

Object Recognition based on a Simplified PCNN

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Abstract: The aim of the paper is to propose a region-based object recognition method to identify objects from complex real-world scenes. The proposed method firstly performs a colour image segmentation by a simplified pulse coupled neural network (SPCNN) model, and the parameters of the SPCNN are automatically set by our previously proposed parameter setting method. Subsequently, the proposed method performs a region-based matching between a model object image and a test image. A large number of object recognition experiments have proved that the proposed method is robust against the variations in translation, rotation, scale and illumination, even under partial occlusion and highly clutter backgrounds. Also it shows a good performance in identifying less-textured objects, which significantly outperforms most feature-based methods.

1 INTRODUCTION

To identify a given object from complex background in an image or video sequence is an important branch of the study of object recognition (Ullman et al., 2001). In real-world scenes, objects may pose randomly under clutter and partial occlusion in illumination-changing environment. So an object in clutter backgrounds may encounter complex variations in viewpoints, translation, scale, rotation, and illumination, even under partial occlusion. Thus, the capability of identifying an object from complex varying viewing conditions is a significant aspect of a promising object recognition method.

There have been a large number of works aiming at endowing computers with the ability to recognize objects from the real-world scenes. Nowadays, the feature-based methods, such as Lowe's scale invariant feature transform (SIFT) (Lowe, 2004) and its extension methods (Abdel-Hakim and Farag, 2006; Bay et al., 2008; Bosch, et al., 2008; Burghouts and Geusebroek, 2009; Ke and Sukthankar, 2004; Mikolajczyk and Schmid, 2005; van de Sande et al. 2010; Weijer et al., 2006), have become become active and dominant methods of object recognition because of their high accuracy and fast speed (Mikolajczyk and Schmid, 2005; van de Sande et al., 2010).

However, the performance of the above feature-based methods has two critical limitations. One limitation is that the feature-based methods would inevitably include background information into local invariant feature descriptors when keypoints locate near object boundaries (Stein and Hebert, 2005). This has been a bottleneck when objects are identified from heavy clutter environments or objects that occupy only a small part of the images (Stein and Hebert, 2005). The other limitation is that when the feature-based methods are used to identify less-textured objects (such as doorknob, sofa, TV, fridge), the number of repeating keypoints that are correctly matched between model object and test image is usually very low, and the corresponding descriptors are usually not discriminative either.

In order to overcome the above limitations, we develop an region-based object recognition method based on colour segmentation performed by a simplified pulse couple neural networks (SPCNN) model (Chen et al., 2011; Johnson, 1994; Johnson and Padgett, 1999) whose parameters could be automatically set by our previously proposed method (Chen et al., 2011).

we conduct a number of experiments to show the robustness of the proposed object recognition method in resisting the variances in translation, rotation, scale, and illumination (even under partial occlusion and clutter environments). Moreover, in

order to verify the validity of the proposed method, we compare it with the state-of-the-art method.

The following part of this paper is organized as follows. Section 2 simply describes the SPCNN model with automatic parameters. Section 3 elaborates the proposed object recognition method with an illustrated example. Section 4 demonstrates more experimental results. And the last section gives a conclusion.

2 SIMPLIFIED PCNN WITH AUTOMATIC PARAMETERS

Pulse coupled neural network (PCNN) was derived by Johnson et al. (Johnson, 1994; Johnson and Padgett, 1999) from Eckhorn's cortical model which was developed on the basis of synchronous dynamics of neuronal activity in cat visual cortex (Eckhorn et al. 1990). In order to achieve lower computational complexity, we employ a simplified pulse coupled neural network (SPCNN) with parameters automatically set by the automatic parameter setting method proposed in our previous paper (refer to the equations (33), (40), (41), (48), and (49) in Chen et al., 2011). The SPCNN model was derived from SCM model (Zhan et al., 2009) and can be described as:

$$U_{ij}[n] = e^{-\alpha_f} U_{ij}[n-1] + S_{ij} (1 + \beta V_L \sum_{kl} W_{ijkl} Y_{kl}[n-1]) \quad (1)$$

$$Y_{ij}[n] = \begin{cases} 1 & \text{if } U_{ij}[n] > E_{ij}[n-1] \\ 0 & \text{else} \end{cases} \quad (2)$$

$$E_{ij}[n] = e^{-\alpha_e} E_{ij}[n-1] + V_E Y_{ij}[n] \quad (3)$$

where

$$W_{ijkl} = \begin{bmatrix} 0.5 & 1 & 0.5 \\ 1 & 0 & 1 \\ 0.5 & 1 & 0.5 \end{bmatrix}. \quad (4)$$

In this model, there are two inputs for the neuron N_{ij} in position (i, j) : input stimulus S_{ij} which is the image pixel intensity, and a simplified linking input which is the sum of the eight neighbouring neuron outputs $Y_{kl}[n-1]$ linked by a constant synaptic weight W_{ijkl} . Moreover, the amplitude of the simplified linking input is denoted by V_L . These two inputs are modulated by a linking strength β to yield an internal activity $U_{ij}[n]$. The internal activity also records the previous neuron state by an

exponential decay factor $e^{-\alpha_f}$. The neuron N_{ij} outputs a pulse in iteration n ($Y_{ij}[n]=1$) only when the current internal activity $U_{ij}[n]$ surpasses the last dynamic threshold $E_{ij}[n-1]$. Subsequently, if neuron N_{ij} fires, the dynamic threshold will increase by amplitude V_E ; otherwise, the dynamic threshold will decay by a factor $e^{-\alpha_e}$ (Lindblad and Kinser, 2005).

3 PROPOSED OBJECT RECOGNITION METHOD

PCNN has broad applications in image processing (Lindblad and Kinser, 2005; Ma et al., 2010), hereinto, object detection is one of the most potential applications (Gu, 2008; Kinser, 1996; Ranganath and Kuntimad, 1999; Yu and Zhang, 2004). Object detection by PCNN is usually implemented by generating features which result from encoding the spatial distributions of a 2D image into a unique temporal sequence (Johnson, 1994; Gu, 2008; Zhan et al., 2009). This would result in the loss of image spatial information that may facilitate the object detection.

In this paper, we propose an object recognition method named RBOR-SPCNN (region-based object recognition with SPCNN), which detects a desired object from a complex real-world environment. The proposed method makes use of both spatial and temporal information. Specifically, the proposed method employs a specific colour transformation before using the SPCNN with automatic parameters (Chen et al., 2011) to segment the colour image into several syn-firing areas, and finally employs a region-based matching to output recognition result.

3.1 Colour Space Transformation

In order to resist light intensity change and light intensity shift that are caused respectively by a constant gain and an equal offset in all channels, we carry out a colour space transformation on both object model image and test image. The colour space transformation integrates normalized rgb colour space (scale-invariant) in (5) with opponent colour space (shift-invariant) in (6) (van de Sande et al., 2010). Thus, we call the resulting image an "rgb-opponent" colour image.

$$\left(r = \frac{R}{R+G+B}, \quad g = \frac{G}{R+G+B}, \quad b = \frac{B}{R+G+B} \right) \quad (5)$$

$$\left(O_1 = \frac{r-g}{\sqrt{2}}, O_2 = \frac{r+g-2b}{\sqrt{6}}, O_3 = \frac{r+g+b}{\sqrt{3}} \right) \quad (6)$$

Since all the values in the O_3 channel in (6) are equal to constant $\frac{1}{\sqrt{3}}$, we replace the O_3 intensity channel by the normalized gray image and note it as O_3 channel:

$$O_3 = \frac{I_g - I_{g_{\min}}}{I_{g_{\max}} - I_{g_{\min}}} \quad (7)$$

where I_g denotes the original gray image.

Due to the subtraction, the O_1 and O_2 channels may contain some negative values which do not respond to the SPCNN process. Thus, we supplement O_4 and O_5 channels by reversing the O_1 and O_2 channels as follows:

$$O_4 = -O_1 \quad (8)$$

$$O_5 = -O_2. \quad (9)$$

3.2 Colour Segmentation by SPCNN

As for a specific object model, the SPCNN parameters (Chen et al., 2011) could be estimated according to the normalized gray object model image O_3 .

After the proper SPCNN parameters are estimated, the SPCNN model with these parameters could be applied to each of the transformed channels O_1, O_2, O_3, O_4 , and O_5 for object model and test image, respectively.

In order to guarantee the physical meaning of image segmentation, we assume that once a pixel in a channel fires twice, it will be prevented from firing again (Chen et al., 2011). And we record the second firing times of the pixels in each channel into a firing-order matrix. The matrix has the same size as the image channel.

Thus, we obtain five firing-order matrices corresponding to the five channels O_1, O_2, O_3, O_4 , and O_5 for object model and test image, respectively:

$$[C_1^m; C_2^m; C_3^m; C_4^m; C_5^m] \quad (10)$$

$$[C_1^t; C_2^t; C_3^t; C_4^t; C_5^t]. \quad (11)$$

Subsequently, we could gather the pixels firing synchronously throughout all the five channels as an image segment called "syn-firing area". Thus, an image could be segmented into several "syn-firing areas". Specifically, we construct a firing-order

vector for each pixel. For example, the firing-order vector of the pixel at position (i, j) consists of five elements extracted from the five firing-order matrices at the same position (i, j) as follows:

$$v_{(i,j)}^m = [c_{1(i,j)}^m \quad c_{2(i,j)}^m \quad c_{3(i,j)}^m \quad c_{4(i,j)}^m \quad c_{5(i,j)}^m] \quad (12)$$

$$v_{(i,j)}^t = [c_{1(i,j)}^t \quad c_{2(i,j)}^t \quad c_{3(i,j)}^t \quad c_{4(i,j)}^t \quad c_{5(i,j)}^t]. \quad (13)$$

Thus, a syn-firing area can be formed by grouping the pixels with the same firing-order vector. In this manner, the object model and the test images could be segmented into several syn-firing areas according to the different firing-order vectors. An example of a sharpener is shown in Fig. 1.

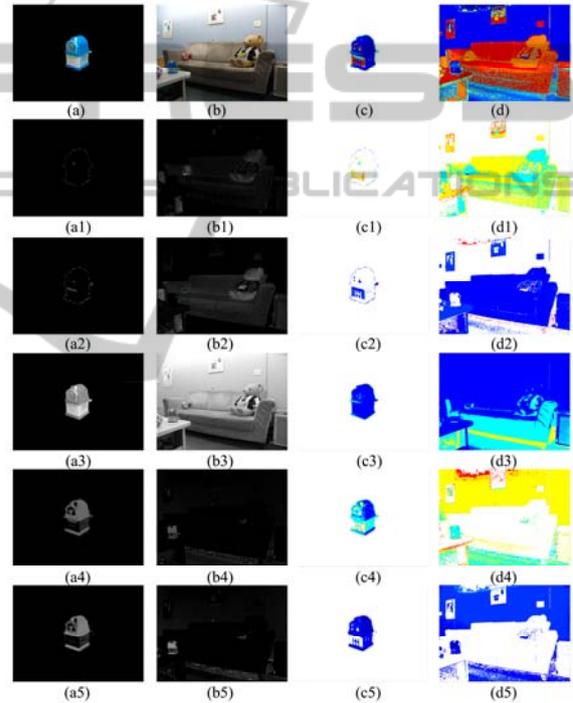


Figure 1: The O_1, O_2, O_3, O_4 , and O_5 transformed channels of a sharpener image (a) and its test image (b) are shown in (a1) - (a5) and (b1) - (b5), respectively. And the corresponding SPCNN firing-order matrices of the five channels are shown in (c1)-(c5) and (d1)-(d5) in Pseudo-colours. And the image segmentation results represented by several syn-firing areas depicted with different Pseudo-colours are shown in (c) and (d).

3.3 Matching Syn-Firing Areas

We suggest a hypothesis that the same object possesses the same SPCNN firing-order vectors no matter how background varies and how object poses.

Based on this assumption, a specific object

model could be identified from a test image of complex real-world scenes, by means of extracting the syn-firing areas with the same firing-order vectors as the syn-firing areas in the object model. And we define these pairs of syn-firing areas between the object model and test image as pairs of matching syn-firing areas. Thus, the test matching syn-firing areas are the potential regions to contain the desired object in the test image.

3.4 Region Blobs

The matching syn-firing areas in test image often disperse and usually include both object and background pixels. In order to separate the background pixels and the object pixels, it is necessary to divide the matching syn-firing areas into smaller region blobs which are expected to contain either part of object pixels or part of background pixels.

In order to speed up the experiments, we remain only the pairs of matching syn-firing areas whose model syn-firing area component is larger than 1/50 of the total area of the object model and further split them into smaller region blobs.

In the process of region splitting, we successively apply a morphological closing (with a disk-shaped structuring element of 3-pixel radius) and an 8-connected components labelling to each pair of matching syn-firing areas. And the resulting connected components are labelled as separated region blobs of the pair of matching syn-firing area.

Since there may still exist some region blobs that are too small to be meaningful, we only remain the region blobs with more than 100 pixels (image size: 640*480) in our experiments.

For each of the remained region blobs, we calculate the region properties, such as 'area', 'major axis length', 'minor axis length', 'weighted centroid' and 'eccentricity' (refer to "regionprops" in Matlab).

3.5 Removal of Test Region Blobs with Irrational Size

Since there may exist many background region blobs in test image, we may easily remove the obvious ones by comparing their rough sizes with that of the object model.

In our experiments, we firstly remove the very large test region blobs whose area is larger than τ_{large} times of the test image area (if any), since they are probably generated by the broad background

$$A^{\text{test blob}} > \tau_{large} \times A^{\text{test image}} . \quad (14)$$

Secondly, we remove the test region blobs that distribute loosely in a large space. That is to remove the test blobs that are larger than τ_{loose} times of the coarse distribution area of the object model:

$$L_{\text{major axis}}^{\text{test blob}} \times L_{\text{minor axis}}^{\text{test blob}} > \tau_{loose} \times (L_{\text{major axis}}^{\text{model}} \times L_{\text{minor axis}}^{\text{model}}) . \quad (15)$$

Besides, since the very long test region blobs are usually outliers, we could remove the test blobs whose major axis lengths are larger than τ_{long} times of the maximum major axis length of the model region blobs in the pair of matching syn-firing areas:

$$L_{\text{major axis}}^{\text{test blob}} > \tau_{long} \times \max(L_{\text{major axis}}^{\text{matching model blobs}}) . \quad (16)$$

It is noted that the above weight constants are application-dependent, and we employ $\tau_{large}=0.25$, $\tau_{loose}=2$, and $\tau_{long}=3$ in our experiments based on a number of experiments.

3.6 Cluster Formation

After the above removal of obvious outlier test region blobs, the test image has been fragmented and has many large or small gaps among the object and background region blobs. Since the desired object can only occupy a cluster of nearby test region blobs, we could group the remained nearby test region blobs into several clusters under a certain radius distance constraint which is adjustable according to a specific object model.

Inspired by the cluster seeking method proposed by Ranganath and Kuntimad (Ranganath and Kuntimad, 1999), we form clusters as follows:

Step-1: Sort all the test region blobs in a list in descending order of areas.

Step-2: Mark the test region blob that has the largest area as the root region blob.

Step-3: Calculate the distances of intensity-weighted centroids between each test region blob and the root region blob.

Step-4: Form a cluster by grouping together the adjacent test region blobs surrounding the root region blob, under the constraint of a certain specific cluster radius threshold.

Step-5: Set the area of the root region blob to be "0" in the list to make sure that this root region blob cannot become root region blob again in the following iterations.

Step-6: Repeat *Step-1* to *Step-5* until the areas of all the region blobs are set to "0" in the list.

In order to make sure that the cluster radius threshold is adjustable for different object models,

the cluster radius threshold could be set as follows:

$$d_{thr} = \text{mean}(d_m) + \mu \times \text{std}(d_m) \quad (17)$$

where d_m denotes the distances between the intensity-weighted centroids of each pair of model region blobs; and $\mu = 0.5$ is empirically set based on plenty of experiments.

3.7 Cluster Refinement

Since some of the obtained clusters are outliers, we perform a cluster refinement process as follows:

(A) Eliminate the repetitive clusters by retaining only one of them.

(B) Delete the clusters with areas less than τ_{low} times or larger than τ_{high} times of the total area of the model region blobs.

$$A^{\text{cluster}} < \tau_{low} \times A^{\text{model region blobs}} \quad (18)$$

$$A^{\text{cluster}} > \tau_{high} \times A^{\text{model region blobs}} \quad (19)$$

(C) Lastly, remove the clusters with the eccentricity larger than $\tau_{eccentr}$ times of the eccentricity of the object model, if any.

$$E^{\text{cluster}} > \tau_{eccentr} \times E^{\text{model}} \quad (20)$$

In the above equations, the weigh constants are empirically set as $\tau_{low} = 0.1$, $\tau_{high} = 3$, and $\tau_{eccentr} = 7$ based on a number of experiments.

3.8 Cluster Matching and Object Recognition Results

After obtaining the above clusters, the next step is to pick out the cluster which is of the highest probability to contain the desired object and output it as the final object recognition result.

In our study, a Bhattacharyya distance of colour histograms is employed to measure the distance between each test cluster image and the model image that is filtered by the model region blobs

$$D(h_{\text{model}}, h_{\text{cluster}}^i) = \left(1 - \sum_{n=1}^N \sqrt{h_{\text{model}}(n)h_{\text{cluster}}^i(n)} \right)^{\frac{1}{2}} \quad (21)$$

where h denotes a colour histogram; n denotes the n th element of the histogram and i denotes the i th cluster in the test image.

The histogram is constructed by $N = N_{O_1}N_{O_2} + N_{O_3}$ bins (N_{O_1} , N_{O_2} and N_{O_3} are the bins in O_1 , O_2 and O_3 channels, respectively). In our experiments, the histogram dimension is

$$N = N_{O_1}N_{O_2} + N_{O_3} = 20 \times 20 + 30 = 430. \quad (22)$$

As a result, the test cluster with the minimal Bhattacharyya distance of colour histograms is outputted as the final object recognition result shown as in the right side of Fig. 2 (e). And the compared result performed by the state-of-the-art OpponentSIFT (Burghouts and Geusebroek, 2009; van de Sande et al., 2010) is shown in Fig. 2 (f) where no matching point is found.

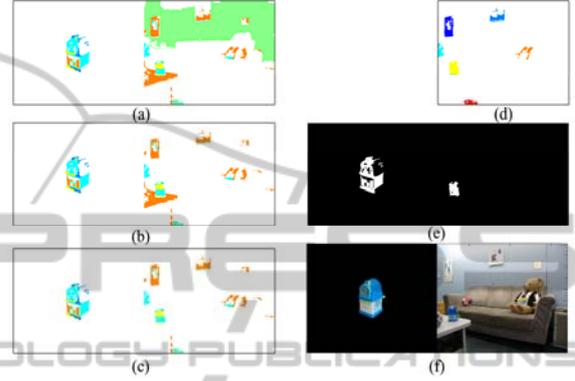


Figure 2: Removal of test region blobs with irrational sizes and object recognition result. (a) shows all the region blobs in the pairs of matching syn-firing areas depicted with different pseudo-colours. The right side of (b) shows the remained region blobs after a test region blob with area larger than 1/4 of the test image is discarded; and the right side of (c) shows the remained region blobs after the long test region blobs and the large but loose ones are discarded. (d) shows that only 7 clusters are left after cluster refinement in test image. (e) shows the object recognition result by the proposed method. For comparison, (f) shows the object recognition result performed by the state-of-the-art OpponentSIFT, where no matching point is found.

4 MORE EXPERIMENTS

In order to examine the general validity of the proposed RBOR-SPCNN method, we apply it to a wide range of diverse objects under various backgrounds. Each object model corresponds to several test images. As an example, the experiments of a sharpener are shown in Fig. 3. In the column (b) of Fig. 3, the sharpeners in the test images are casually placed in highly clutter environments, suffering variations in viewpoints, translation, rotation, scaling, even occlusion.

Moreover, experiments on several other daily necessities are shown in Fig. 4 as examples. Various object models are shown in column Fig. 4 (a); some are less-textured objects, such as cap, chair, and bag. And the test images with complex real-world

environments are shown in column (b). In each test image, the desired object is randomly rotated and scaled. Besides, the tooth past in test image (b2) and the bag in test image (b7) even suffer partial occlusion and illumination change.

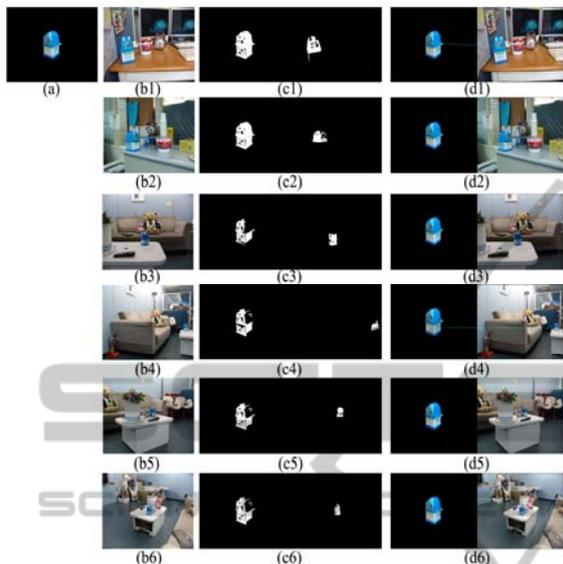


Figure 3: Object recognition results of a sharpener in different poses and various clutter backgrounds. Object model is shown in (a). Six test images with complex backgrounds are shown in column (b). The final object recognition results obtained by the proposed method are shown in column (c). The compared results performed by OpponentSIFT are shown in column (d) where no matching points for most cases (except one matching point appearing in (d1) and (d4), respectively).

Obviously, in both Fig. 3 and Fig. 4, the object recognition results obtained by the proposed method (shown as in column (c)) significantly outperform the compared ones processed by the state-of-the-art OpponentSIFT (shown as in column (d)) (Burghouts and Geusebroek, 2009; van de Sande et al., 2010). It could be seen that the proposed method is not only capable of detecting occluded objects, such as the sharpener in Fig. 3 (b5), the tooth paste in Fig. 4 (b2) and the bag in Fig. 4 (b7); but also capable of detecting less-textured objects, such as the cap, bag, and chair in Fig. 4 (b5)-(b7), respectively. In contrast, the OpponentSIFT fails to find any matching points in such cases.

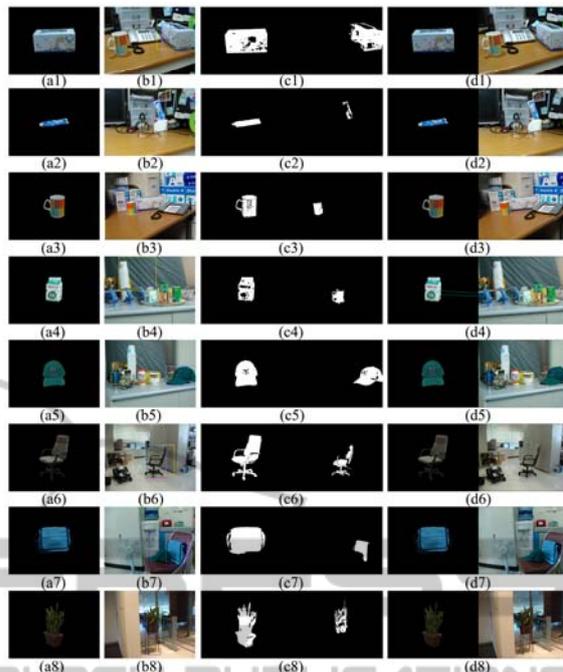


Figure 4: Object recognition results of diverse objects under various backgrounds. Column (a) is object models. Column (b) is test images. All the desired objects in test images are casually placed in highly clutter environments. The variations of objects include variations in rotation, sale and occlusion. The final object recognition results obtained by the proposed method are shown in column (c). The compared results performed by OpponentSIFT are shown in column (d) where no matching point is found in most cases (except two matching points in (d4)).

5 CONCLUSIONS

In this paper, we presented a region-based object recognition method (i.e., RBOR-SPCNN) to identify specific objects from complex real-world environments. The proposed object recognition method performs region-based matching between object model and test image based on colour image segmentation performed by the SPCNN with automatic parameters (Chen et al., 2011).

The proposed method could overcome the limitation of the feature-based methods that inevitably include background information into local invariant feature descriptors (Stein and Hebert, 2005), and the limitation of the feature-based methods that is incapable of identifying less-textured objects. As compared to the state-of-the-art OpponentSIFT, the proposed method showed encouraging results in identifying diverse objects from complex real-world scenes.

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