

# HBD: Hexagon-Based Binary Descriptors

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**Keywords:** Binary Descriptor, Hexagonal Structure, Hierarchical Grouping, Local Feature Matching, Pose Estimate.

**Abstract:** In this paper, two new rotationally invariant hexagon-based binary descriptors (HBD), i.e., HexIDB and HexLDB, are proposed in order to obtain better feature discriminability while encoding less redundant information. Our new descriptors are generated based on a hexagonal grouping structure that improves upon the HexBinary descriptor we reported previously. The third level descriptors of HexIDB and HexLDB have 270 bits and 99 bits respectively fewer than that of *SHexBinary*, due to sampling  $\sim 61\%$  fewer fields. Using learned parameters, HBD demonstrates better performance when matching the majority of the images in Mikolajczyk and Schmid's standard benchmark dataset, as compared to existing benchmark descriptors. Moreover, HBD also achieves promising level of performance when applied to pose estimation using the ALOI dataset, achieving  $\sim 0.5$  pixels mean pose error, only slightly inferior to fixed-scale SIFT, but around 1.5 pixels better than standard SIFT.

## 1 INTRODUCTION

Local feature descriptors are deemed to be one of the most significant research topics in computer vision, since they are required to facilitate computer vision tasks. Approaches to formulating local feature descriptors have been intensively researched and can be divided into two categories: floating-point descriptors and binary descriptors. Floating-point descriptors usually represent the distribution of local gradient information, and the most widely-reported of these is SIFT (Lowe, 2004). Variants of SIFT, have been reported, which aims to improve overall computational efficiency for descriptors, such as PCA-SIFT (Ke and Sukthankar, 2004) and SURF (Bay et al., 2006). However, new algorithms are needed to generate highly efficient feature descriptors in terms of computational and storage requirements because of the increasing demands of real-time applications. BRIEF (Calonder et al., 2010) is such a descriptor having been designed to improve computational efficiency by generating binary bit-strings that encode local pixel intensity comparisons. The performance attained by BRIEF when matching local features has resulted in binary descriptors being investigated intensely. BRISK (Leutenegger et al., 2011) and FREAK (Alahi et al., 2012) are two examples of the binary descriptors also computed by comparing pixel intensity values for different sampling structure configurations.

HexBinary (Liu et al., 2014) is a hierarchical binary descriptor that is based on the hexagonal grouping structure that was first employed by the HexHoG (Liu and Siebert, 2014) descriptor. The HexBinary descriptor employs a hierarchical grouping mechanism which includes combining vectors representing overlapping image regions to improve the feature's discriminability. However, this approach can result in repeated overlapping of the same local image area to produce excessive redundancy, thereby degrading the descriptor's performance. Therefore, the main contribution in this paper is a new hexagonal grouping structure that results in less redundant information, reduced computation and better feature distinctiveness due to it sampling  $\sim 61\%$  fewer fields for the third level descriptor. This new grouping structure has lead us to formulate two new Hexagon-based Binary Descriptors (HBD): Hexagon-based Intensity Difference Binary (HexIDB) and Hexagon-Based Local Difference Binary (HexLDB). In addition, the parameters used to compute HBD are learned by training on a well-known image dataset proposed by (Mikolajczyk and Schmid, 2005). Descriptor variants of the HBD that we have formulated outperform the variants of the FREAK and SIFT descriptors we have used in our local feature matching performance comparisons. Moreover, HBD has been evaluated for use in pose estimation using the ALOI (Geusebroek et al., 2005) image dataset and exhibits competitive performance when compared to fixed-scale SIFT (*US-SIFT*), and

much better performance than the standard SIFT in terms of mean pose error.

## 2 RELATED WORK

In general, real-time applications necessitate descriptors which are inexpensive in terms of computation and storage requirements. BRIEF (Calonder et al., 2010) is such a robust binary string descriptor, which achieves a substantially improved efficiency in terms of computation, matching and storage compared to SURF and U-SURF (Bay et al., 2006). The BRIEF descriptor encodes pairwise intensity comparisons, each sampled over Gaussian weighted image regions; as only the sign of the comparison is stored as a binary bit, such a feature can be represented as a binary string. The similarity between such binary-string descriptors can be efficiently computed using the Hamming distance, rather than  $L_2$  norm distance. ORB (Rublee et al., 2011) is a scale and rotation invariant version of BRIEF. In BRISK (Leutenegger et al., 2011), its support region is sampled in a rotationally symmetric manner, similar to that of the DAISY (Tola et al., 2010) descriptor. Based on the feature detection approach of BRISK, FREAK (Alahi et al., 2012) approximates a retinal sampling pattern whereby the sampling Gaussian kernel size increases exponentially as a function of distance from the feature's centre. This complex configuration has been reported to generate highly discriminative features.

In contrast to the binary descriptors introduced above, Local Difference Binary (LDB) (Yang and Cheng, 2012) descriptors compute the binary bit not only from intensity comparisons, but also from gradient comparisons. The average intensity and gradient in the  $x$  and  $y$  directions are compared between each of two grids to generate a 3 bit vector. HexBinary (Liu et al., 2014) is a hierarchical descriptor generated recursively from a hexagonal grouping structure. The binary bit is computed by comparing the pixel pairs sampled in a hexagonal structure. HexBinary is different to other lightweight descriptors in that it achieves rotation invariance without rotating the local sampling patch, but through utilising the inherent rotational symmetry of hexagonal sampling. HexBinary's hierarchy is constructed by grouping new hexagons within in a hexagonal structure. This produces multiple or "overlapping" encodings of the same image region, and has been adopted since this approach been reported to improve feature discrimination performance (Dalal and Triggs, 2005). However, repeated overlapping of the same image area can produce excessive redundancy. In this paper,

we introduce a new hexagonal grouping structure that has been designed to reduce the overlap frequency of each sampling area. In addition, our new descriptor encodes both the intensity and gradient comparison information to generate the binary bits of a binary-string feature representation. We employ the same approach to compare Gaussian weighted image regions as utilised within the second-order HexBinary descriptor *SHexBinary*. Two new HBD are introduced here: HexIDB and HexLDB, and their matching performance is validated for pose estimation where the descriptor's parameters have been learned.

## 3 APPROACH

In this section, we give the details of how we construct the hexagonal grouping structure to generate new hierarchical binary descriptors: HexIDB and HexLDB. Since the structure is based on that of the HexBinary descriptor, we now briefly describe the HexBinary structure below.

### 3.1 Sampling Structure

The sampling structure used to compute the second level HexBinary descriptor is illustrated in Figure 1 (a). The red  $\star$  indicates the feature point position, and the descriptor for this feature point is computed from the neighbouring region in the hexagonal structure. The validation of the HexBinary descriptor has demonstrated that this hierarchy, up to the third level, is a good trade off between descriptor matching effectiveness and efficiency. Therefore, in this paper, the hierarchy is also only considered up to the third level.

The sampling structure used to construct three levels of HexBinary descriptors is summarised as follows: a hexagon of defined size is constructed centred on the feature point  $p$ , so in total 7 points are sampled at: the 6 vertexes and the central location of the descriptor ( $p$ ). For the first level HexBinary descriptor termed as *HexBinary1* of  $p$ , the binary bits are computed from the 7 sampling points in this single hexagon; For the second level descriptor *HexBinary2*, the 7 sampling positions of the hexagon are treated as 7 feature points. The *HexBinary1* descriptors comprising 7 feature points are similarly computed, and are then concatenated together to form the second level descriptor  $p$ ; Similarly, the third level descriptor *HexBinary3* of  $p$  is generated by concatenating the *HexBinary2* descriptors of the 7 feature points likewise computed, as described above. Therefore, as the grouping level of the descriptor

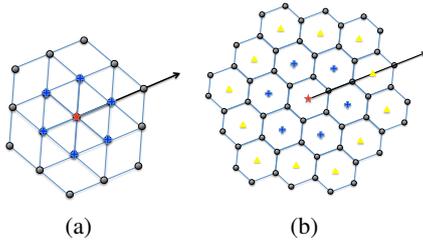


Figure 1: (a) is the second level structure of generating HexBinary. (b) is the new proposed structure of the third level hexagonal descriptor. The red star point represents the key-point position where to sample the local descriptor. The arrow illustrates the dominant orientation of the local region around the key-point. The first level hexagonal grouping structure comprises the basic hexagon centred at the red  $\star$ , and the sampling positions are taken from the hexagon centre and the vertexes. The second level hexagonal structure now covers more image area around the key-point since six more hexagon centres are sampled as shown in blue  $+$ , according to the difference between (a) and (b) structure boundaries. For the third level descriptor, another 12 more hexagon centres as shown in yellow  $\triangle$  in (b) are computed together with the previous 7 hexagon centres around the key-point, while in (a), 7 second level structure will be constructed centred on the red  $\star$  and blue  $+$ . All the black points indicate the sampling positions according to the corresponding hexagonal centre positions.

increases, the information around the 7 sampling positions will be repeatedly overlapped. Although overlapped-sampling can improve the stability of a local descriptor, repeated overlapping will eventually result in excessively redundant information being accumulated, which decreases the discriminability of the feature descriptor. To address the issue of redundant information when generating higher level descriptors, the new proposed hexagonal structure is constructed as in Figure 1 (b). The details of how to compute a three level hierarchy are now presented in the following steps:

1. Localise the key-point position, and compute the dominant orientation of the local area around this key-point.
2. According to the dominant orientation and the given edge length of the hexagon, the sampling positions of the basic hexagon vertexes are defined. Then the first level hexagonal descriptor could be computed according to the binary descriptor generation method described in the following subsection, which is used by *SHexBinary*.
3. Sample another 6 positions to be the new hexagon centres as the blue  $+$  shown in Figure 1 (b). These new hexagon centres are not the same 6 vertexes comprising the basic hexagon generated in first level, which is the main difference from the HexBinary structure in Figure 1 (a). Each new

hexagon shares an edge with the basic hexagon centred at the key-point.

4. The second level hexagonal descriptor is generated by concatenating the 7 first level hexagonal descriptors extracted centred on the 7 basic hexagons.
5. Sample 12 more positions to be the new hexagon centres as the yellow  $\triangle$  in Figure 1 (b). This is a similar process to that of step 3, which also differs from the HexBinary structure.
6. Concatenate these first level descriptors extracted centred on the 19 basic hexagons to generate the third level hierarchical descriptor.

Throughout the above steps, the higher level descriptors are generated by extending the feature area without repeatedly overlapping the central area, while in the HexBinary hierarchical structure, the overlap frequency of the central area is increased as the grouping level of the hierarchy increases. For instance, the blue  $+$  areas in Figure 1 (a) will be repeatedly overlapped by 7 times for constructing the second level descriptor and 49 times for the third level descriptor, while the same positions in Figure 1 (b) will be only overlapped 3 times for all the higher level descriptors over the first level. The pseudocode to generate the new hierarchical HBD is presented in Algorithm 1.

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#### Algorithm 1: Hierarchical HBD Descriptor Generation.

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 $p_0(x,y)$ : Feature Point
 $\theta_0$ : Local Dominant Orientation Centred at  $p_0$ 
 $L$ : Defined Edge Length of the Basic Hexagon
 $V_i(x,y) (i \leftarrow 1, 2, \dots, 6)$ : Vertex Positions of the Basic Hexagon
 $ts \leftarrow \pi/3$ 
for  $i \leftarrow 1 : 6$  do
   $tv \leftarrow (i-1)ts + \theta_0$ 
   $V_i(x) \leftarrow L \times \cos(tv)$ 
   $V_i(y) \leftarrow L \times \sin(tv)$ 
end for
Compute the First Level Descriptor  $HBD1_0$  for Feature point  $p_0$ 
for  $i \leftarrow 1 : 6$  do
   $tv \leftarrow (i-1)ts + \theta_0 + \pi/6$ 
   $p_i(x) \leftarrow 2L \times \cos(\pi/6) \times \cos(tv)$ 
   $p_i(y) \leftarrow 2L \times \cos(\pi/6) \times \sin(tv)$ 
end for
Compute the First Level Descriptor  $HBD1_i$  for  $p_i (i \leftarrow 1, 2, \dots, 6)$ 
Generate the Second Level Descriptor  $HBD2_0$  for Feature point  $p_0$ 
 $HBD2_0 \leftarrow HBD1_0 HBD1_1, \dots, HBD1_6$ 
for  $i \leftarrow 7 : 12$  do
   $tv \leftarrow (i-7)ts + \theta_0$ 
   $p_i(x) \leftarrow 3L \times \cos(tv)$ 
   $p_i(y) \leftarrow 3L \times \sin(tv)$ 
end for
for  $i \leftarrow 13 : 18$  do
   $tv \leftarrow (i-12)ts + \theta_0 + \pi/6$ 
   $p_i(x) \leftarrow 4L \times \cos(\pi/6) \times \cos(tv)$ 
   $p_i(y) \leftarrow 4L \times \cos(\pi/6) \times \sin(tv)$ 
end for
Compute the First Level Descriptor  $HBD1_i$  for  $p_i (i \leftarrow 7, 8, \dots, 18)$ 
Generate the Third Level Descriptor  $HBD3_0$  for Feature point  $p_0$ 
 $HBD3_0 \leftarrow HBD1_0 HBD1_1, \dots, HBD1_{18}$ 

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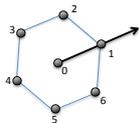


Figure 2: The first level structure. The arrow indicates the local dominant orientation.

### 3.2 Descriptor Construction

To afford the descriptor with rotation invariance, the local dominant orientation is computed as introduced in (Liu et al., 2014). The first level structure is defined according to the dominant orientation as shown in Figure 2. The image is first filtered by a Gaussian kernel of standard deviation  $\sigma$ , and the smoothed intensity values sampled at the hexagon centre and vertices are denoted by:  $I_i(i=0,1,\dots,6)$ . The first level descriptor is then computed by comparing the intensity differences. The binary bit  $\tau$  of the descriptor is corresponding to :

$$\tau(D; i, j) = \begin{cases} 1 & \text{if } D_i < D_j \\ 0 & \text{otherwise.} \end{cases} \quad (1)$$

where  $(\mathbf{D}_i, \mathbf{D}_j)$  is a spatially adjacent pair of intensity difference, e.g.,  $(\mathbf{D}_i = I_1 - I_0, \mathbf{D}_j = I_0 - I_4; \mathbf{D}_i = I_1 - I_6, \mathbf{D}_j = I_2 - I_1)$ . The 9 pairs of  $(\mathbf{D}_i, \mathbf{D}_j)$  in the hexagon are then selected to generate a 9 bit binary string as the first level descriptor. When constructing the next higher level descriptor, each newly constructed hexagon in the structure will generate a first level descriptor, and these are concatenated together to form the higher level descriptor. This new hexagonally structured hierarchical descriptor is termed HexIDB (Hexagon-based Intensity Difference Binary).

Similarly, another new descriptor HexLDB (Hexagon-based Local Difference Binary) is proposed by not only encoding intensity differences, but also by encoding gradient differences. This is similar to but slightly different to the LDB descriptor. LDB generates a 3 bit vector by comparing the differences of the local average intensity, gradients in x and y directions between the pair of grids, respectively. Here the gradient information is also considered but without being divided into x and y directions. A gradient map is computed, then the comparison pair  $(\mathbf{D}_i, \mathbf{D}_j)$  in Function 1 could be the gradient difference pair, e.g.,  $(\mathbf{D}_i = G_1 - G_0, \mathbf{D}_j = G_0 - G_4)$ .  $G_i(i=0,1,\dots,6)$  represents the gradient value of the sampling position. Therefore, for each pair comparison, a 2-bit vector is generated, and in each level of the Hierarchy, HexLDB will have double length of the vector than HexIDB. The descriptor lengths and the number of sampling fields of *SHexBinary* and the new proposed HBD are illustrated in Table 1.

Table 1: The descriptor length ( $L$ ) and the number of sampling fields ( $N$ ).

$L N$	Level1	Level2	Level3
<i>HexIDB</i>	9 7	63 49	171 133
<i>HexLDB</i>	18 7	126 49	342 133
<i>SHexBinary</i>	9 7	63 49	441 343

## 4 PARAMETER LEARNING

Good feature descriptors always rely on the good collaboration amongst their critical parameters. For HBD, which we refer to as HexIDB and HexLDB in this paper, the essential parameters are: the edge length of the basic hexagon and the standard deviation,  $\sigma$ , and support size of the Gaussian sampling kernel. These parameters are learned through local feature matching experiments. We determine the descriptor's matching performance for a specific parameter configuration by measuring the *RecognitionRate* for nearest neighbour (NN) matching, as introduced in (Calonder et al., 2010): *RecognitionRate* is computed as follows:

Firstly,  $N$  key-points are detected in the reference image, and  $N$  corresponding Key-points are inferred in the test image according to the ground-truth geometric relation between the two images; Secondly, we compute the  $2N$  key-point descriptors by the method under consideration, and for each descriptor in the reference image, find its *NN* in the test image. Thereafter, the *RecognitionRate* is given by  $C_n/N$ , where  $C_n$  is the number of correct matches.

Any local feature detector could be employed to indicate where to extract the HBD. FAST (Rosten et al., 2010) is an efficient and widely used detector which is employed in this paper. The HexBinary descriptor reported in (Liu et al., 2014) is parameterised with a hexagon edge length of 3 pixels, and the support size of the Gaussian sampling kernel is  $9 \times 9$  pixels with  $\sigma = 2$  pixels. We apply the same range of numeric values here for HBD to learn the best parameters for the image dataset being matched. When one of the parameters is under test, all the remaining parameters must be fixed. For instance, when learning the  $\sigma$  of the Gaussian sampling kernel, the edge length is set to 3, and the Gaussian kernel support size is set to  $9 \times 9$ .

### 4.1 Dataset

The experiment is performed on the well-known and publicly available image dataset by (Mikolajczyk and Schmid, 2005) as shown in Figure 3. The images contained in this dataset include typical image disturbances occurring in real-world scenarios, such as:

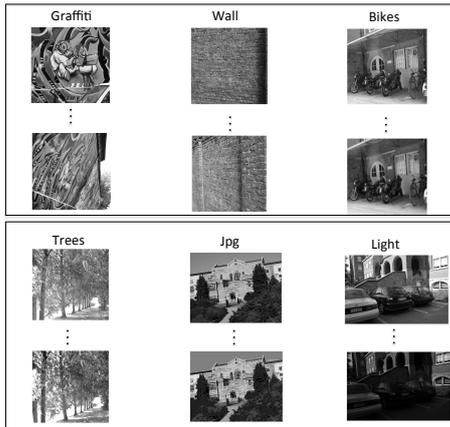


Figure 3: Image sequences: each sequence has 6 images, and only the first and the last images are illustrated here. From the second to the sixth image, the difficulty in matching to the first image increases progressively.

- viewpoint changes: Graffiti and Wall;
- image blur: Bikes and Trees;
- compression artefacts: Jpg
- illumination changes: Light

For each sequence, the test is designed to match the first image to the remaining 5 images to get 5 pairs of matching cases sorted in order of ascending difficulty. Therefore, pair 1|6 is much harder to match than pair 1|2 for each sequence.

## 4.2 Learning Parameters

The Gaussian standard deviation  $\sigma$  is tested in the range of  $[0.2, 4.2]$  pixels. Only the performance of the third level descriptor is presented here because the third level descriptor always performs better than the lower level descriptors. The *RecognitionRate* performance according to different values of  $\sigma$  has been investigated and it was discovered that for each matching pair, the *RecognitionRate* gradually improves as  $\sigma$  increases, but it declines as the difficulty of matching increases, due to the increasing dissimilarity between compared pairs of images. For both of these descriptors, their performance becomes relatively constant when  $\sigma$  reaches between  $[3, 4.2]$  pixels, for all of the matching pairs. Therefore, a  $\sigma$  of 3.4 pixels was chosen as a good compromise value to reduce sensitivity to noise while retaining a distinctive structure to achieve stable descriptors. Based on the above  $\sigma$  value, an appropriately sized Gaussian kernel support size has been selected comprising  $17 \times 17$  pixels (we evaluated different kernel support sizes in the range  $13 \times 13$  to  $23 \times 23$ ).

Having fixed the  $\sigma$  value of the Gaussian sampling kernel and its associated support size, the experiments for learning the hexagon edge length were then conducted and we discovered: there is no significant difference in performance when the edge length varies between 3 to 8 pixels for most images. In the cases of the two blurred images, Bikes and Trees, the larger edge length performs better than smaller edge length, particularly when the image pair is harder to match using more deeply blurred sequences. This may be because the deeply blurred images lose more high frequency information which makes the local point indistinct within a small area. For all the later experiments, an edge length of 3 pixels is employed to construct the hexagonal structure for our local binary descriptors.

Based on the above learned parameters, the matching performance for 3 different grouping levels of HexIDB and HexLDB are given in Figure 4. It is clearly evident that higher grouping levels always outperform the lower grouping levels because of their extended area of image coverage, thereby including more diagnostic image information. For the Graffiti, Wall, Light and Jpg sequences, HexLDB performs better than HexIDB. However, the two sequences with blurring issues: Bikes and Trees, give different results. As the descriptor level increases, HexLDB gradually loses its advantage of including gradient comparison information and when the matching pair comprises more dissimilar image pairs, such as Bikes 1|6, the gradient comparison information appears to disadvantage the HexLDB descriptor. This indicates that the gradient information in the image is being greatly reduced when the image is significantly blurred, which results in gradient signals with a poor SNR.

## 4.3 Performance Evaluation

In order to evaluate the new descriptors with the learned parameters, the local feature True Positive matching rate for the third level grouping of the HBD (including SHexBinary3 (Liu et al., 2014), HexIDB3, HexLDB3) is compared to the performance obtained using state-of-the-art descriptors, FREAK (Alahi et al., 2012) and SIFT (Lowe, 2004). HBDs are claimed to have rotation invariance by directly constructing the sampling structure according to the local dominant orientation. There is no need to pre-rotate the local patch to align with the local dominant orientation, which is the conventional standard way to achieve rotation invariance. In order to have a fair comparison, no scale and no orientation is considered in this test. Both FREAK, SIFT and HBD have been

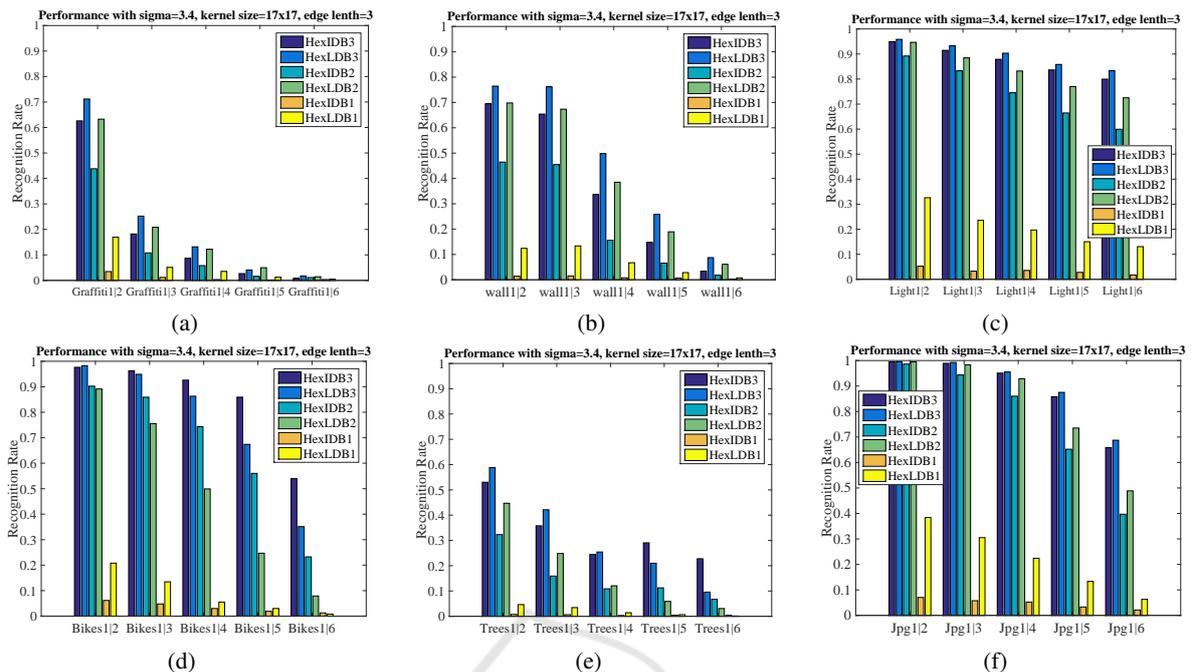


Figure 4: *RecognitionRate* (True Positive descriptor matching rate) performance obtained for Gaussian  $\sigma=3.4$ , kernel size= $17 \times 17$ , hexagon edge length=3. For each image pair, the matching performance obtained for each of the 3 grouping levels used in the *HexIDB* and *HexLDB* descriptors is illustrated.

coupled to the FAST detector for single scale experiments and termed as *U-descriptor*, which indicates that they do not normalise the descriptor orientation. Since SIFT is a multi-scale detected feature, for clarity, SIFT without rotation and scale invariant property is termed as *USO-SIFT*.

Figure 6 illustrates the matching performance of each image pair with different descriptors. It is observed that on all the image sequence pairs except Graffiti, *U-HBD* and *USO-SIFT* both perform better than *U-FREAK*. *U-HexLDB3* always outperforms *U-HexIDB3* on image sequences of Graffiti and Wall. They achieve quite similar results on Light and Jpg image pairs, and also the first three image pairs of Bikes and Trees sequence. For the harder-to-match pairs of Bikes and Trees, *U-HexLDB3* loses its advantage of utilising gradient comparison information. *U-SHexBinary3* is inferior to *U-HexLDB3* and *U-HexIDB3* for almost all the image pairs, which confirms the improvement of distinctiveness for the new proposed hierarchical hexagon structure. *USO-SIFT* achieves similar performance to *U-HexLDB3* and *U-HexIDB3* for most matching pairs comprising Light, Bikes, and Jpg sequences. For the remainder of the sequences, its performance is always inferior to that of *U-HexLDB3*.

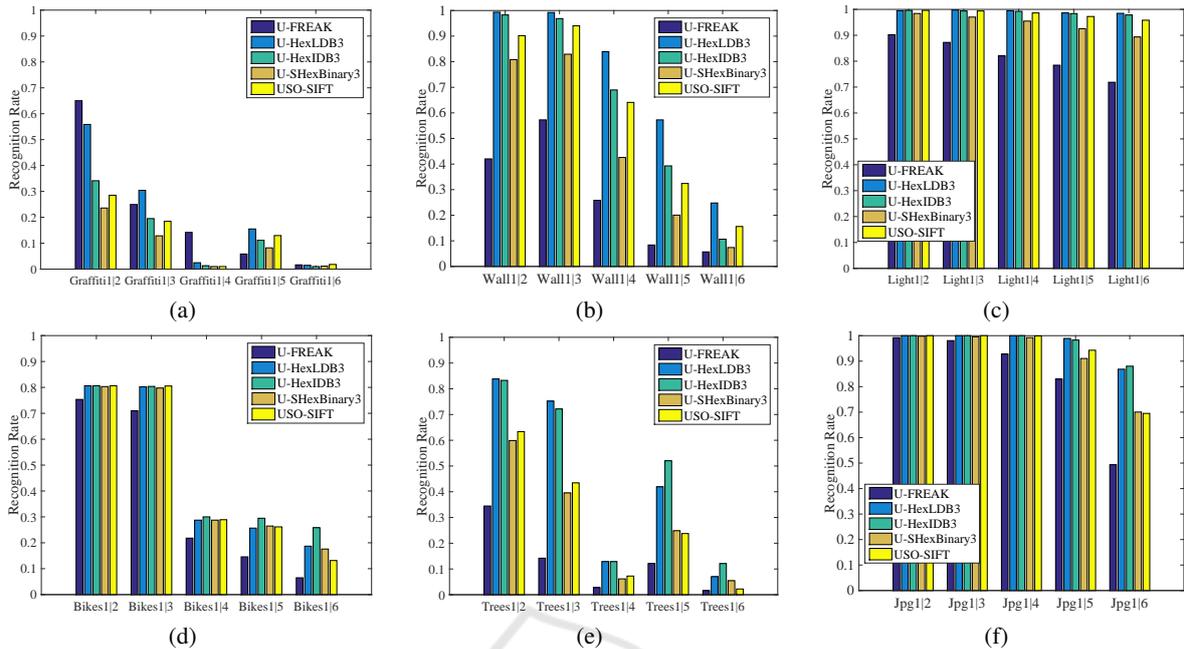


Figure 5: Pose estimate: each test image is only matched to the corresponding reference image for detection and pose estimate.

## 5 POSE ESTIMATION

We have also evaluated the new descriptors for pose estimation and employed the same pose estimation system and the same test dataset from Amsterdam Library of Object Images (ALOI) (Geusebroek et al., 2005), as we presented in (Liu et al., 2014). Because we are focusing on pose estimation, rather than object detection, each test image contains the object of interest set within a cluttered background and this is directly matched to the corresponding reference image, where the target object in set against a pure black background, as shown in Figure 5. Therefore, one-to-one image matching is implemented to detect the object via the Generalised Hough Transform (GHT) and we obtain a pose estimate by means of the RANSAC algorithm.

We evaluate the pose estimation performance of

Figure 6: *RecognitionRate* performance with different descriptors.

our system by computing the mean and standard deviation of the pose errors of all the detected objects. The precise location of the edge contours of the reference object in the test image can be obtained according to the recorded ground-truth information, which specifies the rotation and translation used to embed the reference object pixels into a background image. Similarly, according to the recovered pose estimation using the system, the estimated object edge positions could be labelled by projecting the reference edge positions into the test image. The Euclidean distance between the estimated position and the ground-truth position of each reference edge point is computed to yield a pose estimate error for each matched edge location.

Four different features are tested: standard SIFT (*SIFT*), SIFT without scale invariance (*US-SIFT*), *HexIDB3* and *HexLDB3*. Except *SIFT*, which employs its own feature detector to afford scale invariant matching, all the other features we examined are sampled at locations defined by key-points detected by the FAST detector at a single scale. Each reference image has 5 different corresponding test images with different backgrounds, but without scale changes. 5000 synthetic images are tested and matched to their corresponding 1000 reference images. Our object detection and the pose estimation results are given in Table 2 and Table.3.

In Table 2, The number of detected images having the corresponding pose error is accumulated in different error ranges for each descriptor. Most of the de-

Table 2: Numeric distribution of images detected within a given pose error range (pixels) and the corresponding error ranges.

Error Range	0-0.5	0.5-1	1-1.5	1.5-2	2-3	3-4	4-5	5-Inf
<i>SIFT</i>	270	355	<b>350</b>	<b>359</b>	<b>1348</b>	<b>108</b>	<b>44</b>	146
<i>US-SIFT</i>	<b>2787</b>	387	165	179	69	40	22	132
<i>HexIDB3</i>	2401	<b>471</b>	176	92	88	51	38	<b>1036</b>
<i>HexLDB3</i>	2570	465	175	84	113	50	33	607

Table 3: Number of images successfully detected with a pose error of less than 5 pixels, and their corresponding pose error Mean (*Mean*) and standard deviation (*SDV*) in pixels.

Descriptor	SIFT	US-SIFT	HexIDB3	HexLDB3
<i>Number</i>	2834	<b>3549</b>	3317	3490
<i>Mean</i>	1.9241	<b>0.4209</b>	0.5295	0.5207
<i>SDV</i>	0.9560	<b>0.6541</b>	0.7489	0.7375

tected images have a pose error of less than 5 pixels for all the descriptors examined. Since there is always a one-to-one image match, to better compare the performance of different descriptors, each detected image having pose error bigger than 5 pixels is defined as a failed detection. The *Number* of successfully detected images in Table 3 only accounts the images with pose error smaller than 5 pixels, based on which, the *Mean* and *SDV* of the pose error through the images are computed for each descriptor, respectively.

It is clearly shown in the results tables that, *US-SIFT* achieves the best performance in terms of the mean pose error. It has the biggest number of images having pose error less than half pixel, while *SIFT* has the least number of images successfully detected with the mean pose error close to 2 pixels. The test images do not have scale changes from the reference im-

ages, which might be the reason for *SIFT* exhibiting inferior results to all of the other descriptors. Due to multi-scale detection being applied in this case, the associated Hough parameter space needs one more dimension to be able to detect objects, compared to the hough space generated for the other single scale descriptors, which leads to lower pose estimate accuracy. *HexLDB3* works a little better than *HexIDB3* due to the extra comparison information from the gradient map. In summary, except *SIFT*, all of the other descriptors gave close results in terms of pose estimation, exhibiting an error of approximately half a pixel.

## 6 CONCLUSION

In this paper, we present two new HBD: HexIDB and HexLDB descriptors. The new sampling structure of HBD reduces redundant information being encoded by decreasing the frequency of the same image area being sampled, and produces shorter feature descriptors for the third level of the feature hierarchy, as compared to HexBinary descriptors. Moreover, a gradient map is also employed to generate the binary bits in the same way as the intensity map is encoded. However, it is not a wise choice to use the gradient map when the gradient information representing image features has a low SNR. The HBD outperforms *SHexBinary* and achieves very promising results compared to fixed-scale *U-FREAK* and *USO-SIFT* descriptors (no orientation normalisation). HBD is also compared to the standard *SIFT* and a fixed-scale extracted descriptor *US-SIFT* within an object pose estimation application. Although the parameters used in this application are not learned from the training data, HBD still produces much better performance than the standard *SIFT* and shows competitive performance compared to *US-SIFT*. In future work, we would like to investigate dimensionality reduction methods for HBD to decrease feature storage requirements and improve its discriminability. We would also like to investigate the relationship between such hand-crafted descriptors and those derived through learning techniques, such as Deep Convolutional Neural Networks.

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