

# Rings in the Gulf of Mexico and Stochastic Resonance

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**Abstract:** In this work, we used a nonlinear, reduced gravity model of the Gulf of Mexico to study the effect of a seasonal variation of the reduced gravity parameter on ring-shedding behaviour. When small amplitudes of the seasonal variation are used, the distributions of ring-shedding periods are bi-modal. When the amplitude of the seasonal variation is large enough, the ring-shedding events shift to a regime with a constant, yearly period. If the seasonal amplitude of the reduced gravity parameter is small but a noise term is included, then a yearly regime is obtained, suggesting that stochastic resonance could play a role in the ring-shedding process taking place in the Gulf of Mexico.

## 1 INTRODUCTION

Anticyclonic rings generated by meandering of intense boundary current systems are long-lived, intense near-surface features that dominate the oceanic mesoscale in different regions of the World Ocean. They substantially contribute to determine the water mass characteristics as well as the upper-ocean circulation patterns in these regions and, due to their characteristic self-induced, westward propagation, they often also play an important role in the transfer of chemical and biological properties across frontal zones (Olson, 1991). The large surface temperature anomalies as well as the large surface horizontal velocity shears associated with these rings may profoundly influence human activities. In the Gulf of Mexico (Fig. 1), for instance, the passage of “warm-core” rings detached from the Loop Current is able to disturb oil extraction activities, while it is demonstrated that hurricanes may be intensified by their interaction with the warm ring water (see Halliwell et al., 2011 and references therein).

Predicting the onset and evolution of ring shedding in the Gulf of Mexico (GOM) may substantially contribute to the understanding of the subtle dynamics involved in the local oceanic phenomena and also to the reduction of the impact on human activities caused, directly or indirectly, by these rings. Observations show a nearly bi-modal distribution (the most evident peaks existing around 6 months and 9 to 11 months). Current full-fledged ocean numerical models can explain some of the

observed ring-shedding variability but fail in simulating observed periods (Murphy et al., 1999); (UWelsh and Inoue, 2000); (Romanou et al., 2004).

Simple models, on the other hand are only able to reproduce an almost constant period (Hulbert and Thompson, 1980); (Sturges et al., 1993); (Oey et al., 2003), which was called the “natural” period of the Gulf by Hulbert and Thompson (10-11 months). In part, this deficiency of existing numerical model is undoubtedly the result of inaccuracies induced in the simulated dynamics by the imposed boundary conditions, which unavoidably, tend to introduce in the system an exaggeratedly strong yearly signal. The discrepancy between observations and simulations, however, may be used to gain a deeper understanding of the subtle dynamics governing the process of ring shedding in the Gulf of Mexico. In fact, it results that as the strength of the yearly signal imposed in realistic model simulations decreases, the occurrence of yearly, ring-shedding events also diminishes. This behaviour may indicate that, in numerical models, a synchronization mechanism exists, which is able to shift a “natural” ring-shedding period toward a yearly one.

Considering that the seasonal cycle of sea surface temperature (SST) in the Gulf of Mexico is a natural forcing on the wide spectrum of physical processes taking place there then emerges an attractive possibility: stochastic resonance. If the imposed forcing by the SST is strong enough to drive the system, we can expect that ring-shedding variability will contain spectral energy in the yearly

frequency, but this is not the case, or at least not most of the time. Now, if we include noise as a forcing mechanism, then we can expect that a weak signal in the forcing can be amplified and optimized by the assistance of noise (Gammaitoni et al., 2000). In other words: if in the Gulf of Mexico exists a weak, yearly signal in the forcing, which is not capable of inducing a yearly period in the ring-shedding process, this yearly forcing plus a noisy term could be able to produce ring-shedding events with a yearly period.

Our conjecture may be tested using simple numerical models. To this purpose, we implemented in the Gulf of Mexico a nonlinear, reduced-gravity model simulating an idealized Loop Current through the inflow/outflow of near-surface water through its boundaries (see Fig. 1). This is the simplest model capable of simulating ring shedding (Hurlburt and Thompson, 1980). In this study, it is proposed that a reduced gravity model, where the buoyancy term is seasonally forced and the dissipation term is varied, can explain the observed period of shedding behavior. Additionally, we explore the possibility of stochastic resonance in the ring-shedding process by including a noise term in the seasonally forced buoyancy term.

## 2 MODEL SIMULATIONS

A reduced gravity model (1.5 layers) is used to simulate the eddy-shedding process in the Gulf of Mexico and to study the influence of the seasonal cycle upon it. The upper-ocean temperature is assumed constant in space but varies in time. Thus, by using a linear thermodynamic equation for the density of the upper layer (to make sure that we are being consistent with the planetary geostrophic approximation) a reduced gravity parameter which evolves with the time is obtained.

The domain covers the GOM, the Caribbean Sea, and a portion of the Gulf Stream area in the North Atlantic (see Fig. 1). This choice allows the propagation of anomalies from the western Caribbean Sea through the Yucatan Channel and their possible effect on the ring-shedding process. On the other hand, the eastern open boundary is located sufficiently far from our region of primary interest, thus assuring that the adjustment taking place near the open boundary, and the unavoidable reflection of some waves, does not interfere significantly with the internal dynamics of the GOM.

In each model experiment, the equations are

integrated numerically for a period of 20 years using a forward Euler scheme and an Arakawa C grid for the active layer. All model experiments are performed using a time step of 90 seconds and a horizontal grid with 135 x 153 points and a spacing of 1/4 degree (see Fig. 1). In a first set of experiments, a constant reduced gravity parameter ( $g'$ ) is used. In the second set, a seasonally evolving  $g'$  parameter is considered. Finally, a noisy term is added to the seasonally evolving  $g'$  parameter.

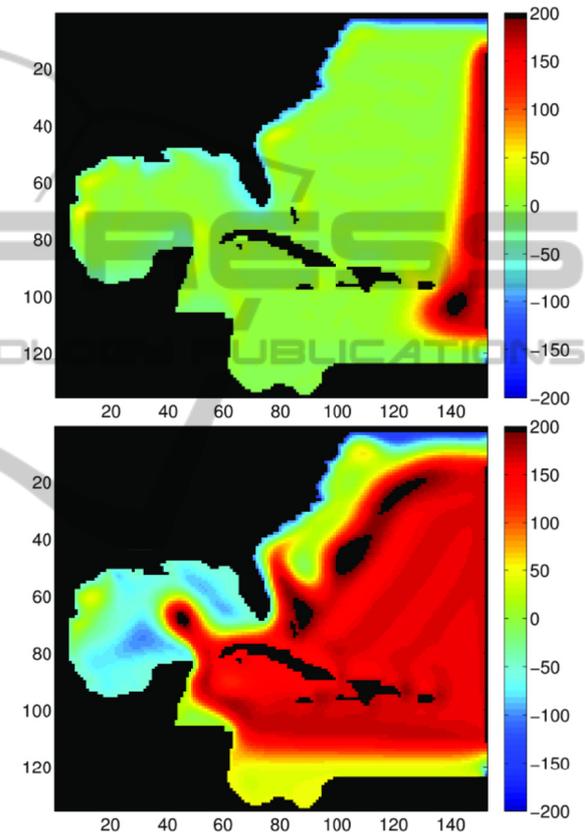


Figure 1: Domain used in our model simulations. There are two eastern open boundaries, which are forced by a flow induced by a meridional gradient of upper layer height. These input and output flows are time invariant. Upper panel: height anomalies at day 50. Lower panel: height anomalies at day 500.

## 3 RESULTS

Without seasonal forcing, a single peak in the ring shedding period is observed, which depends on model geometry, upper layer thickness, diffusion, and  $g'$  value (Fig. 2). A red dot in this figure and the following ones indicate the timing of the detachment of a ring of the Loop Current.

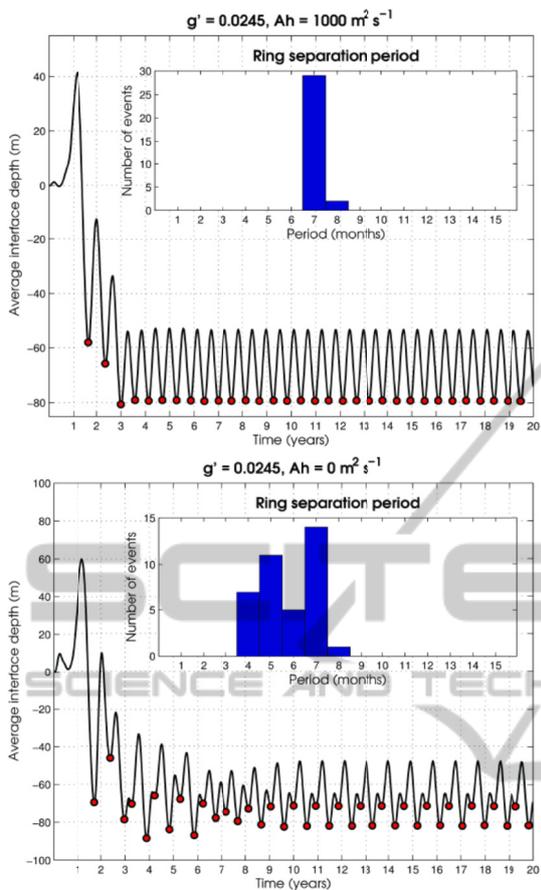


Figure 2: Histograms and time series of area-averaged height anomalies over the ring-shedding region used to estimate the timing of ring shedding events (red dots). By using a diffusion coefficient of  $1000 \text{ m}^2/\text{s}$ , a constant period of seven months is obtained (upper panel), while with zero diffusion period doubling is observed (lower panel).

When the amplitude of the variation of  $g'$  is increased, a more complex behaviour is observed, characterized by a bi-modal distribution, which crucially depends on the amplitude (Fig 4). When the amplitude is large enough, the annual signal clearly dominates, but when it is weaker different bi-modal distributions appear, some of which resemble the observed one.

In the case of large amplitude of the annual signal, a quite simple ring shedding behaviour emerges: constant, yearly ring-shedding events.

Now, we try to answer what happens when the annual signal is weak but high frequency forcing is present. This kind of forcing could be, for example, similar to that associated with turbulent heat fluxes between atmosphere and ocean. A simple way to simulate them is by using a noise term, which

represents heat exchange between the ocean surface and the lower atmosphere.

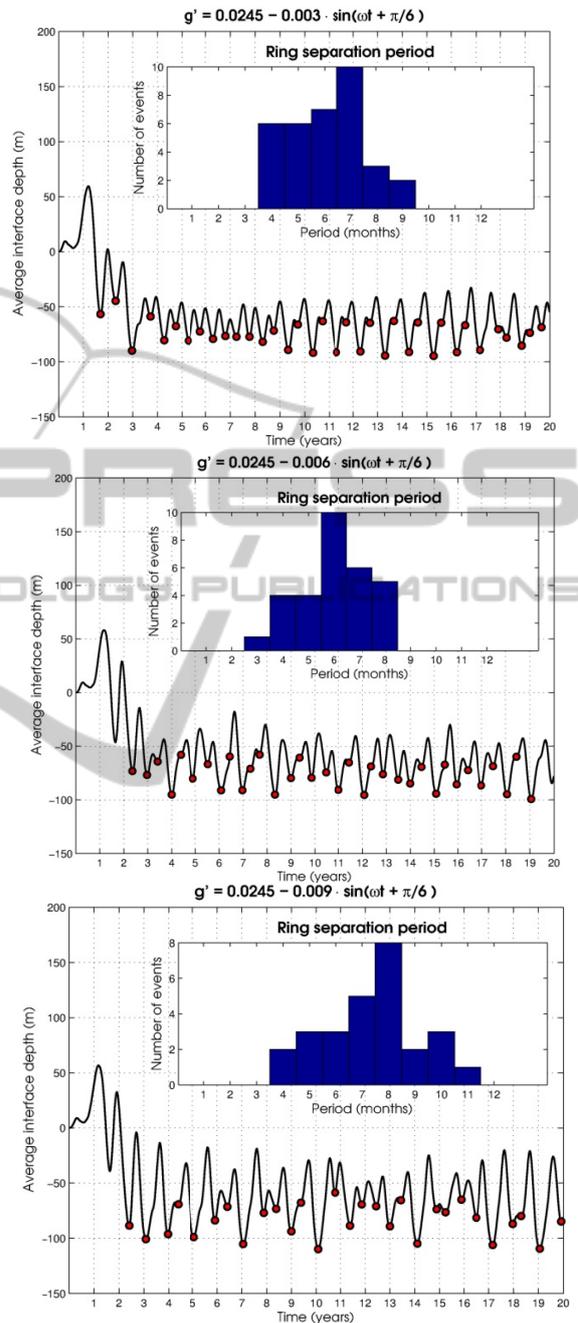


Figure 3: Ring-shedding distributions obtained when a seasonal variation in  $g'$  is included. The phase constant is used to obtain a seasonal variation of density in agreement with the seasonal cycle of SST in the central Gulf of Mexico. Zero diffusion is used.

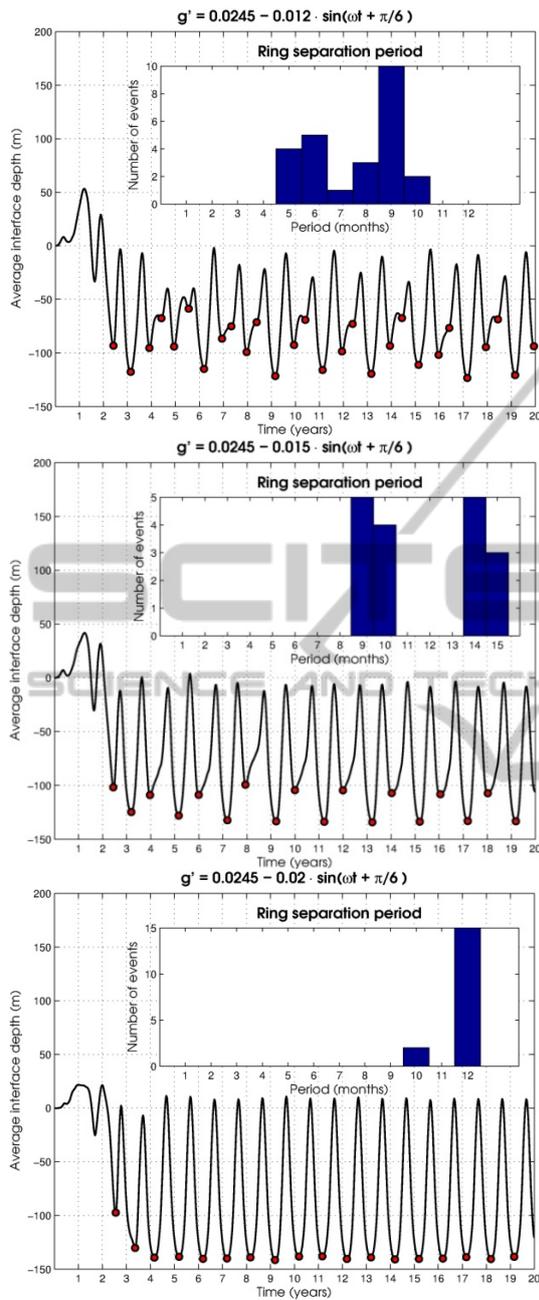


Figure 4: Similar to Fig 3, but with a larger amplitude for the seasonal variation of  $g'$ .

In this case, we used for the stochastic forcing a series of random numbers with zero mean and standard deviation of 0.015. Additionally, we explore the effect of noise magnitude on the ring-shedding process using a factor of two and three in the noise term (Fig. 5).

Fig. 6 shows the ring-shedding period distribution resulting of the seasonal variation of  $g'$ . The amplitude of the seasonal forcing is not able to

produce yearly ring shedding, because it is not large enough (upper panel). The inclusion of a small noise term modifies the distribution of ring-shedding periods but it is not able to induce ring-shedding events with a yearly period. If the noise amplitude is increased three times, then the noise term is able to change this behaviour, inducing a dominance of ring-shedding events with a period close to the yearly one.

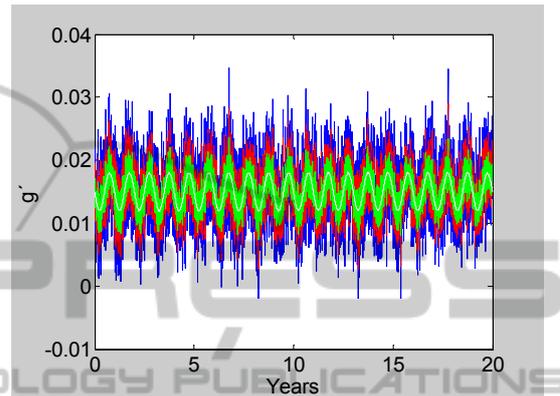


Figure 5: Stochastic forcing. The white curve represents the seasonal variation of  $g'$ . In the green curve, a noise term with zero mean and standard deviation of 0.015 is added. This forcing is multiplied by a factor 2 and 3 in the red and blue curves, respectively.

#### 4 CONCLUSIONS

In the case of constant  $g'$ , it is shown that large values of diffusion lead to ring-shedding events with a constant period of several months, while with zero diffusion the period is doubled.

By considering a seasonal variation of  $g'$ , a more realistic ring-shedding distribution is obtained, which is characterized by a bi-modal distribution that crucially depends on the amplitude. If the annual signal of  $g'$  has large amplitude, a quite simple ring shedding behaviour is observed: a constant, yearly ring-shedding event.

If the amplitude of  $g'$  is not large enough to induce yearly variability in the ring-shedding process, such behaviour can be obtained by including stochastic forcing with a proper intensity. Thus, it has been shown that stochastic resonance could play a role in the ring-shedding process taking place in the Gulf of Mexico.

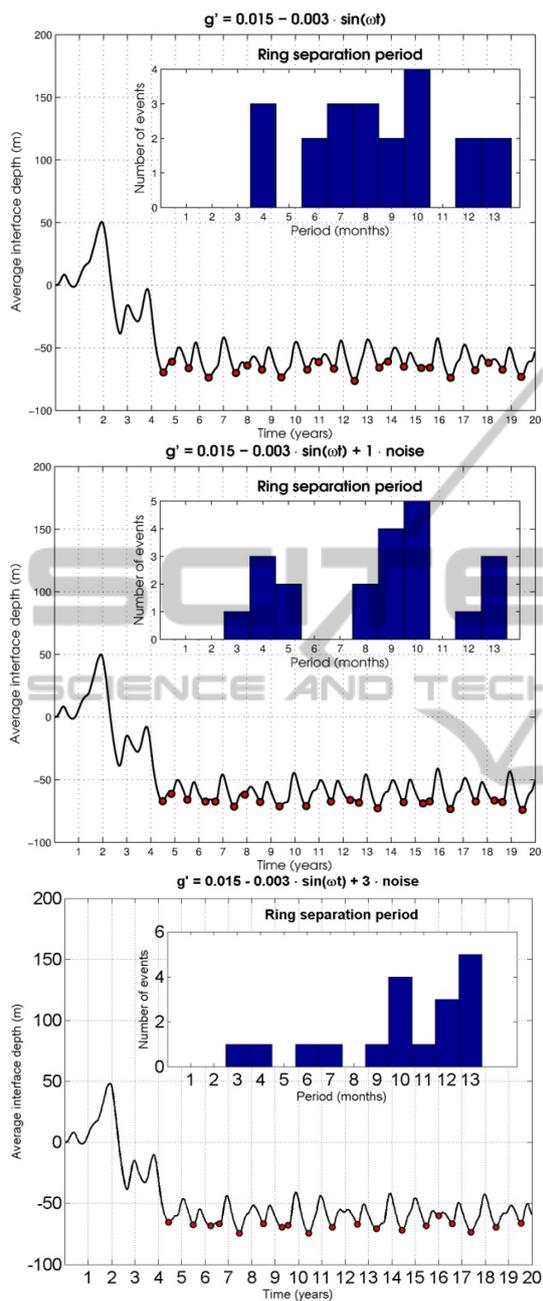


Figure 6: Ring-shedding period distributions using seasonal forcing (upper panel) and seasonal forcing plus noise. See the text for details.

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