	1463
66%	1326	1617	342	1959
75%	1507	1882	425	2307

results thus refine the ratios between the *guard-middle* and *exit* types. Tables 1, 2 and 3 did not take into account the ratio calculated here. Finally, the route analysis confirms the *ratio* found between the number of routers in the *middle* node and the number found in the *exit* node subsets. Indeed, for three samples of about 5,000 routes in which the input router is fixed — according to the default configuration — as well as for a sample of the same size in which there is an input node rotation, the number of routers per type is given in Table 5.

Table 5: Number of top-significant routers for basic configuration.

	Guard	Middle	Exit
Sample 1 (4920)	1	2123	475
Sample 2 (4915)	1	2085	488
Sample 3 (4865)	1490	1976	478

## 5 DISCUSSION ABOUT THE TOR SECURITY

Results presented in Section 4 (especially Tables 4 and 5) prove that it is enough to target a reduced subset of nodes (only 1,463 nodes (1,217 *middle*, of which 1,030 *guards* and 246 *exits*) to control 50% of the traffic in Table 4). The interest for an attacker to identify these routers lies in the fact that it can take control of them and then analyze the traffic to correlate the flows (Johnson et al., 2013). Thus, it would be able to remove the anonymity of users — clients and hidden services — by tracking packets end-to-end through special patterns identified or set up in the packets. It seems that the FBI operated in this way when it dismantled the silk road in 2014 (TOR\_Foundation, 2015). The list of subsets we have identified is available in (Filiol et al., 2017). Similarly, in the case of internal circuits as well as in the case where the input router is a *bridge*, it is possible to identify similar subsets.

These node subsets of higher interest are then privileged targets for DDoS (mandatorily from outside the Tor network) or coordinated targeted malware attacks. Therefore, it is interesting to carry out a security analysis of the ports and services which are opened for each of them, since they can constitute potential entry points (a vulnerability scan to look for 0-day vulnerabilities is also a required step). We have used a massive scan tool designed in our lab to analyze top significant routers involved in 50% of the Tor traffic, as well as the first thousand ports and a few other frequently used ones. Table 6 summarizes the results. The results show that two thirds of routers have

Table 6: Open ports for top significant routers controlling 50% of Tor traffic.

Port	21	22	23	25	53
Number	70	631	17	573	121
Fraction (%)	4.7	42.1	1.1	38.2	8.1
Port	80	109	110	135	139
Number	843	3	64	561	561
Fraction (%)	56.2	0.2	4.3	37.4	37.4
Port	443	445	1133	1134	
Number	811	577	10	7	
Fraction (%)	54.1	38.5	0.7	0.5	

open ports because they also serve as SSH, SMTP, DNS, HTTP, POP, HTTPS servers. In addition, many routers have open ports that expose them particularly well. Ports 135,139 and 445 are of high interest for attackers. In addition, these ports are possible targets that can be overwhelmed by *syn flooding* attacks. This will cause a significant evolution of the *consensus* file, which may then favor some potentially trapped rou-

ters. Indeed, during the vote, the *authorities* will measure a low bandwidth.

As far as *bridge* routers are concerned, a corrupted machine in *middle* position could count the number of network frames it is relaying when constructing a circuit. It could then determine its own position and hence compare the IP address of the machine right before its own position with those listed by the foundation. It would enable to determine whether the input router is a *bridge* or not. In order to prevent such an attack, it is envisaged to always insert a *guard* router between the *bridge* and the *middle* router. Thus, hidden nodes would be drowned within network users.

## 6 CONCLUSION

Our study tends to prove that the security of the Tor network is not optimal. Indeed, since overall security is based on the individual good practices of the router owners, the maximum level that will be reached will not exceed that of the weakest link. The latter can also be set up voluntarily to identify particular users.

It is also important to note that local security (of nodes and servers, protocol strength...) is not sufficient as soon as we deal with a worldwide infrastructure. Having a more global and higher point of view is also important. In this respect, our study has showed the Tor infrastructure too much relies actually on a reduced number of nodes.

Our future work will mostly focus on two aspects. First, we intend to optimize our multi threaded consensus file processing algorithm. The aim is to be able to process any new version of such file and extract top significant node subsets within less than one minute. Second to go on working on the bridge management and its evolution and to refine our extraction algorithm.

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## APPENDIX

### Statistical Model for the TOR Routing Protocol

The results obtained seem to indicate that the distribution of TOR routes follows a power law distribution (general case including Pareto, Zipf, Mandelbrot laws). We will limit ourselves to the discrete case (however, when the number of data is large enough—which is our case—it is possible to work with the continuous version of this law (Clauset et al., 2009). For more detailed information of these laws the reader can refer to (Clauset et al., 2009; Alstott et al., 2014) we also used for statistical analysis.

A discrete variable  $X$  follows a Power law if its probability density is given by

$$p(x) = P[X = x] = C \cdot x^{-\alpha}$$

where  $\alpha$  is a constant parameter called *power parameter* of the law and  $C$  is the proportionality factor. In practice, most of the phenomena obey a power law for some  $x \geq x_{min}$ . The constant  $C$  is given by the value  $x_{min}$  using the fact that

$$\int_{x_{min}}^{\infty} p(x) dx = 1$$

This results in  $C = \frac{\alpha-1}{x_{min}^{-\alpha+1}}$

On a graph with logarithmic scales (log-log representation), the graph of a power law is a line since when noting  $y = P[X = x]$  we can write

$$\log(y) = \alpha \cdot \log(x) + \log(C)$$

Another useful representation is the inverse of the so-called cumulative cumulative distribution function ( $P[X[X > x] = 1 - F(x)$ ). This is the one we will use here to compare the theoretical law obtained with the empirical law of data. In the following we will limit ourselves to the estimation of the parameters  $\alpha$  (maximum likelihood method, validation by the Kolmogorov-Smirnov adequacy test) and  $x_{min}$  (exhaustive estimation on all the values minimizing the  $D$  value of the Kolmogorov-Smirnov test).

It should be noted that in few cases, the theory suggests that empirical data can be described by two laws, without any clear distinction between the two. In our case. In three cases, the log-normal law has been identified as a possible alternative, but relatively close to the power law. Let us recall that a random variable  $X$  follows a log-normal law if  $Y = \ln(X)$  follows a normal law of average  $\mu$  and standard deviation  $\sigma$  (denoted  $LOG - \mathcal{N}(\mu, \sigma)$ ).

For all possible routes (around 10 billions) we have results given in Table 7 and in Figure 5. For

Table 7: Results for all possible TOR routes ( $D$  represents the Kolmogorov-Smirnov distance between data and model).

Data	$\alpha$	$x_{min}$	$D$
Total nodes occurrences	1.89	1850	0.03
<i>Guard</i> nodes occurrences	3.16	5239	0.04
<i>Middle</i> nodes occurrences	3.09	1223	0.03
<i>Exit</i> nodes occurrences	2.45	21361	0.05

*Guard* nodes occurrences, let us mention the fact that the  $LOG - \mathcal{N}(7.38, 0.956)$  law is a possible alternative law.

Table 8 and Figure 6 provides the results for the top one billion routes. For the *Guard* nodes occurrences, we have  $LOG - \mathcal{N}(5.99, 0.661)$  as possible

alternative law while for the *Exit* nodes occurrences,  $LOG - \mathcal{N}(8.47, 0.827)$  can be also an alternative law.

Table 8: Results for 1-billion top TOR routes ( $D$  represents the Kolmogorov-Smirnov distance between data and model).

Data	$\alpha$	$x_{min}$	$D$
Total nodes occurrences	1.87	404	0.03
<i>Guard</i> nodes occurrences	3.09	519	0.04
<i>Middle</i> nodes occurrences	2.89	285	0.03
<i>Exit</i> nodes occurrences	2.99	11083	0.04

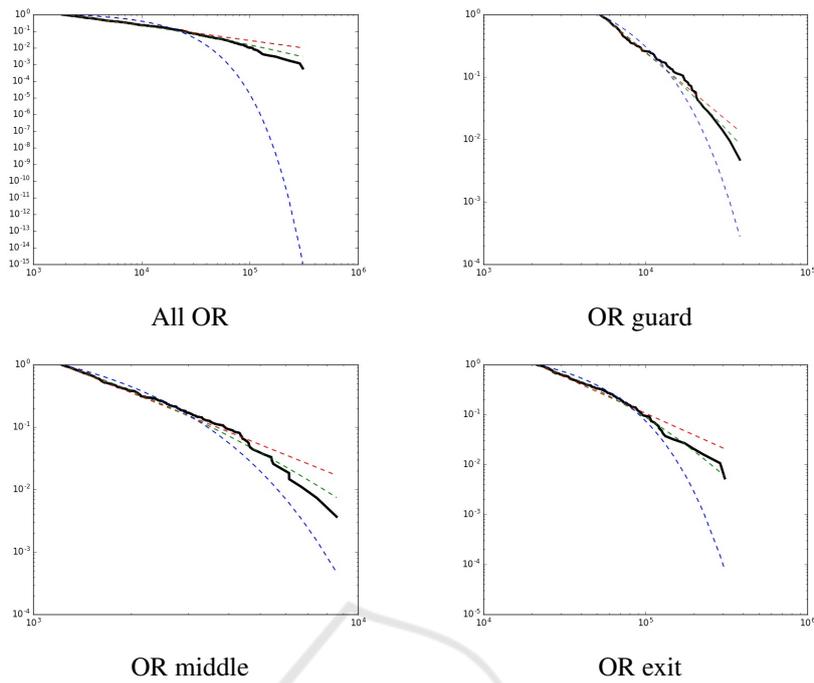


Figure 5: Inverse cumulative density functions of data compared to the fitted law. The red dotted line (resp. green and blue) describes the power law (resp. log-normal and exponential law).

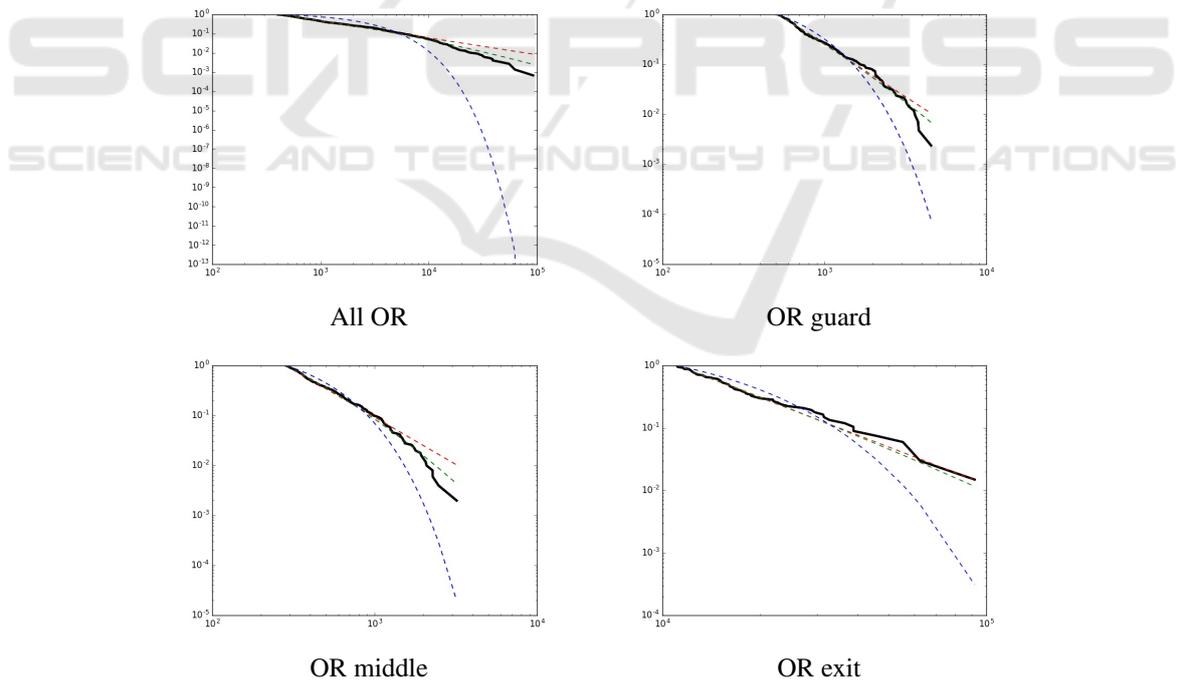


Figure 6: Inverse cumulative density functions of data compared to the fitted law (1-billion top TOR routes). The red dotted line (resp. green and blue) describes the power law (resp. log-normal and exponential law).