

# Downscaling Daily Temperature with Evolutionary Artificial Neural Networks

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**Abstract:** The spatial resolution of climate data generated by general circulation models (GCMs) is usually too coarse to present regional or local features and dynamics. State of the art research with Artificial Neural Networks (ANNs) for the downscaling of GCMs mainly uses back-propagation algorithm as a training approach. This paper applies another training approach of ANNs, Evolutionary Algorithm. The combined algorithm names neuroevolutionary (NE) algorithm. We investigate and evaluate the use of the NE algorithms in statistical downscaling by generating temperature estimates at interior points given information from a lattice of surrounding locations. The results of our experiments indicate that NE algorithms can be efficient alternative downscaling methods for daily temperatures.

## 1 INTRODUCTION

General Circulation Models (GCMs) numerically simulate the present climate as well as project future climate. The output of GCMs, however, cannot be applied to many impact studies due to their relatively coarse spatial resolution (in the order of from 200 km × 200 km to 300 km × 300 km). Downscaling, as an emerge technique, is able to model data from large-scale to smaller-scale. Various downscaling techniques have been proposed in literatures (Xu, 1999). In general, these techniques can be divided into two major categories: dynamic downscaling and statistical downscaling. Dynamic downscaling works based on physically regional climate models, which is computationally expensive. Comparing with dynamic downscaling, statistical downscaling is computationally less demanding. The methods of statistical downscaling are to build models to find the relationship between large regional climatic variables, such as temperature, precipitation, pressure etc., and sub-regional climatic variables. The major sub-categories of statistical downscaling techniques include weather classification schemes, weather generators and regression methods, in which regression methods are most widely used.

Artificial Neural Networks (ANNs), as non-linear regression models, have shown high potential

for complex, non-linear and time-varying input-output mapping (Specht, 1991; Hecht-Nielsen, 1989; Kohonen et al., 1988; Lu et al., 1998). There are various successful applications of ANNs to statistical downscaling in last decades. Snell et al. (1999) introduced ANNs to the downscaling of GCMs and evaluated their use to generate temperature estimates at 11 locations given information from a lattice of surrounding locations. Their results indicated that ANNs can be used to interpolate temperature data from a grid structure to interior points with a high degree of accuracy. Cawley et al. (2003) presented ANN models in statistical downscaling of daily rainfall at stations covering the north-west of the United Kingdom. Their main purpose was to compare different error metrics for training ANNs in statistical downscaling. Dibike and Coulibaly (2006) investigated the capacities temporal neural networks (TNNs) as downscaling method of daily precipitation and temperature series for a region in northern Quebec, Canada. Their experiments demonstrated that the TNN model mostly outperforms other statistic models. Chadwick et al. (2011) developed an ANN model to construct a relationship between a GCM and corresponding nested RCM fields for downscaling of GCM temperature and precipitation. Their ANN model was able to reproduce the RCM climate change signal very well, particularly for the full European domain. Most of the previous

researches with ANNs employed classic back-propagation (BP) as leaning approach to train ANNs for the downscaling of GCMs. However, it has been well-known that BP algorithms have difficulty with local optima, slower convergence and longer training times (Cuéllar et al., 2006).

In this research, we are going to explore and evaluate GCM downscaling with ANNs by using evolutionary algorithms, also names neuroevolutionary algorithms. Evolutionary techniques have been widely and successfully applied to data models optimization (Eiben et al., 1999; Buche et al., 2005; Regis and Shoemaker, 2004), but rarely introduced into statistical downscaling. Genetic Programming (GP) is the major evolutionary technique that has been investigated in atmospheric downscaling, which has been also demonstrated to be superior to the widely used Statistical Down-Scaling Model (SDSM) (Coulibaly, 2004; Zerenner et al., 2014).

This paper presents our initial results of a study for large-scale spatial interpolation of daily temperature at stations in south of Norway. The performances of our model indicate good potential of the neuroevolutionary technique as an effective statistical downscaling method for maximum temperature estimation. The rest of the paper is organized as follows: Section 2 describes the methodology of our model. The experimental results and discussion on the performance of our model are presented in section 3. The concluding remarks, including future work, are given in the last section.

## 2 METHODS

### 2.1 Artificial Neural Networks

An artificial neural network (ANN) is a mathematical model that simulates biological neural networks, which can be used for performing tasks such as classification, control, recognition, prediction, regression and so on. It consists of a set of interconnected nodes. Each node can be regarded as a neuron and each connection between two nodes can be regarded as a synapse. The mathematical models of an ANN and a neuron are shown in Figure 1 and Figure 2. There are three basic elements in an ANN: node, weight and activation function. A node represents a neuron. The weights between interconnected nodes of an ANN model the synapses. Each weight is a real number, which represents the strength of a connection. A positive

value reflects an excitatory connection, while a negative weight reflects an inhibitory connection. All of the inputs are multiplied by the weights and summed according to the following expression:

$$v_i = \sum_{j=1}^n w_{i,j} x_j$$

where  $x_j, j \in [1, n]$  are the inputs to the node  $i$ , and  $w_{i,j}$  is the weight of the connection between the node  $i$  and the input  $j$ . The summing function is input into an activation function. The output of the node  $y_i$  will be the outcome of the activation function on the value of  $v_i$ . The main purpose of using the activation function is to control the amplitude of the output of each node. Common activation functions used in ANNs include step function, piecewise-linear function, sigmoid function and hyperbolic tangent function, in which sigmoid function is mostly used, as well as applied to our model.

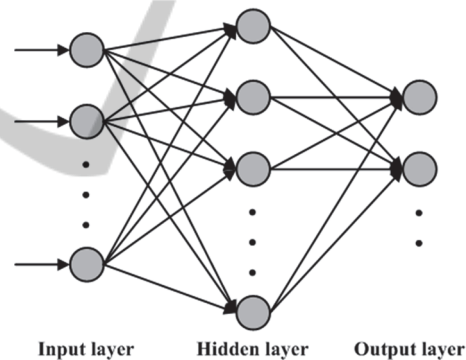


Figure 1: The model of an ANN.

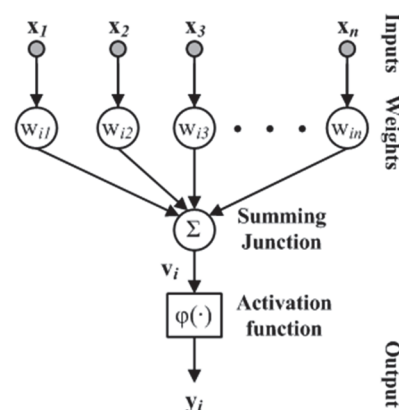


Figure 2: The model of a neuron.

After defining the weights, activation function and topology of an ANN, we will be able to calculate the output of the ANN for a particular input vector. Usually, the output of an ANN has no meaning before the ANN is trained, unless the ANN is configured using prior knowledge. Training is a process of adjusting the weights, topologies or activation function of an ANN, so that the ANN outputs corresponding desired or target responses for given inputs. Various methods have been designed to teach ANNs (Werbos, 1974; Yao, 1999; Brath et al., 2002; Carvalho and Ludermir, 2006). Back-propagation is one of the most popular approaches in climate downscaling as we have introduced previously. In this research, however, Evolutionary algorithm was implemented for the ANNs design, which will be described in the next section.

## 2.2 Evolutionary Algorithms

Biological evolution is a process of change and development of individuals, generation by generation, following the principle of “survival of the fittest”. Evolutionary Algorithms (EAs) loosely simulate the natural evolution in computer problem solving, which has been proven to be robust in solving optimization problems (Bobbin and Yao, 1997; Downing, 1997; Tsai et al., 2004). The implementation of EAs typically begins with a population of stochastic solutions. Each individual in the population presents a solution. A fitness function is defined to evaluate the quality of each individual. The algorithms update the individuals to improve the average quality of the entire population through the operations of selection, recombination, mutation and replacement. The improvement procedure is iterated until a terminal condition is satisfied. A basic pseudo-code of the EAs is shown in Figure 3.

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Algorithm Evolutionary Algorithm
Initialize a population
Evaluate all individuals in the population
repeat
    Select parents from the population
    Recombine parents to generate new individuals
    Mutate individuals
    Evaluate new individuals
    Decide survival individuals for a new population
until terminal condition is satisfied
return the best individual from the population

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Figure 3: A basic pseudo-code of typical Evolutionary Algorithms.

**Initialization.** An encoding scheme is firstly predefined to represent the solutions of a problem.

The algorithms initialize a population with a set of individuals created following the encoding scheme.

**Evaluation.** Evaluation of which individuals are fit and which ones are unfit is performed by the fitness function designed for the problem. A well-designed fitness function is a key factor in the successful application of an EA. The goal of an ideal fitness function is to make an accurate assessment of the qualities of individuals according to the objective of the problem. It guides the algorithm to rank the individuals. Which individuals are discarded and which are reserved will be decided based on the rank.

**Parent Selection.** The evaluation also drives the selection of parents. New individuals are generated through the sexual reproduction of selected parents, known as recombination. All parent selection strategies boil down to one principle: that the individuals who have higher fitness receive higher probabilities of being selected as parents.

**Recombination and Mutation.** Recombination, also called crossover, is actually the exchange of data between two or more individuals to create new individuals. It is one of the most common genetic operators in EAs. Another common genetic operator is mutation, which changes the form of an individual itself.

**Survivor Selection.** The strategies of selecting survival individuals are looser than that of selecting parents. One can select the individuals who have higher fitness to be survivors. In a more generational model, the older individuals are just replaced by their offspring.

**Termination.** The EA circularly performs the evaluation, parent selection, recombination and mutation, and survivor selection. A terminal condition, therefore, has to be defined in order to determine when to exit the evolutionary cycle. The most common way is just to specify a maximum number of generations.

## 2.3 Neuroevolution

The techniques that ANNs design using evolutionary algorithms are so-called neuroevolutionary (NE) algorithms. Yao (1999) roughly summarized three levels of NE algorithms: evolving connection weights, evolving architectures and evolving learning rules. In the past decade, however, researchers have mainly focused on the first and the second level, that is evolving connection weights or simultaneously evolving connection weights and topologies of ANNs (Moriarty and Miikkulainen, 1997; Lubberts and Miikkulainen, 2001; Stanley and

Miikkulainen, 2002; Shi 2008).

In this work, we built our NE model at the level of evolving connection weights, that is also called standard NE. The standard NE evolves connection weights of fully-connected neural networks, where each individual in the population represents a vector with all connection weights of the network, and each value of this vector specifies a weight between two neurons. Each weight  $w_{ij}$  of a network was encoded into a  $m$ -bit binary string, where  $m = 16$  in our experiments. We transformed the binary string into a float value by using the following equation:

$$w_{ij} = \frac{d_i}{2^m} (w_{ij,max} - w_{ij,min}) + w_{ij,min}$$

where  $d_i$  was the integral value of the binary string of  $w_{ij}$ ,  $w_{ij,max}$  and  $w_{ij,min}$  were the upper bound and the lower bound of the decimal value of  $w_{ij}$ , which was defined to be -10 and 10 in our experiments. Other parameters of our NE model are summarized in table 1.

Table 1: Parameters of the NE model.

Parameters	Values
Number of generations	500
Population size	100
Crossover rate	0.7
Mutation rate	0.1
Fitness function	RMSE

### 3 EXPERIMENTS

Our initial work would like to evaluate the use of the NE model for downscaling GCM. We setup our experiments based on the idea from Snell's research (1999). A 4-point grid with coarse spatial resolution was built on the map of south of Norway. Observation data from stations near and within the grid points were used for training and verifying the model. Four stations near the grid points were chosen to be known stations and five stations within the grid points were chosen to be unknown stations. Figure 4 depicts our study area and the details of these stations are presented in table 2.

For this study, we constructed feed-forward networks which consist of three layers, one input layer, one hidden layer and one output layer. There were 9 neurons in the input layer, 10 neurons in the hidden layer and one neuron in the output layer. Usual root-mean-square error metric is defined as the fitness function of our algorithm. The 9 variables

contained in the input layer are illustrated in table 3. The output of the ANN is the maximum daily temperature for an unknown station. An ANN was built for each of the unknown stations.

Table 2: Study stations.

Station	Name	Location
Known station1	Fiskåbygd	62.10N, 5.58E
Known station2	Nedre Vats	59.48N, 5.75E
Known station3	Drevsjø	61.89N, 12.05E
Known station4	Oslo Blindern	59.94N, 10.72E
Unknown station1	Åbjørsbråten	60.92N, 9.29E
Unknown station2	Løken I Volbu	61.12N, 9.06E
Unknown station3	Kise Pa Hedmark	60.78N, 10.81E
Unknown station4	Geilostølen	60.52N, 8.2E
Unknown station5	Skåbu storslåen	61.52N, 9.38E

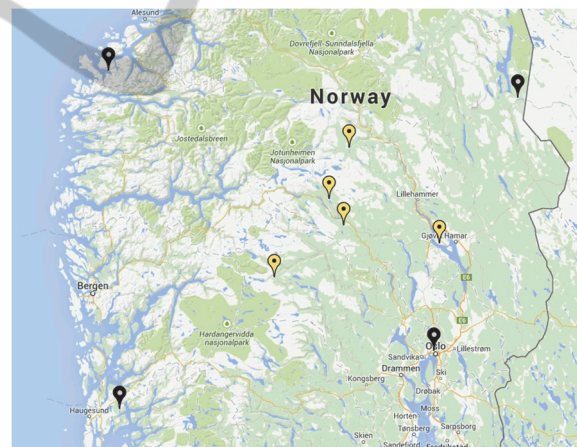


Figure 4: Map of study area. Black markers are known stations and yellow markers are unknown stations.

#### 3.1 Data Preparation

Maximum daily temperatures for a period from 1970 to 2010 were used for training and verifying our model. Because not every day has valid data for all stations due to some observation data missing, the data was pre-processed and all data on invalid date were removed. An invalid date defined in our experiments is a day that anyone of the training stations has missing data.

After pre-processing the dataset was shuffled



before presenting to ANN, in which 80% data were randomly selected for training and 20% data were selected for test. The reason to train our model with shuffled data were two-fold: 1) the model we built in this study is a spatial downscaling model, so to present the training data with sequential order does not make sense; 2) random ordering has been reported to be superior to both sequential ordering and aggregated values by Snell's study (1999).

Table 3: Inputs of the NE model.

Input number	Input
1	Maximum temperature at known station 1
2	Maximum temperature at known station 2
3	Maximum temperature at known station 3
4	Maximum temperature at known station 4
5	Distance between station 1 and unknown station
6	Distance between station 2 and unknown station
7	Distance between station 3 and unknown station
8	Distance between station 4 and unknown station
9	Elevation of unknown station

### 3.2 Experimental Results

We carried out 10 runs for training ANNs to learn the relationship of maximum temperatures between known stations and each of the unknown stations. The average performance of each experiment took about 400 to 600 seconds. Figure 5 shows average learning curves of the ANNs from the 10 runs, and table 4 shows our average test results.

From figure 5 we can see that the average RMSE curves bend down very steeply in the first 100 generations, and then start coming down gently in the rest of generations. As we introduced earlier, EAs are optimal search algorithms. By integrating EAs with ANNs, NE is able to find optimal connection weights and topologies to map the relationship of maximum temperatures between known stations and unknown stations. The learning curves shown in figure 5 indicate that our NE model rapidly found relatively optimal connection weights of ANNs at the early stages of evolution. After that the NE model turned to gradually converge toward global optima. Of course, NE algorithms cannot guarantee to deliver the best ANN topology to a problem, to find relatively optimal solutions, however, are usually reachable.

Table 4: Overall performance measures. Average RMSE and  $R^2$  for test from 10 runs.

Station	RMSE	$R^2$
Åbjørsbråten	2.91	0.898
Løken i Volbu	3.19	0.893
Kise Pa Hedmark	2.85	0.912
Geilostølen	2.78	0.797
Skåbu storslålen	2.79	0.911

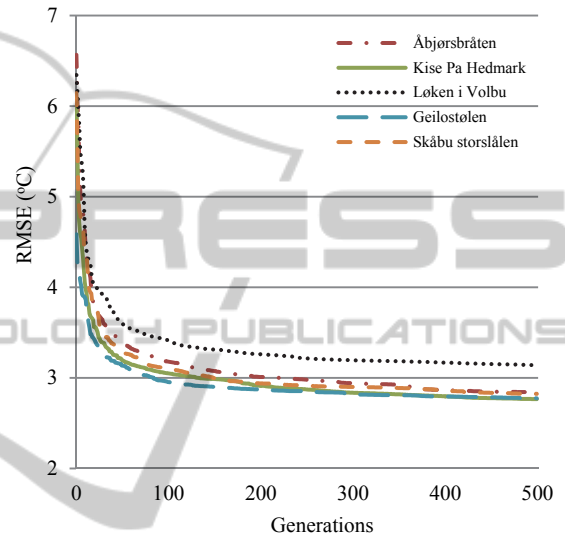


Figure 5: Average learning curves of the ANNs from the 10 runs for the five unknown stations.

If we only measure the RMSE values shown in table IV, the average RMSE achieved by our algorithms are significantly smaller than those reported by some other literatures (Snell et al., 1999; Cawley et al., 2003; Coulibaly, 2004). However, to compare the average  $R^2$  values performed by our model with those reported by others, our model does not appear to be generally superior to other methods. Instead, the average  $R^2$  value for station Geilostølen is a bit low. It is worthy of being mentioned, however, the results reported in this paper were from the average performance of our experiments. The compared results from the above literatures were from the best performance of their experiments.

In EAs, fitness functions play a crucial role to guide how the evolutionary process goes to achieve the objectives of problems. In our current NE algorithm, only RMSE was considered in the fitness function. The goal of our NE algorithm is, therefore, merely to minimize RMSE values. However, a smaller value of RMSE does not indicate a higher value of  $R^2$ . A possible improvement of our NE

model is to evolve ANNs by using multi-objective evolutionary algorithms, which will be able to both minimize the values of RMSE and maximize the values of  $R^2$ .

## 4 CONCLUSIONS

In this paper we have applied a NE model for the spatial statistical downscaling of daily maximum temperature. We demonstrated our approach by interpolating temperature data from a large scaled grid structure to interior points. The results of our method showed good potential for the construction of high-resolution scenarios. The future work of this research can be comparison studies of our model with the state of the art methods for the same study area. In addition, our method can be improved by using multi-objective evolutionary algorithms. Both RMSE and  $R^2$  should be taken into consideration when we design the fitness function of the model.

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