

# A Nano-opto-mechanical Pressure Mapping Sensor via Bragg Structure Waveguide for Biomedical Sensing

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**Abstract:** This paper reports a nano-opto-mechanical mapping sensor based on Bragg structure waveguide. The pressure is measured by monitoring the output spectrum shift which is induced via mechanical deformation of the period of the Bragg structure. In experiments, it measures that the shifting of the output spectra linearly red shift under different position of the Bragg structure when the pressure is increasing. Compared with traditional optical mapping sensor based on Mach-Zehnder interferometer, the nano-opto-mechanical mapping sensor has merits such as high sensitivity and fine resolution which are 1.55pm/kPa and 1.29kPa, respectively. The nano-opto-mechanical mapping sensor has potential applications such as highly accurate measurement of pressure waves, mass sensors array and bio-medical sensors.

## 1 INTRODUCTION

Optical pressure sensors have advantages such as immunity to electromagnetic interference (EMI), lightweight, small device scale, high sensitivity, and ease in signal transmission, etc, compared with electrical pressure sensors which are sensitive to almost everything such as light, temperature, pressure, electromagnetic (EM) field and humidity. During the past thirty years, various ideas have been developed based on optical pressure sensors. Most of the optical pressure sensors are based on either optical fibers, or single waveguide. However, optical fibers pressure sensor occupy large area, the fibers are not easy to be integrated with silicon based photonic chips and cannot be fabricated using standard complementary metal-oxide-semiconductor (CMOS) technology. In MZI structure pressure sensor, the waveguide branches or 3-dB directional couplers making the optical devices long. The single waveguide pressure sensors need additional input and output polarizers to form TM-TE intermodal interference in a single-mode waveguide. Single waveguide structure pressure sensor as well as MZI structure pressure sensors suffer from nonlinear optical intensity output. Pressure sensors have been fabricated using many

different technologies such as glass, piezoelectric quartz crystals, II-VI compound photoconductors, and metal diaphragm. However silicon based pressure sensors are most likely to be commercialized due to their feasibility in mass production and low cost. Although the introduction of silicon cannot guarantee the improvements of the performances, it definitely has great advantage in producing micro-scaled or even nano-scale pressure sensors which can be integrated in photonic circuits. In this paper, the Bragg structure in silicon waveguide is induced in the pressure sensor. A novel nano-opto-mechanical pressure sensor based on Bragg structure waveguide is proposed to provide a reliable optical pressure sensor with high sensitivity, good linearity of the output, CMOS compatibility and ease in constructing sensors array.

## 2 DESIGN AND THEORETICAL ANALYSIS

The design of the proposed pressure sensor is shown in Fig. 1(a). The pressure sensor consists of a  $820 \times 820 \mu\text{m}^2$  diaphragm, five waveguides with Bragg structure. The coordinate (0,0) is set at the center of the diaphragm with the unit length as  $1 \mu\text{m}$ . The

centers of the Bragg structures are located at (0, 0), (45, 45), (-45, -45), (84, -84), (-84, 84), respectively. The period of the Bragg structure  $a$  is 0.6  $\mu\text{m}$ . The diameter of the hole  $d$  is 0.3  $\mu\text{m}$  as shown in Fig. 1(b). The diaphragm consists of  $\text{SiO}_2$  layer and Si layer with thickness of 2  $\mu\text{m}$  and 18  $\mu\text{m}$ , respectively as shown in Fig.1(c).

The pressure applied to the diaphragm causes the shear stress displacement. The shear stress displacement results in the change of the period of the Bragg structure  $\Delta a$  as shown in the Fig 1(b). The  $\Delta a$  influences the effective refractive index of the Bragg structure  $\Delta n_{\text{eff}}$ . Both the  $\Delta a$  and the  $\Delta n_{\text{eff}}$  results in the resonant wavelength shift of the Bragg structure  $\Delta\lambda$ . The  $\Delta\lambda$  could be read out from the output spectrum of the waveguide. The pressure applied to the diaphragm is detected by the  $\Delta\lambda$ .

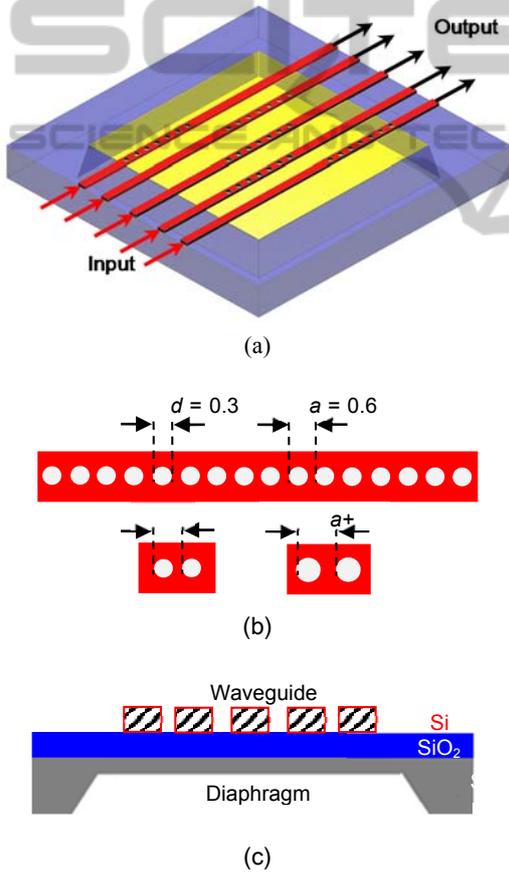


Figure 1: (a) Schematic of the nano-opto-mechanical pressure sensor, (b) Bragg structure, and (c) cross-section of the pressure sensor.

## 2.1 Mechanical Design

The deformation of the diaphragm in  $x$ ,  $y$  and  $z$  direction is necessary to calculate the period change

of the Bragg structure  $\Delta a$  due to the applied pressure on the diaphragm. The deflection of diaphragm along  $z$ - direction  $w$ , the displacement along  $x$ -direction  $u$ , and displacement along  $y$ - direction  $v$  are the solution of the differential equation of diaphragm are expressed as,

$$\nabla^4 w - \gamma^2 \nabla^2 w = \frac{P}{D_{eq}} \quad (1a)$$

$$\gamma^2 = \frac{12}{h^2} \left[ \frac{\partial u}{\partial x} + \frac{\partial v}{\partial x} + \frac{1}{2} \left( \frac{\partial w}{\partial x} \right)^2 + \frac{1}{2} \left( \frac{\partial w}{\partial y} \right)^2 \right] \quad (1b)$$

$$D_{eq} = \sum_{i=1}^n \frac{E_i h_i^3}{12(1-\nu_i^2)} \quad (1c)$$

where  $\gamma$  is the constant of integration,  $P$  is the uniform pressure,  $D_{eq}$  is the bending rigidity of the equivalent single-layer,  $n$  is the number of the layer,  $E_i$  is the Young's modulus of the  $i$  layer material,  $i$  equate 1 or 2 in our design for  $\text{SiO}_2$  layer or Si layer,  $h_i$  is the thickness of  $i$  layer,  $\nu_i$  is Poisson's ratio of  $i$  layer,  $h$  is the thickness of the whole diaphragm.

Finite Element Method is used to calculate the membrane deformation. Fig 2(a) shows the deflection of diaphragm  $w$  along  $z$ -direction, when the  $P$  is 60 kPa. Fig2(b) illustrates the displacement along  $x$  direction  $u$ . The  $P$  is 12 kPa, 42 kPa, and 60 kPa, respectively. The diaphragm position is along the diagonal of the diaphragm plane. Fig. 2(c) shows the relation between the change rate of  $u$  and the position of the diaphragm along diagonal of the diaphragm. The change rate of  $u$  reaches the maximum  $58.9 \times 10^{-6}$  when the position of the diaphragm is (0,0). The  $P$  is 12 kPa, 42 kPa, and 60 kPa, respectively. The thickness of the waveguide is 0.22  $\mu\text{m}$ , which is much less than 20  $\mu\text{m}$ . Therefore, the shear stress of the diaphragm could influence both the top and bottom edges of the air holes in the Bragg structure. In this condition, the value of  $\Delta u$  between edges of the two adjacent air holes equal to  $\Delta a$  along  $x$  direction.

The relation between the  $\Delta a$  and  $P$  is shown in the Fig 2(d). The  $\Delta a$  is proportional linearly to the change of pressure  $\Delta P$  for different position of the Bragg structure.

$$\Delta a = C_1 P \quad (2)$$

where  $C_1$  are 0.592 pm/kPa, 0.539 pm/kPa and 0.412 pm/kPa, respectively, when the centre position of the Bragg structure are (0, 0), (45, 45), and (-84, 84) as shown in Fig. 2 (d).

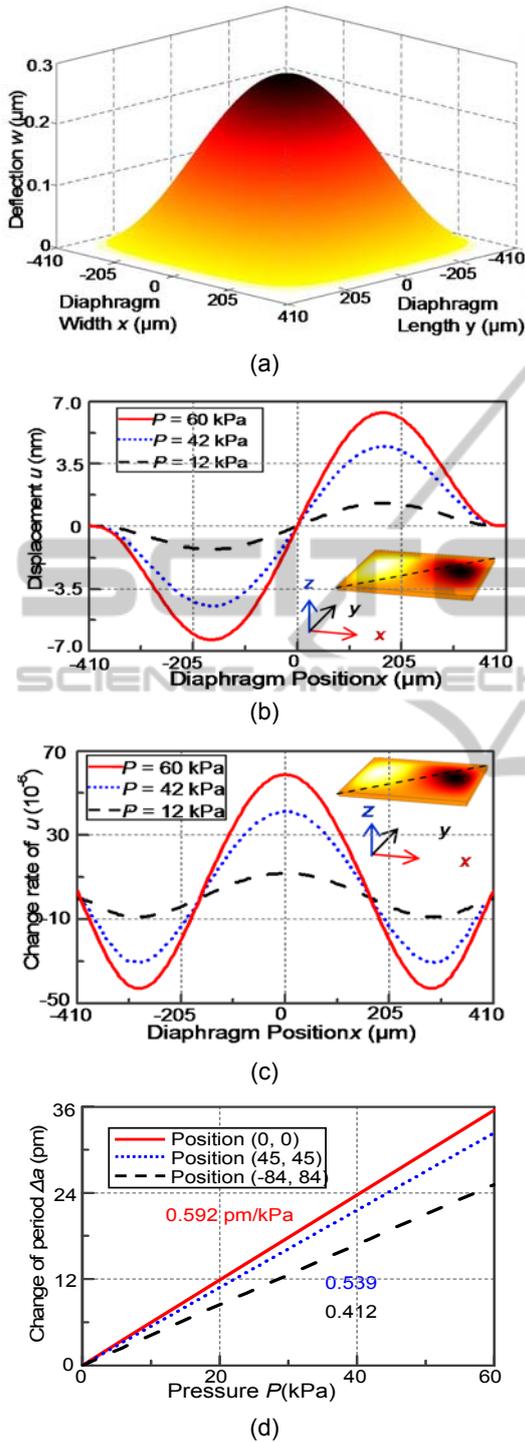


Figure 2: (a) The deflection along z-direction, and (b) the displacement along x-direction of the diaphragm when the applied pressure is 60 kPa. The different  $y$  value are 0  $\mu\text{m}$ , 45  $\mu\text{m}$ , and 84  $\mu\text{m}$ , respectively. (c) The change rate of displacement along x-direction (d) The period change of Bragg structure  $\Delta a$ , when the centre position of the Bragg structures are (0, 0), (45, 45), and (-84, 84). The applied pressure is from 0 to 60kPa.

## 2.2 Optical Design

The pressure applied on the diaphragm can be read out by the wavelength shift. The resonant wavelength  $\lambda$  can be inferred from the following equation based on the coupling condition of the Bragg waveguide,

$$2n_{\text{eff}}a = m\lambda \quad (3)$$

where  $m$  is the mode number. Calculated by the Finite-difference-time-domain (FDTD) method,  $n_{\text{eff}}$  is 2.6553, when  $a$  is 0.6  $\mu\text{m}$ , and pressure is zero. The resonant wavelength shift  $\Delta\lambda$  as a function of  $\Delta n_{\text{eff}}$  and  $\Delta a$  can be written as

$$\Delta\lambda = \frac{2(n_{\text{eff}} + \Delta n_{\text{eff}})(a + \Delta a)}{m} - \frac{2n_{\text{eff}}a}{m} \quad (4)$$

The  $\Delta a$  causes the change of the horizontal hole radius ratio to the lattice period  $r/a$  which results in the change of the Bragg structure  $\Delta n_{\text{eff}}$ . Calculated by Finite Element Method, The relation between the  $\Delta n_{\text{eff}}$  and  $\Delta a$  can be written as:

$$\Delta n_{\text{eff}} = C_2 \Delta a \quad (5)$$

where  $C_2$  are  $-0.071 \times 10^{-6} / \text{pm}$ ,  $-0.064 \times 10^{-6} / \text{pm}$  and  $-0.060 \times 10^{-6} / \text{pm}$ , respectively, when the centre position of the Bragg structure are (0, 0), (45, 45), and (-84, 84) as shown in Fig. 3. The relation between the  $\Delta n_{\text{eff}}$  and  $\Delta a$  is linear.

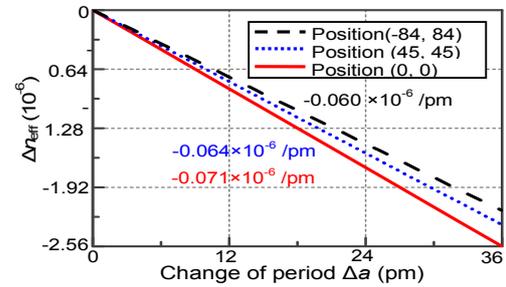


Figure 3: Change of effective refractive index  $\Delta n_{\text{eff}}$  due to the change of period  $\Delta a$ .

The Eq. (4) can be expressed as:

$$\Delta\lambda = \frac{2(n_{\text{eff}}\Delta a + \Delta n_{\text{eff}}a + \Delta n_{\text{eff}}\Delta a)}{m} \quad (6)$$

$$\approx \frac{2(n_{\text{eff}}\Delta a + \Delta n_{\text{eff}}a)}{m}$$

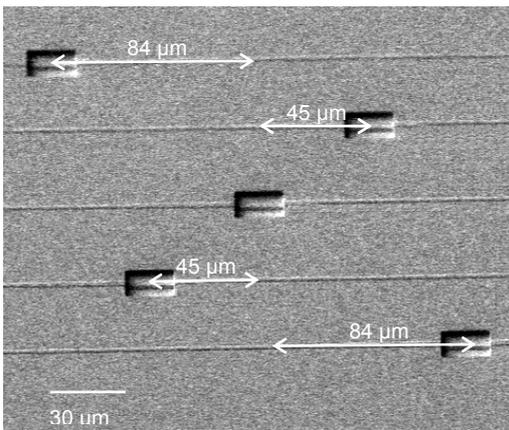
$\Delta n_{\text{eff}}\Delta a$  is  $9.2 \times 10^{-17}$  which can be ignored. The relationship between  $\Delta\lambda$  and  $P$  is obtained by substituting Eq. (2) and Eq. (5) into Eq. (6).

$$\Delta\lambda = \frac{2[n_{\text{eff}}C_1 + C_1C_2a]P}{m} = C_3P \quad (7)$$

where  $C_3 = \Delta\lambda/P$  is the sensitivity of the nano-opto-mechanical pressure sensor,  $m$  is 2. Here, transverse electric (TE) and transverse magnetic (TM) mode is defined as the propagating mode with the electrical field parallel and perpendicular to the diaphragm plane, respectively. Only TE mode polarization exists in the ring resonator and the bus waveguide since the thickness of the waveguide is designed to be smaller than the cutoff width of TM mode. Therefore,  $n_{\text{eff}}$  refers to the effective index of TE mode only. The variation of  $n_{\text{eff}}$  caused by the photo-elastic effect is approximately  $10^{-7}$  which has trivial effect, compared with the change of the period, on  $\Delta\lambda$ .

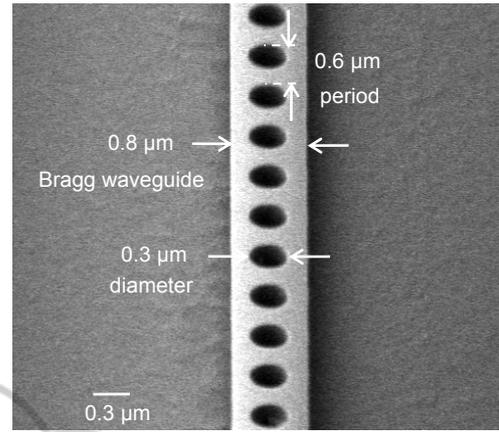
### 3 EXPERIMENTAL RESULTS AND DISCUSSIONS

The SEM images of the fabricated nano-opto-mechanical pressure sensor are shown in Fig. 4. All structures are fabricated on a standard silicon-on-insulator (SOI) wafer with a silicon structure layer of 220 nm. The thickness of silicon dioxide ( $\text{SiO}_2$ ) layer and back side substrate is 2  $\mu\text{m}$  and 720  $\mu\text{m}$ , respectively. The waveguide and the Bragg structure are patterned by deep UV lithography, followed by Reactive Ion Etching to transfer the photo resist pattern into the silicon structure layer. Potassium hydroxide (KOH) wet etching is used to form the backside open of diaphragm with thickness of 20  $\mu\text{m}$ . For comparison, five different parameters are used for the fabrication of the nano-opto-mechanical pressure sensors which are the center position of the Bragg structure: (0, 0), (45, 45), (-45, -45), (-84, 84), and (84, -84).



(a)

Figure 4: SEM images of (a) pressure sensor, and (b) zoom view of the Bragg structure.



(b)

Figure 4: SEM images of (a) pressure sensor, and (b) zoom view of the Bragg structure (cont.).

Fig. 4(a) shows the overview of the pressure sensor with a footprint of 1.8 mm  $\times$  1.8 mm which is the same size as the etching window of backside open. Fig. 4(b) shows the zoom view of the the Bragg structure of the waveguide. The cross-section of the Bragg structure is 800 nm  $\times$  220 nm. The period of the Bragg structure is 0.6  $\mu\text{m}$ . The diameter of the air hole is 0.3  $\mu\text{m}$ . These nano-scaled structures are used to keep the single-mode propagation of the light.

The nano-opto-mechanical pressure sensor is tested by using the fiber-to-chip alignment system PS-1000 from SURUGA SEIKI CO.,LTD. The incident broadband source is Amplified Spontaneous Emission which has 8-mW output power over the spectrum ranging from 1570 nm to 1608 nm. The light is input from one end of the bus waveguide and monitored from the other end using an optical spectrum analyzer AP2052A from Apex Technologies.

The output spectra of the nano-opto-mechanical pressure sensor at different pressures applied to the diaphragm is shown in Fig. 5(a). Here, the diaphragm thickness is 20  $\mu\text{m}$ . The measured propagation loss of the waveguide is approximately 1.9 dB/cm. The resonance dip wavelength red shifts from 1593.194 nm to 1593.287 nm when the pressure on the diaphragm is increasing from 0 kPa to 60 kPa. The quality factor of the resonance peak is around  $8.92 \times 10^3$  which is slightly broadened because of the deformation of the ring resonator and the bus waveguide induced by the pressure applied to the diaphragm. Fig. 5(b) shows the wavelength shift  $\Delta\lambda$  versus pressure  $P$  measured from three different samples. The symbols and the lines

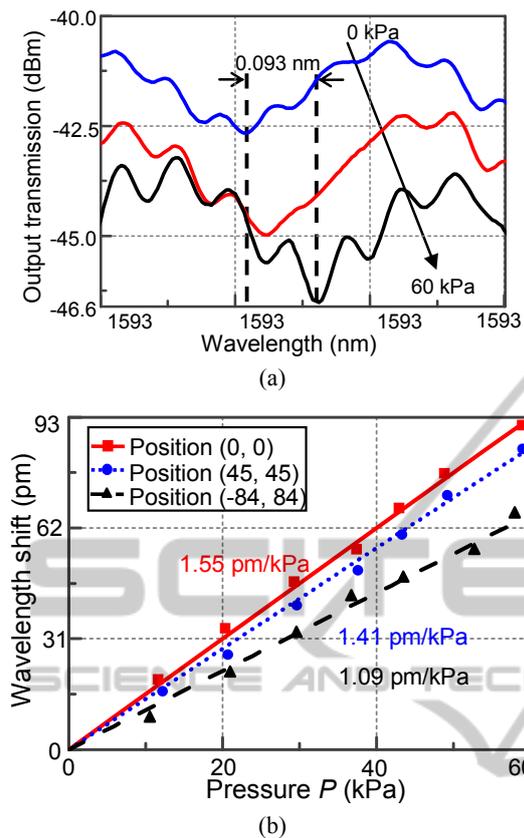


Figure 5: Transmission spectra at various applied pressures on the diaphragm. The centre position of the Bragg structures are (0, 0), and (b) wavelength shift versus the pressure when the centre position of the Bragg structure are (0, 0), (45, 45), and (-84, 84).

represent the measured and simulated results, respectively. The solid, dotted and dashed line show the  $\Delta\lambda$  as the function of  $P$  when the center position of the Bragg structure is (0, 0), (45, 45), and (-84, 84), respectively which shows a good linearity between the output of the pressure sensor and the measured pressure. The slopes of the lines  $C_3 = \Delta\lambda/P$  is equal to the sensitivity of the nano-opto-mechanical pressure sensor.  $C_3$  is  $1.55 \times 10^{-3}$  nm/kPa, when the center position of the Bragg structure is (0, 0) which is at least 1.42 times larger than that of the (-84, 84). The resolution of the nano-opto-mechanical pressure sensor is limited by the resolution of the optical spectrum analyzer used in the experiment. The optical spectrum analyzer allows for a spectral resolution of approximately 2 pm. Consequently, the pressure resolution is 1.29 kPa which can be obtained by the Eq. (7).

## 4 CONCLUSIONS

In summary, a highly sensitive nano-opto-mechanical pressure mapping sensor based on Bragg structure is designed, fabricated and characterized for pressures ranging from 0 kPa to 60 kPa. The sensitivity as high as 1.55 pm/kPa has been experimentally achieved which is in good agreement with numerical prediction. The pressure sensor structure make it possible to detect the shear stress displacement distribution in highly accurate measurement with low-cost advantages. The characteristics indicate potential for various applications such as mass sensor, bio-medical sensors and optical integrated circuits etc.

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