A Single Performance Characteristic for the Evaluation of Seeker Tracking Algorithms

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Abstract. This paper presents a single numerical performance characteristic for the evaluation of seeker tracking algorithms. It concentrates on ship IR seeker tracking algorithms. Assessing the threat from guided missiles needs a sound evaluation of their performance. The main goal is to introduce a characteristic which is able to assess the threat for ships depending on various scenario parameters. It is shown that for these applications such a single characteristic is sufficient. In order to achieve this seven popular tracking algorithms are used for this. Synthetic IR image sequences are generated to simulate a large set of attack approaches and assemble sufficient statistics on the behavior of the algorithms. The introduced characteristic can also be used for investigations on algorithms themselves, e.g. for sensitivity analyses and parameter optimization of a single algorithm, and for comparison of different algorithms.

1 Introduction and Related Work

Automated tracking is essential in a wide area of applications. In order to determine the best tracking algorithm for a given application and to optimize the parameters of the algorithm, comprehensive quantitative evaluation characteristics are required. Different scenarios may require different characteristics, but in particular for optimization and comparison a single numeric characteristic is desirable.

Characterizing trackers on image sequences with multiple objects of interest, clutter objects and complex background – such as in surveillance applications – is quite a challenge. For those scenarios a lot of different metrics have been proposed. But defining a single characteristic in those cases is particularly difficult (see e. g. [1, 2, 3, 10, 17]).

For simpler scenarios - single object of interest and relatively homogenous background – that is easier. For such applications usually simple tracking algorithms are used. This relative simplicity should allow finding a single appropriate quantitative characteristic of the tracking algorithm.

The application also dictates whether it is preferable to integrate the performance characteristic over the whole video sequence or only on the last frame. E.g. for automated tracking of vehicles or people in a surveillance task the behavior of the tracker should be averaged over the whole sequence. However, for a seeker head only the last

frame is of interest – intermediate detours do not alter the overall success. This idea was implicitly used in [13, 14].

This paper concentrates on the protection of ships against infrared (IR) guided missiles. This application requires assessing the behavior of an IR missile seeker in its perception/action control loop in the scenario of interest. Today such threat assessment is regarded very important and intensively researched [6, 7, 12, 11, 13, 14]. Quantitative, automatically acquired performance measures were not in the focus of these works. Instead, for example in [13, 14] the tracker performance has been analyzed manually and only hit point positions were registered. Thus it is difficult to get a representative statistic and to compare the results of these papers with results of other authors. Additionally a method for automatic quantitative analysis of the effectiveness of the countermeasures is needed.

Real data – i.e. videos from real flights of IR missiles against ships – are not available. Alternatively, partially synthetic image sequences (based on real IR videos of ships) can be used, where approaching is simulated by zooming. This also causes high costs. Moreover, results based on such data cannot be compared and reproduced by other authors. Synthetic data – i.e. rendered image sequences - for the characterization are standard in literature (see e. g. [13, 14, 16]).

This allows rendering the next image according to the tracker results and thus simulating control actions based on previous images. Such procedure is called closed loop simulation. So called "open loop simulation" renders one high resolution video first. The size of the images is much bigger than the field of view (FOV) of the seeker. Seeker actions are modeled by simply choosing an appropriate section from each image. This causes much less computational efforts for extensive experimenting and allows simple repeating of the process with for example different start positions or different algorithm parameters. Discussions on open and closed loop simulation can be found in [13, 14].

2 Data and Algorithms

2.1 Sources of Synthetic Imagery

Open loop seeker simulation is used in this investigation. Inputs are synthetic sequences of 16-Bit images of a target ship with sea foreground and sky background. The sequences were rendered using three simulation tools: *SeaSimul* (Fraunhofer-IOSB-tool), *ShipIR/NTCS* (http://www.wrdavis.com) and *POV-Ray* (http://www.povray.org). All these programs allow simulating 16-Bit sequences and synchronously simulating binary sequences with the contour of the target, the so called mask-sequences (See Fig. 1). These mask-sequences together with the knowledge about the distance to the target are used as ground-truth information.

Preliminarily, the objective is to develop a numerical characteristic for seeker simulations. Therefore simple sequences are simulated: without effects caused by atmospheric transmission, sun radiation, vibration and so on. All sequences have 25 fps and 800*600 pixels with FOV 109.08x81.81 mrad. As starting distance 25 km were chosen. The approach velocity was fixed to 300 m/sec.
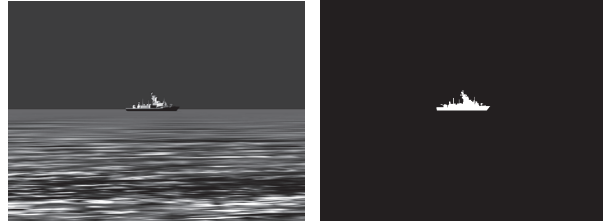
Fig. 1. Example created by the *SeaSimul* program: one frame from the synthetic sequence and from the corresponding mask-sequence.

2.2 Seeker Tracking Algorithms

Seven known seeker tracking algorithms [4, 5, 8, 9, 15] were implemented for characterizing. A priory there are good arguments to assume that at least two of them (*Centroid* and *FixedCorrelation*; see Table 1) cannot perform well for the considered scenarios. The analysis below approved this fact.

Table 1. Infrared seeker algorithms and corresponding FOVs.

Algorithm	Abbreviation	FOV (mrad)
RisingSun	*RSun*	6 x 6
Centroid	*Cent*	16 x 8
BinaryCentroid	*BCent*	16 x 8
ThresholdCentroid	*TCent*	16 x 8
FixedCorrelation	*FCor*	16 x 8
RefreshCorrelation	*RCor*	16 x 8
AverageCorrelation	*ACor*	16 x 8

The first one, the rising-sun reticle algorithm, simulates non-imaging system. Its field of view (FOV) is a circle. Other algorithms simulate imaging systems with rectangular FOVs.

2.3 Description of the Experiments

Each approach simulation is started at one of the frames (the starting frame) and ends at the last frame corresponding to the distance of about 3 km. At that distance the final homing algorithm is assumed to take over. Such special final homing algorithms are not a topic of this contribution.

The simulation terminates on the last frame and it will be characterized there and only there. So only the last frame will be used for construction of the characteristics. The position of the seeker's FOV (blue rectangle: see Fig. 2) is known. Its middle point will be called hit point (**HPT**). This point and the real position of the target (the corresponding mask) are used in the construction of all characteristics.

The number of pixels within the FOV (FOVArea) and the number of pixels on the target within the FOV (IntersectionArea) can be registered.
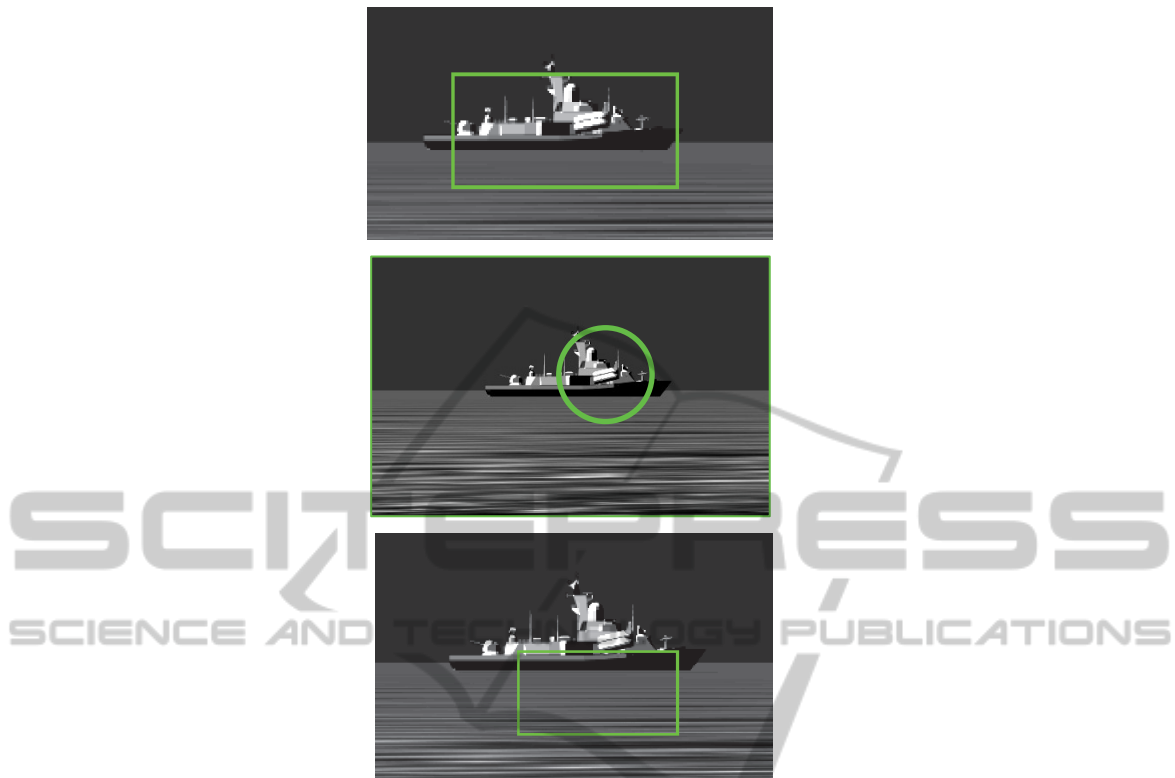
Fig. 2. Three examples of the terminal position after simulation. The rectangle (circle) is the seeker's FOV.

On the last image a rectangle **RLast** is constructed including the most important part of the ship. It is the circumscribing rectangle of the mask shrunk on all sides while the number of target's pixels in each "row" and in each "column" is smaller than 10% of the complete rectangle's length or height respectively (See Fig. 3.).

Fig. 3. A rectangle **RLast** includes the most important part of the ship.

Each simulation may also terminate prematurely either because of interior break criteria of the algorithm or because the open-loop simulation tries to leave the image.

3 Used Characteristics

The construction of the performance characteristics is done in three steps.

3.1 Single Simulation Characteristics

If the simulation is terminated prematurely it will be counted as complete failure and all five characteristics defined below get the value 0. Otherwise the following five characteristics can be calculated. By these constructions we have used some ideas of [11, 13, 14].

The **first characteristic H** (*Hit*) takes value 1 if **HPT** lies on the target and 0 otherwise.

Further the feature **CQ** (*Covering Quota*) can be calculated:

$$CQ := \text{IntersectionArea} / \text{FOVArea}.$$

(Compare with [11] where the performance is based on the amount of overlap between the ground-truth and tracker boxes. See also [1].)

It depends extremely on the contour of the target, on the seeker's FOV, and on **HPT**. Under all possible **HPT**s the *Largest Covering Quota* (**LCQ**) can be established. The **second characteristic NCQ** (*Normalized Covering Quota*) is defined as follows:

$$NCQ := CQ/LCQ.$$

It does not depend so much on these parameters.

The **third characteristic HR** (*Hit Rectangle*) gets the value 1 if **HPT** lies in the **RLast** and 0 otherwise. The **fourth** and **fifth characteristics PA1** and **PA2** (*Probability Assessments*) are defined via formulas:

$$PA1 := \frac{l}{l+2*\Delta X} * \frac{w}{w+2*\Delta Y} \,,$$

$$PA2 := \exp\left(-\left(\frac{\Delta X}{l/2}\right)^2 - \left(\frac{\Delta Y}{w/2}\right)^2\right).$$

Here l and w are the length and the width of the rectangle **RLast**. The vector (ΔX, ΔY) is the difference between centers of the rectangle **RLast** and **HPT** (see Fig. 4). (In [17] analogically distance is defined as $\sqrt{\Delta X^2 + \Delta Y^2}$ and accordingly it does not depend on the width and height of the target.)
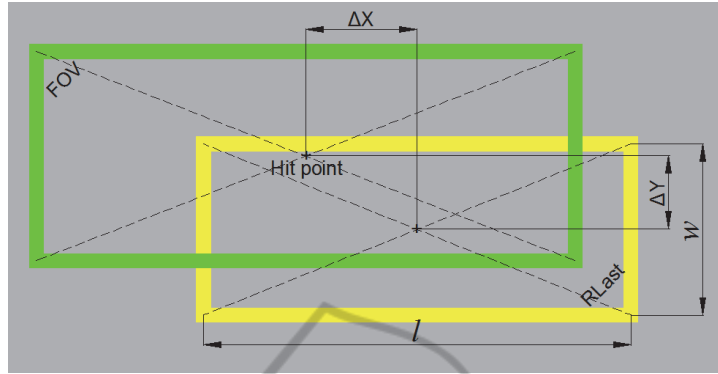
Fig. 4. FOV with **HPT** and **Rlast.**

3.2 Volley's Characteristics

Each simulation needs a lock-on position in the starting frame. As default value the center of gravity of the target will be taken. Experiments indicated that small variations of the lock-on position can lead to large differences of **HPT**s and all the five characteristics. In order to characterize the track algorithm this effect has to be reduced. One possibility to do this is starting several simulations with lock-on positions in a regular grid around the default value. In this investigation 25 simulations are used where the position is moving ±10 and ±20 pixels in horizontal and vertical directions. Such a set of simulations is called a *volley*.

For each element of such volley all five simulation's characteristics were registered. Corresponding averages **AH**, **AHR**, **ANCQ**, **APA1** and **APA2** (The first letter A stands for *Averages*) were taken as characteristics of a volley. Note that all these values lie between 0 and 1. Each of them can be interpreted as probability assessment for the seeker's homing phase to score a hit. It will be shown that it is sufficient to use only one of them.

The first experiments registered the behavior of the characteristics **AH**, **AHR**, **ANCQ**, **APA1** and **APA2** as functions of the starting distance. A series of volleys was started from frame numbers 1, 51, 101, and so forth to the frame number 1751 (corresponding to distances between 25 km and 4 km). Fig. 4 shows exemplarily the characteristics as function of starting frame number for *RisingSun* and *ThresholdCentroid* trackers.

It can be seen that all the characteristics are well correlated. This is a general experience from almost all our experiments. Particular good correlation is found between the characteristics **APA1**, **APA2** and **ANCQ**. Three situations can be distinguished:

1) Good situations (bad for the ship): all characteristics are nearly constant with small standard deviations. In this case the correlation coefficient can be relatively small (>0.25). This situation is characterized with relatively large values for large distances to target (small frame numbers).

2) Bad situations (good for the ship): all characteristics increase if the starting distance decreases and have large standard deviations. In this case the correlation coeffi
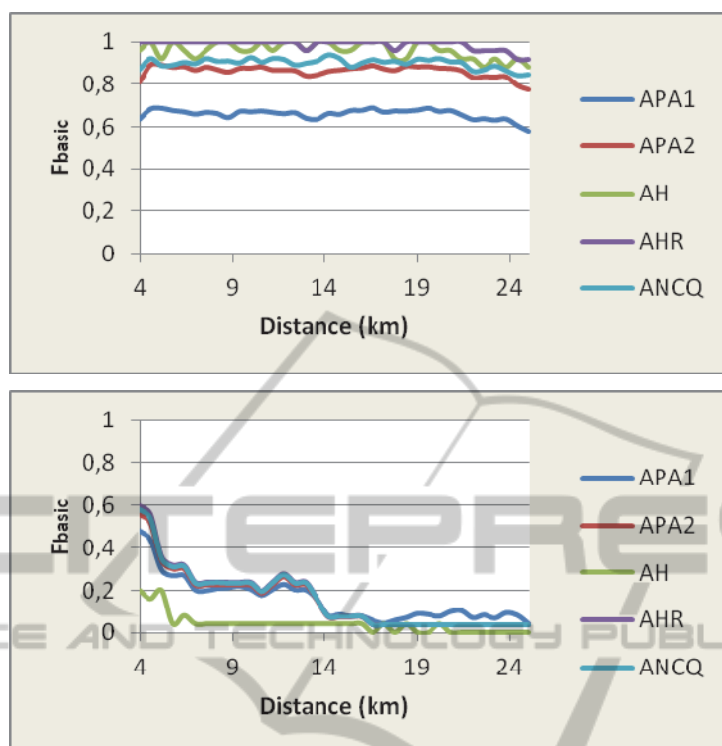
Fig. 5. Typically dependences of the characteristics on the starting distance (km) for two algorithms: *RisingSun* – above and *ThresholdCentroid* – below.

cients are greater than 0.6. This situation is characterized with relatively small values for large distances to target.

3) Very bad situation (ideal for the ship): all characteristics are extremely small. In this case the correlation coefficients are not interesting.

The characteristics **AH** and **AHR** are discrete. So they are not appropriate as an objective function for optimization. The three other characteristics can be considered as continuous. They are preferred. The calculation of the characteristic **ANCQ** is more difficult to automate than that of the characteristics **APA1** or **APA2**. Finally, the characteristic **APA2** is less sensitive than **APA1** for small values of ΔX and ΔY.
In conclusion it can be stated that

- The behavior of these five volley's characteristics can be used to estimate the quality of a track algorithm and to compare two algorithms or two simulations;
- Because these characteristics are well correlated, it is sufficient and preferable to use only one of them;
- It is reasonable to use only the characteristic **APA2** for further work.

3.3 Integrated Characteristic

Calculating diagrams as displayed in Fig. 5 causes considerable computation even for

APA2 only. But it is not necessary, because the values of **APA2** for few large distances characterize the overall behavior well enough. On the other hand using the value of **APA2** for only one fixed distance may be error prone because of random spikes in such curves. Three values of different starting distances, namely 20, 15, and 10 km were picked, and as proposed singular characteristic the averaged integrated characteristic is defined as

$$\textbf{F}_\textbf{basic}:=(\textbf{APA2}(20)+\textbf{APA2}(15)+\textbf{APA2}(10))/3.$$

All following experiments were made with this characteristic.

4 Applicability of the Integrated Characteristic

The characteristic **F**basic can be used as well for investigation how the tracking algorithms react on different scenario parameters (see the following section) as for estimation of algorithms themselves and for optimization of their parameters. But we emphasize that the characteristic **F**basic can also be used for a wide variety of other investigations.

4.1 Assessment of Algorithms

Here **F**basic is used for the assessment of the seven algorithms. Three experimental sequences were conducted using the three available rendering tools (see above) with the same parameters and similar ships as targets. For each sequence and for each track algorithm values of the characteristic **F**basic were calculated. The results are summarized in Table 2.

Table 2. Assessment of the algorithms.

	Fbasic		
Algorithm	SeaSimul	ShipIR	POV-Ray
RSun	0.87	0.41	0.32
Cent	0	0	0.07
BCent	0.08	0	0.07
TCent	0.11	0	0.07
FCor	0.02	0.11	0.11
RCor	0.34	0.20	0.31
ACor	0.41	0.26	0.52

Characteristic **F**basic obviously arranges the algorithms in a similar order for all three sequences. Four of the algorithms seem to be not useful at all. Recall that for algorithms *Centroid* and *FixedCorrelation* this was expected. Only three algorithms (*RisingSun*, *RefreshCorrelation* and *AverageCorrelation*) show acceptable values of the characteristic **F**basic. Therefore only these were used for further investigations.

4.2 Assessment of Scene Parameters

Exemplarily, the influence of the frame rate and vibration were tested.

In order to find the impact of the frame rate on the performance of the algorithms the tool *SeaSimul* was used to generate three image sequences with frame rate 5, 10 and 50 fps additionally to the sequence with the frame rate 25 used above. The values of the characteristic **Fbasic** for these sequences are summarized in Table 3. It turns out they do not depend seriously on the frame rate. For further investigations this means that the parameter 'Frame rate' in not very relevant. This can also help saving effort for future experiments.

Table 3. Dependence on frame rate.

	Frame rate			
	5	10	25	50
Algorithm	**Fbasic**			
RSun	0.83	0.83	0.87	0.86
RCor	0.35	0.34	0.34	0.35
ACor	0.36	0.39	0.41	0.43

In order to test the influence of the vibration a lot of sequences with different values for yaw, pitch and roll vibration separately were generated. The results for yaw and roll vibrations are summarized in Tables 4 and 5 respectively.

Table 4. Dependence on yaw.

	Yaw parameter				
	0	0.05	0.1	0.2	0.3
Alg.	**Fbasic**				
RSun	0.87	0.86	0.62	0.42	0.27
RCor	0.34	0.35	0.06	0	0
ACor	0.41	0.41	0.10	0	0

The algorithms that use correlation strongly react on yaw-vibration. The *Rising-Sun* algorithm is more stable. The results for the pitch-vibration are similar.

Table 5. Dependence on roll.

	Roll parameter						
	0	0.1	0.2	0.3	0.4	0.5	0.6
Alg.	**Fbasic**						
RSun	0.87	0.86	0.77	0.77	0.8	0.79	0.78
RCor	0.34	0.38	0.40	0.44	0.42	0.42	0.32
ACor	0.41	0.49	0.39	0.49	0.46	0.54	0.55

The roll-vibration is less important for the seekers algorithms because the target is always near the center of the image.

5 Discussion and Conclusions

The experiments indicate that a small number of simulations cannot characterize track algorithms properly, not even for a fixed starting frame. Very large numbers of simulated approaches are needed. Open loop simulation on synthetic data opens the way to perform such experiments with acceptable effort.

In order to characterize a seeker tracking algorithm with single characteristic five different numeric characteristics have been introduced and investigated for a selected number of scenarios. It was shown that they are tightly correlated. In the end only one quantitative and continuous characteristic F_{basic} was constructed. It allows automatic analysis of the tracking results.

Further experiments showed that it can be used for numeric characterization of combinations of tracking algorithms and image sequences. Exemplarily, it was shown how the different algorithms can be compared and how the influence of different scenario parameters can be investigated. Important conclusions for the reduction of the over-all run time of the simulation work were possible.

The scenario used here is admittedly limited. Such statements as "algorithm is bad" may not be generalized too far. Maybe, the parameters of the algorithm should be chosen differently or maybe for sequences of different nature other characteristic values emerge. This does not concern the appropriateness of F_{basic} for assessing such purposes.

Preliminary, the characteristic should be used as objective function for the optimization of parameters inside of the algorithms. The optimal setting of parameters is of great interest and importance for further experiments. Only a quantitative and continuous characteristic allows finding of such optimal setting.

As future work also the influence of such parameters like atmospheric transmission, sun radiation, etc. will be investigated.

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