

BAYESIAN NETWORK ANALYSIS OF RELATIONSHIPS BETWEEN NUCLEOSOME DYNAMICS AND TRANSCRIPTIONAL REGULATORY FACTORS

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Abstract: Intergenic regions are unstable, owing to *trans*-regulatory factors that regulate chromatin structure. Nucleosome organization at promoter has been shown to exhibit distinct patterns corresponding to the level of gene expression. Post-translational modifications (PTMs) of histone proteins and transcriptional regulators, including chromatin remodeling complexes (CRCs), general transcription factors (GTFs), and RNA polymerase II (PolII), are presumably related to the establishment of such nucleosome dynamics. However, their concrete relationships, especially in gene regulation, remain elusive. We, therefore, sought to understand the functional linkages among these factors and nucleosome dynamics by deriving a Bayesian network (BN)-based model representing their interactions. Based on the recovered network, learnt from 8 PTMs and 15 transcriptional regulators at 4034 *S.cerevisiae* promoters, we speculate that nucleosome organization at promoter is intentionally volatile in various regulatory pathways. Notably, interactions of CRCs/GTFs and H3 histone methylation were inferred to co-function with nucleosome dynamics in gene repression and pre-initiation complex (PIC) formation. Our results affirm the hypothesis that extrinsic factors take part in regulating nucleosome dynamics. More thorough investigation can be made by adding more factors and using our proposed method.

1 INTRODUCTION

Eukaryotic genomes are packaged inside cell nucleus under chromatin structure like a bead-on-string fiber of nucleosomes. As a fundamental unit, nucleosome contains a core of octamer histone proteins wrapped around by 147bp of DNA (Luger et al., 1997). More than DNA packaging, chromatin involves in various cellular processes such as transcription, DNA replication, etc., by occluding the access of biological machineries to *cis*-regulatory elements and/or modifying related epigenetic information. To overcome the obstacle imposed by chromatin, cells have developed complicated pathways (Li et al., 2007), in which nucleosome must be dislocated from chromatin to provide access to the underlying DNA sequences. While positioning are strongly influenced by intrinsic DNA sequence preference (Kaplan et al., 2010), the rearrangement can be flexibly modulated by extrinsic factors, e.g., DNA-binding factors and CRCs (Wan et al., 2009). They help to maintain the periodicity, hence the corresponding transcription activities, by directly altering nucleosome organization in various manners (Venters and Pugh, 2009). PTMs were shown in vari-

ous works to be related to nucleosome spatial organization (Cui et al., 2010). These two factors interact in that PTMs serve as their targeting marks, and in turn, the locations of PTMs is modulated by those regulatory proteins. Such series of highly regulated interactions may necessarily be characterized by a network featuring variable correlations. Since the data in use here are all related to transcriptional activities, we referenced to the common resulting effects on gene expression to infer possible functional linkages.

Taken together, we speculated that in complex interaction network, the nucleosome dynamics at promoter may play an intermediate role, i.e. affecting as well as being affected by other factors, in regulatory pathways, assuming that there are two classes of promoters, *unstable* with periodic nucleosome arrangements, and *stable* without. We employed Bayesian network (BN), a class of probabilistic graphical models that can capture not only co-occurrence pattern but also interaction/dependency among variables, for interaction modeling. BN has been used to reconstruct many kinds of cellular networks, such as gene regulatory networks and protein interaction networks (Friedman et al., 2000). Compared with previous

findings, we showed that the built network can recover known relationships as well as functional linkages consistent with knowledge about various DNA-mediated processes.

2 METHOD

2.1 Datasets

The experimental data of 24 features *Saccharomyces cerevisiae* were gathered as follows: Two classes of 4043 yeast promoters, including 1355 *unstable/dynamic* (no periodicity and high expression) and 2688 *stable* (explicit periodicity and low expression) were obtained from (Wan et al., 2009); 8 PTMs (from -1000bp to TSSs) were obtained from (Pokholok et al., 2005); 15 transcriptional regulators including 6 GTFs, 1 PolII component, and 8 CRCs from (Venters and Pugh, 2009). Data was discretized using proportional k-interval discretization (PIKD) (Yu et al., 2008) with intervals of [33%, 66%], [20%, 80%], [40%, 60%], and determined by K-means clustering ($k = 3$). As a result, [20%, 80%] proportional 3-interval scheme gave us the most reasonable network (data not shown).

2.2 Bayesian Networks

2.2.1 Definition

A Bayesian network for a set of variables $\mathbf{X} = \{X_1, X_2, \dots, X_n\}$ is a probabilistic model consisting of two components (Heckerman, et al., 1995):

- A network structure S , which is a directed acyclic graph, representing conditional (in)dependence relationships among variables in \mathbf{X}
- A set P of local probability distributions associated with each variable.

Because the main target of our work is to uncover the relationships among the PTMs so we are interested in the problem of learning BN structure. We employed the score-based search method (Jensen and Nielsen, 2007) to learn a BN structure representing relationships among PTMs. To score a candidate network, we used a Bayesian scoring metric, namely BDe (Bayesian metric with Dirichlet prior and equivalence) (Heckerman, et al., 1995).

2.2.2 Bootstrapping and Selection of Cut-off Threshold

The search-and-score method generates a different network on each run, and only one with highest score

is output. Hence, we employed the bootstrapping method (Friedman et al., 2000) to estimate the confidence level for each edge in the resulting network. Then following hybrid method was proposed to derive a suitable threshold value for confidence level of each edge in the resulting network:

1. Divide data into n datasets using n -fold cross-validation, t times.
2. At each time, n bootstrapped consensus BNs $N_1 \dots N_n$ are output, using a fixed τ . Then, n cross-validated networks are combined into one by including edges agreed by θ graphs. Thus, with each pair of (τ and θ), one final network N is learnt.
3. To measure the goodness of the learnt network, accuracy (acc) and coverage (cov) are used and plotted as receiver operating characteristic (ROC) curve. Co-ordinates of each point in the curve is the average of t times (with standard deviation). The chosen network has τ and θ that generate the largest area under the curve (AUC).

$$acc_i = \frac{\#(N_i \cap N)}{\#N_i}, cov_i = \frac{\#(N_i \cap N)}{\#N}, i = 1, \dots, n \quad (1)$$

where the numerator is the number of overlapping edges of each network with the common one; the denominator is the number of edges in each network and the common one, respectively.

In our experiment, we split data into 5 datasets (according to 5-fold cross-validation) for $t = 50$ times; on each, we bootstrapped 100 times ($m = 100$), which totally resulted in 25,000 input datasets for learning. Each edge in the consensus network has a related confidence score, measured by the number of times it appears in 100 bootstrapped ones. Threshold τ was chosen in the range of [0.5, 0.8] with the step of 0.05. The combined network consisted of overlapping edges by $\theta = \{2, 3, 4\}$ cross-validated ones. We then chose parameters $\theta = 3$ and $\tau = 0.65$ to produce a network with 24 features as its nodes and 36 edges representing the functional linkages among PTMs, transcriptional regulators, and nucleosome dynamics (Fig. 1).

3 RESULTS AND DISCUSSION

3.1 Network Recovers Reliable Functional Linkages

Comparing our network (Fig. 1) with previous findings, we found a remarkable consistency with original results reported in (Venters and Pugh, 2009). CRCs

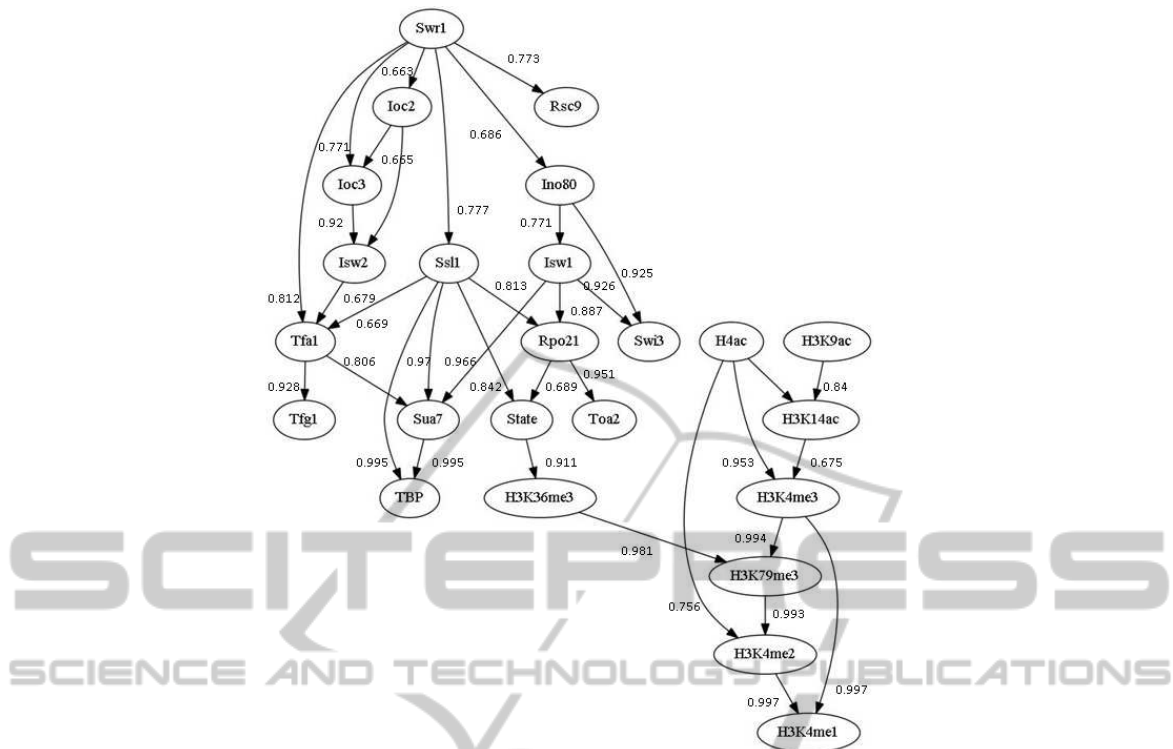


Figure 1: PTMs, TFs, and nucleosome dynamics network with confidence level (in range [0,1]). Note that the edge directionality does not show definite causality, due to the nature of the learning algorithm; thus in most cases, we inferred correlations or interactions among network nodes.

with subunits such as *Swr1*, *Ioc2*, *Ioc3*, *Ino80*, etc., appear in the upper part of the network, showing causal relationships towards GTFs, which generally reflects the role of CRCs as an ATP-dependent nucleosome translocator giving way to GTFs accessing the buried DNA. From the network topology, it is clear that nucleosome dynamics bridges two groups of transcriptional regulators and PTMs, for which, unfortunately, we have yet to find direct evidence. Nodes of high out degree (number of edges pointing away from node), such as *Swr1* (out degree of 6) and *Ssl1* (out degree of 5), may play a central role; *Swr1*, (subunit of *SWR-C*), is implicated in the deposition of histone variant *H2A.Z* in promoter, which provides a molecular mechanism to regulate transcription and DNA repair (Luksend et al., 2010). Especially, together with *NuA4*, an essential histone acetyltransferase, they function in *NuA4/SWR-C/H2A.Z* pathway to regulate chromosome stability.

3.2 Nucleosome Dynamics in Regulatory Processes

3.2.1 PIC Formation by GTFs and PolIII Affects Nucleosome Dynamics

It is agreed that GTFs assemble at promoter to form pre-initiation complex (PIC). The interactions among them have been well investigated, and the related subgraph ($TFIIH(Ssl1) \rightarrow TFIIIE(Tfa1) \rightarrow THIE(Tfg1) \rightarrow TFIIIB(Sua7) \rightarrow TBP \rightarrow PolIII(Rpo21) \rightarrow State$ in our network is consistent with previous findings (Samorodnitsky and Pugh, 2010). Especially, these factors were considered in (Samorodnitsky and Pugh, 2010), a modeling work (PathCom) towards the ordering of PIC assembly/disassembly at the genes of yeast. The proposed assembly order was recruitment of *TBP*, *TFIIIB* first, then *PolIII* and other GTFs (*TFIIIB*, *TFIIIE*, *TFIIF*, *TFIIH* in order); disassembly goes backwards. Interpretation from our network that the binding of factor at child node correlates with that of parent node in an order manner, i.e., the binding of parent affects that of child, not vice versa, is reasonably consistent with this model. Hence, from our network, nucleosome organization (node *State*) may

inferably alter along with PIC forming (most importantly, *PolIII*), which well matches with the known hypothesis that nucleosome dynamics facilitates access to GTFs (Morse, 2007) and CRCs.

3.2.2 Limited Gene Expression by CRCs is Related to Periodic Nucleosome Organization at Promoter

We analyzed the chain of *SWR-C(Swr1) → INO80(Ino80) → ISW1a/b(Isw1) → PolIII(Rpo21) → State* to understand the mechanism of gene repression, which is observable in our data as the periodic nucleosome organization of limitedly expressed genes. As pointed out in (Lindstrom et al., 2006), *Isw1* shows parallel functions with *NuA4* and *Swr1* complexes in repressing genes. *ISW1a/b* plays a role in repressing transcription (Pinskaya et al., 2009). Hence, the interactions of *Swr1*, *NuA4*, *Isw1*, and *Rpo21* at promoter can reasonably reason the gene repressing directionality. In our network, however, *INO80* stands as a bridge between *Swr1* and *Isw1*, which is explainable because *INO80* is essential in *H2A.Z* correct deposition (Lindstrom et al., 2011) and may catalyze the removal of unacetylated *H2A.Z*. We, therefore, speculated that the presence of *NuA4* as histone acetyltransferase and *INO80* as remover of unacetylated *H2A.Z* at promoter in repressing pathway defines the low level of gene expression; and that in the pathway, *INO80* help establishing the periodicity of nucleosome organization.

4 CONCLUSIONS

We present here the reconstruction of interaction network among various PTMs and transcriptional regulators, with focus on their relationships with the dynamic nucleosome organization at promoter. Having a large number of relationships correctly recovered, the network features the regulatory processes that show their presence by changing nucleosome organization at promoter, e.g., gene repression, postinitiation regulation and PIC assembly/disassembly. Also, we provide evidences for the hypothesis that nucleosome dynamics at promoter is regulated by extrinsic factors, such as CRCs and GTFs. With these results, the reliability of our method is proved, in addition to the proposed valid learning procedure; hence, it can be used to build networks of other factors.

REFERENCES

- Cui, P., Zhanga, L., Lina, Q., Dinga, F., Xina, C., Fanga, X., Hua, S., and Yua, J. (2010). A novel mechanism of epigenetic regulation: Nucleosome-space occupancy. 391(1):884–89.
- Friedman, N., Linial, M., Nachman, I., and Peer, D. (2000). Using bayesian networks to analyze expression data. 7(3-4):601–20.
- Heckerman, D., Geiger, D., and Chickering, D. (1995). Learning bayesian networks: The combination of knowledge and statistical data. 20:197–243.
- Jensen, F. and Nielsen, T. (2007). Bayesian Networks and Decision Graphs. Springer-Verlag, New York, 2nd edition.
- Kaplan, N., Moore, I., Fondufe-Mittendorf, Y., Gossett, A., Tillo, D., Field, Y., Hughes, T., Lieb, J., Widom, J., and Segal, E. (2010). Nucleosome sequence preferences influence in vivo nucleosome organization. 17:918–20.
- Li, B., Carey, M., and Workman, J. (2007). The role of chromatin during transcription. 128(4):707–19.
- Lindstrom, K., Vary, J., Parthun, M., Delrow, J., and Tsukiyama, T. (2006). *Isw1* functions in parallel with the *nua4* and *swr1* complexes in stress-induced gene repression. 26(16):6117–29.
- Lindstrom, K., Vary, J., Parthun, M., Delrow, J., and Tsukiyama, T. (2011). Global regulation of *h2a.z* localization by the *ino80* chromatin-remodeling enzyme is essential for genome integrity. 144(2):200–13.
- Luger, K., Mader, A., Richmond, R., Sargent, D., and Richmond, T. (1997). Crystal structure of the nucleosome core particle at 2.8 Å resolution. 389:251–60.
- Luksend, E., Ranjan, A., FitzGerald, P., Mizuguchi, G., Huang, Y., Wei, D., and Wu, C. (2010). Step-wise histone replacement by *swr1* requires dual activation with histone *h2a.z* and canonical nucleosome. 143(5):725–36.
- Morse, M. (2007). Transcription factor access to promoter elements. 102(3):560–70.
- Pinskaya, M., Nair, A., Clynes, D., Morillon, A., and Mellor, J. (2009). Nucleosome remodeling and transcriptional repression are distinct functions of *isw1* in *saccharomyces cerevisiae*. 29(9):241930.
- Pokholok, D., Harbison, C., Levine, S., Cole, M., Hannett, N., Lee, T., Bell, G., Walker, K., Rolfe, P., Herbolsheimer, E., Zeitlinger, J., Lewitter, F., Gifford, D., and Young, R. (2005). Genome-wide map of nucleosome acetylation and methylation in yeast. 122(8):517–27.
- Samorodnitsky, E. and Pugh, B. (2010). Genome-wide modeling of transcription preinitiation complex disassembly mechanisms using chip-chip data.
- Venters, B. and Pugh, B. (2009). A canonical promoter organization of the transcription machinery and its regulators in the *saccharomyces* genome. 19(3):360–71.
- Wan, J., Lin, J., Zack, D., and Qian, J. (2009). Relating periodicity of nucleosome organization and gene regulation. 25(41):1782–8.
- Yu, H., S, S. Z., Zhou, B., Xue, H., and Han, J. (2008). Inferring causal relationships among different histone modifications and gene expression. 18(8):1314–24.