# On the Implicit Cost Structure of Service Levels from the Perspective of the Service Consumer

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Abstract: As services are ubiquitous in the modern business landscape, there is the need to define them in a binding legal framework, the Service Level Agreement (SLA). The most important aspect of a SLA is the agreed service level, which specifies the availability of the service. In this work, we discuss a simple mathematical service model, where the availability of a service is based on a singular resource. In this model one can relate the parameter of a linear cost structure to the purchased service level. Based on this relation we formulate a rule of thumb enabling a service consumer to check if an agreed service level fits their cost structure.

### **1 INTRODUCTION**

Driven by economic pressure to increase revenue and to adapt to market changes (Allen and Higgins, 2006, Cherbakov et al., 2005, Oliva and Kallenberg, 2003), organizations increasingly incorporate cloud services into their operations (Wieder et al., 2011). The control objectives for services are negotiated in terms of Service Level Agreements (Office of Government Commerce, 2007), which define not only scope and responsibilities but also quality and availability of a specific services into an enterprise architecture, both system engineers and senior management have to decide on the appropriate service level to purchase.

There is comprehensive literature discussing the optimal infrastructure allocation for providing a certain service level (Chaisiri et al., 2012, Della Vedova et al., 2016), calculate the Return-on-Investment of different cloud strategies (Misra and Mondal, 2011) or to estimate their costs (Truong and Dustdar, 2010), or quality-of-service management in general (Ardagna et al., 2014). However, there are hardly any guidelines for cloud computing customers on how to select a cost-optimal service level for a service.

On the other hand, for specific applications such as single and multi-stage inventory systems planing, it is known from operations research that restrictions about the availability of a service entail assumptions about the underlying cost structure (Van Houtum and Zijm, 2000). By applying and extending the concepts of an inventory planning model to the perspective of a cloud service, we are able to derive a relation between cost structures and cost-optimal service levels. This link is based on the stochastic demand of the service for a singular resource, which is typically modeled as a probability density function and can be computed by predictive analytics and machine learning approaches. The calculations will result in a simple rule of thumb enabling system engineers and senior management to either calculate the cost-optimal service level to purchase from a known cost-structure, or estimate the assumed cost-structure from actual service-levels.

We develop an elementary service model, which considers both service level restrictions and cost structures in Section 2. Assuming piecewise-linear cost functions, the service model allows to determine cost-optimal decisions (Section 3) and to estimate the ratio of investment and opportunity costs from the perspective of the service consumer. Finally, the model allows to directly relate a specific service level to the internal cost structure of the service consumer (Section 4). The paper closes with a discussion of related work (Section 5) and a conclusion (Section 6).

## 2 THEORETICAL BACKGROUND

In economics, a service is an intangible commodity. Contrary to goods it cannot be stored nor owned. Vargo and Lusch (2004) define a service as the ap-

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plication of competences for the benefit of another entity. Their service-dominant logic concludes that all economic activity is an exchange of service for service. Examples for services might be the guaranteed uptime of an elevator (thyssenkrupp Elevator AG, 2016), machinery (Yan, 2015), the highperformance computing infrastructure for executing big data pipelines (Kempa-Liehr, 2015), or the cloud provisioning of infrastructure, platform or software (Furht and Escalante, 2010).

For our purpose, the service definition of Vargo and Lusch (2004) is too general. Instead, we precisely have to define our service and the respective model: Because our service model takes the perspective of the service consumer, it is assumed that the service directly depends on a specific technology artefact, which might be characterized by its availability (e.g. production machine) or a measurable capacity (e.g. network bandwith or computational resource). Further, we assume that the demand of the service for the singular resource is non-deterministic. It is not known beforehand exactly how much of the resource the service will consume in a given time interval.

**Definition 1** (The service model). We inspect a singular service, which depends on a specific resource with adjustable capacity  $\hat{Y}$ . The consumption of the resource is non deterministic and is modelled as random variable Y with probability density / mass function  $f_Y$ , the so-called demand function, which is estimated from historic demand. The service availability might have one of three different relations with respect to the provided capacity  $\hat{Y}$ :

- S1 The service is not available if and only if  $\hat{Y} < Y$ ,
- *S2* the service is not available if and only if  $\hat{Y} > Y$ , or
- S3 another more complex relation.

Similar mathematical formulation of services can be traced back to the 1960s, originating from the field of statistical decision theory (Schlaifer and Raiffa, 1961). However, the review of Chase and Apte (2007) explains that the scientific discourse on service operations already started in the beginning of the last century.

For the following considerations, we assume service relations of type S1 or S2. A service of type S1 cannot be provided, if its capacity  $\hat{Y}$  has been underestimated. The same situation would arise for a service of type S2, if its capacity had been overestimated. Essentially, providing capacity  $\hat{Y}$  is a decision concerning the expected demand Y as observed from historic data. In cases, for which the costs for underestimating and overestimating the demand are similar, one wants to choose  $\hat{Y}$  as close to Y as possible, in order to minimize the costs resulting from prediction errors.

As an example for a S1 relation, Y could denote the workload of a specific web server cluster (Roy et al., 2011). If the cluster is generously sized in order to serve even historically observed peak loads, most of the infrastructure will be idle most of the time. Thus resources are waisted. On the other hand sizing the cluster only to the expected average workload will discourage consumers and decrease revenue.

Regarding the type S2 relation, one could think of a service consisting in operating a machine without any incidents (Yan, 2015). Then, Y could for example denote the remaining lifetime of a critical part of such machine, and  $\hat{Y}$  would be the next inspection interval. If the lifetime of this part comes to an end before the machine has been inspected, the machine will break. Hence, by overestimating the lifetime, so  $\hat{Y} > Y$ , and triggering the replacement too late, the machine could stop, resulting in high costs.

From the perspective of decision modeling, the most important information for sizing the service is the demand function  $f_Y$ . In order to illustrate  $f_Y$ , we inspected the Click data set from Meiss et al. (2008). It contains all unencrypted HTTP requests that fit into a single 1,500 byte Ethernet frame, pass through TCP port 80, and have been captured by a FreeBSD server positioned at the edge of the network of the Indiana University. Figure 1a contains the captured number of packets for one week, summed up to thousand packages per hour.

Applying concepts of machine learning and predictive analytics, the demand function can be estimated from historic data either as stationary distribution or as conditional distribution depending on day of the week and time of the day (Fig. 1b). The conditional density functions depicted in Fig. 1b have been computed with Bayesian linear regression (Bishop, 2006) both for workdays (blue) and weekends (green). In this example it has been assumed that the monitored service had been oversized, such that the observed traffic hasn't been influenced by infrastructure restrictions and the service was available for all times ( $Y < \hat{Y}$ ). In light of our service model, this refers to a S1 type service relation.

### 2.1 The Service Model for Multiple Periods

Now we expand our service model from Definition 1 to a possibly infinite number of periods by applying it to each period as illustrated in Figure 2.

For this purpose, the conditional demand distribution  $f_Y$  is assumed to be estimated from historic data (cf Fig. 1b).

With our model being observed over multiple pe-



Figure 1: Network traffic at Indiana University (Meiss et al., 2008). (a) HTTP packets per hour for an exemplatory week. (b) Conditional demand functions for weekdays  $f_{Y|Mo-Fr}(h)$  (blue) and weekends  $f_{Y|Sa,So}(h)$  (green). The shaded areas indicate the  $2\sigma$ -confidence interval of the predicted demand function. The dotted curves represent the  $Q_{95}$  quantiles and adjusting the respective resource to these quantiles would realize service levels of 95%.

riods, we can inspect the number of periods where the service was available. In logistics or supply chain management the related  $\alpha$  or type 1 service level is the probability that all customers' orders will be handled (Yıldırım et al., 2005). This is a measure for the Quality-of-Service (QoS), which we will now formalize:

**Definition 2** ( $\alpha$  service level). An  $\alpha$  service level describes the availability or uptime of a service, the percentage of time periods a service is available. It is calculated by taking the ratio between the time the service is available and the time it is observed.

In our service model, the  $\alpha$  service level denotes the percentage of periods for which the respective service is offered. It is the percentage of periods where  $\hat{Y} > Y$  for relation S1 or  $\hat{Y} < Y$  for relation S2. For ex-



Figure 2: Extension of the service model to multiple periods. This figure shows an exemplary service of relation type S1 where the same amount  $\hat{Y}$  of the resource is provided for all periods. For one period (red bar) the service is not offered due to the stocked amount  $\hat{Y}$  being lower than the consumption Y by the service.

ample, an  $\alpha$  service level of 50% means that a service will be up for half the periods that it was under investigation. Further, if the length of the periods converges to 0, the  $\alpha$  service level will converge to the overall availability of the service.

By Definition 1 the availability of the service only depends on one resource. Hence, we can relate the  $\alpha$  service level to the resource demand distribution  $f_Y$ :

**Lemma 3** (Relation between  $\alpha$  service level and quantile of demand function). For service model S1 with known demand function  $f_Y$  the  $\alpha$  service level of y% is realized by restricting the available capacity  $\hat{Y}$  to quantile  $Q_y$  of demand function  $f_Y$ . In the opposite service relation case S2 the quantile  $Q_y$  of  $f_Y$  corresponds to an  $\alpha$  service level of (1-y)%.

Lemma 3 allows to calculate the amount of  $\hat{Y}$  that we need to assure a defined service level availability:

**Example 4.** Consider a service that consists of offering a fast high speed internet connection to a client. Then, let Y be the maximal used bandwidth over the individual periods and  $\hat{Y}$  the provided bandwidth. If the maximal usage during the peaks are higher than the offered bandwidth, so  $\hat{Y} < Y$ , the clients will experience slowdowns and the service is not offered. If one continuously adapts the available bandwidth  $\hat{Y}$  to quantile  $Q_{95}$  of the estimated demand function (Fig. 1b), the service will have an average availability of 95%, so in 95% of the periods it will be offered without slowdowns.

Other examples for resources the variable *Y* could quantify are the number of servers, available disk space or offered computational units for cloud services. The majority of cloud relevant examples are

of type S1.

#### 2.2 Cost Structure

Every business process has a related cost structure, that incorporates all relevant aspects such as products, customers, services etc. (Osterwalder et al., 2005, Zott et al., 2011). The cost structure denotes the types and relative proportions of consumption of resources that occur during the operation of a business.

Consider a service, for which the true demand Y is known, after the end of the respective period. In these cases the deviation between provided capacity  $\hat{Y}$  and demand Y of the relevant resource is associated with costs for either underestimating or overestimating the true resource demand of the service. Mathematically this is modelled by cost function C:

**Definition 5** (Service cost function). *The provision of the resource is evaluated by means of a loss function, which is an integrable function*  $C : V_Y^2 \to \mathbb{R}_+$  *fulfilling* 

$$C(\hat{y}, y) \ge 0 \quad \forall \ \hat{y}, y \quad and \quad C(\hat{y}, y) = 0 \quad if \ \hat{y} = y.$$

Function C quantifies the cost of underestimating or overestimating the true value of the variable Y. In economics the cost function is expressed in monetary terms such as profit, costs, missing income, or endof-period wealth. By definition of the cost function C, an estimation  $\hat{Y}$  that is equal to the observed demand Y, a perfect anticipation, has a loss of 0. Generally, a higher value of this cost function stands for higher costs or losses and is regarded as a worse outcome.

In the course of this paper we will mainly consider fixed and linear costs due to the simplicity of the calculations, also such cost functions can approximate more complex cost structures. Our goal is not to calculate optimal cost structures but to give simple insights into the relation of cost structures and service level restrictions.

We now give an example of a possible cost function for a service that relies on memory intensive computation tasks:

**Example 6.** Consider an Analytics-as-a-Service scenario, where knowledge is generated out of data in a cloud based fashion (Talia, 2013). Clients send their data to an analytics provider and expect their analysis reports in a certain time frame.

The computation tasks of the analytics provider are assumed to rely on memory intensive operations. If the maximum peak of memory demand of those operations exceed the available system memory, the service will slow down and the clients' requests cannot be completed in time. Thus resulting in a violation of the SLA between analytics provider and client.

Table 1: Optimal decision for different cost functions.

Cost structure $C(\hat{Y}, Y)$	Optimal decision $\hat{Y}$
$ \hat{Y} - Y $	$\hat{Y}=Q_{50\%}$
$(\hat{Y} - Y)^2$	$\hat{Y} = \int f_Y(y) dy = \mathbb{E}[Y]$
$(1_{\hat{Y} \ge Y}a + 1_{\hat{Y} < Y}b) \hat{Y} - Y $	$\hat{Y} = Q_{\frac{b}{a+b}}$

On the other hand, the platform for such an analytics service can be rented from an IaaS provider. For example, an Amazon m4.large instance having 8 GB of memory costs \$0.108 per hour. So one has to pay \$0.0135 per hour per 1 GB of provided memory. Further we assume that on average the analytics service provider loses \$5000 for each 1 GB of under-provided memory space per hour due to SLA violations. This results in the following cost function

$$C(\hat{y}, y) = 1_{\hat{y} \ge y} \underbrace{(y - \hat{y}) \$0.0135}_{variable \ costs \ of \ over-sized \ memory} + 1_{\hat{y} < y} \underbrace{(\hat{y} - y) \$5000}_{variable \ costs \ of \ under-sized \ memory}$$

So for this service, we expressed both the SLA violation costs and opportunity costs of the analytics provider in one function.

## **3 RESULTS**

By aid of calculations that are contained in the appendix and with Lemma 3 we can derive optimal decisions when service level guidelines are given.

**Theorem 7** ( $\alpha$  service level optimal decision). *In the situation of Lemma 3 where a density mass function*  $f_Y$  is given and a mean  $\alpha$  service level of at least q% is expected, the  $\alpha$  service level optimal decisions are

- S1 Choose  $\hat{Y} = Q_q$ .
- S2 Choose  $\hat{Y} = Q_{1-q}$ .

Theorem 7 shows how to calculate the optimal capacity under service level restrictions.

Additionally, for different cost functions C it is possible to estimate the optimal capacity  $\hat{Y}$  that minimizes the expected cost, see Table 1 for an overview. In the following Theorem we give the cost optimal decision for a linear cost function:

**Theorem 8** (Cost Optimal decision under linear cost function). *The cost optimal decision for the cost function* 

$$C(\hat{Y},Y) = (1_{\hat{Y} \ge Y}a + 1_{\hat{Y} < Y}b)|\hat{Y} - Y|,$$

is  $\hat{y} = Q_{\frac{b}{a+b}}$  for both S1 and S2 type relations.

The coefficient a represents the costs of overestimating and b the costs of underestimating the true value of Y.

Theorem 8 now shows that in the introduced service model, the cost optimal decision only depends on the ratio between *a* and *b*. This is the ratio of opportunity costs to resource binding costs. For *a*, resources are not used by the service and at *b*, the service is not provided. We will denote this ratio  $\frac{b}{a}$  by *c*:

$$c := \frac{b}{a} = \frac{\text{opportunity costs}}{\text{resource binding costs}}$$

Finally, with Theorem 7 and 8 we have optimal decisions  $\hat{Y}$  with respect to two aspects, one that optimizes the expected costs and one that obeys the  $\alpha$  service level restrictions.

### 4 DISCUSSIONS

Now we will interpret the results from both Theorem 7 and 8 and try to conclude the impact on the service offering.

#### 4.1 Rule of Thumb

Both Theorem 7 and 8 show how to calculate optimal decisions that either obey service level restrictions or minimize cost functions. In a business context, a service consumers wants both conditions to be fulfilled. So we have to combine both to derive a simple rule of thumb.

If we assume linear costs for underestimating or overestimating the demand for a service of type *S*1, the cost-optimal  $\alpha$  service level q% can be deduced from Theorem 7 and Theorem 8:

$$Q_q \stackrel{Theorem 7}{=} \hat{Y} \stackrel{Theorem 8}{=} Q_{\frac{b}{a+b}}.$$

It follows that the expected service level is equal to the following cost ratio

$$q = \frac{b}{a+b} = \frac{c}{c+1}$$

So the cost ratio c can be directly linked to an  $\alpha$  service level:

**Theorem 9** (Rule of thumb). *Under a service relation S1 and linear costs we have* 

$$q = \frac{b}{a+b} = \frac{c}{c+1}.$$

For a service relation of type S2 we get

$$q = \frac{a}{a+b} = \frac{1}{c+1}$$

So we managed to connect both service level restriction q and cost ratio c irrespective of the demand function  $f_Y$ . In the next example this connection is used to reflect the evaluation of revenue versus missing revenue for a retail use case. Further, it demonstrate how to deploy the rule of thumb to align cost structure and service level.

**Example 10.** Consider a cloud service providing online payments. Now, an internet based retailer runs a web page for selling a specific product and has subscribed the online payment service with an agreed service level of 98% for successful transactions.

Assuming that linear opportunity costs and a service relation of type S1 are valid here, the resource Y should be the number of payments that the provider is able to process per period. The linear costs correspond to the loss function C from Theorem 8

$$C(\hat{y}, y) = (1_{\hat{y} \ge y}a + 1_{\hat{y} < y}b)|\hat{y} - y|_{\hat{y}}$$

with a being the capital binding and b being the opportunity costs per transaction.

From Theorem 9 now follows a cost-ratio of

$$c = \frac{q}{1-q} = \frac{0.98}{1-0.98} = 49$$

meaning that the costs resulting from a single unsuccessful payment transaction are anticipated to be 49 times higher than the revenue from a successful transaction.

If the service level is strategically defined to be 98% but the cost ratio c is not 49:1, there will be a clash in terms of both optimizing costs and servicelevel. For example, if the retailer identifies his cost ratio to be 5:1, the cost optimal service level for the payment provider has to be set to 83% instead of 98%.

#### 4.2 Calculating Opportunity Costs

For many business cases estimating the opportunity costs is far from trivial. As an example for the retail case, see Campo et al. (2000) for an attempt to understand customer behavior in case of stock-outs.

In contrast, the capital binding costs for a given resource can be followed from the cost structure of the business at hand. But, using the rule of thumb a service consumer can estimate the opportunity costs:

**Theorem 11** (Deriving the opportunity costs). We assume a linear cost function C and a service type relation S1 to hold for the service at hand. Then, given the capital binding costs a and the strategically set service level q, the opportunity costs can be estimated to

$$b = a \frac{q}{1-q}$$
 if  $q \neq 1$  and  $a \neq 0$ .

Now we illustrate the calculation of the opportunity costs by a web hosting example:

**Example 12.** We consider a web hosting provider that offers both a 99.5% and a 99.9% availability of their clients web page. In this scenario, Y denotes the number of visitors on that page and the service consists in serving all visitors requests. Further, we assume that a client of the web hosting provider knows from historical experience that the average revenue per visitor is a = 1. For him this means that he has opportunity costs of

$$b = 1\$\frac{0.995}{1 - 0.995} = 199\$$$

for the first 99.5% availability package and for the service level of 99.9% of the second package he has opportunity costs of

$$b = 1\$\frac{0.999}{1 - 0.999} = 999\$$$

per unserved visitor.

The last example showcased one advantage of Theorem 11: To make the connection between service level and cost structure, one does not need to estimate the distribution function of the resource consumption by the service.

### **5 RELATED WORK**

In this work, we developed a model for generic services that is able to relate service level restrictions to cost structures. This allows to align strategically set service levels to the cost structure of a service.

In the field of cloud computing, there are several contributions that deal with the assigning, planing, aligning and reserving of computational resource in the context of cloud computing or SaaS in general. Those works either aim to obey service-levels or try to minimize the costs of under- or overestimating the resource demand. However, none of those draws the connection between both. Also most of those are written from the point of view of a service provider, not a service consumer.

For example, Chaisiri et al. (2012) compares different strategies for balancing the pre-booking of computational resources against on-demand consumption in order to minimize costs. Based on their clients past usage they optimally reserve computational resources while -like our model- considering different costs for under- or overestimation. This complex reservation decision can be interpreted as an advancement of our resource capacity planing  $\hat{Y}$ . However, in contrast to our model they do not consider a service level to be held.

Emeakaroha et al. (2010) present a framework for service providers to map monitoring metrics to SLA parameters, possibly used to enact counter measures such as dynamic scaling of resources. Their focus however, lies in the framework itself. Resources and how they relate to SLAs are only discussed exemplary.

Della Vedova et al. (2016) optimize the job schedule plan for cloud computing. They minimize the overall monetary cost for the execution service while keeping a certain availability of the service, representing a workload constraint. The different strategies are compared with respect to a fraction of violations, effectively representing a 95% availability service level. But instead of drawing a direct connection between cost structure and service level, they use the service level as a constraint for the schedule optimization problem.

Fu et al. (2014) present point predictors for planning cloud resources. The authors estimate the services demand for computational resources, but instead of discussing the importance of density functions for qualifying the uncertainty of their predictions they settle for point estimators. Further, they do neither include costs structures nor service levels.

Wu et al. (2014) develop resource provisioning algorithms to schedule VMs on a cluster. The only SLI that it considers is the response time of the service. It then balances clients with different service levels. Further it also includes SLA violations and considers the costs for over- and underestimation for the resource demand. The solution of their dynamically reservation strategy is not found analytically but by heuristical approximations.

The use of cost functions for singular periods to derive cost optimal point estimators from the distribution function of the services demand function is known in the predictive analytics literature (Feindt and Kerzel, 2015) as well as the decision modelling literature (Birge and Louveaux, 2011, Schlaifer and Raiffa, 1961). On the other hand, the optimal decisions for service level restrictions have been calculated in the operations research field for single product inventory systems (Van Houtum and Zijm, 2000).

However, to the best of our knowledge, those models are only known to the operations research or statistical decision theory communities and have not been applied to services in general. The novelty of our approach lies in the generalization of these models and their application to services in general. Further, our rule of thumb allows service consumers to quickly check if for a given service both the service level restrictions and cost function align.

### 6 CONCLUSION

During our work as Data Science consultants we observe that service consumers often have strategically set goals regarding the service levels, especially in the field of cloud computing. Further, those clients also have a clear picture of their cost structure. However, most of them are not aware that it is possible to draw a connection between cost structure and service levels. As a result, the strategically set service levels often do not align with the reported cost structure.

In this work we developed a mathematical model that allowed us to relate service levels to cost functions for services whose offering depends on one resource. We derived a rule of thumb to quickly relate the linear cost function ratio to the availability of the service. This rule of thumb allowed us to align the service level and cost structure. Additionally, it solves the otherwise difficult task to estimate the opportunity costs.

In general, we showed that the operations research literature can be applied to the field of services. We feel that the implications of strategically set service levels on the cost structure should gain more attention.

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#### APPENDIX

**Proof of Lemma 3.** The  $\alpha$  service level for a service relation S1 is equal to

$$E[\alpha\text{-service level}] = P(Y \le \hat{Y}) = \int_{-\infty}^{\hat{Y}} f_Y(y) dy = q$$

The solution of this equation is  $Q_q$ . For the service relation of type S2 the expectation of the  $\alpha$ -service level is  $P(\hat{Y} \leq Y) = Q_{1-q}$ .

*Proof of Theorem 7*. Follows directly from Lemma 3. □

**Lemma 13** (Necessary and sufficient condition for cost optimal decision). Let the support of  $f_y$  be denoted by  $V_Y = \{y \mid f_Y(y) > 0\}$ . The decision  $\hat{y}$  that minimizes the cost function *C* fulfills

$$0 = \frac{\partial}{\partial \hat{y}} \int_{V_Y} f_Y(y) C(\hat{y}, y) dy.$$
(1)

Further, it has to fulfill a sufficient condition such as

$$0 < \frac{\partial^2}{\partial^2 \hat{y}} \int_{V_Y} f_Y(y) C(\hat{y}, y) dy.$$
 (2)

*Proof of Theorem 8.* According to Equation 1 of Lemma 13 a cost optimal estimator has to fulfill

$$0 = \frac{\partial}{\partial \hat{y}} \int_{-\infty}^{\hat{y}} f_Y(y) \, a\left(\hat{y} - y\right) dy - \frac{\partial}{\partial \hat{y}} \int_{\hat{y}}^{\infty} f_Y(y) \, b\left(\hat{y} - y\right) dy.$$

We are allowed to interchange the integral and the differentiation by the dominated convergence theorem (Royden and Fitzpatrick, 1988) because  $c_{\hat{y}} f_Y$  for a  $c_{\hat{y}} > 0$  is an integrable majorant to the integrand

$$\left|\frac{\partial}{\partial \hat{y}} f_Y(y)(1_{\hat{Y} \ge Y}a + 1_{\hat{Y} < Y}b)|\hat{y} - y|\right| \le c_{\hat{y}} f_Y(y).$$

This yields

$$a\int_{-\infty}^{\hat{y}} f_Y(y)dy = b\int_{\hat{y}}^{\infty} f_Y(y)dy \Leftrightarrow aF(\hat{y}) = b(1 - F(\hat{y}))$$
$$\Leftrightarrow F(\hat{y}) = \frac{b}{a+b} \Leftrightarrow \hat{y} = F^{-1}\left(\frac{b}{a+b}\right) = Q_{\frac{b}{a+b}}.$$

#### Proof of optimal point estimators in Table 1.

This table contains the optimal decision for several cost structures. We gave a proof for  $(1_{\hat{Y} \ge Y}a + 1_{\hat{Y} < Y}b)|\hat{Y} - Y|$  and with it for  $|\hat{Y} - Y|$ . The missing proof for  $(\hat{Y} - Y)^2$  can be found on page 196 of (Schlaifer and Raiffa, 1961).

**Proof of Theorem 11.** Follows directly from the rule of thumb given in Theorem 9.  $\Box$