

Supporting Strategic Planning with Interactive Visualization

A Case Study of Patient Flow through a Large Hospital

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Abstract: Hospitals collect large amounts of data during their daily operation. Next to its immediate primary purpose, this data also contains implicit information that can be used to improve clinical and administrative processes. We present a case study of how strategic infrastructure planning can be supported by the analysis of enriched patient flow through a hospital. Data from various hospital information systems was collected, enriched with topographical and organizational data, and integrated into a coherent data store. Common analysis tools and methods do not support exploration and sense-making well for such large and complex problems. We therefore developed a highly interactive visual analytics application that offers various views onto the data, and provides fast access to details in order to show them in context. The analysts were able to validate their experiences, confirm hypotheses and generate new insights. As a result, several sub-systems of clinics were identified that will play a central role on the future hospital campus. This approach was successful enough that we envision to extend it towards other process optimization tasks in hospitals.

1 INTRODUCTION

Adoption of information technology in health care has been slow (Jha et al., 2009), (American Hospital Association, 2007), but increasingly health care institutions such as hospitals collect and manage large amounts of data. Next to its eventual use in supporting clinical care, the data is also largely used for administrative purposes such as billing, scheduling, or resource planning (Chaudhry et al., 2006). While there are commercial hospital information systems that perform the core of the data management, there are typically many additional independent systems that are designed to support a specific medical procedure, with a unique patient id often being the only link between them.

For typical strategic planning tasks, this setup allows to answer questions such as how many patients were treated in the cardiology department last year. More complex questions require queries across several of the systems and along different dimensions: Which departments have many transfers between each other? Are there unusual transfers into other departments that deviate from this trend, and how are the involved patients characterized? Is this effect seasonal? If the data is enriched even more, for

example with external data like geographic location of departments, weather conditions, etc. then further investigations become feasible (Alapont et al., 2005).

Even if all the data is available for answering such questions, it is typically large, distributed and only weakly related. Standard tools for analysis of such data sets are limited, and new approaches are needed (Cuzzocrea et al., 2011). These characteristics and the related technology and issues have become known as big data. Definitions of big data vary (Laney, 2001), (Zikopoulos and Eaton, 2011) but data from hospital information systems often share many of these aspects. (Van der Aalst, 2012) argues that X-raying business processes in this huge amount of data, through the application of clever mining algorithms, can be used to gain valuable insights for future strategic planning of organizations.

In this paper, we present a case study where we collected, combined, and enriched data from a large university hospital, and used interactive visualization to access, analyze, and interpret the data to support strategic infrastructure planning.

Hospital sites are developed in an evolutionary manner over a long time span. This leads to physical and organizational layouts of the facilities that are usually not optimal anymore after a certain while.

Strategic planning with time horizons of 25 years and more provides the opportunity to correct this degeneration, and optimize the layout when the campus is enlarged, new facilities are built, or old ones replaced.

The optimal configuration of departments, their organizational units and technical facilities is not always evident. Questions such as “where should the emergency department be placed, and if we locate it in a new building, do we need an additional radiology facility?” should be answered based on evidence and insights rather than intuition, subjective opinions, or obsolete experience. The idea therefore was to use past real data to identify existing clusters of organizational units that are related based on what they actually do, and not on where they are placed in the organization chart. With these insights, it should be possible to define future sub-systems of organizational units and medical functions, optimized for efficiency. These new sub-systems can then be characterized again with the past data for further analysis and communication to stakeholders.

In this case study we built such a system based on the following hypotheses:

- The core questions that arise in strategic planning of hospital infrastructure can be answered by using the flow of patients between organizational units as core data, and enriching it with additional data about cost and performance of medical procedures
- The nature of the problem requires an exploratory approach, since the novel combination and representation of the data will likely lead to the emergence of new insights and hypotheses.

In the following, we present our approach that consists of two parts:

- Aggregate as much data from the various hospital information systems as possible, and make it available in a flexible format
- Provide highly interactive access to and visualization of this information to support exploration and interpretation

2 METHODS

2.1 Data Aggregation

Large hospitals, and in particular university hospitals, typically have a heterogeneous IT-infrastructure due to the fact, that the different clinics are rather autonomous and have different needs for the type of data to store. Often data of one clinic (i.e., orthopedics) is

stored in a specific IT system only used by that specific clinic. To cover specific needs for research, clinics often develop their own applications that are used to store additional research related information. Usually this data can be linked to the patient’s electronic health record by using the patient id or the case id as key, but otherwise data integration is complicated further and indirect clues must be found.

The design of our data store was heavily influenced by the two central dimensions of future queries:

Multi-scale: Case data has to be aggregated into several layers to allow drill-down from the hospital level (e.g., number of patient-days per year) to specific organizational units (e.g., is there a seasonal pattern in patients visits to the pneumology clinic?), and to individual patient cases (e.g., chronology of visits to the radiology department for one specific case).

Multi-aspect: The system shall be able to view the data from different aspects, ranging from the linear temporal view (e.g., chronological view of all events in a patient case), to a two-dimensional geographic map (e.g., where should the radiology department be placed on a campus to minimize travel distances for patients?), to the network topology of relationships between organizational units (e.g., which units transfer the most patient between each other).

In our project, information from several sources was used and linked:

- Inter-organizational transfer histories of stationary patients.
- Case attributes (e.g., diagnosis, treatment, diagnosis related group (DRG)) of stationary cases.
- Times of surgeries (timestamps at the cut and at the end of suturing).
- Transfers to ambulatory facilities (i.e., radiology department).
- Hierarchical organization of the hospital.
- Physical layout of the organizational units of the hospital.

While cleaning and integrating the data, we faced the typical problems that arise during data wrangling (Kandel et al., 2011), confounded by the privacy issues inherent in medical data.

The input data was gathered from numerous CSV formatted database table exports. No input files contained personal information about the patients, and the exports were performed by the hospitals IT staff to ensure patient privacy. No live connection was established to the hospital IT infrastructure. In the data

aggregation step, the data from the different systems and queries were interwoven, mostly by taking the patient id or the case id as a key. Many precautions, filtering and post-processing steps were taken to enrich the data and at the same time to ensure, that the resulting data was consistent (i.e., post-surgical transfers from one clinic to another had to be suppressed in a few specific cases where, although the transfer was present in the input data, in the real world none took place). The output of the data aggregation step consists of a few files in human readable CSV format. As a side effect, we were able to use simple text manipulation tools (e.g., sed, sort, grep, and python scripts) to filter and generate subsets of the enriched data, which was in turn used by the hospital to perform plausibility checks on their data.

Overall, we collected one full year of data from 40 clinics comprising 300 organizational units that treated 40000 cases from 30000 stationery patients, with 320000 transfers between the organizational units.

Standard transactional databases do not typically offer the high data access performance and the versatile data types that highly interactive multi-view visualization applications require (Keim et al., 2010). We therefore build up a dedicated optimized and interlinked in-memory data structure that is created on start-up of the analytics application. This approach leads to a slightly prolonged start-up time, but enables the implementation of the fast and highly responsive user interface described in the next section.

The data aggregation process is shown in Figure 1.

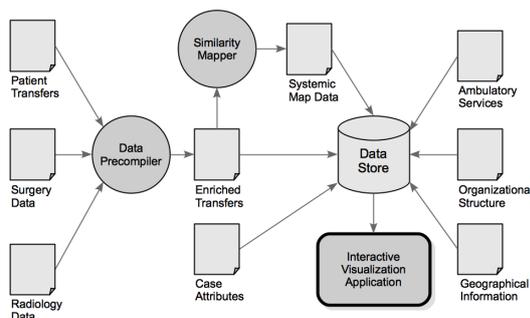


Figure 1: In the data aggregation step information from several sources is enriched and integrated.

2.2 Visual Analytics

With all the data integrated and available, the next challenge was to render it usable for the planning experts. The amount and complexity of the data made it impractical to use common analysis tools such as spreadsheets and standard methods from statistics with static graphs. For the type of problems found

in our case study, analysts often only have vague notions of what they are looking for (“I know it when I see it”). It is therefore crucial to make the data visible from various angles, and to provide highly interactive tools to identify interesting patterns and access details in context. Visual Analytics is a set of methods and technologies from a field defined as the formation of abstract visual metaphors in combination with human interaction that enables detection of the expected and discovery of the unexpected within massive, dynamically changing information spaces (Wong and Thomas, 2004).

Based on this approach, we developed a visual analytics application to support analysts in making sense of the collected data. The application offers four principal views (Figure 2):

- **Organizational:** shows the organizational structure and how the actual medical activities shape the administrative space.
- **Systemic:** reveals the operational structure as it emerges from patients flowing through the hospital.
- **Topographical:** shows the actual physical situation as a structure that evolved through many individual decisions.
- **Chronological:** adds the dynamic view on how events and quantities change over time.

2.2.1 Organizational View

The organizational view ((Figure 2), top left) uses a circular layout to arrange all the major clinics of the hospital. Circular layouts have proven effective to show genetic sequences and relationships between genomic positions (Krzywinski et al., 2009). We adapted this technique to show the flow of patients in relation to the organizational structure of the hospital.

The outer circle shows how many patients enter (blue bars) or exit (red bars) a clinic from outside of the hospital. The inner circle represents the size of the clinic, as measured by the number of individual cases that passes through that clinic, mapped to the thickness of the black bar. The combined bidirectional flow of patients between two clinics is shown as a curved line, whose thickness is proportional to the number of transfers. The lines are drawn semi-transparent to mitigate occlusion problems. The order of the clinics around the circle can be adapted (by department, size, alphabet, etc.) to the current question.

To reveal further information we follow the principle of detail on demand (Shneiderman, 1996). If a clinic is probed (hover with the mouse cursor) then

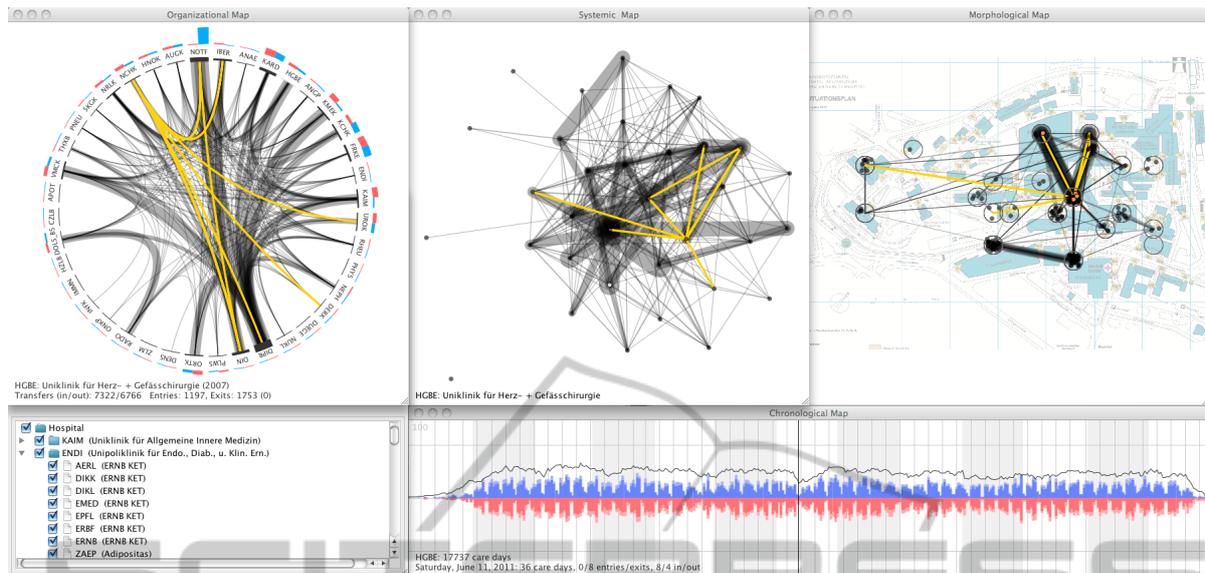


Figure 2: The principal views of the visual analytics application: organizational, systemic, topographic (top row), and chronological (bottom right). All views are coordinated through brushing and linking to support exploration. Filters (bottom left) can be used to limit the display to certain organizational units. The yellow lines represent the trajectory of a single case treated for abdominal metastasis during a four week stay at the hospital.

all the incoming or outgoing transfers from that clinic are overlaid (Figure 5). If a clinic is selected then only the transfers to and from that clinic are shown and all the others suppressed (Figure 6). Probing now shows quantitative information about the number of transfers from the selected clinic to the probed one.

2.2.2 Systemic View

The movement of patients between clinics effectively creates a network of relationships, where clinics that move more patients between them are closer, or more similar, than clinics with fewer or no transfers.

To make this network visible we employ a multidimensional scaling algorithm. Multidimensional scaling is a family of methods that turns information about the similarity of objects into geometric positions in such a way that, as best as possible, similar objects are close together and dissimilar ones far apart. It is particularly well suited for our data because it is able to reproduce non-linear high-dimensional structures in a lower-dimensional (i.e., two-dimensional) geometric representation (i.e., points on a plane).

Our algorithm is implemented as a spring-mass model where the clinics are modeled as masses that are connected pairwise with springs whose resting length is proportional to the strength of the relationship between the clinics.

Starting with a random layout, the positions adapt with each iteration and settle into a (hopefully global)

minimum. The algorithm uses several optimizations to avoid local minima and improve subjective layout quality, and was inspired by (Chalmers, 1996).

Once the positions of the clinics on what we now call the systemic view are determined, the transfers are represented analogous to the organizational view in order to emphasize their complementary aspect (Figure 2, top center).

2.2.3 Topographical View

The topographical view (Figure 2, top right) shows the patient transfers on a geographical representation of the current hospital campus. The clinics can not be represented as single units like in the other views, since the various organizational sub-units of a clinic are not typically located in a single physical location. Distinct locations are therefore symbolized as circles and the organizational sub-units at this location are represented as filled dots within this circle. The layout within a circle is randomized and the dots drawn transparently. This visualization scales well with the greatly varying number of units at a single location.

2.2.4 Chronological View

The time-dependent behavior of the system is shown in the chronological view (Figure 2, bottom right). The in- and out-transfers for each day are shown as a mirrored stacked bar chart. The dark hues in the center close to the time axis show the transfers

from (blue, pointing up) and to (red, pointing down) other clinics, whereas the external entries and exits are stacked on top and shown in light hues. Internal and external transfers can also be shown separately depending on the question, and the mirroring makes it easy to spot imbalances between in- and out-flows.

The net flow for each day is cumulated and over-plotted as a black line. This essentially shows the number of patients that are present in a clinic on a particular day, which can be integrated to compute care days.

2.2.5 Interaction

All the views are coordinated through brushing and linking (Buja et al., 1991), meaning that an action in one view (e.g., probing, selection) is immediately reflected in all the other views. It has been shown that interfaces designed around multiple coordinated views are effective when users need access to details in addition to getting the overview (North and Shneiderman, 2000). They bring benefits of improved user performance, discovery of unforeseen relationships, and integration by interaction in addition to integration by visual design (Shneiderman, 1996).

In order to rationalize and interpret the insights and hypotheses generated with the four principal views, it is necessary to drill-down to the level of individual cases. Cases can be filtered either by organizational unit that they have visited on their journey through the hospital, or by various categorical or numerical case attributes (e.g., destination after discharge, diagnosis, length of stay). When a case is selected from the list of filtered results, its details are shown both as a table of transfers, as well as a visualization of the whole case history (Figure 3), showing admission, surgeries, radiology procedures, ambulatory visits, and transfers between organizational units (vertical axis) on a time-line (horizontal axis). At the same time, the transfers of the selected case are highlighted (yellow) in the main views (Figure 2).

In a separate view it is also possible to show all the filtered cases at the same time. In order to display several hundred case histories in parallel, their representation is condensed to a single line that is only one pixel high, but still preserves the essential information about the case history. Figure 4 shows all the cases that were classified under the DRG “craniotomy with complex procedure”. Lengths of stays vary from 2 to 30 days, with the catalog average defined at 10.1 days. A large number of cases follow the same pattern (surgery on the second day and a transfer on the third), but deviations from this pattern can easily be spotted and further investigated.

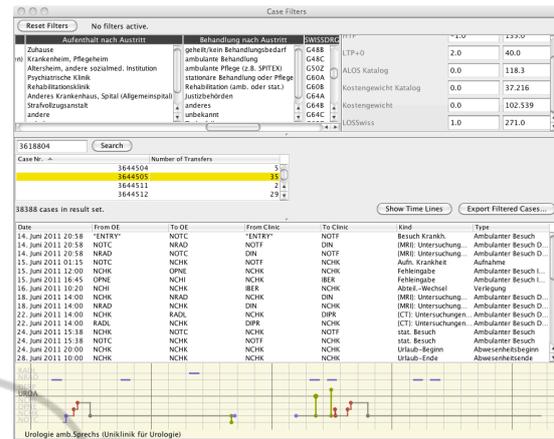


Figure 3: Cases can be filtered by various attributes (top). Individual cases in the filter result can be examined in detail in a table that lists each single transfer (center), or in a visualization of the whole case history (bottom).

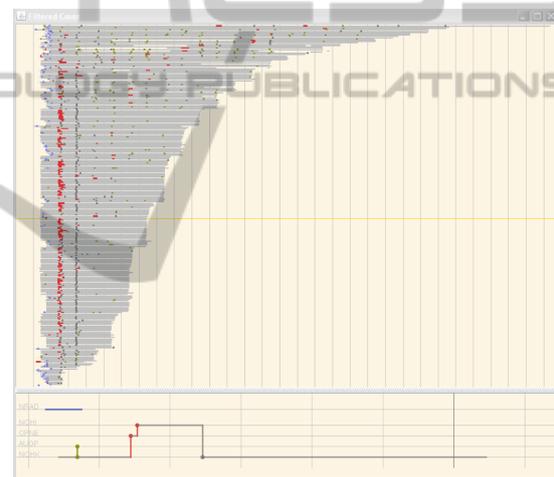


Figure 4: All the filtered cases can be displayed in parallel to find patterns of similarity, or outliers. Case histories are condensed to a single line representation. This image shows the variation in procedures and duration of all cases for a particular DRG, in this example “craniotomy”.

3 RESULTS

The organizational view (Figure 2, top left) shows the overview of how patients flow through the hospital, and serves as the starting point for analysis. The outer ring shows that by far the most patients enter (blue bars) the hospital through the emergency department (NOTF), followed by gynecology (FRKE), pediatric surgery (KCHK), and cardiology (KARD). The clinic for pediatric surgery has a negative balance for entries/exits (red bars) which means that like in the emergency department, patients enter the hos-

pital through this unit but then get transferred into other units. The opposite is the case for the children’s clinic, suggesting a typical path for pediatric patients. This is indeed the case, since the clinic for pediatric surgery also operates an emergency room for children, which accounts for most of these transfers. Another feature that pops out is that while the clinic for gynecology has many external entries and exits, it has very few internal transfers. This is due to most of the women giving birth without further complications.

Looking at the transfers on the inside of the circle, it becomes obvious that the institute for diagnostic, interventional and pediatric radiology (DIPR) plays an important role. Highlighting all the transfers that go out of DIPR (Figure 5) shows that it is a service center for many of the hospital’s clinics.

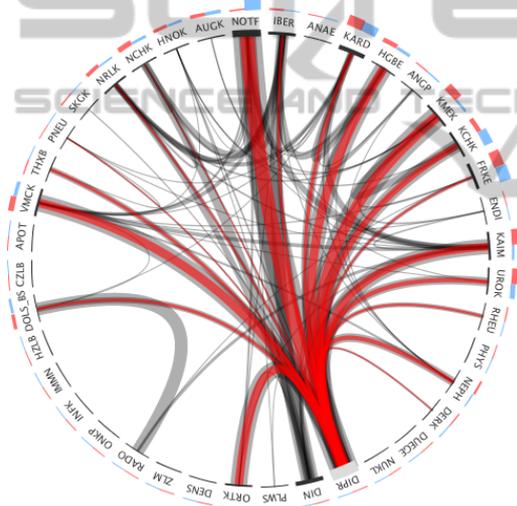


Figure 5: Incoming or outgoing (red) transfers can be highlighted to reveal relationships between clinics. The radiology department (DIPR) plays the role of a service center and is highly connected to the other clinics.

Further examination shows a less pronounced but similar pattern for the cardiology clinic (Figure 6). About 17% of its transfers are from and to the clinic for internal medicine (KAIM) and about the same for the clinics of cardiovascular surgery (HGBE), and neurology (NRLK).

The topographical view in Figure 7 with the cardiology clinic highlighted shows that its sub-units are spread across the whole campus in three different locations, which gives rise to further questions (e.g., level-of detail for analysis).

The systemic view reveals a number of interesting features of the way that the clinics are related based on the actual flow of patients. In Figure 8 we can

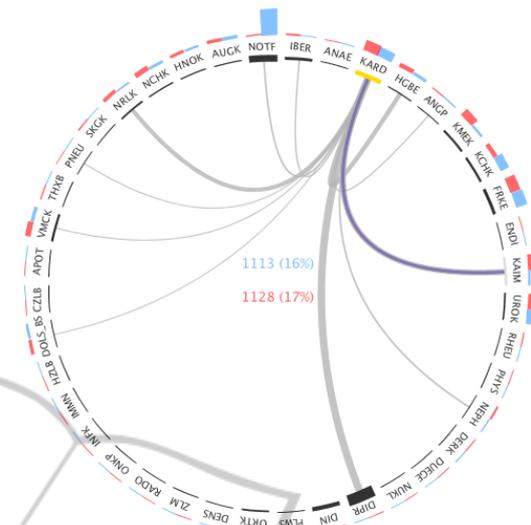


Figure 6: Limiting the view to only transfers that go in or out of one specific organizational unit show that the cardiology clinic (KARD) is also exhibiting a service center characteristic.

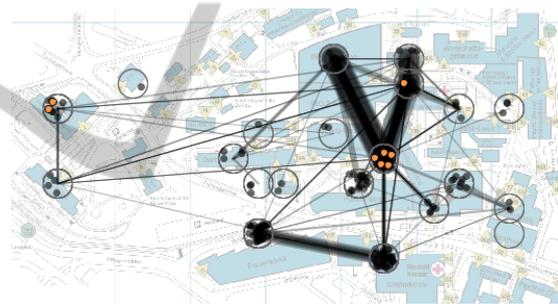


Figure 7: The organizational sub-units of the cardiology clinic are spread across the hospital campus in three different locations.

see a dense core of highly related clinics in the center, surrounded by a ring of clinics with a less central role, and finally followed by a number of clinics that are very peripheral (e.g., clinics of hematology, osteoporosis, oncology, infectiology).

Analysis of the logarithmic histogram of transfer counts showed distinct transitions at thresholds of 300 and 1000 transfers. Figure 9 shows how these thresholds partition the map into three areas. The institute for diagnostic, interventional and pediatric radiology DIPR (highlighted in blue) again plays a central role and sits at the center of the hospital system.

If we limit the view to clinics that have at least 1000 transfers with any of the other clinics, four groups emerge (Figure 10). At the core we have the emergency department (intersection between groups A and B). Group A encompasses the radiology at the center, and clinics such as cardiology, abdomi-

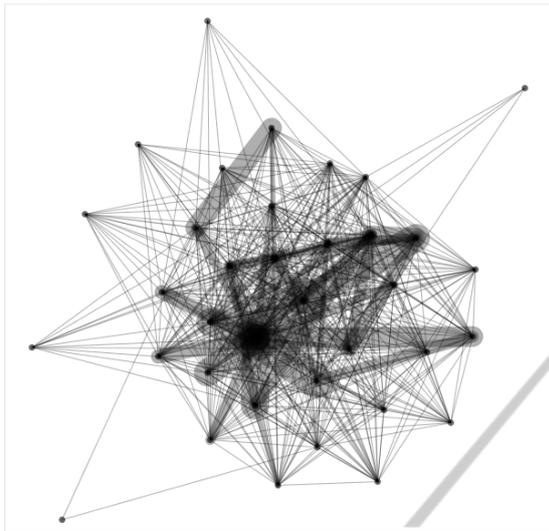


Figure 8: The systemic view shows a core of highly connected clinics surrounded by six clinics that only play a peripheral role.

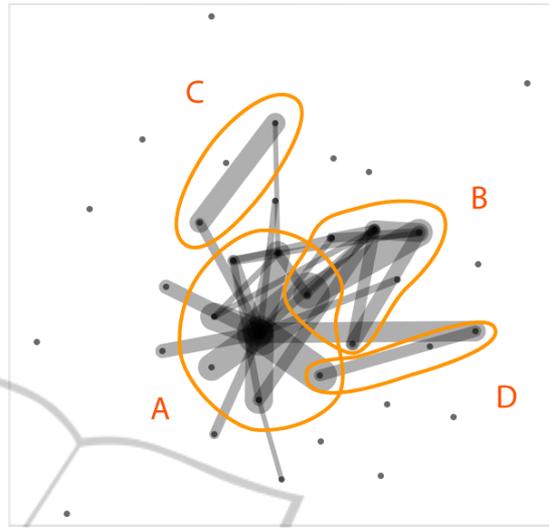


Figure 10: These clinics make up the core of the hospital system, as measured by the number of patients that they exchange (<1000 per clinic per year). Four groups can be distinguished and serve as the basis for defining sub-systems that are central to the future hospital infrastructure.

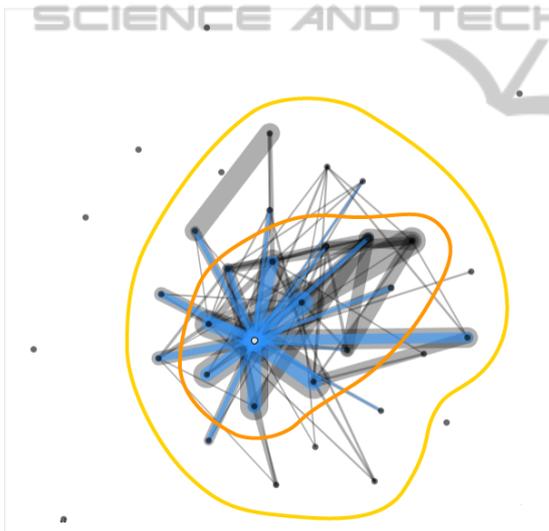


Figure 9: We found two distinct thresholds at 300 and 1000 transfers per clinic that partition the map into three areas. The radiology department (blue) sits at the very center of the system.

nal medicine, orthopedic surgery, or internal medicine surrounding it. Group B also connects to the emergency department, but groups around clinics such as neuroradiology, intensive medicine, neurology, neurosurgery, or immunology and allergology. Groups C (radio-oncology and oncology wards) and D (children's clinic and pediatric surgery) are somewhat separate and less central.

The chronological view provides a view of the patient flow across time. Looking at the whole hospital (Figure 11, top), it can be seen that the number of pa-

tients who stay at the hospital is quite constant (black line), with only minimal seasonal effects. The oscillation pattern is due to the fact, that surgeries tend to take place at the beginning of the week (peaks) and patient discharge takes place preferentially before the weekend (lows).

If we look at the emergency department shown in Figure 11 (bottom left), we can see that only a small number of patients stay at this department for a long time (black line) but there are a lot of patients entering directly from outside the hospital (light blue bars) and are transferred to other clinics within the hospital (dark red bars).

Figure 11 (bottom right) shows the radiology department. The black line stays at zero because no patients stay overnight in this clinic. This department adds to the weekly pattern found in the overall hospital view, since planned interventions are not performed during the weekend.

4 DISCUSSION

The application was developed in an incremental way. Starting with tables and simple views, diagrams were refined, new views added, and interactive functionality increased. With each iteration, the understanding of the relationships in the hospital system was deepened, and the potential for optimizations identified.

In their daily work, people develop an intuition for the relations in a system. The view of the observers

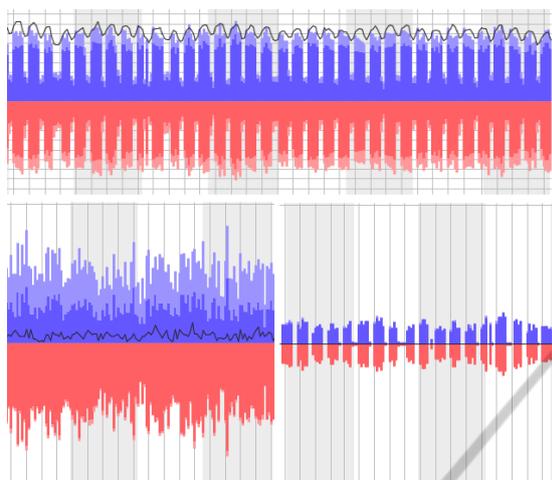


Figure 11: Extracts from the chronological view. The patient flow for the overall hospital (top) shows a weekly pattern but no seasonal variations. The flow in (blue) and out (red) of the emergency department (bottom left) shows no chronological pattern. About two thirds of the patients enter from outside (light hues) but most of them get transferred to other clinics (dark hues). Few patients stay overnight (black line). No patients stay at the radiology department (bottom right) and nothing happens there on weekends. Gridlines denote weeks, with months shown as alternating shaded backgrounds.

however is often limited to their sphere of action. The dependencies on the next or next-to-next source of influence are not taken into account sufficiently. Our analysis with this application however allowed us to gain an overview of the big picture of the hospital system. The details were validated by experiences of specific experts, but we also gained new insights that went beyond particular knowledge.

By making the flow of patients visible, we were able to contrast the hierarchical organizational structure with the actual implemented working relationships. This showed the difference between the operational structures that developed through medical consequences, and the theoretically defined organizational structure. Based on this difference, we were able to describe new sub-systems and identify an organizational form that corresponds to the current actual needs.

It was not really a surprise for instance, that the core functions of a hospital such as emergency department, operating rooms, and diagnostic functions appeared in the center of the system, but it was not expected to be so pronounced. A new insight was the role of the cardiology clinic as an important service center for diagnostics. This led to the decision to also assign it a central role on the campus. Also new was the interpretation of the role of the clinic for in-

ternal medicine as being primarily a receiving station for the emergency room, with the further distribution into the specialized clinics taking place only one or two days later.

In summary, we confirmed our two hypotheses, namely that enriched patient flow data reveals interesting insights into various aspects of a hospital, and that an exploratory approach to analytics, enabled by interactive visualization, leads to insights that can not be gained with standard or automated statistical methods.

5 FUTURE WORK

The current application was primarily built to gain insights into the strategic planning of a new and evolving hospital campus (e.g., which clinics should be placed where to minimize the travel distances for patients and optimize logistics).

Since the application provides access to various aspects of a hospital, from high-level overview to individual treatments within a single case with just a few clicks, it also has large potential for controlling tasks and other purposes. We plan to enrich the data with further treatment cost and performance data, to support process analysis in the DRG-based management context that is currently introduced in our country. If successful, then one will need to investigate the possibility of a direct connection to the various hospital information systems in order to obtain real-time data without compromising the privacy issues.

Another direction of future work is to scale-up the system to support the planning and controlling of regional, jointly administered hospital clusters, by integrating data from several hospitals. Some of the algorithms and views can be directly scaled-up, but others will have to be adapted or developed specifically to address additional issues.

During the analysis and interpretation of the data, the need came up to find clusters of similar patient paths through the hospital. This opens interesting research questions about measures of similarity, and how to find the balance between automated mining and human-guided visual analysis.

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