

Metaheuristic Coevolution Workflow Scheduling in Cloud Environment

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Abstract: Today technological progress makes scientific community to challenge more and more complex issues related to computational organization in distributed heterogeneous environments, which usually include cloud computing systems, grids, clusters, PCs and even mobile phones. In such environments, traditionally, one of the most frequently used mechanisms of computational organization is the Workflow approach. Taking into account new technological advantages, such as resources virtualization, we propose new coevolution approaches for workflow scheduling problem. The approach is based on metaheuristic coevolution that evolves several diverse populations that influence each other with final positive effect. Besides traditional population, that optimizes tasks execution order and task's map to the computational resources, additional populations are used to change computational environment to gain more efficient optimization. As a result, proposed scheduling algorithm optimizes both computation tasks to computation environment and computation environment to computation tasks, making final execution process more efficient than traditional approaches can provide.

1 INTRODUCTION

Today technological progress makes scientific community to challenge more and more complex issues related to computational organization in distributed heterogeneous environments, which usually include cloud computing systems, grids, clusters, PCs and even mobile devices (Boutaba and Cheng, 2012). Day-by-day computational tasks also increase their structure complicity and computational difficulty combining new multiscale and multidiscipline approaches for resolving complicated issues that are imposed by advanced scientific researches. In such heterogeneous environments, traditionally, one of the most frequently used mechanisms of computational organization is a Workflow approach (Yu and Buyya, 2008). It allows to bring complex computational logic in sequential order of executed steps (tasks) linked by input/output data. Due to resources and workflows heterogeneity, one of the most important issues nowadays is the task scheduling as an optimization problem.

Workflow scheduling optimization is NP-complete problem and there are a lot of research dedicated to this area. Most of them are based on

investigations of invented heuristic and metaheuristic algorithms (Yu and Buyya, 2008), as well as on hybrid schemas that take the best parts from both types of algorithms in cooperation (Nasonov and Butakov, 2014). Metaheuristic algorithms include evolutionary methods that contain coevolutionary approach (Back, 1996). In spite of the fact that coevolutionary ideas were proposed a half century ago (Ehrlich and Raven, 1964) a quite new ideas can be applied towards workflow scheduling optimization problem.

One of the main parameters for the optimization in workflow scheduling is makespan that shows the amount of time from the start of workflow's execution to its finish point. Traditionally scheduling algorithms decrease makespan by proposing more efficient task allocation on the available computational resources. Moreover, in cloud computing, cost of execution is also the significant criteria for the scheduling. However, taking into consideration advanced technologies like virtualization, new opportunities can be found in the field of workflow scheduling.

Combining distributed environments features with workflow steps arrangement and resource allocation within coevolutionary principles, we propose the new approaches for workflow

scheduling, which comply more to present-day technologies (in the time of cloud computing) rather than traditional schemas. We propose new coevolution genetic algorithm (CGA), coevolution particle swan optimization algorithm (CPSO) with its ranked and weight ranked extensions' (CRPSO and CWRPSO), as well as coevolution gravity search algorithm (CGSA) for workflow scheduling problem in flexible cloud environment, where computing resources can be modified according to virtualization principles.

2 RELATED WORKS

Palacios et al. (Palacios, 2014) proposed hybrid coevolutionary genetic algorithm (GA) called CELS for fuzzy flexible job shop scheduling problem with heuristic initialization step and additional local species improvement during fitness evaluation. Definition of the problem and developed methods are similar to workflow scheduling problem in the use of mapping and ordering species. Coevolutionary implementation includes mapping and ordering species, which form cooperative populations. However, in our approach the first population optimizes both mapping and ordering, while the second population selects an optimal resources configuration. Also Palacios et al. proposed a different approach for coevolution fitness evaluation with other selection strategy - species coupling is organized according to the best, random, and individual rank.

Huang et al. (Huang and Chen, 2014) offered two coevolutionary algorithms based on GA for job shop scheduling problem with different methods of subpopulation merging. Coevolutionary scheme is based on full task dimension splitting to three subpopulations, thus decreasing the dimensionality of each new population. Whereas our populations develop according to the task characteristic diversity. Huang's work is focused on the selection methods of subpopulations. The first proposed CCGA scheme is based on greedy (by fitness) individual selection from other population while the second DBCCGA computes the distance between individuals and chooses the one from another population according to the obtained distances.

Multi-population PSO (Particle Swarm Optimization) for flow shop scheduling problem was suggested by Liu et al (Liu, 2013). The main idea of this paper is to divide full population into three populations at each iteration and apply different optimization strategies for each population. At the

merging stage the best particles from each subpopulation are used to build a probabilistic model by EDA (Exploratory Data Analysis) and after that to improve the particles, SA (Simulated Annealing) is applied locally to these particles.

In the next work, Jiao et al. (Jiao and Chen, 2011) proposed Cooperative Coevolution PSO based on the catastrophe for fuzzy flow shop scheduling problem. Extended catastrophe operation helps to avoid local optima. Their coevolution interpretation as in the previous works contrasts with our approach in the division of a population into subpopulations.

Verma et al. (Verma and Kaushal, 2014) proposed Bi-criteria priority algorithm based on PSO for workflow scheduling. Their algorithm is hybrid of HEFT (Heterogeneous Earliest Finish Time) heuristic and PSO meta-heuristics. HEFT is used to obtain an order of tasks while PSO is applied for tasks' assignment optimization. The makespan and total cost of result schedule are the main optimization criteria in the paper whereas we consider only the makespan. However, their particle is represented only by task assignment, and ordering of a schedule is performed by Budget HEFT.

The Revised Discrete PSO for cloud workflow scheduling is proposed by Wu et al (Wu, 2010). In this paper authors proposed the bi-criteria optimization of makespan and total cost with initialization by greedy heuristic GRASP algorithm. In comparison to our work, their particle representation contains an ordered vector of pairs (task, node) and particle update is performed only by mapping. During PSO mapping update, the tasks are taken sequentially, in respect to their inner dependencies. Whereas in our work, mapping and ordering are evaluated and updated separately.

Lei (Lei, 2012) offered coevolution GA for fuzzy flexible job shop scheduling. Although merging scheme is different to our scheme, this work is similar in used concepts of coevolution and partially has similar representations of the different species. The algorithm performs selection based on the artificial population of a scheduled solution while we perform a selection only on population of the same species and the selection of different species can be independent.

Gu et al. (Gu, 2010) proposed algorithm to resolve scheduling problem in the field of stochastic job shop scheduling based on GA. According to experiments, their method outperforms standard widely applied GA and some of its modifications. In contrast to our cooperative scheme, besides the field of application, authors use a competitive coevolution scheme.

Flexible Job shop scheduling problem is solved by using Gravitational Search Algorithm and Colored Petri Net by Barzegar et al. (Barzegar and Motameni, 2012). In comparison to several other algorithms, proposed method exceeds these algorithms in a work speed and efficiency of solutions. However, authors considered job shop scheduling problem, while our work is concerned with workflow scheduling using coevolution principles for the population.

3 COEVOLUTION PRINCIPLES

Applicability of coevolution methods can be found in different areas of optimization problem. Workflow scheduling is one of them. The main idea we propose in this paper is hidden in dynamical changes which can be done in the cloud computational environment during execution process. On the one hand, traditional algorithms try to optimize workflow tasks execution order and resource mapping, while the computation environment is specified by initial conditions. On the other hand, almost all present public clouds are based on advanced technologies like virtualization and efficiently use it for energy and budget saving.

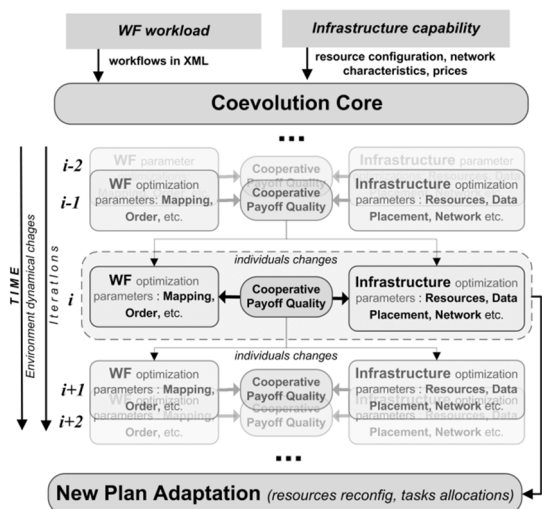


Figure 1: Common schema of coevolution approach for workflow scheduling.

Taking together workflow resource allocation from traditional scheduling optimization and resource configuration optimization from advanced technologies used in cloud computing, new level of efficiency can be achieved. Coevolution idea allows to execute several evolutionary process in parallel

binding them in cooperative manner. On figure 1 the main coevolutionary schema is shown. On the left part, traditional evolutionary process for resource allocation is executed, and at the same time on the right part evolutionary process of resource and data reconfiguration is running. Composite solution payoff quality is estimated on each iteration taking into account both parts of evolutions. Parts are taken according to the used selection strategy and gain payoff quality from the best combination. The best solution is chosen from the current iteration and adapted to the system if it has more efficient execution plan than currently used one.

3.1 Coevolution Genetic Algorithm (CGA)

Scheduling coevolution genetic algorithm (CGA) is built on the cooperation of several populations that search optimized parts of the joint solution. Resources allocation, tasks ordering, data placement and resource configuration optimization can be chosen in the role of those parts. Even traditional GA implementation for workflow scheduling can be divided in two evolutions: task mapping on resources and task execution ordering. Each evolution applies basic schema of crossover, mutation, selection methods with one difference in the fitness function that can estimate new scheduling plans only using part's combination (mapping and ordering together). In (Butakov and Nasonov, 2014) benefits of this approach were shown.

Another idea that can be used in GA is basic scheduling evolution with computation environment evolution together to get even more efficient optimization.

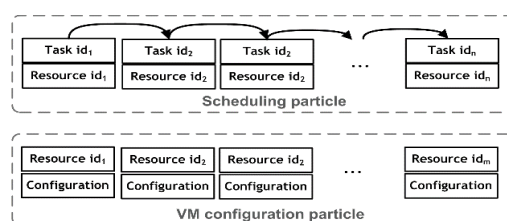


Figure 2: Particles schema in CGA algorithm.

Thus, CGA scheme has two independent populations. The first one optimize scheduling (tasks assignment and their ordering), whereas the second population optimize computing environment for tasks. Since a full solution represents by pair of particles from each population, CGA has additional Merge step, on which populations interact between each other to produce full solution pairs. The

number of produced pairs is an algorithm's parameter called *interactions number*, which should be greater than populations' size. After the Merge stage, we can evaluate fitness function for produced pairs. Each particle receive average fitness of all pairs, where this particle had been. The next steps are mutation and crossover for each population separately.

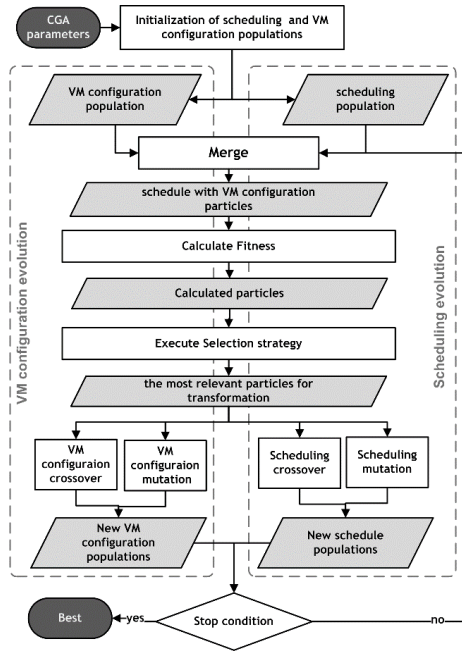


Figure 3: Proposed CGA algorithm main schema.

Particles representation is shown on the figure 2. Mutation for schedule particle is performed by two options: swap two tasks in queue; or randomly change computing resource for a task. We use 2-points crossover to divide the first parent into beginning, middle, and end. Child will contain beginning and end from the first parent, and all other not included tasks from the second parent.

Mutation for a configuration particle has three options: delete resource; add resource; or change a capacity of resource. Crossover is performed by alternately selection of resources from two parents. Tournament selection is used for both populations. Fitness function for all our algorithms is makespan.

3.2 Coevolution Particle Swarm Optimization (CPSO)

PSO is the metaheuristic algorithm proposed by Kennedy and Eberhart (Eberhart and Kennedy, 1995), idea of which was taken from birds flocking

or fish schooling. To find an optimal solution, each particle in the swarm flies according to the personal experience and information about the global best position for whole population. The movement of a particle is defined by its position and velocity, which are updated in each generation. The equations for velocity and position update of the *i*-th particle are:

$$v_i(t + 1) = wv_i(t) + c_1r_1(p_i - x_i(t)) + c_2r_2(g - x_i(t)) \quad (1)$$

$$x_i(t + 1) = x_i(t) + v_i(t + 1) \quad (2)$$

where *t* is current generation, *w* is the inertia coefficient for previous velocity, *c₁* and *c₂* are behaviour coefficients, which define the influence of global best and personal best positions accordingly, *r₁* and *r₂* are random variables in the range [0, 1]. *p_i* is the best position for the current particle and *g* is the global best position for the whole population.

PSO was created for a continuous optimization. To implement PSO for combinatorial space, it is required to define set-based operators between particles and their velocities for computation (1) and (2).

In contrast to other works (Wu, 2010) or (Verma and Kaushal, 2014), our schedule particle representation (figure 2) contains mapping and ordering parts, which allow to generate a more qualitative schedule. In addition, we considered several modifications of basic coevolution PSO scheme to get a broader view of this problem.

Scheme of developed CPSO is shown in figure 4. On the first step, populations are initialized. The first population (Scheduling population) includes particles with mapping and ordering abilities, which are responsible for final tasks scheduling optimization while the second population (VM configuration population) is made of particles that optimize nodes' configuration. On the next step, the populations are merged to obtain individuals for fitness evaluation. To complete the Merge step, *n* particles from one population form pairs with *n* particles from the other population. For each pair the fitness is calculated and then two of the $\log n$ best pairs are selected randomly. The first pair is chosen as a scheduling particle for the configuration population and the second one is chosen for schedule population. In addition, the best pair is checked for the new global best.

After the Merge stage, each population is ready to calculate the fitness for each particle. At the next step, the particles update their velocity and position, according to equations (1) and (2). The last stage is checking all particles for the new best solution. If the Stop condition is not satisfied, the populations

are moved to the next generation. Operators for particles update will be discussed below. These operators are needed to compute (1) and (2).

Let $T = \{t_k\}_{k=1}^M$ – set of tasks, and $R = \{n_l\}_{l=1}^N$ – set of computing nodes.

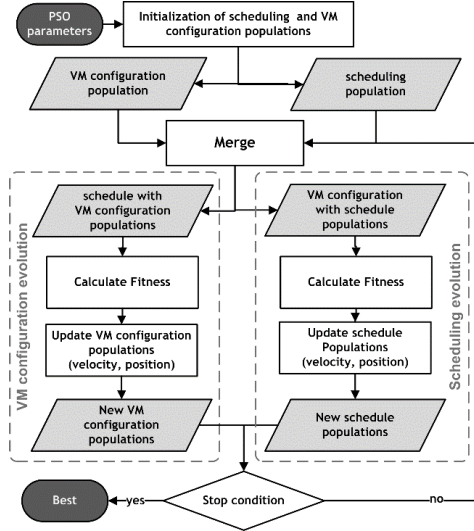


Figure 4: Proposed CPSO algorithm main schema.

3.2.1 Mapping Particle

Mapping particle is represented as a set of pairs of tasks and assignment nodes, that determines which task will run on which node. Position x_i of particle p_i is $x_i = \{t_k, n_l\}_{k=1}^M$, and velocity $v_i = \{t_k, n_l, q_k\}$, where q_k is value in range $[0, 1]$. It should be noted, that position x_i contains elements with all tasks from T , while velocity v_i may contains not all tasks or elements with the same task, but with different nodes.

The first operation is (-) between two particles p_i and p_j returns a velocity of p_i toward to p_j performs via difference of sets:

$v_{i \rightarrow j} = x_j - x_i = x_j \setminus x_i$, that is set of $\{t_k, n_l, 1\}$, where pairs $\{t_k, n_l\} \in p_j$ and $\notin p_i$ with the value = 1 for each pair.

The next operation (\cdot) for velocity v_i and constant c :

$$v_i \cdot c = \{t_k, n_l, q_k \cdot c\}$$

The sum (+) of two velocities v_i and v_j can be estimated as follows:

$v_i + v_j = \cup \{t_k, n_l, \max(q_{ik}, q_{jk})\}$, i.e. the union of velocities with the max value, if velocities contain the same pair (t_k, n_l) .

The last operation is position update (2), which presented by sum (+) of position x_t and velocity v_{t+1} , where t is current iteration. Firstly we generate

random value α in range $[0, 1]$. After that, we compute trimmed velocity tv_{t+1} by cut all elements from v_i with values $q_k < \alpha$, i.e. $tv_{t+1} = \{t_k, n_l, q_k > \alpha\}$, where pairs $(t_k, n_l) \in v_{t+1}$. A new position x_{t+1} performs by random node selection from tr_t for each task t_k . $x_{t+1} = x_t + v_{t+1} = \{t_k, \text{random node}(tv_{t+1})\}$.

3.2.2 Ordering Particle

Ordering particle determines the order of task execution. Position of particle p_i is represented as a $x_i = \{t_k, q_k\}_{k=1}^M$, where q_k is values in range $[-1, 1]$. Tasks queue is determined by sorting these values in the ascending order. On initialization phase we sort tasks by their start time of the current solution, and q_k are assigned for each task depending on the index in the sorted tasks list: $q_k = -1 + k \cdot 2/n$, $k = 1..M$. As in the mapping particle, we shall define operations for (1) computing:

$$(-): v_{i \rightarrow j} = x_j - x_i = \{t_k, q_{kj} - q_{ki}\}_{k=1}^M$$

$$(\cdot): v_i \cdot c = \{t_k, q_k \cdot c\}$$

$$(+): v_i + v_j = \{t_k, q_{ki} + q_{kj}\}$$

and (2):

$$(+): x_{t+1} = x_t + v_{t+1} = \{t_k, q_{kx} + q_{kv}\}$$

After evaluation of new particle position by use PSO equations (1) and (2) and operations, which mentioned above, we can construct new tasks queue by sort the tasks by their values in the ascending order.

3.2.3 Configuration Particle

Above we had defined operations for both parts of schedule particle (mapping and ordering parts). Now we will describe operations to compute (1) and (2) for particles from configuration population. All computing nodes have maximum capacity mr .

Position x_i and velocity v_i of particle p_i are list of nodes' capacities: $x_i = [cap_l]_{l=1}^N$; $v_i = [cap_l \cdot c]_{l=1}^N$. This representation define number of resources N and their capacities.

Operations for (1):

$(-): x_j - x_i = [cap_{lj} - cap_{li}]$, if $|N_j| \neq |N_i|$, than smaller vector is complemented by zeros.

$$(\cdot): v_i \cdot c = [cap_l \cdot c]_{l=1}^N$$

$$(+): v_i + v_j = [cap_{li} + cap_{lj}]_{l=1}^M$$

And for (2):

$(+): x_{t+1} = x_t + v_{t+1} = [cap_{lx} + cap_{lv}]$. After x_{t+1} computing we shall remove elements with not positive $cap_l \leq 0$, and divided elements with $cap_l > mr$ into several elements (mr) and $(cap_l - mr)$. Thus, our configuration particle, beside the

possibility of change nodes capacity, also has possibility to reduce or increase number of nodes.

3.2.4 Coevolution Ranked PSO Modification

The coevolution ranked PSO (CRPSO) modification of ordering particle is based on the predefined ranked list. This rank list with the ranks for each task can be constructed by HEFT or another list based algorithm. Rank list is represented as a set of tasks and their ranks:

$ranks = \{t_k, r_k = HEFT(t_k)\}_{k=1}^M$. These ranks are required to define task by values at particle build step.

Particle's position x_i and velocity v_i are represented as an ordered list of values: $x_i = [q_k]_{k=1}^M$; $v_i = [q_k]_{k=1}^M$. At the initialization step, these values in x_i are determines as ranks of tasks from rank list.

Operations to evaluate (1):

$$(-): x_j - x_i = [q_{kj} - q_{ki}]$$

$$(\cdot): v_i \cdot c = [q_k \cdot c]$$

$$(+): v_i + v_j = [q_{ki} + q_{kj}]$$

And (2):

$$(+): x_{t+1} = x_t + v_{t+1} = [q_{kx} + q_{kv}]$$

On the build step, we should encode this list of values into the tasks queue. To do that, for each q_k in this list we find a value in the rank list with $\min(|q_k - ranks[t_k]|)$ and choose task k .

3.2.5 Coevolution Weight Ranked PSO Modification

Coevolution weight ranked PSO (CWRPSO) is modification of the node selection operation in the mapping part. In the general scheme a new assignment node for each task is chosen randomly from all nodes in the velocity, without relations between tasks. In this case, for each task a new assignment node is chosen from the velocity's pairs (t_k, n_i) with the same task, depending on the velocity's values of these pairs. This method allows particles to move more directly to the other particles. However, particles have more chances to trap into a local optimum.

3.3 Coevolution Gravitation Search Algorithm (CGSA)

The gravitation search algorithm is proposed by Rashedi (Rashedi E., Nezamabadi-Pour, 2009). Idea of method is based on the law of gravity. The algorithm is similar to PSO in particles motion. The main equation for the force computation:

$$F_{ij} = F_{ji} = G(t) \frac{m_i m_j}{R_{ij}} (p_i(t) - p_j(t)) \quad (3)$$

, where $G(t)$ is the gravitational constant, m_i and m_j are the masses of particles, and R is the distance between the particles.

Equations for position and velocity update of particle i :

$$v_i(t+1) = v_i(t) + \sum_{j=1}^{kbest(t)} \frac{F_{ij}}{m_i} \quad (4)$$

, where $kbest(t)$ is number of best particles, which are used to update other particles. $G(t)$ and $kbest(t)$ are decreasing through the time.

$$x_i(t+1) = w \cdot x_i(t) + c \cdot v_i(t+1) \quad (5)$$

GSA is differ to PSO in additional step of computing masses. Masses can be evaluated by:

$$m_i(t) = \frac{fit_i(t) - w(t)}{b(t) - w(t)} \quad (6)$$

, where $fit_i(t)$ – fitness of particle p_i at iteration t , and $b(t)$ and $w(t)$ are the best and the worst fitnesses of population at iteration t . The same scheme (figure 4) and operators are used as in CPSO with all corresponding modifications. In compare to PSO, GSA has more possibility to avoid local optimums, since particles' velocities depend on $kbest$ particles, while in PSO velocities depend only on two: $pbest$ and $gbest$ particles.

4 EXPERIMENTAL STUDY

In order to verify the efficiency of the proposed algorithms, we conducted experiments with CGA, CPSO, CRPSO, CWRPSO and CGSA. According to internal experiments with CGSA modifications, we have left only CWGSA as the best one.

As the experimental environment own implemented simulator was used. In each experiment, a final makespan was calculated as a result of average value that is obtained from series of 1000 runs for each workflow. In addition, the execution cost, which is also informative criteria in the cloud environment, was considered as a restriction for the set of resources. Algorithms were executed on xml representation of workflows: Montage, CyberShake, Inspiral, Sipt, Epigenomics that were taken from (Pegasus, 2014) database with different tasks count as traditional benchmark workflows (Yu and Buyya, 2008). The Montage with 25, 50, 75, 100 tasks and the CyberShake with 30, 50, 75, 100 tasks were left as the most representative. Computational cost of each task is

determined by its runtime, which is an attribute that is contained in the workflow's xml file. Computational resource is represented by a value of its capacity in arbitrary units. For experimental study to keep balance in a set of resources we assume two following rules: maximum resource's capacity is 30 and the total capacity sum of all resources must be 80. The transfer cost for any two different resources is set to constant value 100. Each task is computed only on one resource at one single moment of a time.

For a fair play, all experiments were conducted in same conditions of population size and generations' count. To improve efficiency of the algorithms, in all cases initial populations have one particle, generated by heuristic HEFT algorithm.

Experiments were performed with the following parameters: population size is 100, generations count is 300 and interactions count is 200. For CGA crossover probability 0.3, mutation probability 0.5, and selection method is tournament. In all CPSO cases the inertia coefficient w is 0.5 and behaviour coefficients $c1$ and $c2$ are 1.6 and 1.2 respectively. For the last CGSA type of algorithms inertia $w = 0.2$, acceleration coefficient $c = 0.5$, initial $kbest$ and G are 10. The results are presented in the tables 1 and 2.

Table 1: Makespan for each Montage workflow and each introduced algorithm.

Algorithm	Montage makespan in sec			
	M 25	M 50	M 75	M 100
HEFT	280	345	559	578
CGA	152	264	371	467
CPSO	152	296	450	566
CRPSO	152	297	414	563
CWRPSO	152	340	456	452
CWGSA	152	295	411	544

Table 2: Makespan for each Cybershake workflow and each introduced algorithm.

Algorithm	Cybershake makespan in sec			
	CS 30	CS 50	CS 75	CS 100
HEFT	353	485	652	909
CGA	298	452	620	893
CPSO	311	481	651	909
CRPSO	309	479	649	908
CWRPSO	321	460	638	896
CWGSA	311	467	650	904

It can be clearly seen that HEFT produces worse results than results obtained by proposed schemas. It confirms suitable performance capabilities of

developed algorithms. It is evident, that CGA produced better results in almost all workflows scheduling. It overcomes with up to 82% HEFT algorithms and with up to 11% all other metaheuristics (for M_50 experiment). What is more curious, CPSO beats CGA in the M_100 case (467 against 452, figure 5(c)), that confirms absence of an absolute leader.

We can found that CRPSO modification was better than basic CPSO algorithm, and better than CWRPSO in most cases. Moreover, we can see on figure 5 (b, c), that CWRPSO has high convergence speed, however, has not possibility to avoid local optimums. Thus, CWRPSO can be useful, if algorithm is limited with execution time and have to produce solution on the first iterations. Despite that, CWGSA does not win in any cases, we can see from figure 5, that CWGSA produces a stable average result among all the other algorithms.

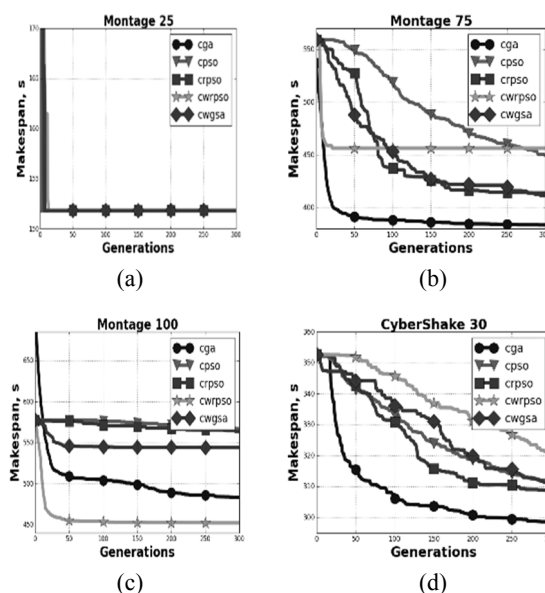


Figure 5: Fitness function improvement for the workflows.

4.1 CGA Parameter Analysis

In order to find the best parameters for CGA algorithm experimental studies were performed for different workflow scenarios. To explore the influence of particle mutation and crossover probability, following range of probability values were selected: 10, 20, ..., 90%. Other parameters were set to: 1) count of interaction individuals – 200; 2) count of generations – 300.

In the experiment, scheduling algorithm was executed for all studied workflows. The final summarised results are presented on figure 6

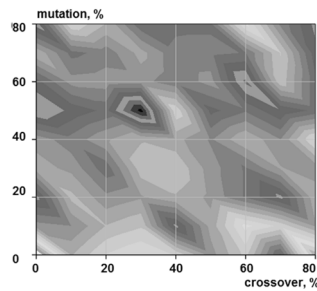


Figure 6: Makespan aggregated rate. (The lowest values corresponds to the closest values to the global optimal solution).

(contour plot). We can observe several local minimum areas (3 points with around $\sim 7.6\%$), but the global minimum can be found at the point (30%, 50%). It has the average result 4.5% worse than the global optimum for each separated result for each workflow and each pair of probability values.

5 CONCLUSIONS

In this paper three coevolution metaheuristic algorithms were compared. As it can be observed from the experimental results of the proposed algorithms, the coevolution idea of binding together traditional scheduling algorithm with technological advantages can be quite productive, especially in the terms of resource dynamic virtualization. The results can achieve up to 84% of performance increasing in comparison to HEFT algorithm as well as for the best CGA approach performance increases up to 11% in comparison to the other metaheuristics.

Summarizing, we can say that CGA is the most effective algorithm in compare to CPSO and CGSA schemes, due to its combinatorial nature. CPSO algorithms are the most diverse and not stable. However, they have greater convergence speed and can provide better solution in limited time. CWGSA is not the most successful algorithm, but more stable, than CPSO schemes. However, there is a great field for new investigations related to algorithms behaviour analysis in dynamically changing environments, data-intensive computation cases, hyperheuristic approach as well as schemas methods improving.

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