

Structural Analysis of Nuclear Magnetic Resonance Spectroscopy Data

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Abstract: From the clinical diagnosis point of view in vivo nuclear magnetic resonance (NMR) spectroscopy has proven to be a valuable tool for performing non-invasive quantitative assessments of brain tumour glucose metabolism. Brain tumours are considered fast-growth tumours because of their high rate of proliferation. Therefore, there is strong interest from the clinical investigator's point of view in the development of early tumour detection techniques. Unfortunately, current diagnosis techniques ignore the dynamic aspects of these signals. It is largely believed that temporal variations of NMR spectra are simply due to noise or do not carry enough information to be exploited by any reliable diagnosis procedure. Thus, current diagnosis procedures are mainly based on empirical observations extracted from single averaged spectra. In this paper, a machine learning framework for the analysis of NMR spectroscopy signals is introduced. The proposed framework is characterized by a set of structural parameters that are shown to be very sensitive to metabolic changes as those exhibited by tumour cells. Furthermore, they are able to cope not only with high-dimensional characteristics of NMR data but also with the dynamic aspects of these signals.

1 INTRODUCTION

The last decade has seen a rise in the application of proton NMR spectroscopy techniques, fundamentally in fields such as biological research (Raamsdonk et al., 2001) and clinical diagnosis (Lisboa et al., 2010). The main goal within the biological research field is to achieve a deep understanding of metabolic processes that may lead to advances in many areas including clinical diagnosis, functional genomics, therapeutics and toxicology. In addition, metabolic profiles from proton NMR spectroscopy are inherently complex and information-rich, thereby having the potential to provide fundamental insights into the molecular mechanisms underlying health and disease. Nevertheless, it is important to note that the main difficulty is not simply how to extract the information efficiently and reliably but how to do so in a way which is interpretable to people with different technical backgrounds. In fact, machine learning techniques (Bishop, 1995; 2006) have recently been recognized by biological researchers (Ebbels and Cavill, 2009) as an important method for extracting useful information from empirical data.

From a clinical diagnosis point of view, proton NMR spectroscopy has proven to be a valuable tool which has benefited from the knowledge and experience acquired through biological research studies. Furthermore, a large number of proton NMR spectroscopy applications have targeted the human brain. Specifically, it has been extensively used for the study of brain diseases and disorders, including epilepsy (Aydin et al., 2007), schizophrenia (Sigmundsson et al., 2003), parkinson's disease (Summerfield et al., 2002) and bipolar disorder (Frye et al., 2007) amongst others. This is mainly due to the fact that proton NMR spectroscopy is a non-invasive technique, which is particularly important in this part of the body where clinical surgery or biopsy is more delicate than in other areas. In addition, it is important to note that it allows in vivo quantification of metabolite concentrations in brain tissue for clinical diagnosis purposes. Moreover, one of the most successful applications of proton NMR spectroscopy has been cancer research (Kwock et al., 2006); (Bottomley, 1984). In this paper, the focus is on proton NMR brain spectroscopy.

Generally speaking, the process of clinical diagnosis involves the analysis of spectroscopy

signals obtained from a well-defined cubic volume of interest (single voxel experiment) in a specific region of the brain during a pre-defined time frame (acquisition time). Two acquisition methods are commonly used, namely point resolved spectroscopy (PRESS) (Frahm et al., 1987) or stimulated echo acquisition mode (STEAM) (Nelson and Brown, 1987). Most of the time, the analysis of the signals is carried out in the frequency domain. The raw signal from the free induction decays (FIDs) is transformed using the discrete fourier transform. Afterwards, a pre-processing stage is also performed to remove artefacts from the acquisition process. Finally, the resulting spectral signals, whose number is approximately equal to the acquisition time divided by the repetition time of the sequence, are averaged and in most cases used for a preliminary diagnosis which relies on a simple visual analysis of the spectra.

However, current diagnosis techniques based on proton NMR spectroscopy are still in their infancy. Firstly, as stated above, powerful tools like machine learning techniques are scarcely applied within this context (Sadja, 2006). Indeed, most of the applications of machine learning techniques have been in the field of systems biology research (Friedman, 2004); (Basso et al., 2005) and have used data from other techniques like liquid chromatography mass spectrometry or gene expression microarray. This is mainly due to the abovementioned problems regarding the interpretability of the information but also because of a lack of effective communication of results between researchers working in different fields. Of particular interest is the fact that current diagnosis techniques ignore the dynamic aspects of these signals. It is largely believed that the information content of temporal variations of NMR Spectra is minimal. Thus, current diagnosis procedures are constrained to empirical observations extracted from a single averaged spectrum. Furthermore, this fact could mask important information concerning metabolic changes, especially in early stages of tumour formation. In this paper, a machine learning framework for the analysis of NMR spectroscopy signals is introduced which is able to exploit both static and dynamic aspects of these signals.

The rest of this paper is organized as follows: In the next section, the principal characteristics and difficulties associated with the processing of H-NMR signals are presented. In section 3, a formal characterization of NMR-based data is introduced from a machine learning point of view. The reliability of the proposed measures is assessed

through careful analysis of the results provided by a specific experimental design in section 4. Finally, section 5 provides a summary of the present study and some concluding remarks.

2 CHARACTERISTICS OF H-NMR DATA

The metabolites detectable with proton NMR spectroscopy include, between others, the resonances of N-acetylaspartate (NAA), N-acetyl aspartyl glutamate (NAAG), alanine (Ala), Choline (Cho), creatine (Cr), gamma-aminobutyric acid (GABA), glutamine (Gln), and a variety of other resonances that might not be evident depending on the type and quality of spectra as well as on the pathological condition. The molecular structure of a particular metabolite is reflected by a typical peak pattern. Furthermore, the area (amplitude) of a peak is proportional to the number of nuclei that contribute to it and therefore to the concentration of the metabolite to which the nuclei belong.

Of particular interest is the fact that even if peak amplitudes change from different samples reflecting a change in concentration, the ratios between the central resonance peak and sub-peaks, composing the metabolite fingerprint, always remain constant. Most of the metabolites have multiple resonances many of which are split into multiplets as a result of homonuclear proton scalar coupling. Despite high magnetic fields increase the sensitivity and spectral dispersion in NMR spectroscopy, at clinical field strengths (from 1.5 up to 3 Teslas), there exists a significant overlap of peaks from different metabolites.

In addition, the response of coupled spins is strongly affected by the acquisition parameters of the NMR sequence, e.g. radio frequency pulses employed and the time intervals set between them (Cloarec et al., 2005). Furthermore, additional difficulties are caused by the presence of uncharacterized resonances from macromolecules or lipids. This is further complicated by small but significant sample to sample variations in the chemical shift position of signals, produced by effects such as differences in pH and ionic strength. As a result of this problem, information coming from a given metabolite contaminates the spectral dimensions containing information from other metabolites. In other words, due to this phenomenon the resonance frequency of certain metabolites can suffer slight variations from sample to sample.

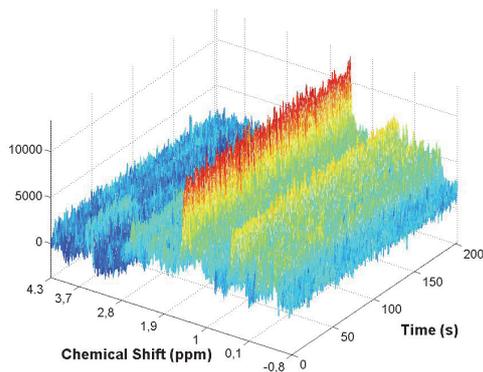


Figure 1: Temporal evolution of the Spectra associated to a short-TE NMR single voxel brain spectroscopy experiment at 3T (3 Teslas of Magnetic field strength). The voxel was located in the visual cortex of a healthy patient. A total echo time (TE) of 23 ms and a repetition time (TR) of 1070 ms were used for the acquisition process conducted during several minutes. The molecular structure of a particular metabolite is reflected by a typical peak pattern. The area (amplitude) of a peak (i.e., the vertical axis of spectra) is proportional to the number of nuclei that contribute to it and therefore to the concentration of the metabolite to which the nuclei belong. The horizontal axes correspond to the chemical shift scale (ppm) axis (which is representing brain metabolites resonances) and the time axis (in seconds) respectively. For instance, the resonance associated to the N-acetylaspartylglutamate (NAAG), a dipeptide of N substituted aspartate and glutamate (that is believed to be involved in excitatory neurotransmission processes) is located at 2.046 ppm.

In order to address these problems, some sophisticated strategies have been proposed (Bruschweiler and Zhang, 2004); (Keun et al., 2008). However, the common factor to all the abovementioned techniques is that they completely ignore the inherent dynamics of NMR spectroscopy signals. Unfortunately, it is largely believed that temporal variations of NMR Spectra (see figure 1) are simply noise or do not carry enough information to be exploited by any reliable diagnosis procedure. For example, in a single-voxel MRS experiment, as a result of the acquisition process, a whole matrix of data is obtained from the region of interest. Furthermore, within that matrix two consecutive rows correspond to signal frames taken with a time difference equal to the repetition time set for the acquisition sequence (usually 1035-1070 ms for short total echo time sequences). Therefore, the number of rows (signal frames) is approximately equal to the acquisition time divided by the repetition time of the sequence. Indeed, there is a small number of frames that are used for water referencing (usually eight) which are suppressed

when generating the data matrix. In addition, each row represents a spectral signal obtained from the volume of interest after a pre-processing stage which transforms the raw FID temporal data into the frequency domain. The frequency domain is usually preferred over the temporal domain (Vanhamme et al., 2001) since this enables visual interpretation.

Moreover, in the frequency domain the NMR signal is represented as a function of resonance frequency. Additionally, each column represents a given metabolite or metabolic signal. The number of columns depends on the particular pre-processing technique used, but is usually 8192 or 4096 dimensions, depending whether or not a zero filling procedure is applied to the transformed signal. In both cases, the associated chemical shift range corresponds approximately to the interval $[-14.8, 24.8]$ ppm. However, as stated above, the range of interest usually taken for brain metabolites is restricted to the interval $[-0.8, 4.3]$ ppm leading to a dimensionality reduction with respect to the original row size. The exact dimension of these vectors depends on the procedure used for generating the chemical shift scale. The water peak and the creatine peak (i.e., one of the 35 known metabolites involved in brain metabolism) are commonly used for this purpose. Nevertheless, it is important to note that the resulting matrix after selecting the appropriate range is still composed of high-dimensional patterns. Afterwards, the temporal variations of the spectra (i.e. the rows of the matrix of data) are averaged in order to obtain a single vector (single spectrum signal). In such vectors each dimension represents the mean value of a particular metabolic signal.

3 STRUCTURAL MEASURES

In the following sub-sections we introduce a set of measures that have been used within the context of supervised learning (Haykin, 1999); (Cherkassy and Mulier, 2007) for the structural characterization of NMR-based data sets. The principal advantage of these characterization parameters is not only their simplicity but also the fact that they do not make any assumption about the underlying nature of the data. Therefore, they are appropriate for dealing with both static and dynamic data sets.

Without a loss of generality let us suppose a data set D_N composed of N patterns belonging to a space of dimension d . Furthermore, it is assumed that each sample of the data set belongs to a category w_i where $i = 1, 2, \dots, C$. In other words,

there are C different pattern categories (or classes) defined in the input space. If we group the input variables x_i into a vector $\vec{x} = (x_1, x_2, x_3, \dots, x_d)$, the data set can be formally defined as a set of vectors \vec{x}^k in d dimensions (i.e., patterns) where $1 \leq k \leq N$, where each pattern belongs to one of the categories defined in the input space, $\forall \vec{x}^k \in D_N$ the category of a pattern \vec{x}^k is represented using the notation $class(\vec{x}^k) = w_i$ where $1 \leq i \leq C$.

3.1 Inertia

Inertia (Blayo et al., 1995) is a classical measure for the variance of high dimensional data. We distinguish here three types of inertia, namely, global inertia, within-category inertia and between-category inertia:

$$I_G = \frac{1}{N} \sum_{k=1}^N \|\vec{x}^k\|^2 \quad (1)$$

$$I_{w_i} = \frac{1}{N_i} \sum_{k=1}^{N_i} \|\vec{x}^k - \vec{g}_i\|^2 \quad \forall \vec{x}^k: class(\vec{x}^k) = w_i \quad (2)$$

$$I_W = \frac{1}{N} \sum_{i=1}^C N_i I_{w_i} \quad (3)$$

$$I_B = \frac{1}{N} \sum_{i=1}^C N_i \|\vec{g}_i\|^2 \quad (4)$$

Where $\|\cdot\|^2$ is the square of the Euclidean norm: $\|\vec{x}\|^2 = \vec{x} \vec{x}'$. Global inertia I_G (see definition (1)) is computed over the entire data set. In contrast, within-category inertia I_{w_i} (see definitions (2) and (3)) is the weighted sum of the inertia computed on each category where \vec{g}_i represents the center of gravity of patterns belonging to category w_i , where the weighting is the a priori probability of each category (N_i is representing the number of patterns belonging to category w_i). Between-category inertia I_B (see definition (4)) is computed on the centers of gravity of each category.

3.2 Dispersion and Fisher Criterion

Generally speaking, in a supervised classification problem, classification performance depends on the discrimination power of the features, that is to say, the set of input dimensions which compose the patterns of the data set. Dispersion and the Fisher criterion are two measures (Blayo et al., 1995) for the discrimination between classes (categories defined in the input space). The overlapping rate between categories is measured by the Fisher criterion (see expression (5)). In addition, a simple measure for the dispersion between categories is the mean dispersion of category w_i in category w_j defined in expression (6). It is important to note that, similar to conditional probabilities, the dispersion matrix is not symmetric.

$$FC = \frac{I_B}{I_W} \quad (5)$$

$$D_{ij} = \frac{\|\vec{g}_i - \vec{g}_j\|}{\sqrt{I_{w_j}}} \quad 1 \leq i, j \leq C \quad (6)$$

As it can be deduced, the discrimination is better if the Fisher criterion is large. Similarly, if the dispersion measure (6) between two categories is large then these categories are well separated and the between category distance is larger than the mean dispersion of the classes. Furthermore, if this measure is close to or lower than one, the categories are highly overlapped. In order to apply the Fisher criterion and dispersion measures the data set is normally pre-processed using a linear re-scaling (Bishop, 1995) so as to arrange all the input dimensions to have similar values. In addition, it is important to note that a high degree of overlapping between two categories does not necessarily imply significant confusion between them from the classification point of view. For instance, that is the case for multimodal or very elongated categories.

3.3 Confusion Matrix

The confusion matrix (Blayo et al., 1995) is a structural parameter of a data set which provides an estimation of the probability for patterns of one category to be attributed to any other or to the original category. Furthermore, it provides a generic measure of classification complexity. Let us denote as ξ the random variable describing the patterns of

the data set. Supposing ξ is a discrete variable, the confusion matrix can be defined as shown below, where f is a discriminating function:

$$C_{ij} = \sum_{k \in \xi} p(\xi_k / w_i) f(\xi_k) \quad (7)$$

More specifically, a classifier is always defined in terms of its discriminating function f which divides the d -dimensional input space into as many regions as there are categories. If there are C categories w_i , $1 \leq i \leq C$, the discriminant function may also be expressed in terms of the following indicator function f_i , where $f_i(u) = 1$ if $f(u) = 1$ and $f_i(u) = 0$ otherwise. The classifier performance may also be expressed by the averaged classification error:

$$E(f) = \sum_{i=1}^C p_i \sum_{j=1}^C C_{ij}(f) \quad (8)$$

The best confusion matrix is that corresponding to the Bayesian classifier (minimal attainable classification error). It can be deduced that the confusion matrix cannot be computed using the Bayesian classifier as it would imply a perfect knowledge of the statistics of the problem (conditional probabilities $p(\xi / w_i)$ and the a priori probabilities p_i). Therefore, the best confusion matrix must be in practice approximated. To this end, the k -nearest neighbour classifier (Bishop, 1995); (Blayo et al., 1995); (Fukunaga, 1990) is often used because of its powerful probability density estimation properties. More specifically, a set of values for k are generated, for instance the following odd sequence $k = 1, 3, 5, 7, 9, 11$. Afterwards, a leave-one-out cross-validation procedure (Haykin, 1999); (Fukunaga, 1990) is performed for the entire dataset for each k from the selected set of values. Finally, the best confusion matrix is that obtained for the value of k which minimizes the performance error defined in expression (8).

4 EXPERIMENTS

In this section we consider that the FIDs (Free Induction Decays) have already been Fourier Transformed to the frequency domain, and the artefact removal stage carried out. Furthermore, we

suppose the data is arranged into a matrix in which each row corresponds to a spectral sample, where two consecutive rows correspond to signal frames taken with a time difference equal to the repetition time of the NMR sequence and each column to a metabolic signal. The metabolic signal corresponds to the spectral intensity at a particular chemical shift. In addition, it is important to note that the metabolic signals (columns in the data matrix) have values that differ significantly, even by several orders of magnitude. Additionally, there are correlations between them (sample dimensions) due to the spectral overlap caused by the proton homonuclear scalar coupling. To take into account the differences in magnitude of metabolic signals, but allowing at the same time the possibility to exploit the existing correlations between them, the whitening transform (Fukunaga, 1990); (Bishop, 1995) was used to normalize all the data sets used in this section.

4.1 Data Set Description

For experimental purposes two data sets were used both of them corresponding to short-TE NMR single voxel brain spectroscopy. Let us denote the first data set as A, which corresponds to data collected from 11 healthy patients of ages ranging from 25 up to 45, with a mean of 31.45 years. The data was collected from different brain regions (see table 1 for details) and with approximately equal voxel sizes. The acquisition time was approximately equal to 5 minutes for all patients, using a total echo time (TE) equal to 23ms and a repetition time (TR) of 1070ms.

Similarly, the second data set (see table 2 for details) is a small data set used for comparison purposes in the experimental settings of section 4.2 and it is composed of data also collected at short TE but with a slightly different parameterization. Let us denote the second data set as B. For these data, the total echo time was set to 35ms and the repetition time to 1500ms and the patients' ages ranged from 30 up to 45 with a mean of 36 years. In addition, the data corresponds to three patients, where data matrix B_1 and B_3 belong to two healthy patients, while data matrix B_2 corresponds to a patient that was diagnosed with a tumour (after a rigorous clinical diagnosis procedure including biopsy). In particular, the data matrix corresponding to patient B_2 represents data obtained exactly from the brain tumour area.

Table 1: Data set A. Illustration of the most relevant characteristics of the dynamic data set used for the first experimental setting. This data set is composed of NMR data collected using a total echo time (TE) equal to 23ms and a repetition time (TR) of 1070ms from 11 healthy patients. Each data matrix A_i ($i = 1, 2, \dots, 11$) is composed approximately of 300 rows and 1068 columns. In other words, the samples belong to an input space of 1068 dimensions. The notation used for the voxel location in NMR Spectroscopy is “Left-Right” (L/R) for the “x” dimension, “Anterior-Posterior” (A/P) for the “y” dimension and “Inferior-Superior” (I/S) for the “z” dimension. Voxel dimensions are expressed in millimetres.

Data Set A TE = 23ms TR = 1070ms	Voxel Location	Voxel Size
[A ₁]	[L,P,I]=[0.9,6.3,17.2]	[20,20,20]
[A ₂]	[L,P,S]=[8.1,27.7,51.5]	[29,20,27]
[A ₃]	[L,P,S]=[6.7,9.5,15.1]	[20,20,20]
[A ₄]	[L,P,S]=[0.3,6.6,44.9]	[20,20,20]
[A ₅]	[L,P,S]=[1.2,18.5,61.6]	[20,20,20]
[A ₆]	[R,P,S]=[0.3,14.6,68.8]	[20,20,20]
[A ₇]	[L,P,S]=[2.79,25.97,60.9]	[20,18,15]
[A ₈]	[R,P,S]=[21.3,92.8,43.2]	[20,20,20]
[A ₉]	[L,P,S]=[27.4,25.63,8]	[20,20,20]
[A ₁₀]	[L,P,S]=[23.2,26.1,38.7]	[20,20,20]
[A ₁₁]	[R,P,S]=[4.1,13.3,45.1]	[29,20,27]

Table 2: Data set B. Illustration of the most relevant characteristics of the dynamic data set used for the second experimental setting. This data set is composed of NMR data collected from 3 patients using a total echo time (TE) equal to 35ms and a repetition time (TR) of 1500ms. Each data matrix B_i ($i = 1, 2, 3$) is composed approximately of 200 rows and 1068 columns. The data matrix B_2 corresponds to a patient who was diagnosed with a tumour. The rest of data correspond to healthy patients. The notation used for voxel location and the units used for the voxel size are identical to those used in table 1.

Data Set B TE = 35ms TR = 1500ms	Voxel Location	Voxel Size
[B ₁]	[L,A,S]=[19.4,14.8,96.3]	[16.5,17.7,17]
[B ₂]	[R,A,S]=[20.9,35.5,76.2]	[20,29,6,20]
[B ₃]	[L,A,S]=[30,16,64.7]	[20,20,20]

All the spectral data were generated and pre-processed using a spectroscopic and processing software package from GE Medical Systems (SAGE). This tool comes with a set of built-in functions (macro reconstruction operations) which provide different useful processing options of raw FID data. We used a macro reconstruction operation which provides internal water referencing, spectral apodization, zero filling, convolution filtering and Fourier transform operation on each of the acquired frames. However, it is important to note that the convolution filtering and water suppression options

were not selected. The result of this processing step is a data matrix where each column represents a temporal series spectrum of a specific metabolic signal and each row represents a sample or pattern from the brain region of interest. Each sample belongs to a space of 1068 dimensions corresponding to a chemical shift range of [-0.8, 4.3] ppm. As mentioned in section 2, this interval corresponds to the range where the main resonances concerning the 35 known metabolites involved in brain metabolism are located.

4.2 Experimental Results

The first experiment conducted was designed to check the variance of the measures corresponding to different healthy subjects. At this point, it is important to remember that both data sets described in the previous section are dynamic. In addition, the set of parametric measures introduced in section 3.2 were proposed in a supervised learning context. In this kind of machine learning paradigm knowledge about the problem is represented by means of input-output examples, specifically, examples in the form of vector of attribute values and known classes. This means that the samples of the data set must be rated as belonging to a predefined set of categories. In our case, the categories are defined according to the number of different subjects that compose the database. For data set A there are samples coming from eleven different individuals, therefore according to the proposed schema we have eleven different categories for the samples. Moreover, samples belonging to subject A_i are rated as belonging to the class C_i where $i = 1, 2, \dots, 11$. At this point, it is important to highlight the fact that we have chosen this categorization scheme for two reasons: firstly, as stated above, in order to check the performance of the proposed structural parameters and secondly, because of a lack of data from patients presenting disorders that could bias the results. Ideally, for diagnosis purposes we would have used just two categories for discriminating disease.

Table 3 (see the appendix for details), shows the results obtained after computing the dispersion for data set A after the categorization procedure described above. The first thing to note is that most of the dispersion values are below one, thereby indicating a high degree of overlapping between classes. These results would suggest that the absence of substantial differences from data collected from different patients and brain regions is a plausible indication of the existence of similar metabolic processes. It is important to emphasize that

metabolic processes associated to tumour cells are radically different when compared to those of the original non-transformed cell types.

However, it is important to note that the dispersion values associated with categories C_2 and C_{11} with respect to the rest of the categories (rows and columns A_2 and A_{11} of the data matrix) are slightly higher when compared with the rest of the elements of the matrix. Indeed, there are dispersion values which are close to unity or even slightly higher than unity. A careful analysis revealed that this effect was caused by the voxel size. The size of the voxel for the “x” and “z” dimensions (see table 1) is slightly bigger for categories C_2 and C_{11} with respect to the standard voxel size [20,20,20]. This is also true for dimensions “y” and “z” on the voxel associated with class C_7 . We observed that the effect is to some extent proportional to the discrepancy between the actual size and the standard voxel size. In order to further validate the results obtained with the dispersion matrix we computed the Fisher criterion obtaining a value of 0.8504 which confirmed the expected overlapping between classes.

In addition, following a similar procedure we computed the confusion matrix associated with the eleven categories composing data set A. Table 4 (see the appendix for details) shows the best confusion matrix (see section 3.3) obtained by the KNN classifier following a leave-one-out statistical cross-validation procedure. It is important to note that the estimations of conditional probabilities between classes shown in the table are multiplied by a factor of 100 to get percentage values. Therefore, it is easy to deduce that there is no apparent confusion between categories as most of the values are zero or close to zero. Nevertheless, samples belonging to class C_6 are apparently the most difficult to classify. Generally speaking, a high degree of overlapping given by the dispersion does not necessarily mean significant confusion between the classes from a classification point of view. This is an indication of the existence of multi-modal or very elongated categories.

The second experiment conducted was designed to check the sensitivity of the structural parameters introduced in section 3.2 for detecting the existence of metabolic changes as a result of including data samples of a patient who was diagnosed with a tumour. In turn, this experimental setting also permitted to assess the influence of the parameters of the PRESS sequences used. To this end, we merged the two available data sets A and B (see section 4.1 for details) to create a unique database.

We followed the same categorization scheme explained before consisting of assigning as many categories as the number of patients, where data samples belonging to the same patient were assigned to the same category.

Let us denote the merged data set as A+B. It is important to remember that the samples associated with data set B were collected using a different parameterization sequence from that used for data set A. In particular, for data set B the echo time used was 35ms and the repetition time 1500 ms. The Fisher criterion computed for this data set led to a value of 0.8262 indicating overlapping between the defined categories.

Table 5 (see the appendix for details) shows the results of computing the dispersion matrix for the data set A+B. The first thing that can be gleaned from the table is that most of the values are below one, thereby indicating the existence of overlapping between classes from the dispersion point of view. Therefore, from a dispersion point of view there is not too much difference between data samples coming from the two different parameterizations, although this can be considered to some degree a logical result taking into account that the echo time of the two sequences are relatively close. Nevertheless, the samples associated with the class representing a disorder (i.e., a patient with a tumour) led to dispersion values much higher than for the rest of the values found in the table, even taking into account the voxel size effect. More specifically, they are very close or bigger than two (see column B_2 from table 5) indicating a dispersion caused by the existence of the disease. At this point, it is important to remember that the dispersion matrix is not symmetric. From a geometrical point of view, according to equations (6) and (10) the strong dispersion presented by the data samples representing a disorder (i.e., a tumour) with respect to the rest of samples indicated a reduced distance in average from these samples to the centroid of their category (i.e., category B_2). In addition, these results seem to indicate that classes from healthy patients are well separated from the class indicating a disease. Although not shown here, this was also confirmed by the confusion matrix. Specifically, from a classification point of view there is no apparent confusion between the category representing the patient with a tumour and the other categories.

Finally, despite our previous considerations concerning the amount of data, in order to deepen and further complement the previous results, we conducted an experiment consisting of using the

entire database $A+B$ but now defining only two categories C_0 and C_1 to indicate “health” and “disease” respectively. The categorization procedure is similar to the procedure described above. All the samples belonging to data matrix B_2 were rated as belonging to class C_1 , while the rest of the samples were rated as belonging to category C_0 . The results of the dispersion matrix and confusion matrix computation are shown in table 6. From the inspection of the table we appreciate that there is a slight confusion for the recognition of category C_1 (“disease”). Specifically, there is a certain probability that patterns belonging to the class “health” may be rated as belonging to the class “disease”, although this probability is small, and from a diagnosis point of view an error of this kind would be less serious when compared to the opposite case which is apparently inexistent.

To summarize, tumour cells exhibit radical genetic, biochemical and histological differences with respect to the original non-transformed cell types. We have shown that the fact of using the dynamical aspects of NMR data together with relatively simple structural measure like dispersion and Fisher criterion could substantially help the diagnosis procedure of the clinical investigator. Indeed, the aforementioned structural measures used in a non-supervised learning context have proven to be very sensitive not only to discrepancies on the specific parameterizations of the NMR measuring process (i.e., voxel size) but also to intrinsic anomalies presented by the NMR data as a result of metabolic changes in the brain tissue studied. At this point, it is important to remember that current clinical diagnosis procedures do not make use of the dynamical aspects of NMR-based data. Indeed, they use averaged data (i.e, mean value of the data matrix of tables 1 and 2). Hence, these results would invalidate the traditional view that disregards the dynamic aspects of MRS data as being devoid of information. This methodical reasoning had been also previously suggested in (China, 2011) where it was shown the information-richness associated to the temporal dynamics of NMR metabolic signals as a result of its chaotic nature.

Moreover, if the tumour size is relatively small when compared to the voxel size the fact of using averages could mask the presence of a tumour. Although further experiments must be carried out, for instance using a much larger amount of data, these preliminary results would suggest that the proposed structural measures for characterization of spectral data could be used for the development of non-invasive early tumour detection techniques. In

addition, these results would also provide a starting point for the application of more sophisticated machine learning techniques (Kolen and Kremer, 2001); (Schölkopf et al., 1999) to dynamic NMR spectroscopy data.

5 CONCLUSIONS

In this paper we have investigated the application of machine learning techniques to characterize magnetic resonance spectroscopy data. Throughout this paper we have focused explicitly on the characterization of dynamic brain MRS data. We have presented a formal description of the problems associated with MRS-based data in terms of its application context in the field of clinical diagnosis research. We have shown that the fact of using the dynamical aspects of NMR data together with relatively simple structural measures (e.g., dispersion, Fisher criterion etc) could substantially help the diagnosis procedure of the clinical investigator. Indeed, the aforementioned structural measures have proven to be very sensitive not only to discrepancies on the specific parameterizations of the NMR measuring process (e.g., voxel size) but also to intrinsic anomalies presented by the NMR data as a result of metabolic changes in the brain tissue studied.

Summarizing, traditional clinical diagnosis methods are characterized by working with averaged data; conversely, this work attempts to identify properties of the underlying dynamics using simple structural measures that were shown to be very sensitive to metabolic changes as those exhibited by tumour cells. The principal advantage of the proposed methodology is not only its simplicity but also its ability to cope with the high-dimensional characteristics of spectroscopy patterns which allowed us to extract the relevant information required for the detection and diagnosis of disease.

Moreover, the framework presented here opens the possibility not only of having a starting point for the use of more complex machine learning techniques but also for the development of reliable non-invasive diagnosis techniques using relatively small experimental data sizes. We hope to have provided sufficient motivation for further studies and applications as we believe it is a great challenge to adopt these methods and to apply them in the clinical research field.

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APPENDIX

Table 3: Illustration of the dispersion matrix computed for data set A when the categories (i.e., classes in a supervised learning context) of the data samples are defined according to the number of different subjects that compose the database. Specifically, samples belonging to subject A_i are rated as belonging to category C_i . Dispersion values close to or lower than one indicates a high degree of overlapping between the involved categories. Conversely, dispersion values bigger than one provide an indication that these categories are well separated.

	A_1	A_2	A_3	A_4	A_5	A_6	A_7	A_8	A_9	A_{10}	A_{11}
A_1	0	0.76	0.21	0.24	0.10	0.14	0.30	0.27	0.20	0.27	0.95
A_2	0.79	0	0.80	0.67	0.73	0.73	1.12	0.96	0.74	0.77	0.46
A_3	0.22	0.80	0	0.29	0.17	0.21	0.28	0.26	0.23	0.30	1.02
A_4	0.26	0.68	0.30	0	0.24	0.23	0.46	0.39	0.26	0.27	0.83
A_5	0.12	0.77	0.17	0.24	0	0.12	0.25	0.23	0.19	0.24	0.97
A_6	0.15	0.72	0.21	0.23	0.12	0	0.31	0.28	0.18	0.21	0.91
A_7	0.26	0.92	0.23	0.37	0.20	0.26	0	0.16	0.31	0.33	1.16
A_8	0.29	0.96	0.26	0.38	0.22	0.28	0.19	0	0.32	0.34	1.18
A_9	0.20	0.71	0.22	0.25	0.17	0.17	0.36	0.31	0	0.21	0.88
A_{10}	0.26	0.71	0.27	0.25	0.21	0.20	0.37	0.31	0.20	0	0.87
A_{11}	0.83	0.38	0.84	0.68	0.76	0.76	1.17	0.98	0.76	0.79	0

Table 4: Best confusion matrix obtained by the KNN classifier computed for the data set A with a Leave One Out statistical cross-validation method when the categories of the data samples are defined according to the procedure described in table 3. The values shown in the table corresponding to the estimation of conditional probabilities were multiplied by a factor of 100 to get percentage values. These results show that there is no apparent confusion between the defined categories.

	A_1	A_2	A_3	A_4	A_5	A_6	A_7	A_8	A_9	A_{10}	A_{11}
A_1	100	0	0	0	0	0	0	0	0	0	0
A_2	0	99.45	0	0	0	0	0	0	0	0	0.54
A_3	0	0	100	0	0	0	0	0	0	0	0
A_4	0.52	0	0	98.94	0	0	0	0	0.52	0	0
A_5	8.42	0	0	0.52	91.05	0	0	0	0	0	0
A_6	14.73	0.52	0.52	1.05	1.57	79.47	0	0	1.05	1.05	0
A_7	0	0	0	0	0	0	100	0	0	0	0
A_8	0	0	0	0	0	0	1.57	98.42	0	0	0
A_9	0	0	0	0	0	0	0	0	100	0	0
A_{10}	0	0	0	0	0	0	0.52	0	0	99.47	0
A_{11}	0	0	0	0	0	0	0	0	0	0	100

Table 5: Dispersion matrix obtained when merging dynamic data sets A and B, both corresponding to short-TE NMR single voxel brain spectroscopy. Most of the values are close to or lower than one indicating that categories involved are overlapped. Nevertheless, the column associated to category B_2 presents a strong dispersion with respect to the rest of categories. The sensitivity of the dispersion for this category is due to the fact that data samples corresponding to category B_2 correspond to brain tissue that exhibited strong metabolic changes because of the tumour cells.

	A_1	A_2	A_3	A_4	A_5	A_6	A_7	A_8	A_9	A_{10}	A_{11}	B_1	B_2	B_3
A_1	0	0.75	0.21	0.24	0.10	0.15	0.30	0.27	0.20	0.26	0.93	0.45	2.24	0.20
A_2	0.79	0	0.79	0.66	0.72	0.72	1.11	0.96	0.74	0.77	0.46	1.32	3.14	0.88
A_3	0.22	0.79	0	0.29	0.17	0.22	0.28	0.27	0.23	0.30	1.00	0.42	2.37	0.23
A_4	0.26	0.67	0.30	0	0.23	0.24	0.45	0.39	0.26	0.27	0.82	0.60	2.08	0.29
A_5	0.12	0.76	0.18	0.24	0	0.12	0.25	0.23	0.19	0.24	0.95	0.41	2.22	0.18
A_6	0.15	0.71	0.21	0.23	0.12	0	0.31	0.28	0.18	0.21	0.89	0.47	2.05	0.21
A_7	0.26	0.91	0.23	0.37	0.19	0.26	0	0.16	0.31	0.32	1.14	0.23	2.47	0.23
A_8	0.29	0.95	0.26	0.38	0.22	0.28	0.19	0	0.32	0.33	1.16	0.20	2.39	0.26
A_9	0.20	0.71	0.22	0.25	0.17	0.17	0.35	0.31	0	0.21	0.86	0.51	2.05	0.28
A_{10}	0.25	0.70	0.27	0.25	0.20	0.20	0.36	0.31	0.20	0	0.86	0.51	1.67	0.29
A_{11}	0.81	0.38	0.83	0.67	0.75	0.76	1.15	0.98	0.75	0.79	0	1.35	2.89	0.93
B_1	0.38	1.06	0.33	0.48	0.31	0.38	0.23	0.16	0.42	0.45	1.30	0	2.74	0.34
B_2	0.58	0.77	0.58	0.50	0.51	0.51	0.74	0.60	0.53	0.45	0.85	0.84	0	0.62
B_3	0.19	0.81	0.21	0.26	0.15	0.20	0.26	0.24	0.27	0.29	1.02	0.38	2.33	0

Table 6: Dispersion and confusion matrixes after merging dynamic data sets A and B and considering only two categories of samples in the input space: “health” and “disease” respectively. In particular, samples belonging to healthy patients are rated as belonging to category C_0 (“health”) and the rest of samples (i.e., samples belonging to data matrix B_2) are rated as belonging to category C_1 (“disease”). Once again the dispersion is sensitive to the resulting metabolic differences presented by the brain tissue. From a classification point of view there is no apparent confusion between both categories.

Dispersion Matrix	C_0	C_1
C_0	0	1.9655
C_1	0.1249	0
Confusion Matrix	C_0	C_1
C_0	95.2721	0
C_1	4.7279	100

