

# Intelligent Path Panning Towards Collision-free Cooperating Industrial Robots

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## 1 INTRODUCTION

Due to raising costs of energy and the increasing request for environment-friendly products, there is a huge demand for lighter vehicles, helicopters or airplanes made of carbon fibre reinforced plastics (CFRP). In the last years the structural weight in percentage of CFRPs in airplane production was clearly rising. The AIRBUS A380 with about 20% and the AIRBUS A350 with about 50% (see Figure 1). Carbon fibres are very thin and have a high tensile strength. Products which are assembled from CFRP offer one of the highest strength-to-weight ratio compared to any other material and also offer superior thermal and conductive properties. These properties makes the material very famous in car, aerospace, marine and sports industry.

To use CFRPs in a mass production it is important to produce lightweight products cost-efficiently in high quality and quantity. To achieve these goals, a high degree of automation is necessary. For this reason, the German Aerospace Center (DLR) developed a robotic portal system within the Center for Lightweight-Production-Technology (ZLP). In this system, large parts of CFRP for e.g. the aerospace industry and the wind energy industry can be manufactured automatically. It supports three portal robots and two industrial robots on a linear track, enabling them to move along the middle beam. Its dimensions are about 30 m in x-, 15 m in y- and 7 m in z-direction, see Figure 2. All robots and portals in the robotic cell share the same workspace so they can work together which makes the programming one the one side very difficult and one the other side very interesting. To achieve the goal of low-cost production, the DLR concentrates on dry fibre placement of large carbon fabrics. This ensures higher lay up rates than tape laying which reduces manufacturing costs of large composite structures. To handle these large and sensitive carbon fibre fabrics, it is necessary to work with cooperating robots, which requires a sophisticated control

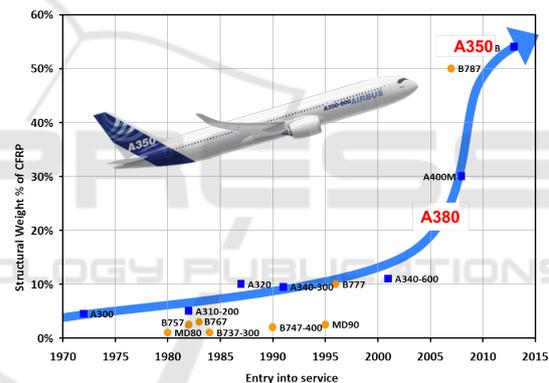


Figure 1: Rising overall structural CFRP weight in airplane production (source: AIRBUS).

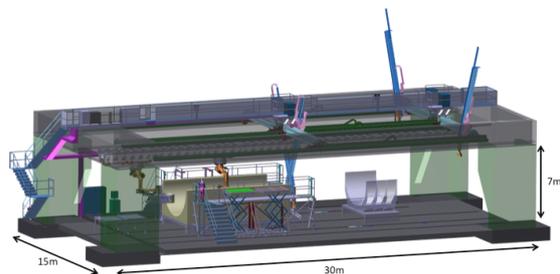


Figure 2: Multi-variant-production cell (MFZ) containing two industrial robots on a linear track and three portal robots in the same working space. The dimensions of the cell are 30 m in x-, 15 m in y- and 7 m in z-direction.

strategy.

## 2 RESEARCH PROBLEM

In conventional industrial robotic cells e.g. in an automotive assembly line the robots execute the same task for a period of many month or years. The movements of the robots are hard-coded for one process with respect to no occurring collision. Normally a high amount of time is needed to program the robots.

A reconfiguration of the cells implies a high resource effort.

In the automotive industry the cycle time is measured in seconds and in the aerospace industry it is measured in hours. One reason for that is that the assemblies e.g. a fuselage or a wing are much bigger. Another reason is that the requirements on the accuracy are very high. Bringing to mind that transporting a dry fibre cut piece is like transporting a table dish it becomes clear that the process speed is not the only challenge rather it is the quality of the process and the resulting product.

Like it is easier to set a table with two persons it is also easier to transport a large four meter dry fibre cut piece with two robots. Figure 3 shows an example process for the layup of carbon fibre cut pieces with cooperating robots. First the cut piece is grabbed from a plane table. For lifting the cut pieces the robots have special designed end-effector which can handle the material very gentle. The material is very permeable to air. Therefore the end-effectors don't work with vacuum to grab the textile but with a high flow rate like a vacuum cleaner. After grabbing the material it is transported on a linear axis to a negative tooling of the assembly. In this case it is the lower half of a fuselage with the dimension of an AIRBUS A320. In the mould the textile is placed and fixated.

The position where the cut pieces must be placed in the 3D mould is defined by the designer in a computer aided design (CAD) tool like CATIA Composites Design (CPD). With that tool different carbon fibre cut pieces with different fibre orientations are put on each other. Depending on the demands of the assembly this can be five up to more than 20 layers with thousands of cut pieces for a whole fuselage. As a result of the design phase the designer exports the exact lay down position of every cut piece. This lay up definition is called plybook. Figure 4 shows the first layer from a plybook for the example process in 3D and unwind to 2D. The coloured lines show the outlines of the cut pieces. The gripping position also comes from the CAD software.

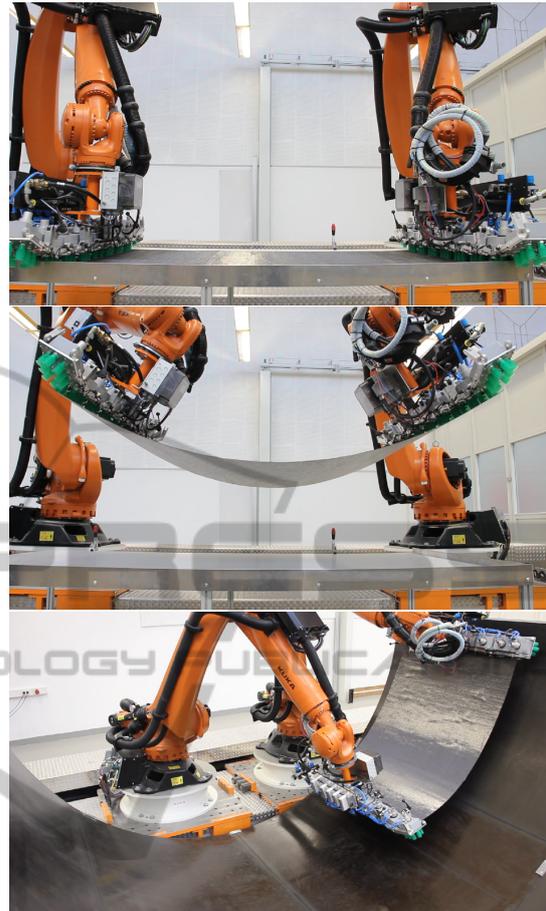


Figure 3: A typical dry fibre placement process for the production of the lower half of an airplane fuselage with the size of an AIRBUS A320 a.) grabbing a 4-6 m cut piece from a flat plane b.) transport from grabbing position to lay up position c.) lay up of cut piece in 3 dimensional mould.

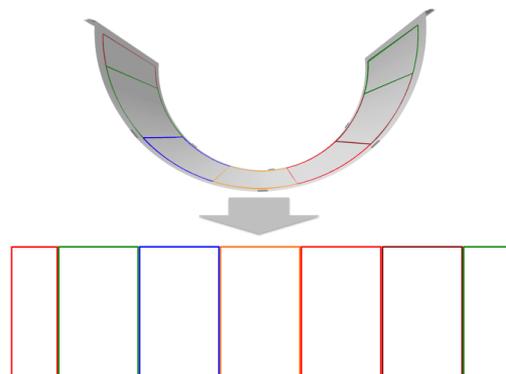


Figure 4: First layer of the plybook of the lower half of a fuselage in 3D and unwind to 2D.

### 3 STATE OF THE ART

This chapter shows the state of the art of collision detection and path planning both in science and in industry.

### 3.1 State of the Art in Science

#### 3.1.1 Collision Detection

Industrial manipulators have high masses which are moved. That makes it very important to detect collisions of the robot with other robots or the environment reliable.

Most collision detection algorithms distinguish between a broad- and a near-phase (Kockara et al., 2007). In the broad-phase objects are detected which are inspected more accurately in the near-phase.

The most common methods to check the broad-phase are exhaustive search, sweep and prune (Baraff, 2001) (Lin and Manocha, 1993) and hierarchical hash tables (Mirtich, 1996). In industrial robot applications the position of the robot is known at every time with an accuracy of about  $\pm 3$  mm. This makes the detection of the broad-phase very easy.

The algorithms to calculate the near-phase are mostly divided into four groups: feature-based, simplex-based, image-space and Spatial Data Structures (Mirtich, 1996). Feature-based algorithms directly work on the primitive form of the object. Famous representatives are polygonal intersection (Moore and Wilhelms, 1988), Lin-Canny (Lin and Canny, 1991), V-Clip (Mirtich, 1998) and SWIFT (Ehmann and Lin, 2000).

Simplex-based algorithms are based on a geometrical approach which describes a n-dimensional polygon which is the convex hull of n+1 vertices. With increasing dimensionality this results in the following objects: point, line, triangle, triangular pyramid. The Gilbert-Johnson-Keerthi (GJK) distance algorithm is the most famous representative (Gilbert, 1988) (Cameron, 1997) (van den Bergen, 1999) (van den Bergen, 2001) (Gilbert and Foo, 1990).

The family of Image-Space algorithms (ISB) detects collisions by the calculation of overlappings. For the detection of collisions in dynamic environments the ISBs are very efficient, because the calculation can be parallelized very easy and put on a graphical processing unit (GPU). Famous examples are (Jang, 2006) (Stewart, 2008) (Heidelberg, 2004) (Jang et al., 2007) (Myszkowski et al., 1995) (Heidelberg et al., 2003).

Bounding Volume Hierarchies (BVH) belong to the family of Spatial Data Structures. In (Figueiredo et al., 2006) an overview over the different types can be found. One kind are Bounding Spheres (Bradshaw and O'Sullivan, 2004). The use of Bounding Spheres is very famous for collision detection because the calculation cost are very simple and fast. Another group are the Bounding Boxes (BB) which describe objects

better than spheres. They are often used in applications like ray-tracing. Special forms of the bounding boxes are Axis-Aligned Bounding Boxes (AABB), which are aligned on the coordinate axes. They are normally defined by two points which define the vertices on the cross diagonal. Another form are arbitrarily oriented boxes called Oriented Bounding Boxes (OBB). Furthermore objects can be defined by polyhedrons. These bounding boxes are called k-Discrete Oriented Polytopes (k-DOP). In contrast to OBB, k-DOPs allow more bounding surfaces wherefore they can describe objects better.

Due to the fact that modern measuring systems, like a laser-scanner or a depth camera often create point clouds as representation of the environment another possibility of collision detection is the direct calculation on these clouds (Klein and Zachmann, 2004) (Pan et al., 2011) (Yakut, 2010).

In the industrial environment there are just a few approaches which deal with collision avoidance based on environment data without external sensors. In (Fawaz et al., 2009) a virtual simulator is introduced which allows an on-line collision monitoring. (Pedrocchi et al., 2009) picks an algorithm based on potential field method as central theme which can detect and avoid collisions between industrial robots. In (Cheng, 1995) a four dimensional (three spatial dimensions and time) real-time collision detection technique for the UPS arm, a ten degree-of-freedom hybrid serial-and-parallel redundant robotic arm is shown. For the collision detection the geometrical information is separated from the time by s-formulations. After the separation the occurring collisions can be calculated by bisection method in real-time. In (Hermann, 2013) a real-time collision detection system, which is optimized for the calculation on CUDA Graphical Processing Unit (GPU), is presented. The system is based on two voxelmaps which are put on the GPU.

#### 3.1.2 Path Planning of Industrial Robots

The main goal of motion or path-planning is to find a continuous motion that connects a starting- and destination-point, while avoiding collisions with known obstacles. For the calculation the robot and the obstacles must be defined in a 2D or 3D workspace. Normally the coordinates that define the position and the orientation of a coordinate frame that is attached to a rigid body in three-dimensional space define its configuration space. In robotics the configuration space defines all positions of an end-effector which is attached to a robot in three-dimensional space (Craig, 2005).

Another space which describes a position of a

robot is the joint space. The set of joint positions for each link of the robot is called joint space. The forward and backward kinematic of a robot manipulator is the mapping between the configuration space and the joint space. The forward kinematic maps the joint positions to the coordinate positions and the backward from coordinate to joint positions. Finding a path for a robot also means to find the path in the configuration space and afterwards map it back to joint space.

For the determination of two- or tree-dimensional path planning problems exist different grid based methods, where a grid is put over the working space of the robot. Famous examples are depth-first search, breadth-first search, Dijkstra and A\*. A very good explanation of these algorithms can be found here (LaValle, 2006).

Another group are the geometrical algorithms, including Visibility Graphs (Scott and Vuillemin, 1986) and Cell Decomposition (LaValle, 2006). A Visibility Graph reflects the free view between different vertices in a scene. By adding a start and an endpoint the shortest path can be found with the Dijkstra algorithm. The Cell Decomposition algorithm divides the scene in smaller regions (cells). After that the shortest and easiest connection between different cells is calculated with a tree data structure.

Path planning for robotic manipulators in scientific of industrial applications is very interesting and challenging problem especially if the environment of the robot is not static e.g. when there is human-machine interaction or multiple robots are in the same workspace.

For high dimensional path detection problems the Potential Field Method is very practical. The basic concept of that method is that obstacles and the robot are seen as electrified particles with opposite sign and the goal has the same sign as the robot. The algorithm calculates a path where the distance between the robot and the obstacles is big enough and the length between the start- and the endpoint is as small as possible (Barraquand et al., 1992) (Daily and Bevly, 2008) (Kitamura et al., 1995) (Tang et al., 2010).

**Single Robot Path Planning.** There are some examples for the path planning of a single robot manipulator both off-line and on-line using computational intelligence methods.

In (Saravanan et al., 2007) an off-line algorithm based on an evolutionary algorithm is presented which calculates an optimal trajectory for a PUMA560 6-DOF manipulator. The aim of the algorithm is to minimize the multi-criterion cost function with actuator constraints, joint limits and payload constraints by considering dynamic

constraints by motion. In (Ting et al., 2002) a collision free off-line path planning algorithm is introduced which is based on the assigned marked number of the passable region via wave expansion method. In (Klanke et al., 2006) an on-line path planner for a redundant Mitsubishi PA-10 arm with 7-DOF is introduced which can deal with stationary, non stationary or unknown environment. The method works with the grid based dynamic wave expansions neural network (Lebedev et al., 2005). In (Huang and Lian, 1997) a model-free hybrid fuzzy logic and neural network algorithm was proposed to control a 4-DOF manipulator. A conventional fuzzy controller was used for the rough adjustment of each joint. Another controller which used a back-propagation (BP) neural network was designed to control the coupling between the links. By the combination of fuzzy and neural network the learning time of the neural network could be dramatically reduced. In (Zavlangas and Tzafestas, 2000) a fuzzy approach is presented for the on-line local navigation and obstacle avoidance for an industrial 3-DOF robotic manipulator. The system is divided into separate fuzzy units each of them controlling a robotic joint separately. In (Cueva and Ramos, 2002) a method based on genetic algorithm is presented to calculate collision free paths in 2D for redundant or non redundant manipulators. In (Kazem et al., 2008) a genetic algorithm is proposed to optimize the point-to-point trajectory of a redundant 3-link arm. The algorithm can find a collision free path with minimum travelling time and space. In (Gosselinj, 1994) an approach is presented using neural network and fuzzy logic for the path planning of a 3-link manipulator in 2D. The neural network is used to predict in real-time the trajectory of a moving object filmed by a camera to be caught by the manipulator. The fuzzy logic is used to control the joints of the robot.

**Cooperating Robots Path Planning.** Path planning for cooperating mobile robots is a popular research area however in the area of cooperating industrial manipulators are just a few research results.

In (Juan C. Fraile and Dodds, 1999) a trajectory planning system is introduced which calculates trajectories with a minimum time performance for three industrial manipulators each with five joints sharing the same workspace and working on the same workpiece. (Tzafestas et al., 1998) present a path planning system, for a cooperating three-robot system transferring a large object from a start to a final position. The method is based on the master-and-two-slave mode where one robot is the master pretending to do the movements and the other robots are following. (Ali et al., 2002) present a path planning algorithm using

coevolutionary genetic algorithm (CGA) for two cooperative robots. A coevolutionary genetic search is performed on the configuration space to find the minimum and collision free path. Finally the CGA method is compared against A\* and genetic algorithms (GA). In (Curkovic et al., 2013) a coevolutionary algorithm for the collision free motion planning of two 6-DOF industrial manipulators with overlapping workspaces is presented. The planning is based on a hall of fame - Pareto-based co-evolutionary algorithm which allows the real-time calculation of the path. (Garg and Kumar, 2002) present a strategy for the determination of an optimal path for multiple 2-link robots in 2D requiring the least amount of torque with genetic algorithm. (Li et al., 2012) introduce a system using neural network for the control of multiple redundant manipulators moving the same payload together. Each module in the neural network controls one manipulator and all networks together solve the common task.

## 3.2 State of the Art in Industry

### 3.2.1 On-line Programming

A common on-line programming technology is the manual teach-in of a robot. This means the process of generating a sequence of robot poses or instructions the robot has to do to accomplish the desired task. To do that the programmer has to know the programming language and the teach panel of the robot he uses. Normally the teach panel has buttons for saving and editing the program and buttons or a 3D mouse to move the robot. The programmer can move the robot in different coordinate systems which makes the positioning more intuitive. The robot offers a Cartesian world coordinate system and a tool center point (TCP) Cartesian coordinate system. Furthermore the robot offers the possibility to define a base coordinate system for a work piece. Another possibility is to move the joints of the robot. Between the point the programmer can define in which motion profile e.g. linear or point-to-point and with which acceleration and velocity the robot should move.

The advantage of the teach-in process is that it is very clear for the user because he has a concrete reference to the process while programming. A task in a working space without many obstacles is easy to program. If the working space is very complex with many obstacles and a multiple bent work pieces where many interpolation points are needed the teach-in is very difficult. Another disadvantage of this method is that it is a very time consuming process. After a raw teach-in follows another very time consuming optimization of the trajectory of the robot by optimizing

single points and adapting the velocity profile for the movements. To do that the programmer has to run the created program on-line on the robotic cell. The result of the teach-in is one solution for the trajectory of the process which depends on the skills and experience of the programmer.

For the programming of cooperating robots the robot manufacturer KUKA offers an application package called RoboTeam which makes it possible that up to 15 robots can work in a team. RoboTeam makes it possible that robots can do load sharing or workpieces can be processed during a transfer from different robots. The robots keep their standard controller and are connected and synchronized with a local network. The application package offers two functionality types. The motion cooperation and the program cooperation.

In this way, all tasks that directly affect the robot group are also carried out autonomously by the group. By setting shared synchronization markers, it is possible to synchronize the program sequences of several robots e.g. the synchronized grabbing of a workpiece. The distributed sequence control of complete manufacturing programs is carried out decentralised within the networked robot group. Each robot in the group can start a manufacturing program on another robot or wait for the end of a manufacturing program. This means that it is possible to dispense with an external PLC in many cases, leading to significant cost reductions for the production cell. The program operation allows the synchronization and monitoring of shared workspaces of the robots.

The motion cooperation allows to geometrically connect the TCPs of the robots. As a result it is possible to couple the geometric path of the robots. This allows a flexible solution for all processes where very heavy or very large workpieces have to be transported by more than one robot.

The teach-in of cooperation robots has additional disadvantages adverse to the teach-in of one robot. One is that it is very difficult to have an overview off the teaching process. To avoid collisions while the teach process there should be minimum one more person. Another disadvantage is that the programming of two robots is not very user friendly. The programmer has to switch between the teach panels of the two robots all the time.

### 3.2.2 Off-Line Programming (OLP)

Off-line programming is a simulation based programming of a robot. The robot cell is modelled in the computer. This can be done by containing obstacles, tools, jigs and the robots. For the modelling the geometry and the size of all things which are in the cell and

necessary for the process must be exactly known. The quality of the OLP program significantly rises with the quality of the model. After the cell is modelled a collision free path can be manually generated by moving the robot in the virtual world. Afterwards the path can be optimized for a fast execution. After the optimization the path must be exported to a real robot program in the appropriate robot language.

The OLP programming has a lot of advantages. It is possible to test different scenarios of the process before the cell is built. After that an optimization of the installation of the process stations can be done before the cell is built. Another advantage is that the cell can be taken into operating state directly after completion.

But OLP has also some disadvantages which are inappropriate for the use in CFRP production. The biggest drawback is that cooperating robots are not supported. Another one is that the resulting program is static and it is not possible to put correction values to the production process. So the whole quality of the resulting assembly mainly depends on the accuracy of the virtual model of the cell in the OLP tool.

## 4 METHODOLOGY

The goal of this thesis is to accurately examine fuzzy logic, artificial neural network and evolutionary computing methods on the applicability for path planning for cooperating industrial manipulators in a CFRP production environment. First each of these methods will be examined stand-alone without optimization. In that stage the advantages and disadvantages of every method will be identified and compared.

After the analysis the strength of the methods will be combined for the path planning of cooperating robots. The process which will be considered is the pick, transport, drape and lay up of dry fibre carbon material. While the path planning it will always be important to focus on the gentle handling of the material. The raw material is very sensitive and its characteristic are a little bit similar to cloth. In a later step more robots could be involved in the path planning. Two robots could be responsible for the lay up and a third robot could do a quality check e.g. with a camera or a laser in the same working space. In conventional robotic cells the other robots would stop so that the measuring robot can do his job. To use the robotic cell shown in Figure 2 economically well the processes should not be mutual exclusive but rather different jobs should run parallel.

Additionally the fuzzy logic, artificial neural network and evolutionary computing methods will be compared with classical path planning methods like

e.g. Dijkstra, A\* and potential field method. A special focus will be set on the reaction of the different methods on local minima. The potential field method e.g. is very famous for getting stuck in local minima (Stroulia et al., 1997).

Another point which will be examined is the complexity of calculating a path for a scenario. Normally exact motion planning with complex constraints in a high-dimensional system is computationally very expensive. According to (Eberhart and Shi, 2007) computational intelligence methods need very less computation power and nevertheless it is possible to solve problems which are otherwise impossible or impractical. According to the author computationally intelligence tools do offer solutions to some problems which are not able to solve with any other method.

A very important point on which will be focussed while the examination of the path planning is the collision detection. Typical path planning application have a collisions checker which tries to avoid collisions between the robot and static obstacles in the path. The path planning in this thesis should also consider possible collisions between different robots which are moving objects. Another important consideration in that thesis are intended collisions between the robot tool and the jigs which are necessary for the lay up process. The robot tools have silicon vacuum cups which are needed to press the material on the jigs. These volitional collisions should be considered by the path planning.

All test for this thesis should firstly be simulated. After successful testing the methods should be tested in a real production scenario in an industrial scale in the multifunctional robotic cell in Figure 2. For the testing of the algorithms a simulation environment has been implemented in C#, which allows the visualisation of 6-DOF industrial robots. The environment is called CoCo-Framework. CoCo stands for Collisions-free Cooperation which reflects the main aim of that thesis. In these framework it is possible to import obstacles for the scene from CAD data or from external sensors like depth cameras. It also allows to attach end-effectors to the robots which are used for the production process. For the movement of the robots a forward- and inverse kinematic are implemented. Furthermore typical motion profiles like linear, point-to-point and circ movement are implemented. While moving the robots in the simulation environment occurring collisions can be detected by different bounding box based algorithms like e.g. GilbertJohnsonKeerthi distance algorithm (GJK).

Figure 5 shows a screenshot of the visualisation of the CoCo environment. The scene shows a dry fibre placement process for cooperating robots. The robots

are equipped with special end-effectors to handle dry fibre textiles. The half cylinder shows the lower half of a fuselage. The colourful outlines show the placing position for the fibre cut pieces. Figure 6 shows the path planning for a single robot process in the CoCo simulation framework. On the left side an industrial robot can be seen. Each link is surrounded by a bounding box for collision checking. The red box in the middle represents an obstacle in the process. The grey half cylinder represent the destination. In this scene the shortest TCP path is calculated with cell decomposition.

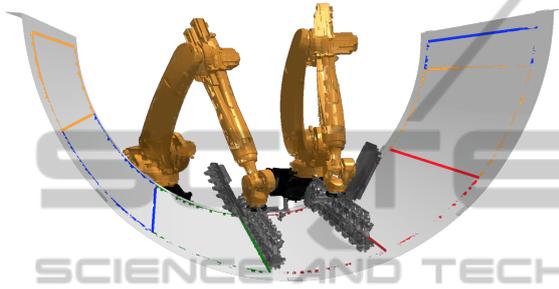


Figure 5: Cooperating robots in CoCo simulation framework putting a dry fibre cut piece in the lower half of a fuselage.

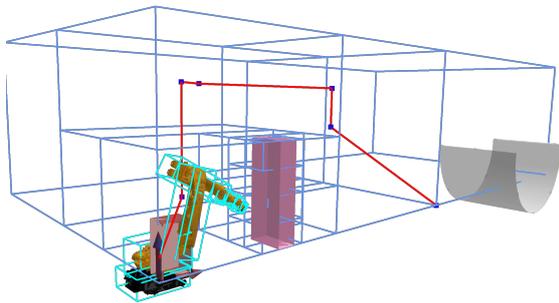


Figure 6: Path planning for a single robot with the CoCo simulation framework. The red box represents an obstacle. The blue lines show the cell decomposition of the workspace and the red line shows one possible path of the TCP from the actual position of the robot to the lay up position.

## 5 EXPECTED OUTCOME

For a CFRP process the state-of-the art cooperating teaching methods are not suitable. There is the need for an economic possibility to generate robot programs to produce high quality CFRP parts. To achieve that cooperating robots should work more material based. The normal master-slave control mode which is state of the art is not satisfactory. The objective

of that thesis is to develop a system which allows the collisions free path planning for cooperating industrial robots in the CFRP airplane production. For the system come into operation methods of computational intelligence to which belong fuzzy-logic, artificial neural networks and evolutionary computing.

## 6 CONCLUSION

In industrial environment where many robots share the same workspace it is essential to find feasible, collision free paths for the robots. As already shown by other authors computational intelligence methods are appropriate for the path planning of single robots. For cooperating robots the collision free path planning is even more complex. However here computational intelligence methods are very promising candidates for the planning.

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