

# Enterprise Level Security with Homomorphic Encryption

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**Abstract:** Enterprise Level Security (ELS) is an approach to enterprise information exchange that provides strong security guarantees. It incorporates measures for authentication, encryption, access controls, credential management, monitoring, and logging. ELS has been adapted for cloud hosting using the Virtual Application Data Center (VADC) approach. However, a key vulnerability in placing unprotected data in the cloud is the database that stores each web application's data. ELS puts controls on the end-to-end connection from requester to application, but an exploit of the back-end database can allow direct access to data and bypass ELS controls at the application. In a public cloud environment the data and web application may be vulnerable to insider attacks using direct hardware access, misconfiguration, and redirection to extract data. Traditional encryption can be used to protect data in the cloud, but it must be transferred out of the cloud and decrypted to perform processing, and then re-encrypted and sent back to the cloud. Homomorphic encryption offers a way to not only store encrypted data, but also perform processing directly on the encrypted values. This paper examines the current state of homomorphic encryption and its applicability to ELS.

## 1 INTRODUCTION

Enterprise Level Security (ELS) provides a way to secure access to web resources (Chandersekaran, 2008; Chandersekaran, 2012; Foltz, 2016a; Foltz, 2016b; Foltz, 2016c; Simpson, 2011; and Simpson, 2016). It provides end-to-end authentication, confidentiality, and integrity from web browser to web resource provider. When combined with an external solution for availability, it promises a comprehensive enterprise solution for security of web resources.

Most web service providers are partitioned into a front-end web application and back-end stored data. ELS provides secure communication to the web application, and the Virtual Application Data Center (VADC) model extends this to cloud hosting (Foltz and Simpson, 2016b). However, ELS extends only from requester to application, and it does not include the stored data. This data is often the enterprise's most valuable digital asset, and the boundary of ELS between the application and database provides a potential access path that bypasses ELS protections. To maintain ELS security levels in a cloud environment, some means of protecting the data is

required.

In addition to the data, the web application may be vulnerable to attacks in a public cloud. Cloud operators may have access to all data in the cloud, and through virtual machine managers they may also gain visibility into the application code running on the servers.

Homomorphic encryption provides a way to manipulate encrypted data to perform computations without decrypting the data. This is useful for the ELS stored data problem because it allows a web application's stored data to remain encrypted at all times, even during data operations. An attacker at the stored data has no access to plaintext values.

Homomorphic encryption also addresses the web application problem because the web application code can be recompiled to operate on homomorphic encrypted data. Attackers viewing the web application cannot extract computational process information or unencrypted data from the computation.

When implementing an ELS system on a private data center there is an implicit safe zone where data and applications can be run. The machines remain under physical control, and the people working on

them are part of the enterprise. When moving to the cloud, this safe zone is replaced by a potentially hostile or compromised environment, which threatens to expose sensitive data. Homomorphic encryption offers a way to reclaim this safe zone while maintaining many of the benefits of cloud hosting.

This paper discusses the methods and issues in using homomorphic encryption within an ELS architecture. The following sections describe ELS and homomorphic encryption, discuss integrating homomorphic encryption into ELS, and provide an analysis of the security and performance implications.

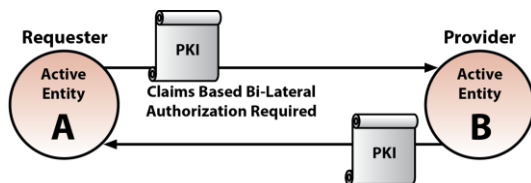
## 2 ENTERPRISE LEVEL SECURITY

The ELS design addresses five security principles:

- Know the Players – enforce bi-lateral end-to-end authentication;
- Maintain Confidentiality – maintain end-to-end unbroken encryption between data requester and provider;
- Separate Identity from Access and Privilege – use separate authentication and authorization credentials;
- Maintain Integrity – validate that what was received is exactly what was sent;
- Require Explicit Accountability – monitor and log transactions.

### 2.1 Know the Players

In ELS, the identity credential is an X.509 Public Key Infrastructure (PKI) certificate (DoDI, 2011; RSA, 2012). This identity is required for all active entities, both person and non-person, as shown in Figure 1. PKI credentials are verified and validated. Ownership is verified by a holder-of-key check. Supplemental authentication factors may be required from certain entities, such as biometric data (Chandersekaran and Simpson, 2008).



Active Entity may be: User, Web Application, Web Service, Aggregation Service, Exposure Service, Token Server, or any element that can be a requester or provider.

Figure 1: Bi-lateral Authentication.

### 2.2 Maintain Confidentiality

Figure 2 shows how ELS establishes end-to-end Transport Layer Security (TLS) encryption through the numerous intermediaries that may route, scan, or process data between requester and application (W3C, 2008). The red line indicates the path of encrypted data from end to end through routers, relays, proxies, firewalls, and load balancers, which may view and manipulate the encrypted content. ELS end-to-end encryption ensures they are not able to view or modify the raw unencrypted content without triggering an error at the endpoints.

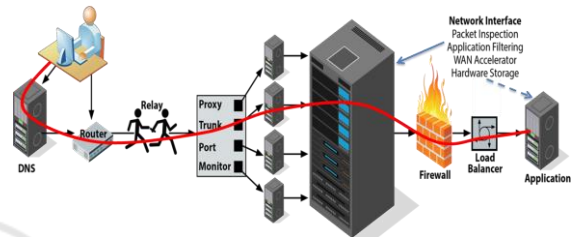


Figure 2: End-to-End Encryption.

### 2.3 Separate Access and Privilege from Identity

ELS can accommodate changes in location, assignment, and other attributes by separating the use of associated attributes from the identity. Whenever changes to attributes occur, access claims are recomputed based on new associated attributes, allowing immediate access to required mission information. As shown in Figure 3, access credentials use the Security Assertion Markup Language (SAML) (Ragouzis et al., 2008). SAML authorization tokens used with ELS differ from the more commonly used single-sign-on (SSO) authentication tokens (Chandersekaran and Simpson, 2012). Authentication is performed through TLS using PKI credentials. This separation prevents a compromised SAML token from providing immediate access. The credential for access and privilege is bound to the requester by ensuring a match of the distinguished name used in both authentication and authorization credentials.

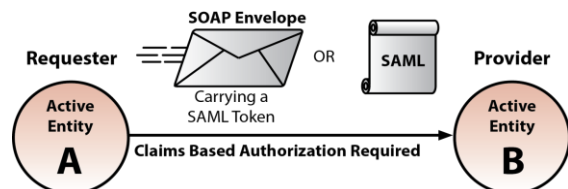


Figure 3: Claims-Based Authorization.

## 2.4 Maintain Integrity

Integrity is implemented by end-to-end TLS message authentication codes (MACs), as shown in Figure 4. Chained integrity, in which trust is passed on transitively from one entity to another, is not used because it is not as strong as employing end-to-end integrity. At the application layer, packages (SAML tokens, etc.) are signed by the sender, and signatures are verified and validated by the receiver.

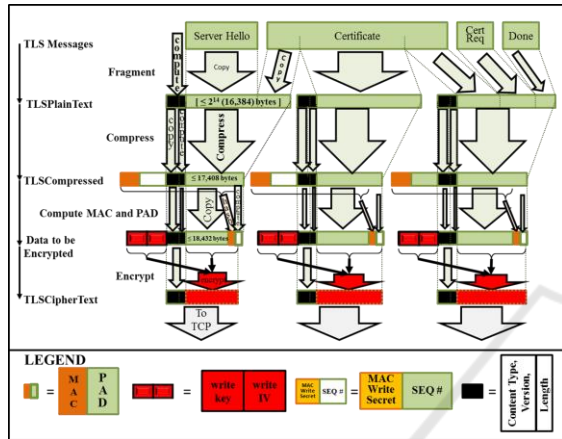


Figure 4: Integrity Measures.

## 2.5 Require Explicit Accountability

As shown in Figure 5, ELS monitors specified activities for accountability and forensics. The monitor files are formatted in a standard way and stored locally. For enterprise files, a monitor sweep agent reads, translates, cleans, and submits records to an enterprise database for recording log records periodically or on-demand. Local files are cleaned periodically to reduce overall storage and to provide a centralized repository for help desk, forensics, and other activities (Simpson and Chandrasekaran, 2011). However, the principle of accountability requires unambiguous identification of the entity performing these actions. This means that proxies, go-betweens, and impersonators acting “on behalf of” other entities are not allowed.

By abiding with the tenets and principles discussed above, ELS allows users access without accounts by computing targeted claims for the enterprise. ELS has been shown to be a viable, scalable alternative to current access control schemas. A complete description of ELS basics is provided in (Foltz and Simpson, 2016b).

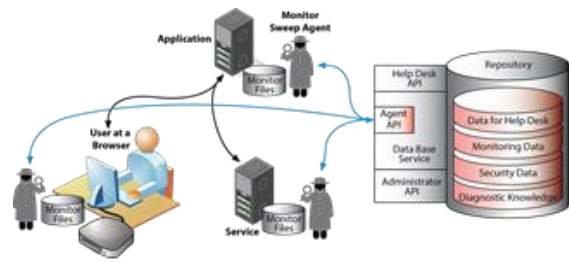


Figure 5: Accountability through Centralized Monitoring.

## 3 HOMOMORPHIC ENCRYPTION

Homomorphic encryption refers to methods of encryption that allow operations on the ciphertext to map to corresponding operations on the underlying plaintext. For example, raw, unpadded RSA encryption is performed as follows to compute ciphertext  $c$  from plaintext message  $m$ :

$$c = ENC(m) = m^e \pmod{n}. \quad (1)$$

The product of two encrypted values

$$c_1 = ENC(m_1) \quad (2)$$

and

$$c_2 = ENC(m_2) \quad (3)$$

is

$$c_1 \cdot c_2 = m_1^e \cdot m_2^e \pmod{n} \quad (4)$$

$$= (m_1 \cdot m_2)^e \pmod{n} \quad (5)$$

$$= ENC(m_1 \cdot m_2) \quad (6)$$

The product of the encrypted values is just the encrypted product of the corresponding plaintext values.

Different homomorphic encryption schemes have different operations, and the ciphertext and plaintext operations can differ. Paillier encryption, for example, has the property:

$$ENC(m_1 + m_2) = ENC(m_1) \cdot ENC(m_2). \quad (7)$$

In this case, multiplication of ciphertext corresponds to addition of plaintext.

For both RSA and Paillier, only a single operation is possible. In 2009, Gentry published his thesis describing an encryption scheme that allows both addition and multiplication (Gentry, 2009). With these two operations it is possible to compute  $1 + (-1) \cdot (a \cdot b)$  for two inputs  $a$  and  $b$ . If  $a$  and  $b$  are binary values, this is the computation of the NAND function, which can be used to build a logical circuit that can perform any computation. Therefore, such a homomorphic encryption method allows the

computation of any function on encrypted data. This is called Full Homomorphic Encryption (FHE).

Methods, such as RSA and Paillier, that allow some computation but not arbitrary functions are called Partial Homomorphic Encryption (PHE). Another class of homomorphic encryption allows the computation of any function on encrypted data, like FHE, but only for a limited number of executions of an operation. For example, it may allow any number of additions, but only up to  $n$  multiplications for some number  $n$ . These Somewhat Homomorphic Encryption (SWHE) methods are often related to FHE methods. In particular, Gentry's FHE method builds on SWHE and removes the limit on the number of multiplications through bootstrapping.

Even FHE has its limitations for providing security. Although confidentiality is maintained by keeping data encrypted at all times, integrity requires additional work. An operation on homomorphic data does not leak the value of the data, but the result of such a computation in the cloud has no method of verification. The cloud provider could, for example, replay results of previous computations or encrypt its own chosen results using known public keys.

A solution that provides verifiable computing is presented in (Gennaro, Gentry, and Parno, 2010). The representation of the circuit that computes the function is garbled in a way that the entity doing the computation does not know what is being computed. This method builds on homomorphic encryption to monitor the integrity of results.

This integrity check is critical to ELS cloud hosting. Because the homomorphic encryption approach provides confidentiality and integrity, it extends ELS security properties into a hostile cloud environment.

## 4 HOMOMORPHIC ENCRYPTION WITH ELS

This section discusses the integration of homomorphic encryption into an ELS architecture. However, before examining homomorphic encryption, we first examine the limitations of standard encryption.

### 4.1 No Homomorphic Encryption

One approach using standard encryption is to host the application locally and store encrypted data in

the cloud. The browser and application are outside the cloud in a controlled environment, and the database is inside the cloud. The application encrypts data before sending it to the cloud database and decrypts it after retrieval. The cloud is simply a place to store data. All computation occurs on local, trusted machines. Cryptographic keys are maintained by the local application.

This scenario maintains confidentiality, since only encrypted content is sent to the cloud. However, all processing of data requires retrieving it, decrypting it, and performing the computation locally. If the results of the computation are to be stored, they must be encrypted and sent back to the cloud. Such a model for cloud security works well for all data set sizes, but the size of data that is retrieved and sent must be small and the computation must be quick. In such a case, the main resource requirement is the storage, and the network transmissions and local computation are relatively minor. This could be the case for a forensics archive, in which large amounts of data are stored for potential use but only small portions are actually ever used.

The problem with traditional encryption comes when a computation requires access to all of the data, such as computation of an average or maximum value. In such a case, all of the encrypted data must be retrieved and decrypted, and then the computation can take place on the decrypted values. With limited network bandwidth and potentially limited requester computation resources the traditional approach has significant overhead. Homomorphic encryption, in contrast, only requires encrypting the request and decrypting the response. The computation is performed on the encrypted values.

The following discussion covers solutions that use homomorphic encryption.

### 4.2 FHE with Full Application in Cloud

The most desirable implementation for security is to place the application and data in the cloud, each with homomorphic encryption, and use verifiable computation for the application logic. Figure 6 provides the basic concept. This provides confidentiality and integrity of the data and computation results even when hosting in a hostile environment. The requester would need a way to encrypt request data to the application and decrypt encrypted responses from the application.

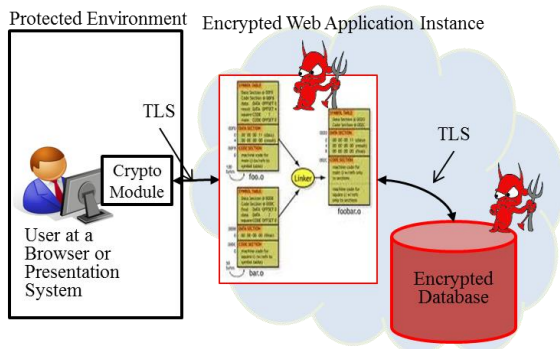


Figure 6: Full Homomorphic Concept.

One approach is for the requester browser to manage this encryption and decryption, along with the key generation and management. However, this requires rewriting the browser. A simpler approach is to have a separate module that is attached to the browser and modifies outgoing and incoming traffic to encrypt and decrypt content, respectively. This enables the browser functionality and cryptography to be modular so that browser updates do not break cryptography and changes in cryptography do not require rewriting browser code.

To the browser, nothing has changed. The cryptographic module handles translation of plaintext requests to homomorphically encrypted requests. The server code is recompiled to operate on encrypted data with verifiable computing. No homomorphic keys are stored in the cloud, and any server keys for encryption, signatures or other operations remain encrypted under homomorphic encryption. The browser cryptographic module takes the responsibility of managing and using homomorphic encryption keys.

### 4.3 FHE with Only Data in Cloud

Recompiling applications to operate on homomorphically encrypted data is not always desirable. In these cases the application can be hosted locally while the data is hosted in the cloud. The data itself is encrypted for homomorphic operation. This concept is shown in Figure 7.

There are two possibilities for how the database is hosted in the cloud. It can be recompiled for homomorphically encrypted operation or it can remain as-is and only the data is encrypted. The case in which the database code is recompiled is identical to the case in which the application is recompiled, except that the cryptographic module now attaches to the application calling the database instead of the browser calling the application.

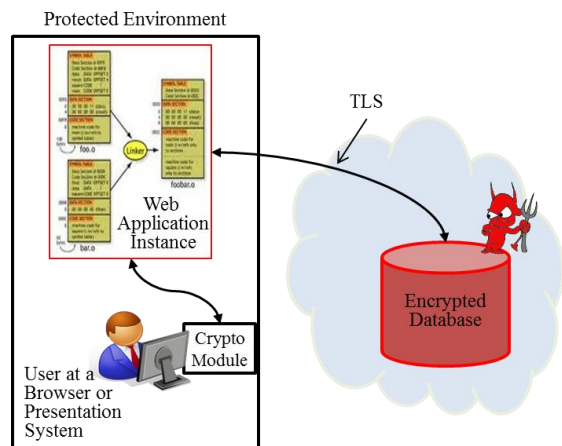


Figure 7: Protected Application Homomorphic Concept.

For the encrypted data in the unmodified database, there are some additional considerations. For homomorphic encryption in which the operations on the plaintext and ciphertext differ, the database commands may need to be rewritten to account for this difference. For example, if addition of plaintext values is accomplished by multiplying ciphertext values, then all database requests to add values must be changed to multiplication requests.

Even if the operations are the same, the data types and sizes of plaintext and ciphertext may be different. The necessary types and sizes for the ciphertext must be available in the database.

The main advantage of this method over placing the full application data and logic in the cloud is that the application and database code require no changes. The only change is the addition of the cryptographic module to the application to translate database commands into homomorphically encrypted commands.

### 4.4 Performance Considerations

Homomorphic encryption solves many of the security problems for ELS cloud hosting, but this security comes at a cost. Homomorphic encryption algorithms are a small subset of possible encryption algorithms, and all of the currently available homomorphic algorithms are slower than traditional encryption algorithms.

However, the comparison is not that simple. Traditional encryption has only two operations: encryption and decryption. Homomorphic encryption has these two as well as operations on the data itself. Typically, addition and multiplication are the plaintext operations, but the operations on the ciphertext may be more complicated operations or

similar operations on larger data values, both of which can incur performance penalties. To assess the performance of homomorphic encryption, it is important to understand how the fundamental operations of encryption, decryption, addition, and multiplication are used. These different operations often have different performance, which must be combined or averaged to provide an overall performance assessment.

There are two generic use cases for homomorphic encryption in the cloud. The first is a bulk load of existing plaintext data and applications. This requires encrypting all the data and applications. This is an infrequent event, but for large data sets or applications, it can be very resource-intensive. It is often highly parallelizable, so the main issue is throughput. The time taken will depend on the size of the data set, the available resources, and the computation requirements of encryption. For this first use case, the baseline for comparison is encrypting the data with the Advanced Encryption Standard (AES) encryption algorithm.

The second use case for encryption is user access to encrypted data. If individual users perform the encryption and decryption of requests and responses in a distributed way, the performance of the requests is unlikely to be significantly affected. Unless large data sets are transferred, the encryption or decryption of data will incur only a small latency based on local encryption or decryption of requests and responses.

If a central server manages keys and performs cryptographic operations, this frees users from key management, but it creates a central bottleneck for performance. The central server must do all encryption and decryption, which may require dedicated computing resources to manage the throughput.

Addition and multiplication are used to manipulate data in the cloud. Such operations do not decrypt or encrypt data, so performance depends only on the performance of the ciphertext operations that are used to implement the additions and multiplications on the underlying plaintext.

If the application itself is encrypted, the code will involve different additions and multiplications in order to do computation. This is another area where the specific application will influence performance.

The operational model for an application will be some mix of additions, multiplications, uploads, and downloads. As a result, it is not possible to determine the performance penalty of using homomorphic encryption without knowledge of the

application itself. We examine instead the individual operations, which enable further analysis for specific applications.

To track the degradation in performance, a sample data base was used with both plaintext and homomorphic searches as a model in (Gligor, 2014). Real-world testing of various homomorphic encryption methods (Gentry, Halevi, and Smart, 2012; Cheon et al., 2013; Doroz, Hu, and Sunar, 2014; Lauter, Naehrig, and Vaikuntanathan, 2011; and Joppe et al., 2013) shows that FHE encryption incurs a performance penalty of a factor of about  $10^{10}$  compared to AES encryption. For example, a 1-microsecond AES encryption would take about 3 hours using FHE. This is prohibitively slow, and there is no indication that this will become feasible for real-world applications in the near future.

SWHE methods can be orders of magnitude faster than corresponding FHE methods. Encryption can be roughly  $10^{2.5}$  times slower than AES, which is approaching feasibility for specific use cases. However, encryption for operations on data are much slower. Encryption for homomorphic addition is  $10^{3.8}$  times slower, and encryption for multiplication is  $10^{7.5}$  times slower. These factors make current and near-future adoption unlikely.

An important consideration for real-world performance is the actual time taken, not just the factor above the non-homomorphic operation, since encryption, addition, and multiplication, although all very fast, have different performance. For the current numbers, however, the message is clear that homomorphic encryption retains significant performance penalties and little or no probability that improvements in commodity hardware will be able to reduce these penalties to acceptable levels. The few options available for FHE and SWHE are more like existence proofs than performance-optimized standards. As a result, performance suffers significantly compared to the highly optimized symmetric encryption methods like AES that are in use today.

#### 4.5 A Possible Compromise

Full Homomorphic Encryption enables arbitrary computations on encrypted data. This allows any functions on any data to be computed. However, many use cases are more restricted in their computations and this full generality is not always needed. At the other extreme of full generality is a case in which a simple comparison operation is all that is needed.

For example, a database stores a list of values,

and the only operations on the data are to add new values, delete values, or ask whether a particular value already exists. In this case, any deterministic encryption algorithm is sufficient. To add or delete, just add or delete the encrypted value. To query a value, just encrypt it and ask whether that encrypted value is present. This is again a very narrow use case in which traditional encryption is sufficient.

Methods, such as RSA, Paillier, and other PHE methods may offer a good compromise between FHE and traditional encryption. These PHE methods allow some computation beyond simple comparisons with traditional encryption while being orders of magnitude faster than FHE or SWHE (Gligor, 2014). The smaller performance penalty might make it feasible for specialized applications for which PHE operations provide sufficient data manipulation capabilities.

Recent simulations with PHE suggest a manageable performance overhead when restricted to standard SQL queries. This approach was initiated by CryptDB (Akin and Sunar, 2015; Dayioğlu et al., 2015; Naveed, Kamara, and Wright, 2015; Popa et al., 2012; Wang, Agrawal, and Abbadi, 2012). This suggests that ELS with PHE at the database may be a promising future direction for investigation.

## 5 CONCLUSIONS

Homomorphic encryption shows promise as a solution to ELS cloud security issues. FHE allows data and processing to be protected in the cloud for confidentiality. With some modification to the application, it is also possible to provide integrity. However, real-world implementation is not likely to be feasible in the near future due to the performance overhead of current FHE implementations. PHE shows promise for current use. The functions and architectures that can be used are limited, but performance overhead is relatively small. More work is needed to investigate exactly which functions can be implemented with PHE and whether such functions can operate with adequate performance.

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