

# Fuzzy Base Predictor Outputs as Conditional Selectors for Evolved Combined Prediction System

Athanasiros Tsakonas and Bogdan Gabrys

*Smart Technology Research Centre, Bournemouth University, Talbot Campus, Fern Barrow, Poole, BH12 5BB, U.K.*

**Keywords:** Ensemble Systems, Fuzzy Rule-based Systems, Function Approximation, Genetic Programming.

**Abstract:** In this paper, we attempt to incorporate trained base learners outputs as inputs to the antecedent parts in fuzzy rule-based construction of hybrid ensembles. To accomplish this we adopt a versatile framework for the production of ensemble systems that uses a grammar driven genetic programming to evolve combinations of multilayer perceptrons and support vector machines. We evaluate the proposed architecture using three real-world regression tasks and compare it with multi-level, hierarchical ensembles. The conducted preliminary experiments showed very interesting results indicating that given a large pool of base predictors to choose from, the outputs of some of them, when applied to fuzzy sets, can be used as selectors for building accurate ensembles from other more accurate and complementary members of the same base predictor pool.

## 1 INTRODUCTION

The popularity of ensemble systems in real-world tasks is a natural result of their effectiveness for a range of tasks, where single predictors or classifiers can overfit or provide weak solutions. A primary property in ensemble systems, contributing to their ability to generalize better is a combination of individual performances and diversity among individual learners (Brown et al., 2005). Recently, fuzzy approaches have been considered in order to combine learners within the ensemble framework. The fuzzy inference tries to model human perception when imprecision is encountered. As a result, the model often achieves equally good or better performance while at the same time maintaining human readability. There are many ways to incorporate fuzziness into computational intelligence models including evolutionary, neural and heuristic ones. The evolutionary fuzzy models have some additional desirable properties, such as handling multi-objective constraints (Ishibuchi, 2007), or implicit diversity promoting, which is desirable in ensemble building (Brown et al., 2005).

Various evolutionary training schemes have been proposed, both at the learner level and at the combinations. Evolutionary training of learners is demonstrated in (Chandra and Yao, 2004), where neural networks are trained using evolutionary algorithms, focusing on maintaining diversity among the learner po-

ol. Training by evolutionary means at the combiner level is shown in the GRADIENT model (Tsakonas and Gabrys, 2012) for generating multi-level, multi-component ensembles, using grammar driven genetic programming. GRADIENT incorporates, among others, multilayer perceptrons and support vector machines, and its performance is successfully compared with other state-of-the-art algorithms. The main advantage of the aforementioned model is the versatility provided by its architecture which incorporates a context-free grammar for the description of complex hierarchical ensemble structures. Multi-component, hybrid ensemble systems are most commonly built utilising independent training phases between the individual learners and their combinations. Building a simple combination of trained learners does not require access to the training data for the combination to be performed as only outputs of the base predictors are required. When a fuzzy rule-based system is trained, the rule antecedents make use of the data attributes. Consequently, a fuzzy rule-based system that combines learners is expected to make use of the data attributes in its antecedents which would lead to a divide and conquer strategy, as it was illustrated in one of our previous papers (Kadlec and Gabrys, 2011) or is quite common in some of the local learning approaches to build global predictors. However, there can be cases where for security or other reasons, the data are not available at the combination training phase, but only base predictor out-

puts from the whole pool are accessible. The idea of this paper, is to investigate the effectiveness of a system that produces a fuzzy model for combining learners, but which also restricts itself to knowledge about the underlying problem. Such a model, named hereinafter as *PROFESS (PRedictor-Output Fuzzy Evolving SyStem)* uses trained learners to feed the fuzzy antecedents of the rules whose consequents are evolved combined predictors. Based on GRADIENT's versatile framework, PROFESS extends the ensemble generation ability by providing a model for the creation of fuzzy rule-based controlled ensembles, where the fuzzy antecedent inputs are also the learners. To accomplish this, a new context-free grammar is introduced which enables the creation of ensembles consisted of fuzzy rules having learner combinations as a consequent part, and learners in their antecedent part.

The paper is organized as follows. Next section describes the background on related research. Section 3 includes a detailed description of the system. In section 4, we present our results from synthetic and real-world data domains, and a discussion follows. Finally, section 5 includes our conclusions and suggestions for further research.

## 2 BACKGROUND

Genetic programming (GP) is a successful branch of evolutionary computing, with a number of desirable properties (Koza, 1992). The main advantage of GP resides in its ability to express arbitrarily large hierarchical solutions representing functional equivalents. Standard GP implementations derive simple tree structures that describe programs or mathematical formulas. Later advances incorporated grammar systems to GP enabling the production of more complex solution forms, like Mamdani fuzzy rule based systems (Alba et al., 1996), multilayer perceptrons (Tsakonas, 2006) or Takagi-Sugeno-Kang fuzzy rule based systems (Tsakonas and Gabrys, 2011).

Other enhancements on GP include splitting the evolving population into semi-independent subpopulations, in the so-called *island models*. These subpopulations, also called *demes*, evolve independently for a requested interval and periodically exchange a number of individuals (Fernandez et al., 2003). The improved diversity levels apparent to island models made them attractive means for the implementation of ensemble building systems. Such a model is presented in (Zhang and Bhattacharyya, 2004), where GP is used to produce base classifiers which are then combined by majority voting. A similar approach is proposed in (Hong and Cho, 2006), however with the

learner combination taking into account the diversity of the classifiers. In an advanced approach (Folino et al., 2003), a cellular GP is used to combine decision trees for classification tasks.

Incorporating fuzziness into ensembles can take the form of fuzzy application at base level, at combination level, or both. At the combination level, a fuzzy inference engine may be used for global selection of base learners or for complete ensembles (Duin, 2002). A comparison between fuzzy and non fuzzy ensembles is presented in (Kuncheva, 2003), where the authors design combinations of classifiers using boosting techniques, in the AdaBoost environment. In that work, the fuzzy ensembles are shown to achieve better performance in most of the tasks addressed. Combining learners using fuzzy logic has been applied in classification tasks in (Evangelista et al., 2005). In that work, a fuzzy system aggregates the output of support vector machines for binary classification, in an attempt to reduce the dimensionality of the problems. The proposed model is tested on an intrusion detection problem, and the authors conclude that it is promising and it can be applied to more domains. Another work (Jensen and Shen, 2009), presents three methods to apply selection in an ensemble system by using fuzzy-rough features. The suggested models are shown to produce ensembles with less redundant learners. Other promising methods to apply fusion using fuzziness include fuzzy templates and several types of fuzzy integrals (Ruta and Gabrys, 2000).

Although extended research has been accomplished for incorporating fuzziness into ensemble building, most research deals with the application of fuzziness to either base level, or to the combination level for global selection of base learners (Sharkey et al., 2000). Hence, few work has been done on fuzzy rule based selection of ensembles, and the use of base learner output for the antecedent part of such systems has not been investigated yet. Still, the potential of positive findings regarding the performance of an ensemble system that creates combinations without explicit access to the original data - but only through its learners - is significant. This work therefore, aims to explore this configuration. Concluding the presentation of related background, we continue in the next section by providing the system design details.

## 3 SYSTEM DESIGN

Following the principles of GRADIENT, three basic elements form the architecture of PROFESS (Tsakonas and Gabrys, 2012):

- Base learner pool. These learners are individually trained at the beginning of the run.
- Grammar. The grammar is responsible for the initial generation of combinations, and the subsequent control during evolution, for the production of combined prediction systems.
- Combination pool. The combination pool is implemented as the genetic programming population and evolves guided by the grammar in the second phase of training.

Training in PROFESS includes the following steps:

1. Creation of a learner pool.
2. Training of individual learners.
3. Creation of initial population of combined predictors.
4. Evolution of combined predictors until termination criterion is satisfied (*combined predictor search*).

*Step 1* allocates resources for the generation of the requested learner pool. In *Step 2*, the available learners are trained, using standard training algorithms, such as backpropagation for neural networks. *Step 3* generates the GP population, consisted of combined prediction systems. One complete combined prediction system represents one individual in the GP population. The final step, *Step 4*, evolves the population until a specific criterion is met. Considering the importance of the grammar as a descriptor of PROFESS, we continue this section with a presentation of the adopted grammar. We then describe the learner settings for this work and this section concludes with a presentation of the evolutionary environment that is applied during the combined predictors search phase.

### 3.1 Grammar

The proposed grammar aims to restrict the search space and facilitate the generation of a fuzzy rule base for the selection of ensembles. The fuzzy rules use the output of base learners in the antecedent parts. The fuzzy membership functions are further tuned by evolutionary means, using two parameters: *skew*  $S_k$  and *slide*  $S_L$ . The first parameter (skew) extends or shrinks the shape of the membership function, while the second one (slide) shifts the center of the membership function. The resulting function output  $z_{A_k}$ , for a Gaussian membership function  $A_k$  is calculated using Eq.1-3.

$$z_{A_k} = e^{\left(\frac{x-c_{A_k}}{w_{A_k}}\right)^2} \quad (1)$$

```

N = { RL, RULE, IF, AND, THEN}
T = { LOW, MEDIUM, HIGH, ANN1, ANN2, ..., ANNn,
      SVM1, SVM2, ..., SVMp }
P = {
<TREE> ::= <RL> | <RULE>
<RL> ::= RL <TREE><TREE>
<RULE> ::= RULE <COND><COMB>
<COND> ::= <IF > | <AND>
<IF > ::= IF <PRED><FSET><SLIDE><SKEW>
<AND> ::= AND <COND> <COND>
<FSET > ::= LOW | MEDIUM | HIGH
<COMB> ::= <FUNC><PRED><PRED> |
             <FUNC><PRED><PRED><PRED> |
             <FUNC><PRED><PRED><PRED><PRED> |
             <FUNC> ::= MEAN | MEDIAN | QUAD
             <PRED> ::= ANN1 | ANN2 | ... | ANNn |
                         SVM1 | SVM2 | ... | SVMp
             <SLIDE> ::= <NUMBER>
             <SKEW> ::= <NUMBER>
             <NUMBER> ::= Real value in [-L,L]
}
S = { RL }

```

Figure 1: Context-free grammar for PROFESS.

$$c_{A_k} = c_{mf} + \alpha_k S_k \quad (2)$$

$$w_{A_L} = w_{mf} + \alpha_L S_L \quad (3)$$

where  $c_{mf} \in \{0, 0.5, 1\}$ ,  $w_{mf} = 0.25$ ,  $\alpha_L = 0.125$ ,  $\alpha_K = 0.2$ , with the last two parameters expressing the preferred sensitivity of tuning, their selection depending on the expressiveness preference of the resulted fuzzy rules. As base learners, multilayer perceptrons and support vector machines are available. The rule is in the following form:

$$\begin{aligned} R_i : if \ F_m \ is \ A_{k1} \ [and \ F_p \ is \ A_{k2} \ ...] \\ then \ y = E_i \ with \ C \\ i = 1, \dots, m, \ C \in [0, 1] \end{aligned} \quad (4)$$

where  $C$  is the certainty factor,  $F_m, F_p$  are selected predictors,  $E_i$  is a selected ensemble, and  $A_{kn}$  are fuzzy sets characterized by the membership functions  $A_{kn}(F_n)$ . In this work, *Gaussian* membership functions were applied. Three fuzzy sets per attribute were available (*Low*, *Medium*, *High*). A grammar is defined by the quadruple  $N, T, P, S$  where  $N$  is the set of non-terminals,  $T$  is the set of terminals,  $P$  is the set of production rules and  $S$  is a member of  $N$  that corresponds to the starting symbol. The description of the grammar for PROFESS is shown in Fig. 1.

### 3.2 Learners Setup

From the available learner and pre-processing library of GRADIENT, for illustration purposes we selected to include in PROFESS, multilayer perceptrons and support vector machines. The multilayer perceptrons

Table 1: Learners configuration ( $\mathcal{T}$ : transfer function in hidden layers).

Parameter	Value
MLP-NN #predictors	100
MLP-NN #hidden layers	2
MLP-NN sigmoid $\mathcal{T}$ prob.	0.5
MLP-NN stepwise sigmoid $\mathcal{T}$ prob.	0.1
MLP-NN gaussian $\mathcal{T}$ prob.	0.3
MLP-NN elliot $\mathcal{T}$ prob.	0.1
MLP-NN Iterations	3,000
SVM #predictors	100
SVM Max. Iterations	50,000
SVM RBF $\gamma$ lowest	$10^{-5}$
SVM RBF $\gamma$ highest	$10^{15}$
Predictors subset size	60%
Predictors subset domain	Global

consist of two hidden layers. The number of neurons in every hidden layer  $N_k^{l,i=1,2}$  of a neural network  $K$ , is randomly set according to Equation 5:

$$N_k^i = (0.5 + U(1))n_k \quad (5)$$

where  $U(1)$  returns uniformly a random number in  $[0, 1]$  and  $n_k$  is the positive root of Equation 6 for  $P_k$  attributes (network inputs),  $T_k$  training rows and  $l$  hidden layers (here  $l = 2$ ).

$$n_k = (l - 1)x^2 + (1 + P_k)x - \frac{T_k}{2} \quad (6)$$

The transfer functions in hidden layers were also randomly set, selecting among Sigmoidal, Gaussian and Elliot functions. The resilient backpropagation algorithm was preferred for training. We trained a pool of 100 multilayer perceptrons. The support vector machines incorporated a radial basis function kernel, and the  $\gamma$  parameter was randomly selected from  $[10^{-5}, 10^{15}]$ . In the learner pool, 100 support vector machines were available. The training datasets for learners consist of randomly sub-sampled sets of the available training data sets (Tsakonas and Gabrys, 2012). Table 1 summarizes the learner settings.

### 3.3 Evolutionary Setup

After the training phase of learners is completed in PROFESS, the next stage involves creation and training of the pool of combined predictors. Individuals in the evolutionary population are created and trained under the constraints of the defined grammar. Each individual corresponds to one fuzzy rule base of ensembles. As combiners, the arithmetic mean and the median were available. This training makes use of a multi-population genetic programming framework.

Table 2: Evolutionary parameters.

Parameter	Value / Value range
GP System	Grammar-driven GP
Subpopulations	5
Subpopulation topology	Ring
Isolation time	7 generations
Migrants number	7 individuals
Migrants type	Elite individuals
Total population	150 individuals
Selection	Tournament
Tournament size	7
Crossover rate	0.7
Mutation rate	0.3
Max.individual size	150/500 nodes
Max.generations	50

In this work, five subpopulations are used, a value which is typical in multi-population models (Fernandez et al., 2003). These subpopulations are trained for a period of 7 generations, and they exchange 7 individuals, under a *ring scheme* of migration. This process is repeated until 50 generations are completed. As fitness function, the mean-square-error (MSE) is used. A summary of the parameters for the evolutionary training of the combined predictors is shown in Table 2.

### 3.4 Data

We compared PROFESS with regression models using a synthetic data problem, and with GRADIENT using three real-world datasets, taken from the UCI Machine Learning repository (Frank and Asuncion, 2010). The properties of the datasets are shown in Table 3. We created three data permutations for every real-world problem. In all cases, we used one third of the data as a test set. The synthetic data task was the Jacobs data (Jacobs, 1997) that involves five independent attributes  $x_1, \dots, x_5$ . All attributes are uniformly distributed at random over  $[0, 1]$ . The function output is calculated by Equation 7.

$$y = \frac{1}{13}(10\sin(\pi x_1 x_2) + 20\left(x_3 - \frac{1}{2}\right)^2 + 10x_4 + 5x_5) - 1 + \epsilon \quad (7)$$

where  $\epsilon$  is Gaussian random noise with  $\sigma_\epsilon^2 = 0.2$ . We generated a dataset consisting of 1,500 rows.

## 4 RESULTS AND DISCUSSION

We applied PROFESS to the available datasets, using the configuration shown in Tables 1 and 2. Ta-

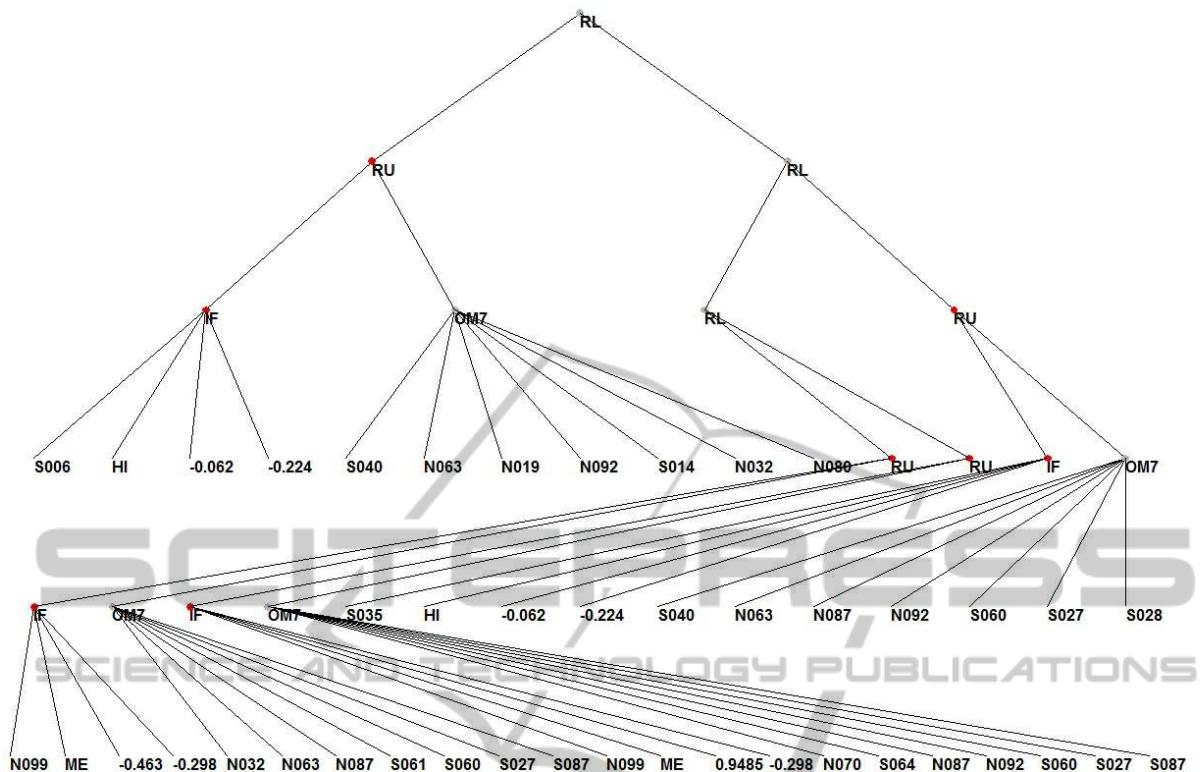


Figure 2: Evolved combined system for the Slump test problem.

Table 3: Datasets used.

Domain	Instances	Attributes
Jacobs	1500	5
Slump test	103	7
CPU Performance	209	6
Boston housing	506	13

ble 4 shows a comparison with WEKA (Hall et al., 2009) regression methods for the synthetic data problem. The results of our experiments for real world data, as compared to GRADIENT are shown in Table 5. In this table, the results are expressed in average mean-square-error (MSE) with 0.95% confidence intervals. As it can be seen in the table, PROFESS managed to achieve lower average MSE than GRADIENT in the problems addressed. As an example of output, the evolved solution for the first permutation of the Slump test problem is shown in Fig.2. This solution is corresponding to the following rule base:

$R_1 : \text{if } S006 \text{ is High}(-0.06219, -0.22473) \text{ then}$

$\text{Median}(S040, N063, N019, N092, S014, N032, N080)$

$R_2 : \text{if } N099 \text{ is Medium}(-0.46393, -0.29883) \text{ then}$

$\text{Median}(N032, N063, N087, S061, S060, S027, S087)$

$R_3 : \text{if } N099 \text{ is Medium}(0.94855, -0.29883) \text{ then}$

$\text{Median}(N070, S064, N087, N092, S060, S027, S087)$

$R_4 : \text{if } S035 \text{ is High}(-0.06219, -0.22473) \text{ then}$

$\text{Median}(S040, N063, N087, N092, S060, S027, S028)$

where the first variable in the fuzzy set corresponds to the *slide* parameter of the membership function  $S_L$ , and the second is the *skew* parameter  $S_K$ . The evolved membership functions are shown in Fig.3. It is worth noting, that the most common case observed was that learners feeding the antecedent parts were not appearing in the consequent part of any rule.

Tables 6, 7 and 8 compare the best obtained results using the proposed system to results found in the literature.

- In Slump test data, we compared the results using the Pearson correlation coefficient for compatibility with the results reported in the literature. In this case, the best model resulting from PROFESS was not better than the other reported models, with the best model of GRADIENT having the higher correlation coefficient.
- In CPU performance data, the Pearson correlation coefficient for PROFESS was the highest among the compared approaches.

Table 4: Comparative results on Jacobs data.

Model	RMSE
RBF network <sup>1</sup>	.1659
Isotonic Regression <sup>1</sup>	.1469
Pace Regression <sup>1</sup>	.0966
SMO Regression <sup>1,2</sup>	.0960
PROFESS (this work)	.0958

1. (Hall et al., 2009).  
 2. (Scholkopf and Smola, 2002).

- In Boston housing data, the best model of PROFESS had lower error than the reported literature ones.

Table 5: Results in three real-world datasets. Values are average MSE from three permutations, with 0.95% confidence intervals.

Domain	GRADIENT	PROFESS
Slump test	$40.33 \pm 19.23$	$39.83 \pm 9.53$
CPU	$9575 \pm 7789$	$9461 \pm 6267$
Boston housing	$13.43 \pm 1.04$	$10.68 \pm 2.97$

Table 9 compares the evolved size, measured in the number of nodes, of the solutions. The implementation of a grammar for fuzzy systems requires a large number of intermediate functions to allow the incorporation of a similar number of base learners. For this reason, we have set in our experiments the maximum possible solution size to 500 nodes for PROFESS, while for GRADIENT a maximum of 150 nodes was kept since it could express similarly sized (in terms of learner participation) ensembles.

Although the maximum size was set high, PROFESS managed to evolve comparable solutions, in terms of size, to GRADIENT’s. This resulted in producing rule bases with a small number of rules, which we consider is a result of the expressiveness of PROFESS’s grammar. The latter conclusion is more clearly depicted in Table 10, where the average number of learner instances in a solution is shown. In this table, it is clear that PROFESS required, on average, a significantly smaller number of learner participation to evolve competitive results. As expected, the values shown in Table 10 concern only the learner instances that appear in combined predictors, and they don’t take into account the occurrence of the learners in the antecedent part of PROFESS’s rules.

Table 6: Slump test data comparison on unseen data. Results for PROFESS correspond to the Pearson correlation coefficient of best model.

Model	$R^2$
Neural network <sup>1</sup>	.922
P2-TSK-GP (3 MF) <sup>2</sup>	.9127
GRADIENT(NN-30/Mean) <sup>3</sup>	.9694
PROFESS (this work)	.8257

1. (Yeh, 2008).  
 2. (Tsakonas and Gabrys, 2011).  
 3. (Tsakonas and Gabrys, 2012).

Table 7: CPU performance data comparison on unseen data. Results for PROFESS correspond to the Pearson correlation coefficient of best model.

Model	$R^2$
<i>Original Attributes</i>	
M5 <sup>1</sup>	.921
M5 (no smoothing) <sup>1</sup>	.908
M5 (no models) <sup>1</sup>	.803
GRADIENT (NN-30/Median) <sup>2</sup>	.970
PROFESS (this work)	.978
<i>Transformed Attributes</i>	
Ein-Dor <sup>3</sup>	.966
M5 <sup>1</sup>	.956
M5 (no smoothing) <sup>1</sup>	.957
M5 (no models) <sup>1</sup>	.853

1. (Quinlan, 1992).  
 2. (Tsakonas and Gabrys, 2012).  
 3. (Ein-Dor and Feldmesser, 1984).

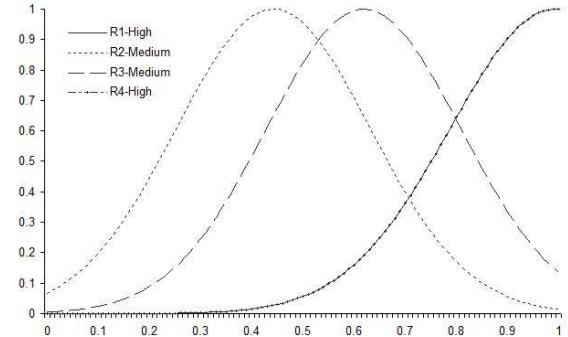


Figure 3: Evolved membership functions for Slump test problem.

## 5 CONCLUSIONS AND FURTHER RESEARCH DIRECTIONS

This work presented a system for the generation of multi-component fuzzy rule-based ensembles using

Table 8: Boston housing data comparison on unseen data. Results for PROFESS correspond to the best model.

Model	RMSE
GASEN <sup>1</sup>	10.68
Random Forest <sup>2</sup>	3.26
Fuzzy CART <sup>3</sup>	3.40
Fuzzy CART + PLM <sup>3</sup>	3.10
Fuzzy CART + Bagging <sup>3</sup>	3.26
Fuzzy CART + Smearing <sup>3</sup>	3.21
GRADIENT (NN-30/Mix) <sup>4</sup>	2.66
PROFESS (this work)	2.639

1. (Zhou et al., 2001).
2. (Liaw and Wiener, 2002).
3. (Medina-Chico et al., 2001).
4. (Tsakonas and Gabrys, 2012).

Table 9: Average evolved solution size (in nodes).

Domain	GRADIENT	PROFESS
Slump test	106.1	181.5
CPU	101.6	165.9
Boston housing	72.6	75.0

base learners in the antecedent part of fuzzy rules. To accomplish this, we have decided to modify the grammar of a versatile environment for the production of multi-level, multi-component ensembles, named GRADIENT. The new proposed model, named PROFESS, features a novel grammar that produces arbitrarily large fuzzy rule bases that enable the selection of complete ensembles, using the output of base learners as criterion. This approach can facilitate the development of combined predictors, in environments where only access to the base learners is possible, and any use of the original training dataset is restricted to base learning level.

To examine the effectiveness of the proposed model, we tested it on a synthetic data problem and three real-world datasets. The results from our experiments show that the model is able to provide competitive performance as compared to the standard approach. This conclusion facilitates the definition of environments where a set of trained learners may substitute the original data in tasks where the formation of an ensemble is required. Applications of this approach can include situations where for security or other reasons, the access to the original data is not possible or highly restricted.

We consider that our initial findings presented in this paper deserve further investigation. In the conducted experiments we observed that, commonly, selected learners in the antecedent part were not included in consequent parts of the rules. We will therefore further investigate this case. It is clear that the

Table 10: Average evolved solution size (in learner instances appearing in combinations).

Domain	GRADIENT	PROFESS
Slump test	67.6	40.4
CPU	35.2	22.6
Boston housing	71.6	54.8

complementary information resides in the whole pool of base learners and while some of them are not accurate enough to be used for prediction, they seem to play an important role in the selection process of ensembles consisting of a number of other predictors from the pool. This finding is completely novel and the analysis of the relationships between the "selector" learners used in the antecedents of the fuzzy rules and the "combined predictors" which form the consequent part of these rules is a fascinating subject to follow. Finally, further tuning of the evolutionary parameters will take place, in an attempt to reduce the required resources and increase the algorithmic efficiency.

## ACKNOWLEDGEMENTS

The research leading to these results has received funding from the European Commission within the Marie Curie Industry and Academia Partnerships and Pathways (IAPP) programme under grant agreement n. 251617.

## REFERENCES

- Alba, E., Cotta, C., and Troya, J. (1996). Evolutionary design of fuzzy logic controllers using strongly-typed gp. In *Proc. 1996 IEEE Int'l Symposium on Intelligent Control*. New York, NY.
- Brown, G., Wyatt, J., Harris, R., and Yao, X. (2005). Diversity creation methods: a survey and categorisation. *Inf. Fusion*, 6(1):5–20.
- Chandra, A. and Yao, X. (2004). Divace: Diverse and accurate ensemble learning algorithm. *LNCS 3177, IDEAL 2004*, 17(4):619–625.
- Duin, R. (2002). The combining classifier: to train or not to train? In *Proc. of the 16th Int'l Conf. on Pattern Recognition*, pages 765–770.
- Ein-Dor, P. and Feldmesser, J. (1984). Attributes of the performance of central processing units: A relative performance prediction model. *Commun. ACM*, 30(30):308–317.
- Evangelista, P., Bonissone, P., Embrechts, M., and Szymanski, B. (2005). Unsupervised fuzzy ensembles and their use in intrusion detection. In *European Sym-*

- posium on Artificial Neural Networks (ESANN'05). Bruges, Belgium.
- Fernandez, F., Tommassini, M., and Vanneschi, L. (2003). An empirical study of multipopulation genetic programming. *Genetic Programming and Evolvable Machines*, 4(1).
- Folini, G., Pizzuti, C., and Spezzano, G. (2003). Ensemble techniques for parallel genetic programming based classifiers. In C.Ryan, T.Soule, M.Keijzer, et al.(Eds.), *Proc. of the European Conf. Gen. Prog.(EuroGP 03), LNCS 2610*, pages 59–69. Springer.
- Frank, A. and Asuncion, A. (2010). *UCI Machine Learning Repository* [<http://archive.ics.uci.edu/ml>]. CA: University of California, School of Information and Computer Science, Irvine.
- Hall, M., Frank, E., Holmes, G., Pfahringer, B., Reutemann, P., and Witten, I. (2009). The weka data mining software: An update. *SIGKDD Explorations*, 11(1).
- Hong, J. and Cho, S. (2006). The classification of cancer based on dna microarray data that uses diverse ensemble genetic programming. *Artif. Intell. in Med.*, 36(1):43–58.
- Ishibuchi, H. (2007). Multiobjective genetic fuzzy systems: Review and future research directions. In *IEEE Int'l Conf. on Fuzzy Systems (FUZZ-IEEE 2007)*, pages 59–69. Imperial College.
- Jacobs, R. (1997). Bias-variance analyses of mixture-of-experts architectures. *Neural Computation*, 0:369–383.
- Jensen, R. and Shen, Q. (2009). New approaches to fuzzy-rough feature selection. *IEEE Trans. on Fuzzy Systems*, 17(4):824–838.
- Kadlec, P. and Gabrys, B. (2011). Local learning-based adaptive soft sensor for catalyst activation prediction. *AIChE Journal*, 57(5):1288–1301.
- Koza, J. (1992). *Genetic programming - On the programming of computers by means of natural selection*. The MIT Press, Cambridge, Massachussets, USA.
- Kuncheva, L. (2003). Fuzzy versus nonfuzzy in combining classifiers designed by boosting. *IEEE Trans. on Fuzzy Systems*, 11(6):729–741.
- Liaw, A. and Wiener, M. (2002). Classification and regression by randomforest. *Expert Systems with Applications (Under Review)*.
- Medina-Chico, V., Suarez, A., and Lutsko, J. F. (2001). Backpropagation in decision trees for regression. In *ECML 2001, LNAI 2167*, pages 348–359, Springer Verlag.
- Quinlan, J. R. (1992). Learning with continuous classes. In *AI'92*, Singapore: World Scientific.
- Ruta, D. and Gabrys, B. (2000). An overview of classifier fusion methods. *Computing and Information Systems*, 7(2):1–10.
- Scholkopf, B. and Smola, A. (2002). *Learning with Kernels - Support Vector Machines, Regularization, Optimization and Beyond*. The MIT Press, Cambridge, Massachusetts, USA.
- Sharkey, A., Sharkey, N., Gerecke, U., and Chandroth, G. (2000). The test and select approach to ensemble combination. *Multiple Classifier Systems, LNCS 1857*, pages 30–44.
- Tsakonas, A. (2006). A comparison of classification accuracy of four genetic programming evolved intelligent structures. *Information Sciences*, 17(1):691–724.
- Tsakonas, A. and Gabrys, B. (2011). Evolving takagi-sugeno-kang fuzzy systems using multi-population grammar guided genetic programmings. In *Int'l Conf. Evol. Comp. Theory and Appl. (ECTA'11)*, Paris, France.
- Tsakonas, A. and Gabrys, B. (2012). Gradient: Grammar-driven genetic programming framework for building multi-component, hierarchical predictive systems. *Expert Systems with Applications*, DOI:10.1016/j.eswa.2012.05.076.
- Yeh, I.-C. (2008). Modeling slump of concrete with fly ash and superplasticizer. *Computers and Concrete*, 5(6):559–572.
- Zhang, Y. and Bhattacharyya, S. (2004). Genetic programming in classifying large-scale data: an ensemble method. *Information Sciences*, 163(1):85–101.
- Zhou, Z., Wu, J., Jiang, Y., and Chen, R. (2001). Genetic algorithm based selective neural network ensemble. In *17th Int'l Joint Conf. Artif. Intell.*, pages 797–802, USA, Morgan Kaufmann.