

# A GENERAL MOTION REPRESENTATION

## *Exploring the Intrinsic Viewpoint of a Motion*

Gutemberg Guerra-Filho

Department of Computer Science and Engineering, University of Texas at Arlington,  
500 UTA Blvd, Arlington, TX, U.S.A.

Keywords: Motion Capture Format, Motion Representation, Pre-rotation Transformation.

Abstract: We propose a novel motion representation, named General Motion Representation (GMR), which explicitly contains the absolute world coordinates of the meaningful joints, while still specifying every other joint with rotational data relative to their respective parent joints. More specifically, our representation supports multiple roots where any joint can be a root due to the use of a novel pre-rotation format for the construction of local transformation matrices. Hence, our general motion representation allows for all intermediate data structures between fully rotational and fully translational data. The use of multiple roots also implies the representation of partial motion considering a subset of joints. We introduce the general motion representation to consider multiple roots with the support of three operations (shift root, split skeleton tree, and join skeleton trees). These operations allow reduced skeletal complexity because of the application of pre-rotation local transformation matrices which eliminates the requirement for dummy joints. We also present procedures to convert from raw marker data or post-rotation formats. We demonstrate the highly efficient computation of per-frame joint positions and orientations. Our experimental results show that GMR outperforms traditional motion formats in both speed and flexibility. At the full translational configuration, GMR is around seven times faster than *bvh*.

## 1 INTRODUCTION

A fundamental issue for problems involving the synthesis and analysis of human movement is the representation for three-dimensional human motion. With regards to human motion representation, motion capture records the skeletal motion of a human body by reconstructing the evolution of the angles of articulated joints in a skeleton model.

In this paper, we address the problem of finding a skeletal motion representation that allows the explicit description of only the essential joints for a particular motion in terms of world coordinates while the non-essential joints are described by rotational data inferred according to a skeleton model. Formally, given a set  $M$  of three-dimensional points representing the Cartesian location of markers placed on the skin of the human subject at each time frame during motion capture; a skeleton model  $S(G, R)$  that consists of an adjacency graph  $G$  (where nodes represent articulated body parts and edges represent joints connecting these body parts) and a relation  $R$  between markers and body parts stating which markers belong to each body part; and a set  $E$

of essential joints; we want to find a motion representation such that essential joints are described by 3D Cartesian points and non-essential joints are described by rotational angles. Our main objective is to find algorithms to construct this generalized motion representation in order to consider any possible set of essential joints. The motion representation is obtained either from marker data (as stated above) or from other existing representations (*e.g.*, single-root motion capture data). A secondary objective is to develop the necessary operations to allow the transformation of the motion representation from any current set of essential joints  $E_o$  to any other target set of essential joints  $E_t$ .

We propose a novel motion representation, named General Motion Representation (GMR), which supports all combinations of root joint configurations (*i.e.*, any joint can be a root and multiple roots are supported), highly efficient computation of per-frame joint positions and orientations, and partial motion representations. This is only possible because we propose a more general method of constructing transformation matrices

using pre-rotation transformations instead of the standard post-rotation transformations in the bvh and asf/amc formats. The main contributions of this paper are: (1) a general motion representation that considers multiple roots, (2) the introduction of three operations to support this data structure (shift root, split skeleton tree, and join skeleton trees), (3) the procedures to convert from raw marker data or post-rotation formats (*e.g.*, bvh and asf/amc) to our pre-rotation format, and (4) experimental results showing the time and space performance of our new motion representation. At the full translational configuration, GMR is around seven times faster than bvh. Our experiments are centered on the rendering of joint positions. However, similar experiments based on the computation of joint coordinate frames are equivalent to ours since joint coordinate frames are necessary to the rendering of joint positions.

The remaining of this paper is organized as follows. Section 2 presents a review on work related to skeletal motion representation. Section 3 discusses the differences between existing post-rotation formats (bvh and asf/amc) and our pre-rotation format. Section 4 presents the General Motion representation and its three operations. Section 5 describes the generation of GMR from raw marker data or from a post-rotation format. Section 5 summarizes the experimental results on time and space performance comparing the bvh format and our GMR representation.

## 2 RELATED WORK

Existing motion capture formats, such as bvh and asf/amc, lack modeling flexibility by providing a single skeletal root joint for all motions. These formats implicitly restrict the choice of the root joint by requiring that the root's children behave as a rigid body (*i.e.*, a single rigid motion for all children of a joint). This restriction is a consequence of the way that local transformation matrices are composed to derive global coordinates for joints according to these formats. A formal proof of this fact is avoided here due to a lack of space. However, this rigid body constraint applies actually to any joint having more than one child in the skeleton tree. For this reason, artificial dummy joints are necessary to model independent motion for multiple children of a single joint. A simple inspection of existing motion files at joints with more than one child, in bvh format for example, suffices to verify the need for dummy joints to allow independently moving joints with a

single parent. This is a significant drawback of state-of-art motion representations by creating additional time and space requirements and algorithmic complications to handle exceptions and degeneracy in motion-based techniques.

In the area of skeletal motion representations, Brostow *et al.* (2004) introduced the concept of spines in order to discover an articulated creature's skeleton directly from time-varying volumetric structures. Coleman *et al.* (2008) introduce staggered poses as a generalization of poses in traditional key-framed motion. This generalization allows for explicitly encoded timing refinements, where each refinement is slightly offset in time. The relationships between these timing refinements determine how the character will pass through the extreme values of the pose and are important for modeling believable propagation of force and intention through a body. Kulpa *et al.* (2005) created a morphology-independent representation of motions for interactive human-like animation. Their aim was to enable real-time adaptive animation using a sparse motion capture database. Unlike their approach, our aim was to create a data structure with the flexibility to provide multiple root joints for the same motion.

Research has been done in the area of modeling figures with complex skeleto-muscular relationships based on human anatomy (Scheeper *et al.*, 1997). Complex motion control algorithms, which have been developed for primitive articulated models better suit robot-like characters than they do human figures (Magenat-Thalmann and Thalmann, 1991). GMR-based skeletal models more closely resemble actual human skeletons than post-rotation-based skeletal models because GMR does not require dummy skeletal joints.

## 3 POST-ROTATION AND PRE-ROTATION FORMATS

Existing motion representations compose each joint's local transformation matrix in a post-rotation order, which forces the children of each joint to behave as a rigid body. Existing post-rotation formats overcome this restriction through the use of artificial dummy joints which corresponds to additional time and space requirements. For example, when the pelvis is the root joint, the left hip joint, right hip joint, and lower back joint (the pelvis joint's children in the skeleton tree) cannot move independently of one another. More importantly, it is impossible to make any desired

joint the skeletal root when using a post-rotation format. For example, if the neck joint were to be the root, then the head, left shoulder, and right shoulder would not be able to move independently unless a cumbersome scheme with artificial dummy joints is used, which is clearly a problem.

To remedy the limitations of post-rotation formats, GMR composes each joint's local transformation matrix in a pre-rotation order that allows for any joint to be a root. We describe the post-rotation and pre-rotation concepts below.

### 3.1 Global Transformation Matrices

Here we describe the general approach for composing a joint's global transformation matrix from local transformation matrices. Let  $d$  indicate the depth of joint  $j$ ,  $p(j)$  indicate the parent of joint  $j$ , and  $p^k(j)$  indicate the  $k$ th ancestor of joint  $j$ . Note that the root joint is denoted by  $p^d(j)$ . Let  $L_j$  and  $M_j$  indicate the local and global transformation matrices for joint  $j$ , respectively. Let  $G_r$  indicate the transformation matrix with just the global offset of the skeleton. Then,

$$M_j = G_r L_{p^d(j)} \dots L_{p^2(j)} L_{p(j)} L_j \quad (1)$$

Let  $P_j$  indicate the 3-dimensional, homogeneous position of joint  $j$  described by multiplying  $M_j$  with the origin of the world coordinate system:

$$P_j = M_j \begin{bmatrix} 0 & 0 & 0 & 1 \end{bmatrix}^T$$

Also, let  $I$  indicate the 3x3 identity matrix, and  $o$  indicate the zero column-vector,

$$o = \begin{bmatrix} 0 & 0 & 0 \end{bmatrix}^T$$

### 3.2 Post-rotation Order

The bvh and asf/amc formats use the post-rotation order of composing local transformation matrices, as shown in the following equation,

$$L_j = \begin{bmatrix} I & t_j \\ o^T & 1 \end{bmatrix} \begin{bmatrix} R_j & o \\ o^T & 1 \end{bmatrix} = \begin{bmatrix} R_j & t_j \\ o^T & 1 \end{bmatrix}, \quad (2)$$

where  $R_j$  and  $t_j$  are the rotation matrix and the offset for joint  $j$ .

From Equations (1) and (2), note that the rotation  $R_j$  is not applied to the joint  $j$ . Consider the root  $r$  of a skeleton tree, the root's rotation is the only rotation that is applied to its children, which means that each of the root's immediate children cannot rotate independently of one another. Hence, the root and its

immediate children behave as a rigid body. This constraint is valid for any joint with more than one child in the skeleton tree.

This behavior limits the flexibility of all post-rotation formats because only certain joints can be roots. That is, any joint with more than a single child, where its immediate children do not behave as a rigid body, cannot be a root. For example, the neck joint cannot be a root.

### 3.3 Pre-rotation Order

The pre-rotation order of composing local transformation matrices is shown in the following equation,

$$L_j = \begin{bmatrix} R_j & o \\ o^T & 1 \end{bmatrix} \begin{bmatrix} I & t_j \\ o^T & 1 \end{bmatrix} = \begin{bmatrix} R_j & R_j t_j \\ o^T & 1 \end{bmatrix}, \quad (3)$$

where  $R_j$  and  $t_j$  are defined as in the post-rotation order. Equation (3) removes the restriction that a root and its children must behave as a rigid body. Intuitively, GMR gains this flexibility because each joint possesses its own independent rotation that is applied to both its children *and itself*.

## 4 THE GENERAL MOTION REPRESENTATION

The GMR format is structurally similar to post-rotation formats. A GMR file begins with a joint-based skeleton specification, with frame motion data following after. Each joint specifies a static offset from its parent joint, a list of required rotation channels ( $x$ -rotation,  $y$ -rotation,  $z$ -rotation), and a list of optional translation channels ( $x$ -translation,  $y$ -translation,  $z$ -translation). The order of the rotation channels specifies the order in which the rotation matrix should be composed.

### 4.1 GMR Operations

GMR has three basic operations that allow the conversion of a motion from a fully rotational representation to a fully translational representation, and all representations in between. We present the correctness proof for each operation in the supplemental material.

Now, we need a way to differentiate between symbols before and after one of the three GMR operations is applied. Let every symbol  $X_j$  indicate a value before an operation is applied, and every symbol  $X_j'$  indicate a value after an operation is

applied, where  $X$  is a rotation matrix, a translation vector, a local transformation matrix, or a global transformation matrix.

**4.1.1 Shift Root Operation**

The shift root operation is essentially a rotation of the skeleton tree, meaning that it swaps the existing root and one of its immediate children (see Figure 1). The repeated application of this operation allows for shifting the root to any desired joint in the skeleton tree.

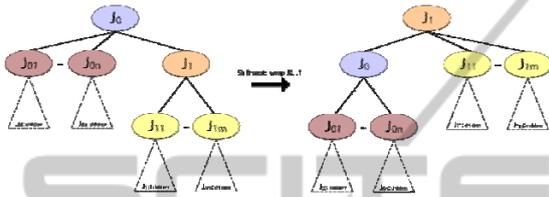


Figure 1: The skeleton tree before and after the shift root operation.

Using the notation defined in Section 3.2, we specify the solution for the shift root operation below. The following values should be recomputed for each frame of the motion:

$$\begin{aligned}
 G_0' &= R_0 R_1 t_1 + t_0, & t_1' &= o, \\
 R_1' &= R_0, & t_0' &= -t_1, \\
 R_0' &= R_1, & t_{0i}' &= t_{0i}, \\
 R_{0i}' &= R_1^{-1} R_{0i}, & t_{1j}' &= t_{1j}, \\
 R_{1j}' &= R_1 R_{1j}
 \end{aligned}$$

**4.1.2 Split Tree Operation**

The split tree operation creates an additional root by promoting an arbitrary joint to root status (see Figure 2). Repeated applications of this operation allow the conversion to a fully translational representation. That is, this operation allows for a representation where all joints are roots with 3D Cartesian coordinates. Intuitively, a skeleton with  $n$  joints may be represented as a single tree with  $n$  joints or as a forest with  $n$  trees with a single joint.

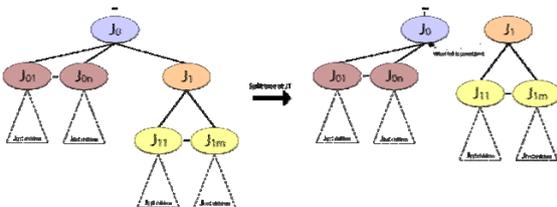


Figure 2: The skeleton trees before and after the split tree operation.

Let  $J_1$  be the joint to promote to root status and  $J_0$  be the parent of  $J_1$ .  $J_0$  may or may not have a parent joint. Note that the original tree structure is preserved by a “soft” link from  $J_1$  to its original parent,  $J_0$ . This link is necessary in order to undo this split tree operation in the join tree operation described next.

The global transformation matrix,  $M_1$ , for  $J_1$  before the split operation is

$$M_1 = G_r L_r \dots L_0 L_1 = \begin{bmatrix} R_s & t_s \\ o^T & 1 \end{bmatrix}, \tag{4}$$

where  $G_r$  is the transformation matrix with the global offset of the skeleton,  $L_r$  is the local transformation matrix for the root joint,  $R_s$  is the rotation matrix associated with  $M_1$ , and  $t_s$  is the translation vector associated with  $M_1$ . The calculation of  $J_1$ 's global transformation matrix changes after promoting  $J_1$  to root status, so

$$M_1' = G_1' L_1' \tag{5}$$

However, the global transformation matrix  $M_1'$  must be equal to  $M_1$ , so that we avoid changing the local transformation matrix for each child of  $J_1$ . This allows us to set Equation (4) equal to Equation (5):

$$M_1 = G_1' L_1' = \begin{bmatrix} R_s & t_s \\ o^T & 1 \end{bmatrix}. \tag{6}$$

Factoring Equation (6) and using the notation defined in Section 3.2, we specify the solution for the split tree operation. Note that, before the split,  $J_1$  did not possess a global translation, but after the split, it does. The following values should be recomputed for each frame of the motion:

$$\begin{aligned}
 R_1' &= R_s, \\
 t_1' &= o^T, \\
 G_1 &= \begin{bmatrix} I & t_s \\ o^T & 1 \end{bmatrix}.
 \end{aligned}$$

**4.1.3 Join Trees Operation**

The join trees operation is the inverse of the split tree operation. Where the split tree operation promotes an arbitrary joint to root status, the join trees operation demotes a root to a non-root joint status (see Figure 3). This operation fails if applied to the last remaining root, which is intuitively correct because a skeleton cannot have zero roots.

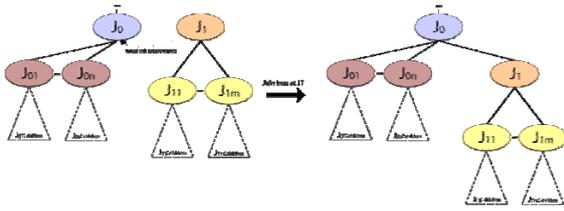


Figure 3: The skeleton trees before and after the joint tree operation.

Let  $J_1$  be the joint to demote and  $J_0$  be the original parent of  $J_1$  before a split operation.  $J_0$  may or may not have a parent joint. The global transformation matrix  $M_0$  for  $J_0$  is

$$M_0 = G_r L_r \dots L_0 \quad (7)$$

From the solution to the split operation, we know that  $M_1 = M_1'$ . Also, applying the concept that a joint's global transformation matrix may be constructed incrementally by multiplying the parent joint's global transformation matrix with the current joint's local transformation matrix, we have,  $M_1 = M_0 L_1$ . Moreover, since  $M_1 = M_1'$ , we have,  $M_0 L_1 = M_1'$ .

$L_1$  is the matrix that we are solving for to undo the effects of the split operation. Solving for  $L_1$ , we have,  $L_1 = M_0^{-1} M_1'$ . Furthermore, we make the following definitions:

$$M_0 = \begin{bmatrix} R_p & | & t_p \\ o^T & | & 1 \end{bmatrix}, \quad M_1' = \begin{bmatrix} R_s & | & t_s \\ o^T & | & 1 \end{bmatrix}.$$

Applying the pre-rotation form of constructing local transformation matrices from Equation (3), we have,

$$L_1 = \begin{bmatrix} R_1 & | & R_1 t_1 \\ o^T & | & 1 \end{bmatrix}.$$

Now, we specify the final solution to the joint trees operation. The following values should be recomputed for each frame of the motion:

$$\begin{aligned} R_1 &= R_p^{-1} R_s, \\ t_1 &= R_s^{-1} (t_s - t_p). \end{aligned}$$

## 5 GMR GENERATION

Ideally, GMR should be generated directly from marker-data obtained in the motion capture process. In this case, GMR will use the simplest, most

intuitive skeleton hierarchy possible, avoiding the use of dummy joints. The conversion from post-rotation formats, such as bvh and asf/amc is possible, but preserves undesirable artifacts of the post-rotation formats, such as the dummy joints.

### 5.1 From Marker Data

To convert directly from raw marker data to GMR, first we have to find the global transformations for the parent bone's coordinate system and the child bone's coordinate system. If we let  $M_c$  represent the global transformation for the child bone and let  $M_{p(c)}$  represent the global transformation for the parent bone, then to compute the incremental transformation from the parent coordinate system to the child coordinate system we construct the following equation,

$$M_c = M_{p(c)} L_c.$$

In the above equation,  $L_c$  is the local transformation matrix for the child bone. The derivation of  $L_c$  is nearly identical to the derivation of the solution for the GMR joint trees operation and has been omitted for the sake of brevity.

### 5.2 From a Post-rotation Order Representation

It is also possible to convert directly from a post-rotation order format, but doing so preserves undesirable features of the original formats. For example, a direct conversion from bvh to GMR preserves all joints, even the joints that are no longer required, such as the dummy joints contained in the original bvh format. An improved conversion method should automatically detect and remove dummy joints before creating the GMR skeleton. However, here we include the direct conversion method.

Let  $M_r$  be the root's global transformation matrix. We define these symbols as,

$$M_r = \begin{bmatrix} R_r & | & t_r \\ o^T & | & 1 \end{bmatrix}.$$

Now, let  $R_{p(j)}$  indicate the rotation for the parent of node  $j$  before conversion, where  $j$  is an internal or leaf node. For the sake of brevity, we only include the solution,

$$\begin{aligned} R_r' &= I, \\ t_j' &= t_j, \\ R_j' &= R_{p(j)}. \end{aligned}$$

## 6 EXPERIMENTAL RESULTS

We tested the time and space performance of bvh and GMR. We constructed an experiment that computes the position of each joint for each frame of motion. Our motion dataset consisted of 37 distinct bvh motion capture files with 14.223 total minutes of motion capture data (over 100,000 frames at 120 frames-per-second). We converted each bvh file to the GMR format, where we tested GMR performance using an optimized rendering loop that took advantage of translational information in root nodes. In the best case, GMR performs around 7 times faster than bvh. The results are summarized by the graph in Figure 4. Although the time cost is a single microsecond per frame in our experiments, this speed up is significant especially in the context of applications where very limited computation power is available such as gaming and humanoid robotics.

The left-most GMR point on the graph contains one single root, while the right-most GMR point on the graph contains 26 roots. For this experiment, we define a GMR configuration  $C_k$  as a GMR containing  $k$  roots, for  $k = 1, \dots, 26$ . We constructed ten GMR instances  $C_k$  for each  $k$  by selecting random sets of  $k$  joints as roots, in order to ensure fairness and prevent artificially inflated performance results. We then recorded the performance of each instance. To compute the data points on the graph above, we averaged the recorded times for GMR configurations with matching numbers of roots.

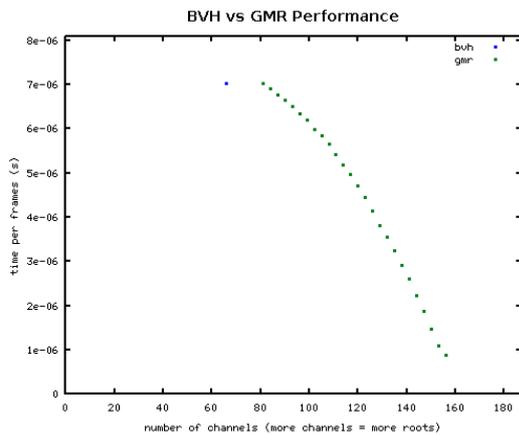


Figure 4: Performance of GMR configurations compared with BVH.

## 7 CONCLUSIONS

We introduced the general motion representation to

consider multiple roots with the support of three operations (shift root, split skeleton tree, and join skeleton trees). These operations allow reduced skeletal complexity because of the application of pre-rotation local transformation matrices which eliminates the requirement for dummy joints. We also present procedures to convert from raw marker data or post-rotation formats.

We also demonstrate the highly efficient computation of per-frame joint positions and orientations. Our experimental results show that GMR outperforms traditional motion formats in both speed and flexibility. At the full translational configuration, GMR is around seven times faster than bvh. These benefits make GMR a good candidate for computationally intensive, time-sensitive tasks such as real-time gaming applications. With respect to alternate viewpoints, GMR also opens many avenues of research that were once difficult to explore. Additionally, GMR retains the familiarity and simplicity of expression of the BVH file format.

## REFERENCES

- Brostow, G., Essa, I., Steedly, D., Kwatra, V., 2004. Novel skeletal representation for articulated creatures. *Lecture Notes in Computer Science*, vol. 3023, pp. 66-78.
- Coleman, P., Bibliowicz, J., Singh, K., Gleicher, M., 2008. Staggered poses: A character motion representation for detail-preserving editing of pose and coordinated timing. In *Symposium on Computer Animation*, pp. 137-146.
- Kulpa, R., Multon, F., Arnaldi, B., 2005. Morphology-independent representation of motions for interactive human-like animation. *Computer Graphics Forum*, vol. 24, pp. 343-351.
- Magenat-Thalmann, N., Thalmann, D., 1991. Complex models for animating synthetic actors. *IEEE Computer Graphics and Applications*, vol. 11, no. 5, pp. 32-44.
- Scheepers, F., Parent, R., Carlson, E., May, S., 1997. Anatomy-based modeling of the human musculature. In *Annual Conference on Computer Graphics and Interactive Techniques*, pp. 163-172.