Towards a Temporal Extension to OWL 2: A Study based on tOWL Language

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Abstract: The Semantic Web is becoming fundamental in the Web. The amount of data available in the Web is increasing in great proportions, it is very important to find ways to deal with this trend. The Semantic Web can help with this, by giving meaning to this data in a way that machines can understand what information it contains and automatically process it. In this paper we present a study about the compatibility between the latest version of the Web Ontology Language (OWL 2) and the Temporal Web Ontology Language (tOWL), based on the first version of OWL. We analyze which constructs of tOWL can be used and modified into OWL 2 maintaining decidability aspects. The current version of OWL does not have resources to represent complex time information and the main contribution of this work is a new proposal to represent time in OWL 2.

1 INTRODUCTION

One of the biggest obstacle to provide better support for Web users is the fact that a large part of the Web content is not accessible by machines (Berners-Lee et al., 2001). There are tools capable of collecting texts, separating it in parts, verifying its orthography and counting words. However, regarding the interpretation of phrases and extracting useful information for the users, the current tools are very limited (Staab and Studer, 2013). To be able to understand the content of information contained in the Web, machines and humans need to share some understanding of the real world, i.e, we need to be able to represent the world or parts of the world inside the machine.

The Semantic Web has several tools that provide aid for machines to understand the meaning of texts contained in the Web, optimizing the communication between humans, machines, as well as communication between humans and machines. Using Semantic Web tools we can represent real aspects of the world inside the computer and reason with that representation (Davis et al., 1993).

When representing the world, we want this representation to be as close to reality as possible to avoid making false assumptions about the world. To be able to do this, we also need to be capable of representing time. Time is an important aspect of human life. Many environments require temporal awareness, one known example is air traffic control, each aircraft needs to follow a strict schedule to avoid any incidents. Therefore, time should also be part of real world representations.

The Web Ontology Language (OWL) is the official standard for representing ontologies in the Semantic Web (Group et al., 2009), with this language we can represent several aspects of the world inside computers, but not complex time information. The underlying semantics of this language is based on a Description Logics (DL) fragment called SROIQ (Horrocks et al., 2006). This fragment has been proved to be decidable, that means we can reason with our world representation, finding implicit knowledge from it and verifying its consistency.

The Temporal Ontology Language (tOWL) (Milea et al., 2012) is a temporal language built as an extension of the first version of OWL. With tOWL we can represent complex aspects of time, such as points in time and intervals. This language adds Concrete Domains to OWL, making it possible to use Concrete Domains predicates and datatypes, but limiting the expressiveness of the language to avoid undecidability (Baader and Hanschke, 2011).

In this paper we perform a study on the compatibility between tOWL and OWL 2, verifying which structures of tOWL are compatible with OWL 2 and which ones need some modification to keep decidability. The first version of OWL has been very success-

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ful, but lacked several important elements for ontology modelers (Grau et al., 2008a). One of these elements is qualified cardinality restriction. With this structure we can represent not only cardinality, limiting the number of elements that a property can take, but we can also qualify this cardinality, limiting the type of elements a property can take. This structure is added to OWL 2, however, since tOWL is based on OWL 1, we can't use this structure with tOWL.

As a result of this study, we present modifications to the tOWL language, allowing it to have the expressiveness of OWL 2 without compromising the decidability of the language. If both languages have the same expressiveness, we can use all OWL 2 constructs, including qualified cardinality restriction, next to tOWL constructs, providing a temporal extension for OWL 2.

Since OWL 2 does not use Concrete Domains, the use of tOWL structures together with OWL 2 could lead to undecidability. We modify some of the existents OWL 2 constructs in such a way that we can add the temporal constructs from tOWL, maintaining decidability at the same time. We present a new layer to tOWL, replacing the Layer of Concrete Domains. This new layer acts as a glue between tOWL and OWL 2.

This paper is organized as follows: Section 1 presented the introduction for this work. Section 2 presents a theoretical background for this study, presenting a short introduction on Description Logics, OWL 2 and tOWL. Section 3 presents the modifications and adaptations that were made into tOWL, making it compatible with OWL 2. Section 4 presents an application for this modified version of tOWL next to OWL 2. At Section 5 we present the conclusion for this work and possible future work.

2 BACKGROUND

This Section presents some definitions for the Description Logics SROIQ, which is the basis for the semantics of OWL 2. We also present some of OWL 2 principles and the tOWL language.

2.1 SROIQ

Description Logics (Baader and Nutt, 2003) is a name given to a family of formalism from Knowledge Representation that represents concepts from a domain and uses these concepts to specify properties of objects and individuals that are in this domain. A Knowledge Representation system provides the resources to define knowledge bases, reason about its content and also manipulate it (McGuinness and Borgida, 1995).

A knowledge base usually contains two elements, the TBox and the ABox (Krötzsch et al., 2012). The TBox presents the vocabulary of the application domain and the ABox contains assertions about the individuals named according to the vocabulary. The vocabulary is composed by concepts (or classes) and roles (or properties), which denotes the set of individuals and express binary relations between such individuals, respectively.

There are many fragments for Description Logics and they are named according to the allowed operators. The OWL 2 semantics (Motik et al., 2009b) is based on the fragment SROIQ of Description Logics, where S is for the AL (attributive language, a basic fragment for DL) with C (complex concept negation), R is for complex role inclusion axioms, O is for nominals, I is for inverse properties and Q is for qualified cardinality restrictions.

Formally, each DL ontology is based on three finite set of symbols, a set N_I of individual names, a set N_C of concept names and a set N_R of roles names. The set of roles expressions R is defined by the following grammar (Krötzsch et al., 2012) (Eq.1):

$$R ::= U \mid N_R \mid N_R^- \tag{1}$$

where U is the universal role and N_R^- is the inverse of N_R .

The set of concept expressions *C* is defined as:

$$C ::= N_C | (C \sqcap C) | (C \sqcup C) | \neg C | \top | \bot |$$

$$\exists R.C | \forall R.C | \ge nR.C | \le nR.C | \exists R.Self | \{N_I\}$$
(2)

The axioms can be defined by Eqs.3, as follow:

$$ABox: C(N_I) R(N_I, N_I) N_I \approx N_I N_I \not\approx N_I$$
$$TBox: C \sqsubseteq C C \equiv C$$
$$RBox: R \sqsubseteq R R \equiv R R \circ R \sqsubseteq R Disjoint(R, R)$$
(3)

The fragment $S\mathcal{R}OIQ$ has been proved to be decidable (Horrocks et al., 2006), that implies we can reason with this fragment.

2.2 OWL 2

OWL is the acronym for Web Ontology Language (Hitzler et al., 2009a), is a Web Semantic language developed to represent knowledge about things, group of things and relationship between things. It is used to represent ontologies as a logic based language. This implies that the knowledge expressed in OWL can be reasoned by software to verify the consistence of the knowledge base and to find new implicit knowledge (Hitzler et al., 2009a).

The basic concepts of OWL are:

- Axioms: Basic expression declarations that can be true or false. A set of declarations can be consistent when all declarations are true in the same situation, or inconsistent when it is not possible to find such situation. The reasoners (Sirin et al., 2007; Shearer et al., 2008) are tools for OWL that can automatically compute if a declaration is consequence of others.
- Entities: Elements used to refer to real world objects (Group et al., 2009). They are atomic concepts of declarations, such as, objects, categories, relationships, etc. OWL objects are treated as individuals, categories are treated as classes and relationship are treated as properties. The properties are divided in object properties, datatype properties and annotation properties.
- Expressions: Combinations of entities to form complex descriptions from basic elements. We can combine entities names into expressions using constructors. For example, the atomic classes "animal" and "mammal" can be combined to describe classes of animals that are mammals. This new class would be represented in OWL by a class expression, that could be used in declarations or in other expressions.

2.3 tOWL

The tOWL (Milea et al., 2012) (Temporal Web Ontology Language) is an OWL extension that allows the communication between machines in contexts including temporal information. The tOWL language allows inferences of implicit knowledge in contexts that need temporality when a temporal dimension is involved.

This language was developed as an extension of OWL DL (Motik et al., 2009a), a profile from the first version of OWL, with addition of the time unit. The OWL DL fragment considered was SHIN(D), i.e., OWL without the use of nominals, referred as OWL DL⁻.

The tOWL implements two aspects of time: temporal infrastructure and change. Temporal infrastructure refers to the representation of time as intervals or instants.

Using tOWL, changes can happen in values of concrete attributes, in relationship between entities and in transition of states.

The language was developed in three layers: (i) Layer of Concrete Domains, (ii) Layer of Temporal Reference and (iii) Layer of 4D Fluents.

2.3.1 Layer of Concrete Domains

This layer allows representation of restrictions using binary predicates from concrete domains. In tOWL we can represent feature chains, $f_1...f_n$, composed with a concrete feature g, creating a concrete feature path (CFP), which is equivalent to the following composition:

$$f_1 \circ f_2 \circ \dots f_n \circ g, \tag{4}$$

where $n \in N$. The CFP is added to tOWL as the construct ConcreteFeatureChain. One example of such composition would be the abstract feature time composed with the concrete feature start, in the following manner:

$$time \circ start.$$
 (5)

This construction denotes the beginning of a point in an interval. Table 1 summarizes the semantics introduced for this layer, with the abstract syntax proposed for the tOWL constructs.

2.3.2 Layer of Temporal Reference

This layer presents timepoints, relationships between timespoints and intervals. The intervals are defined using the predicate of concrete domain < and two concrete features, start and end, to define that the beginning of an interval must be strictly smaller than the end of the interval, as described in Eq.6.

 $ProperInterval \equiv \exists (begin, end). < (6)$

2.3.3 Layer of 4D Fluents

This layer presents a perdurantist view of individuals, allowing representation of complex temporal aspects, as state transitions in processes. Table 2 presents the axioms of TBox corresponding to the timeslices/fluents layer.

The language tOWL is limited in expressiveness compared to OWL 2. It is based on the fragment SHIN(D) while OWL 2 uses the fragment SROIQ. Thus, several constructs that are available for OWL 2 cannot be used with tOWL.

One of the main innovations of OWL 2 is the addition of qualified cardinality restriction (Grau et al., 2008a). With this construct we can represent sentences such as "this airplane has 108 seats of the type economic class and 48 seats of the type first class". That means we can add not only cardinality to properties, we can also qualify it, this is not possible in tOWL and it is fundamental for the development of several ontologies (Horrocks et al., 2006).

tOWL abstract syntax	Theoretical Model semantics
ConcreteFeatureChain(f_1 f_2 f_n g)	$\{(a_1,b)\in\Delta^I\times\Delta_{\mathcal{D}}\mid \exists !a_2\in\Delta^I,,\exists !a_{n+1}\in$
	$\in \Delta^{I} \land \land \exists ! b \in \Delta_{\mathcal{D}} : (a_{1}, a_{2}) \in f_{1}^{I},$
	$(a_n, a_{n+1}) \in f_n^I \wedge g^I(a_{n+1}) = b\}.$
dataSomeValuesFrom $(u_1 \ u_2 \ p_d)$	$\{x \in \Delta^I \mid \exists ! q_1 \in \Delta_{\mathcal{D}}, \exists ! q_2 \in \Delta_{\mathcal{D}}:$
	$u_1^I(x) = q_1 \wedge u_2^I(x) = q_2 \wedge (q_1, q_2) \in p_d^I \}.$
dataAllValuesFrom $(u_1 \;\; u_2 \;\; p_d)$	$\{x \in \Delta^I \mid \forall q_1 \in \Delta_D, \forall q_2 \in \Delta_D:$
	$u_1^I(x) = q_1 \wedge u_2^I(x) = q_2 \wedge (q_1, q_2) \in p_d^I)\}.$

Table 1: Semantics for the Layer of Concrete Domains (Milea et al., 2012).

Table 2: tOWL axioms for the	e Layer of 4D Fluents (Milea et al., 2012).

Constructs tOWL 4dFluents	tOWL Axioms in OWL-DL ⁻	
Class(TimeSlice)	$\exists time.Interval \sqcap (= 1 time) \sqcap \exists timeSliceOf.$	
	¬(TimeSlice∟Interval∟ rdfs:Literal)⊓	
	(=1 timeSliceOf)	
Class(Interval)	∃(start,end). ≤ ⊓∃start.dateTime⊓	
	$\neg \exists end.dateTime \neg (= 1 \text{ start}) \neg (= 1 \text{ end})$	
Class(FluentProperty)	FluentProperty C rdf:Property	
Class(FluentObjectProperty)	FluentObjectProperty FluentProperty	
Class(FluentDatatypeProperty)	FluentDatatypeProperty FluentProperty	
Property(timeSliceOf)	≥ 1 timeSliceOf \sqsubseteq TimeSlice	
	$\top \sqsubseteq \forall timeSliceOf. \neg (TimeSlice \sqcup Interval \sqcup$	
	⊔rdfs:Literal)	
Property(time)	≥ 1 time \sqsubseteq TimeSlice	
	$\top \sqsubseteq \forall time.Interval$	
Property(start)	≥l start⊑Interval	
	$\top \sqsubseteq \forall start.dateTime$	
Property(end)	≥ 1 end \sqsubseteq Interval	
LE AND TEL	$\top \sqsubseteq \forall end.dateTime$	

Furthermore, OWL 2 also adds the complex roles inclusion and a richer set of datatypes compared to the first version of OWL (Grau et al., 2008a).

Unfortunately, we cannot simply use tOWL with OWL 2 because of the undecidability added by the concrete domains constructs used in tOWL (Milea et al., 2012). To be able to use tOWL with the level of expressiveness of OWL, some modifications are needed.

3 COMPATIBILITY OF TOWL CONSTRUCTS WITH OWL 2

In this Section, we describe the main constructs changes made in tOWL to achieve compatibility with OWL 2.

3.1 Layers

OWL 2 does not allow the full use of concrete domains since the use of concrete domains next to nominals can lead to undecidability (Milea et al., 2012).

The current version of OWL (Hitzler et al., 2009a) uses datatype maps to add concrete roles and datatypes to the language, unlike the first version, which used a simplified version of concrete domains to represent datatypes (Grau et al., 2008b).

To be able to use tOWL as OWL 2 constructs, we need to make a few modifications in the language, specially in the aspects related to Concrete Domains. Considering this, we propose the following layers as an extended version of tOWL: *Layer of Concrete Path, Layer of Temporal Reference* and *Layer of 4D fluents*, as described in Figure 1.

The Layer of Concrete Path adds constructs that are equivalent to the ones in the tOWL Layer of Concrete Domains using constructs that are similar to ones already present in OWL 2, not affecting the decidability of the language. All the constructs of the Layer of Concrete Domains were removed from the original tOWL and the following ones are added: DatatypePropertyChain and SubDatatypePropertyOf. These constructs



Figure 1: Layers of tOWL compatible with OWL 2.

will be explained in detail in the next subsection. The constructs dataSomeValuesFrom and dataAllValuesFrom already have a version in OWL 2, so we don't need to add this constructs to this layer, as shown in Table 3. In the Table 3 u_1 and u_2 are concrete feature chains, p_d is a concrete domain predicate, $S_1 \dots S_n$ are concrete roles and dr is a data range.

The Layer of Temporal Reference defines the intervals and points in time, we add to this layer the Allen's 13 intervals relations (Allen, 1981) to establish relations between intervals, tOWL also implements these relations, but the details were not made available. An interval *i* is considered a pair of real ordered numbers, (x_1, x_2) , with $x_1 \le x_2$. Considering this, an interval can be defined as shown in Eq.7.

$$Interval = (start \le end) \tag{7}$$

A pair of intervals groups two intervals as first and second:

$$Pair = \exists first.Interval \sqcap \exists second.Interval \qquad (8)$$

The Layer of 4D Fluents adds temporality for intervals, including the concept of fluents defined as properties which the value can change with time. This layer also adds the concept of timeslides, timeslices are intervals when a certain fluent is valid. For example, an aircraft can have as a fluent the property of phase of the flight, and we could have a timeslice for the interval when this aircraft is on the phase of taking off. This layer does not need any modification to be compatible with OWL 2. These constructs have been already presented in Table 2.

3.2 DatatypePropertyChain and SubDatatypePropertyOf

One of the reasons the Layer of Concrete Domains was added into tOWL was to allow the use of the Con-

crete Feature Path (CFP). An example of a CFP was presented in Equation 4 and is represented in tOWL as the construct ConcreteFeatureChain. This construct is fundamental for the tOWL language, since we need composition of features to represent constructs related to time, such as the one shown in Equation 5. The tOWL language uses features, i.e., functional properties that can assume abstract or concrete values. Features are also part of Concrete Domains.

Since OWL 2 does not use Concrete Domains, we are not able to use elements from Concrete Domains, such as concrete and abstract features. Since we cannot use features, we are also not able to represent CFP as defined in tOWL. However, in OWL 2, we have similar definitions to features: concrete roles and abstract roles (Hitzler et al., 2009b). Abstract roles connects individuals to individuals and concrete roles connects individuals to data values, i.e., elements that have datatypes.

To make this glue between tOWL and OWL 2, we need to be able to represent Concrete Feature Path using elements that are present in OWL 2.

In OWL 2, we can have the composition of abstract roles, as shown in Table 4, where $R_1 \dots R_n$ are concrete roles, with $n \in \mathbb{N}$.

Based on this construct, which already exists in OWL 2, we can create compatibility with tOWL presenting a new construct with an equivalent function to ConcreteFeatureChain: the DatatypePropertyChain. This structure creates the compatibility between tOWL and OWL 2, thereby, we do not have to rely on Concrete Domains to represent composition of abstract roles and concrete roles. We can create compositions of n abstract roles and one concrete role, as shown in Table 5.

Using the construct shown in Table 5, we also add a new construct to increase the expressiveness of the language: complex role inclusion with concrete roles. This structure is not present in tOWL, we present this as an addition to the language to simplify the representation of concrete roles. With the expressiveness of SROIQ, we can have role axioms as described in Eq.9.

$$R_1 \circ R_2 \sqsubseteq R_3, \tag{9}$$

where R_1 , R_2 and R_3 are abstract roles.

Using the construct DataPropertyChain, we can extend the construct shown in Eq. 9, named *Complex Role Inclusion*, to also apply to concrete roles. Table 6 introduces a new construct added to tOWL, defined as SubDatatypePropertyOf, where $R_1 ldots R_n$ are abstract roles, and S_1 and S_2 are concrete roles.

Having defined this new construct, we can now create new concrete roles using role composition. It

Table 3: tOWL constructs vs OWL 2	constructs.
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tOWL Construct	OWL 2 Construct
dataSomeValuesFrom $(u_1 \ u_2 \ p_d)$	DataSomeValuesFrom $(S_1 \ \ S_n \ dr)$
dataAllValuesFrom $(u_1 \ u_2 \ p_d)$	DataAllValuesFrom $(S_1 \ \ S_n \ dr)$

Table 4: Composition of abstract roles.

OWL 2 Construct	DL Syntax	DL Semantics
ObjectPropertyChain($R_1 \ \ R_n$)		$\{(a,b)\in\Delta^I imes\Delta^I $
		$\exists c \in \Delta^{I}.(a,x_{1}) \in R_{1}^{I} \land (x_{1},x_{2}) \in$
		$R_2^I \wedge \ldots \wedge (x_{(n-1)}, b) \in R_n^I \}$

Table 5: Semantics and Syntax of DatatypePropertyChain.

tOWL Construct	DL Syntax	DL Semantics
DataPropertyChain(R_1 R_n S)	$R_1 \circ R_2 \circ \ldots \circ R_n \circ S$	
		$\exists c \in \Delta^{I}.(a, x_1) \in R_1^{I} \land (x_1, x_2)$
		$\in R_2^I \land \dots \land (x_{n-1}, b) \in S^I \}$

is possible to create a new role to denote the beginning of an interval, using the composition shown in Eq. 5 combined with Eq.10.

$$time \circ start \sqsubseteq startOfInterval \tag{10}$$

The same algorithm used to evaluate the composition of abstract roles can be adapted to evaluate the concrete feature chain (Horrocks et al., 2006), keeping decidability of the language.

4 CASE STUDY: PHASES OF FLIGHT

In this section we present an application for the tOWL version compatible with OWL 2. We propose an ontology for representing the phases of an airline flight. Usually, a flight is divided in the following phases: (i) take-off, (ii) climb, (iii) en route, (iv) descent and (v) landing (Seyfarth et al., 2002).

In such an ontology, each flight is connected to a flight phase in a certain timeslice. The timeslice represents the interval when such a relation is true, in this case, the interval when a flight is in a certain phase.

Figure 2 presents an example for a flight that is in the stage en route. We have two classes, Flight and FlightPhase that are both subclass of Class. We represent a flight of number TK1041 as iFlight#TK1041, an instance of the class Flight. Similarly, we present the phase en route as iEnRoute, a instance of FlightPhase. The constructs iFlight#TK10141_TS1 and iEnRoute_TS1 are both instances of the class TimeSlice, and they are connected by the property timeSliceOf to iFlight#TK1041 and iEnRoute, respectively. Each timeslice is associate with an interval and since the flight and the flight phase belong to the same timeslice, the values of the intervals should be the same.

Using the constructs already presented in OWL 2, we can represent the fact that the start of iInterval1 should be smaller than the end:

```
EquivalentClasses(iInterval1
  DataAllValuesFrom(start end
  DataComparison(Arguments(x y)
  leq( x y ))))
```

However, without extending OWL 2 we cannot represent a role that is made of a composition of an abstract role and a concrete role. For example, to create a new role that is the start of a interval. This can be done with the constructs presented in this paper, creating the role startOfInterval:

```
SubDatatypePropertyOf(
   DataPropertyChain(time start)
   startOfInterval)
```

We can use such a role in this ontology to define the start of an interval for the timeslice that defines the relation between flight TK1041 and the flight phase en route:

```
DataPropertyAssertion( :startOfInterval
    a:iInterval1 "2014-06-12T04:00:00-05:00"
    ^^xsd:dateTime )
```

tOWL Construct	DL Syntax	DL Semantics
SubDatatypePropertyOf($R_1 \circ R_2 \circ \ldots \circ R_n \circ$	$R_1^I \circ R_2^I \circ \ldots \circ R_n^I \circ$
DataPropertyChain(R_1 R_n S_1) S_2)	$\circ S_1 \sqsubseteq S_2$	$\circ S_1^I \subseteq S_2^I$

Table 6: Semantics and Syntax of SubDatatypePropertyOf.



Figure 2: Application of tOWL for stages of the flight.

In tOWL we don't have enough expressiveness to represent the fact that an aircraft can have 108 seats of the type economic class and 48 seats of the first class. With the extension shown in this paper, we can use tOWL with the expressiveness of OWL. Therefore, we can represent such a statement:

```
ClassAssertion(
```

```
ObjectMaxCardinality( 108 :hasSeats
:EconomicClass ) :iFlight#TK1041 )
```

ClassAssertion(
 ObjectMaxCardinality(48 :hasSeats
 :FirstClass) :iFlight#TK1041)

5 CONCLUSION AND FUTURE WORK

In this paper we presented a study on the compatibility between construct of the temporal language tOWL and the Semantic Web language OWL 2. We propose the addition of constructs that can replace the cause of incompatibility: concrete domains. Using constructs that are already in OWL 2, we can adapt tOWL constructs in a way that we keep decidability in the language.

There are many advantages for adapting tOWL to OWL 2, we have more expressiveness in the language, we can use tools that are only available for the newest version of OWL and we can be up-to-date with the current standards from Semantic Web.

For future work, we will implement a reasoner capable of reasoning with time, adapting reasoners that already exists for SROIQ.

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