

Reducing Variant Diversity by Clustering

Data Pre-processing for Discrete Event Simulation Models

Sonja Strasser and Andreas Peirleitner

Institute for Smart Production, University of Applied Sciences Upper Austria, Wehrgrabengasse 1-3, Steyr, Austria

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Abstract: Building discrete event simulation models for studying questions in production planning and control affords reasonable calculation time. Two main causes for increased calculation time are the level of model details as well as the experimental design. However, if the objective is to optimize parameters to investigate the parameter settings for materials, they have to be modelled in detail. As a consequence model details such as number of simulated materials or work stations in a production system have to be reduced. The challenge in real world applications with a high variant diversity of products is to select representative materials from the huge number of existing materials for building a simulation model on condition that the simulation results remain valid. Data mining methods, especially clustering can be used to perform this selection automatically. In this paper a procedure for data preparation and clustering of materials with different routings is shown and applied in a case study from sheet metal processing.

1 INTRODUCTION

Manufacturing companies are faced with challenging market situations. An increasing number of high customized products have to be produced in shorter periods of time in order to be competitive. The fulfilment of customized orders results in a high variant diversity and a high process variety (Jiao et al., 2005). To manage this complexity successfully, optimized decisions in production planning and control are essential. As a result of optimized planning decisions low costs, a high service level, short lead times and a stable production can be achieved.

Since analytical models for optimization often lack the practical applicability, discrete event simulation can be used to study the impact of certain decisions in production planning and control. With simulation the influence of different production planning strategies (Huang et al., 1998, Jodlbauer and Huber, 2008) or different dispatching rules for production systems (Kutanoglu and Sabuncuoglu, 1999) can be compared and capacity estimations of production systems can be made (Abdul-Kader and Gharbi, 2002). For a discrete event simulation study the most time consuming phase is the input data collection and the model development (Perera and Liyanage, 2000, Randell and Bolmsjo, 2001). So

efforts are made to develop flexible discrete event simulation structures in an object oriented environment (Borenstein, 2000, Anglani et al., 2002). The developed simulation generator (SimGen) for analysing production planning problems enables the implementation of simulation models which are parameterized by a database (Hübl et al., 2011). Running simulation models can become a runtime intensive task for instance in combination with heuristic optimization methods for determining optimized production planning parameters. So the number of different materials which can be simulated is limited, however real data from manufacturing companies often include a high variant diversity. The challenge for building a simulation model under such conditions is to reduce the number of materials while maintaining valid simulation results. Doing this selection manually can become a very time consuming task and so a framework using methods from data mining, in particular clustering, is proposed in this paper.

First related work for clustering products or processes is discussed. Then the simulation generator SimGen and its necessary input data are described in more details. In the next section a framework for data pre-processing including the reduction of material numbers by clustering is presented. Towards the end of the paper the proposed framework is applied in a case study from sheet metal processing.

2 RELATED WORK

Clustering is an unsupervised method in data mining. Unlike classification (supervised learning), clustering doesn't rely on predefined classes. Clustering partitions data sets into groups according to their similarity. Within one cluster, examples are similar to one another and are dissimilar to objects in other clusters (Han and Kamber, 2006). In manufacturing the major areas where clustering is used are customer service support, fault diagnostics, yield improvement and engineering design (Choudhary et al., 2009).

In variant design it is advantageous to organize the wide variety of products in clusters of similar products (product families). Therefore it is necessary to measure the distance between products based on bill of materials (Romanowski and Nagi, 2005). A bill of materials (BOM) is a hierarchical, structured representation of products that contains information about necessary parts, raw materials and quantities. Forming generic bills of material (GBOMs) that represent the different variants in a product family can be used to facilitate the search for similar previous designs and the configurations of new variants (Romanowski and Nagi, 2004).

Another framework for identifying product families based on data mining techniques is presented in Chowdhury and Nayak, 2014. Here an Extended Augmented Adjacency Matrix (EAAM) is proposed as a representation of the BOM. Cosine similarity is used to generate a similarity matrix of the EAAM representations which is the input for a clustering algorithm.

High product variant diversity results in a high process variety and raises the importance of addressing the correspondence between these varieties in order to make good planning decisions and maintain a stable production (Jiao et al., 2005). In their approach the coordination between product and process variety is based on the unification of BOM data and routing data. Routing data describes the sequence of operations which are executed to manufacture a certain product and includes specifications for production planning like set-up and processing time. With a product-process variety grid, for each customer order, the product design in terms of BOM and production process can be configured.

Companies face a similar challenge when generating assembly process plans in an environment with high product and process complexity. Clustering techniques can be used to identify similar products or assembly processes and to group them according to the similarity of their characteristics. Beyond that, classification can be applied to classify new assembly

structures into the identified clusters (Wallis et al., 2014).

Another application of clustering algorithms is the solution of cell formation problems in the design of cellular manufacturing systems. This requires the identification of machine groups that can produce parts with similar processing requirements. Alhourani, 2013 developed a procedure for solving the machine-part grouping problem using the Similarity Coefficient Method. In this approach important production data such as operations sequence, production volume, lot size and routings are considered.

In the framework presented in this paper, similar production data is taken into account, but here the objective is to group similar materials together in a cluster, not the machines. In our approach it is not proposed how to arrange machine into manufacturing cells, this is assumed as given. In contrast the goal is to identify similar materials. This is the prerequisite for reducing a huge number of materials to a manageable variant diversity for simulation modelling.

3 SIMULATION OF PRODUCTION SYSTEMS

A central issue of discrete event simulation in the field of production planning and control is the investigation of different parameter settings and planning strategies in order to minimize overall costs for inventory, setup and tardiness or maximize service level. In the following the Simulation Generator SimGen and the necessary input data for the simulation models is presented.

3.1 Simulation Generator SimGen

The Simulation Generator SimGen, as presented in Hübl et al., 2011, Felberbauer et al., 2012 or Felberbauer et al., 2013 is a generic, scalable simulation model and is parametrized by a database. The advantage of the generic and scalable simulation model is, that on model start up the necessary data is loaded from the database and the production system structure is generated automatically. Thereby, different simulation scenarios can be defined without any adaptation of the simulation model itself and model functionalities can be reused. The logic is implemented in the simulation model but the parametrization is stored in the database and loaded on model start up. In the simulation model a

hierarchical production planning concept is implemented, using Material Requirements Planning (MRP). For all materials MRP production orders are generated including start and end dates and quantities. Then the four steps netting, lot sizing, backward scheduling and BOM explosion are performed. The input parameters for MRP are, among others, planning parameters for the materials and the BOM.

3.2 Input for Simulation Models

The input data for the simulation model is exported from the Enterprise Resource Planning Systems, pre-processed and then stored in the database. Necessary input data sets are:

- BOM
- Routing data including setup and processing times
- Production planning parameters like lot sizes, planned lead times and safety stock for all materials
- Shift calendars defining the available capacity, including holidays
- Skill groups and number of employees
- Production program and forecast for end items
- Customer demand, order amount size and corresponding customer required lead times

If product variant diversity is very high, this leads to long computation times and an inappropriate level of model details. Therefore for a simulation study on optimal settings of planning parameters it is desirable to reduce the number of materials to a reasonable amount which does not harm the objective of the simulation study.

4 FRAMEWORK FOR REDUCING VARIANT DIVERSITY

In this section a framework for selecting representative raw materials from a huge number of existing materials is presented. This framework can be divided in two phases. In the first phase, the necessary input-data has to be collected and different data preparation steps are done. These steps are necessary to make the data useable for the application of the following clustering steps in the second phase.

4.1 Input-data

For the proposed approach two input data sets are needed: a data set with the information of the bill of

material and another data set with the corresponding routing of the materials in the production process.

4.1.1 Bill of Material Data (BOM Data)

The relationships between end items, subassemblies (SA) and raw materials (RM) is described by the bill of material (see Figure 1). We assume that P different end items are built from N subassemblies and each subassembly can consist of different raw materials which we denote shortly by materials. The number of different materials is indicated with M .

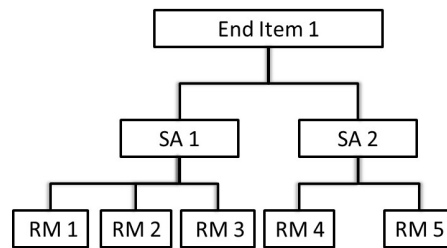


Figure 1: Bill of Material.

BOM data is stored in a company's database, but there are no common guidelines concerning the formatting and the attributes. For our purpose we need a table of BOM data with the following attributes (in columns):

- Material ID to identify each material uniquely.
- Subassembly ID related to the material in the first column to identify the corresponding subassembly uniquely.
- End item ID related to the subassembly and the material in the first two columns to identify the corresponding end item uniquely.
- Applied lot size policy for the material in the first column, e. g. fixed order period (FOP), lot-for-lot (LFL), fixed order quantity (FOQ), consumption-based (CB).

If there are multiple end items with the same combination of raw material and subassembly then multiple rows in this input file are needed. The material ID and end item ID are mandatory attributes. All the other attributes are optional and can be complemented by other attributes which are important in a certain production environment.

4.1.2 Routing Data

A routing describes the sequence of workstations passed through by a material in the production process (Hopp and Spearman, 2008). The necessary routing data has to be stored in a table with the following attributes (in columns):

- Material ID to identify each material uniquely.
- Work station (identified with a unique ID)
- Standard time at the corresponding work station.
- Operations sequence number to define at which position this work station is used to process the material

If the standard time isn't available by default, it can be calculated by the sum of processing time and the quotient of set-up time and average lot-size. Since commonly each material is processed by several work stations, there are multiple rows in the routing data table which correspond to the same material in order to represent the whole operations sequence.

4.2 Data Preparation

In the first phase of the framework four steps of data preparation are carried out (see Figure 2).

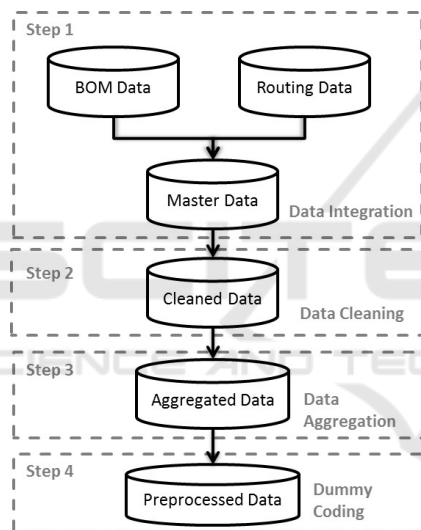


Figure 2: Data Preparation Steps.

4.2.1 Data Integration

As a first step the BOM-data and the routing data have to be joined into a common master table, whereby the material ID serves as primary key attribute. The master table includes the attributes material, subassembly, end item, lot size policy, work station, standard time and operations sequence number.

4.2.2 Data Cleaning

In the data cleaning step examples with missing values should be removed just like duplicate rows which can occur for various reasons. Work stations which are not relevant for building the simulation model can be filtered. In some situations it can be

useful to combine similar work stations to a new group of work stations if they perform the same processing step. Finally for the sake of clarity the master table should be sorted by end item, subassembly, material and operations sequence number. Now the operations sequence of each single material of a certain subassembly and end item can be read in subsequent rows.

4.2.3 Data Aggregation

The goal of this step is that the operations sequence of each material appears in a single row and the sequence of the workstations is displayed as a new attribute. This can be achieved by data aggregation for each end item and each subassembly in nested loops. The data is grouped by material ID and the other attributes in the aggregated data table are the mode of the lot sizing policy, the sum of the standard times, the operations sequence, subassembly ID and end item ID.

4.2.4 Dummy Coding

There are two categories of attributes in the aggregated data. On the one hand attributes like lot size policy, sum of the standard times, operations sequence and subassembly are attributes which will be used for clustering in the second phase of the proposed framework. On the other hand the attributes material ID and end item provide information for a unique identification and should not be included for building clusters.

Further the operations sequence as a single nominal attribute is not appropriate for clustering. Measuring similarity of two materials would deliver 1 if there are identical sequences and 0 otherwise, even if there is only a slight difference. For this reason the operations sequence is split up into single work stations and new attributes are generated by dummy coding. Every work station defines a new attribute which has value 1 if the material is processed at this work station and 0 otherwise. In this way we get various numerical attributes instead of one nominal attribute. But measuring similarity of two materials has more gradations now. The only thing which cannot be detected by this kind of coding is the chronological order of the operations. Operations sequences A-B and B-A have identical attributes and therefore a distance of 0. For practical application this is negligible. Usually, due to technical dependencies, the sequence of operations cannot be changed (e.g. turning – milling – drilling).

In order to get only numeric attributes, dummy coding is also applied to the lot size policy and the

subassembly ID. This enables the use of k-means clustering in the next step.

4.3 Clustering and Selection of Materials

The goal of the second phase of the proposed framework is the selection of representative materials for each end item to reduce the high variant diversity. This phase consists of two steps: The application of a clustering method for each end item and the selection of representative materials of each cluster (see Figure 3). For clustering the k-means algorithm is applied because k-medoid results in considerable longer calculation times and worse performance regarding the average distance within each cluster.

4.3.1 k-Means Clustering

As all attributes in the prepared dataset are numeric, k-means clustering can be applied. There are two parameters which have to be defined for this data mining method: the number of clusters k and a measure to define the similarity of two examples. In the proposed framework clustering is applied for every end item. As end items consist of different numbers of materials the number of clusters has to be adjusted to the number of materials:

$$k_i \approx \frac{m_i}{c} \quad (i=1, \dots, P) \quad (1)$$

where k_i denotes the number of clusters and m_i the number of materials of end item i . The number k_i is rounded to the next integer. Constant c is determined by selecting a number K of desired representative materials (so that running the simulation model is within an acceptable time-frame) and the assumption that every cluster delivers one representative:

$$K = \sum_{i=1}^P k_i = \frac{1}{c} \sum_{i=1}^P m_i = \frac{M}{c} \Rightarrow c = \frac{M}{K} \quad (2)$$

For measuring the similarity of two materials we use cosine similarity:

$$\cos(A, B) = \frac{A \cdot B}{\|A\| \|B\|} = \frac{\sum_{i=1}^I A_i B_i}{\sqrt{\sum_{i=1}^I A_i^2} \sqrt{\sum_{i=1}^I B_i^2}} \quad (3)$$

where A and B are two row vectors in our dataset with I attributes. RapidMiner provides different numerical measures for clustering. But an analysis with the data

of the case study (see section 5) reveals that cosine similarity outperforms other numerical measures comparing them by averaging the distance between the centroid and all examples of a cluster.

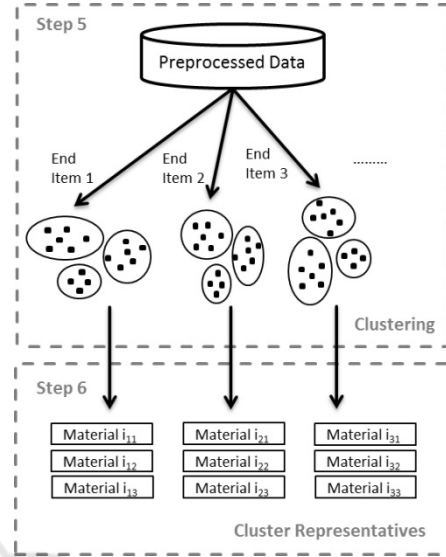


Figure 3: Clustering Steps.

The basic idea of k-means can be described by the following steps:

- Step 1:* Initialize k different cluster centroids.
- Step 2:* Calculate the similarity between every example and every cluster centroid
- Step 3:* Assign each example to the most similar cluster centroid.
- Step 4:* Update the cluster centroid for each cluster by calculating the arithmetic mean of all corresponding examples.
- Step 5:* Repeat steps 2, 3 and 4 iteratively until no change in the mapping of the examples occur.

This data mining method is applied to every end item i and the result is the grouping of all relevant materials into k_i clusters.

4.3.2 Selection of Cluster Representatives

As a final step the selection of cluster representatives is performed. Choosing the cluster centroid as cluster representative results in unrealistic values of attributes, because for instance decimal values can occur for integer attributes. So the material with the highest similarity to the cluster centroid is selected as cluster representative. This step delivers k_i representative materials for end item i and all in all K materials are selected for the further use in the simulation model.

5 CASE STUDY

The described concept is applied to real-life manufacturing data from sheet metal processing. The high variant diversity in this production is represented by 40,000 different material numbers, 400 subassemblies, 40 end items and up to 1,500 production orders every day. In a simulation model of the complete sheet metal processing different questions of production planning and control have to be studied.

To guarantee a reasonable calculation time for the simulation runs, the number of different materials has to be reduced to a size of approximately 1000. Doing this manually is a challenging and time consuming task. So the framework shown above was applied with RapidMiner 7.3, an open source software tool for data mining and machine learning (Mierswa et al., 2006).

5.1 Input Data

From the company’s databases the necessary input data was extracted and saved in two different Excel-files. The BOM-table includes 54,265 examples with five different attributes:

- material ID
- subassembly ID
- end item ID
- corresponding business unit
- applied lot size policy

The routing-table consists of 369,535 examples with six different attributes:

- material ID
- material name
- work station
- process ID
- operation description
- planned standard time (in hours)

The process ID includes information about the sequence of the sheet metal processing steps. Sorting the examples of the routing-table with a particular material ID by ascending process ID results in a correct sequence of the work stations which are run by this material.

5.2 Data Preparation Steps

In the first phase of the framework the data preparation steps according to section 4.2 are performed. In the data cleaning step the business unit which should be simulated is selected and only work stations for in-house-manufacturing are extracted. (External processing is not part of the simulation

model.) Another simplifying step was the aggregation of all work stations with laser cutting.

To get the right sequence of work stations for every material ID (for a certain end item and subassembly) the examples are sorted by end item, subassembly ID, material ID and process ID (see Table 1). For instance for end item 1, subassembly 135 the material 30700 is passed from work station W1 to W5 and W4 with lot size policy fixed-order quantity 1. The standard times on these three work stations are 0.011, 0.15 and 0.022 hours. After this preparation step the dataset contains 183,103 examples.

Now all examples are aggregated by material ID and the work stations are concatenated as a string to represent the operations sequence for this material. The attribute process ID is omitted in this aggregation, it only served as an auxiliary attribute for the sequence generation. Before proceeding with clustering the sequence of work stations, the sub assembly ID and the lot size policy are transformed by dummy coding as described in section 4.2.4. The result for the sample dataset after this aggregation is shown in Table 2. For instance, material 21000, which belongs to subassembly 135 and end item 1, passes through the work stations W1 and W2 with total standard time of 0.084 hours and lot size policy Fixed-Order Period 28. After the aggregation step 34,192 examples with 119 attributes are available. Apart from the end item, material ID and the total standard time 75 different work stations, 37 different subassemblies and 4 different lot size policies generate the remaining attributes.

Table 1: Sample dataset after data preparation.

| End Item | Sub assembly ID | Material ID | Work Station | Process ID | Lot size policy | Standard time |
|----------|-----------------|-------------|--------------|------------|-----------------|---------------|
| 1 | 135 | 21000 | W1 | 1 | FOP28 | 0.044 |
| 1 | 135 | 21000 | W2 | 2 | FOP28 | 0.040 |
| 1 | 135 | 30700 | W1 | 1 | FOQ1 | 0.011 |
| 1 | 135 | 30700 | W5 | 3 | FOQ1 | 0.150 |
| 1 | 135 | 30700 | W4 | 4 | FOQ1 | 0.022 |

Table 2: Sample dataset after aggregation by material ID.

| End Item | Material ID | Total standard time | W1 | W2 | W3 | W4 | W5 | Sub assembly = 135 | FOP28 | FOQ1 |
|----------|-------------|---------------------|----|----|----|----|----|--------------------|-------|------|
| 1 | 21000 | 0.084 | 1 | 1 | 0 | 0 | 0 | 1 | 1 | 0 |
| 1 | 30700 | 0.173 | 1 | 0 | 0 | 1 | 1 | 1 | 0 | 1 |

5.3 Clustering Steps

In the second phase of the framework the k-means clustering algorithm is performed on the aggregated dataset for 37 different end items separately. The

number of desired representative materials is specified with $K = 2,000$ considering that various materials will appear in multiple clusters of different end items and so the number of different representative material will be much smaller than 2,000. The number of clusters k_i for end item i is calculated according to formula (1) and it varies from 5 to a maximum of 141.

Then immediately before the clustering algorithm, the standard time is transformed to a range of 0 to 1 to make it comparable to all other attributes which are binary. Cosine similarity is used to measure similarity between examples and k-means clustering is applied to every end item. The results are 37 cluster models with different number of clusters and materials. For instance 562 materials which are part of end item 35 are grouped in 28 clusters. Within one cluster there are materials with similar properties concerning the operations sequence, the type of subassembly, total standard time and lot sizing policy. To illustrate the result of this cluster model, the number of materials and the number of different operations sequences are displayed in Figure 4.

In the final step the cluster centroids are calculated for every cluster of each end item. Then for every cluster the similarity between the cluster centroid and all examples belonging to this cluster is calculated. Cosine similarity is used here again and the material with the highest similarity is chosen as representative material for this cluster.

This procedure results in a list of 1711 representative materials. This number is smaller than $K = 2000$, because it can happen that some of the clusters are empty. Furthermore some materials appear multiple times in this list of representatives. For instance the most frequent representative material can be found in 18 different end items. But the majority of 945 materials are unique. All together we determined 1183 different materials by this approach. This is a magnitude of material which can be used in SimGen to generate a simulation model of the sheet metal processing.

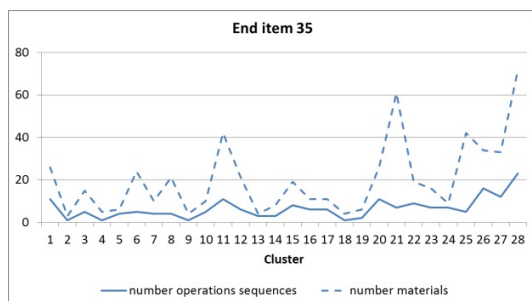


Figure 4: Number of materials and operations sequences for end item 35.

Table 3: Frequencies of representative materials.

| absolute frequency | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 11 | 18 |
|--------------------|-----|-----|----|----|----|---|---|---|---|----|----|
| number materials | 945 | 112 | 58 | 28 | 18 | 9 | 6 | 4 | 1 | 1 | 1 |

6 CONCLUSIONS

Real world manufacturing environments are generally too complex to be modelled in discrete event simulation accurately. The proposed framework shows how to select a manageable and representable number of materials for simulation modelling. For this purpose the necessary input data and preparation steps are shown in a first phase of the framework. In the second phase a clustering algorithm is applied to group similar materials and finally one representative material is selected from each cluster. This approach was applied in a case study to real world manufacturing data from sheet metal processing.

In further research the proposed framework should be applied to other real world scenarios and a comparison to other heuristic approaches for selecting material is planned. The results of multiple simulation runs have to be compared in order to evaluate if the proposed framework delivers better results than simple heuristic selection criteria. If the results are promising this framework should be integrated in the developed simulation generator SimGen as an automatic data pre-processing step for simulation modelling.

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