

DIFFERENTIAL EVOLUTION TO MULTI-OBJECTIVE PROTEIN STRUCTURE PREDICTION

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Abstract: Protein structure prediction (PSP) is one of the most challenging problems nowadays and an important Bioinformatics research topic. In this paper we propose an optimization method based on differential evolution for PSP problem. We model PSP as an optimization problem in order to minimize the potential energy using *ab initio* approach. This problem is handled here as multi-objective optimization, and it is solved by the evolutionary method of Differential Evolution (DE). An innovative way of choosing the best individual of the population is proposed in this work: the minimum distance to the empirical ideal point. The idea is to guide the population individuals to areas of the Pareto front that correspond to a good compromise of the bonded and non-bonded energies. The proposed approach is validated on some peptides with promising results.

1 INTRODUCTION

Proteins are composed of one or more polypeptide chains, each one containing from several to hundreds or even thousands amino acids, and are responsible for many different biological functions.

In order to understand the functions of proteins at a molecular level, it is often necessary to determine their three dimensional structure. Indeed, this information is important to design new drugs capable of combating diseases (Cohen and Kelly, 2003). When a protein is in its folded state, its free energy conformation is the lowest one.

In this paper we propose an optimization method based on differential evolution (DE) for Protein Structure Prediction (PSP), the MODE-P - *Multi-Objective Differential Evolution for PSP problem*. We model PSP as an optimization problem in order to minimize the potential energy. This problem is handled here as multi-objective optimization, to be solved by the evolutionary method of DE. Our approach is an attempt to contribute to the PSP problem by means of an evolutive method - that uses a different way for picking the individual that will guide the evolutionary process.

2 BACKGROUND

DE is a stochastic, population-based search strategy developed by Storn and Price (Storn and Price, 1997). Summarized, DE adds the weighted difference between two population vectors (difference vectors) to a third vector (target vector). The term *differential evolution* comes from the fact that the process of this evolutionary algorithm is based on *difference* between individuals in the population. In this paper we used DE/*best/1/bin* variation, where (Storn and Price, 1997).

General Multi-Objective Optimization Problem (MOP) is defined as minimizing (or maximizing) $F(x) = (f_1(x), \dots, f_k(x))$ subject to $g_i(x) \leq 0$, $i = \{1, \dots, m\}$, and $h_j(x) = 0$, $j = \{1, \dots, p\}$ $x \in \Omega$. A solution minimizes (or maximizes) the components of a vector $F(x)$ where x is a n -dimensional decision variable vector $x = (x_1, \dots, x_n)$ from some universe Ω .

In this work we use CHARMM (v.27) force field calculated as a function of terms for internal (bonded) and external (interaction or non-bonded) contributions. They represent the two objective functions to be separately minimized in the evolutionary process.

The concept of empirical ideal point used in this work to select the best individual in DE is: let $z^* = (z_1^*, z_2^*, \dots, z_i^*)$, where $z_i^* \in Z$ is such that $f_i(x_i^*) = \min f_i(x), x \in A \cup B$ and A represents the solutions int

the current population and B represents the solutions in non-dominated archive. Z contains all possible values that can be assumed by $F(x)$. In this work, the decision maker choose the final solution based on the empirical ideal point.

Our approach has its contribution relative to other works ((Cutello et al., 2006), (Tudela and Lopera, 2009), (Becerra et al., 2010)) in the use and test of DE with an innovative way of choosing the best individual used during differential mutation based on the empirical ideal point. Also, instead of using the knee concept (Coello et al., 2007), like most of the above approaches does, our decision maker also uses the empirical ideal point concept.

3 MODE-P

In the current work, in order to represent the candidate solutions, we adopt a model based on off-lattice and an internal coordinates representation - the torsion angles - with backbone and sidechain torsion angles to model proteins. Each residue type has a pre-established number of torsion angles in order to reach a conformation of a protein. The backbone of each residue is represented by 3 dihedral angles: ϕ , ψ , ω . The sidechains are represented by χ_i angles.

In order to reduce the search space, we use the restricted range of angles showed in Sun et al. (1997). The secondary structure constraints for peptides were predicted here using Pollastri et al. (2002).

Our proposed approach is called MODE-P (Multi-Objective Differential Evolution for PSP problem), follows the basic scheme of DE with some modifications to deal with the bi-objective PSP problem. The process involves the identification of non-dominated solutions, their storage and further inclusion into the population. In order to store the non-dominated solutions the same storage procedure applied in Pareto Archived Evolution Strategy (PAES) is used. The whole procedure of MODE-P is presented by the following algorithm.

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Reset the generation counter,  $g = 0$ ;
Initialize the control parameters,  $F$  and  $CR$ ;
Create and initialize the population,  $pop(0)$ ,
  of  $ns$  individuals accordingly to the
  secondary structure constraints regions;
Evaluate  $pop(0)$ ;
Create nondominated archive,  $ND\_archive$ 
for  $g = 1$  to  $MAX\_GEN$  Do
  for each individual,  $x_i(g)$  belonging to
     $pop(g)$  do
    Select the best individual;
    Randomly select two distinct individuals;
    Create the trial vector,  $u_i(g)$  by

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    applying the mutation operator;
  Create an offspring,  $x'_i(g)$ , by
    applying the crossover operator;
  Evaluate  $(x'_i(g))$ ;
  if  $(x_i(g)$  dominates  $x'_i(g))$ 
    discard  $x'_i(g)$ 
  else
    if  $(x'_i(g)$  dominates  $x_i(g))$ 
      Update  $ND\_archive$ ;
      Replace  $x_i(g)$  by  $x'_i(g)$  in  $g$ 
    else
      if  $(x_i(g)$  and  $x'_i(g)$  are nondominated)
        and
        ( $x'_i(g)$  is nondominated by  $ND\_archive$ )
          Update the  $ND\_archive$ ;
          Replace  $x_i(g)$  by  $x'_i(g)$  in  $g$ 
    end for
  end for
end for

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For each parent individual, the routines of DE/*best/1/bin* are executed.

The evaluation phase calculates potential energy from the set of angles using TINKER Molecular Modelling Package to compute the bond and non-bond energy values accordingly to the CHARMM force field model.

The choice of the best individual is based on the solution that has the shortest euclidean distance from the empirical ideal point of the current generation. The empirical ideal point is composed by the current minimum values found separately for bond energy and nonbond energy at that exact moment in the evolution. This way for choosing the best individual is a contribution of this work.

At the end of the evolutionary process, the archive with nondominated solutions is returned to the decision maker. In this work, the decision maker choose the final solution based on the empirical ideal point. The individual who has shortest euclidean distance from the empirical ideal point is returned to user.

4 EXPERIMENTS AND RESULTS

This section reports the results obtained for 30 independent runs (with different seeds for each run) of MODE-P algorithm. The population size is 400 chromosomes and the number of generations is 350. The DE parameters, CR and F , are set as equal to 0.7 and 0.2, respectively. In order to assess how similar is the predicted conformation to the native structure, the RMSD (Root Mean Square Deviation) metric is used (Tramontano, 2006).

MODE-P was applied to *Met-Enkephalin* peptide (1PLW) and two others protein sequences from PDB (Protein Data Bank): *Crambin* (1CRN) and *Disulphide-stabilized mini protein A domain* (1ZDD).

Table 1 summarizes the results for each protein. MODE-P decision maker is applied to the archive with nondominated solutions of the best run. We assume that the *best run* is the one that returned the individual with the lowest energy among all executions.

Met-Enkephalin is a polipeptide with 5 amino acids used as classical test for algorithms designed for PSP problem. Decision maker found the solution with energy value of $-33.11 \text{ kcal mol}^{-1}$ that matches the crystal structure of 1PLW obtained from PDB with $\text{RMSD}_{\text{all-atoms}} = 3.144 \text{ \AA}$ e $\text{RMSD}_{C\alpha} = 1.814 \text{ \AA}$. Figure 1 shows the comparison between predicted conformation chosen by MODE-P decision maker and 1PLW.



Figure 1: Comparison between predicted conformation (black) and 1PLW conformation for Met-enkephalin peptide. Figure generated by PyMOL.

1CRN is a 46-residue protein with two α -helix and a pair of β -strands. MODE-P decision maker found the solution with energy value of $408.53 \text{ kcal mol}^{-1}$ that matches the crystal structure from PDB with $\text{RMSD}_{\text{all-atoms}} = 5.590 \text{ \AA}$ e $\text{RMSD}_{C\alpha} = 5.559 \text{ \AA}$. Figure 2 shows the comparison between predicted conformation chosen by MODE-P decision maker and the crystal structure of 1CRN.

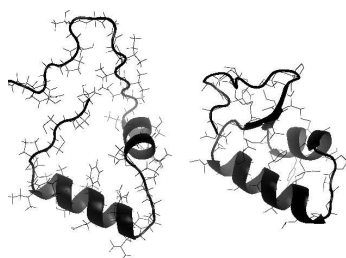


Figure 2: Comparison between predicted conformation (left) and 1CRN protein. Figure generated by PyMOL.

1ZDD is a two-helix peptide of 34 residues. Decision maker found the solution with energy value of $-1050.85 \text{ kcal mol}^{-1}$ that matches the crystal structure from PDB with $\text{RMSD}_{\text{all-atoms}} = 6.213 \text{ \AA}$ e $\text{RMSD}_{C\alpha} = 3.846 \text{ \AA}$. Figure 3 shows the comparison between predicted conformation chosen by MODE-P decision maker and the crystal structure of 1ZDD.

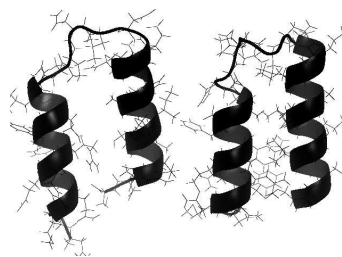


Figure 3: Comparison between predicted conformation (left) and 1ZDD protein. Figure generated by PyMOL.

Table 1: Results obtained by MODE-P for peptides.

Protein	Amino acids	Energy (kcal mol ⁻¹)	RMSD _{Cα} (Å)
<i>Met-Enkephalin</i>	5	-33.11	1.814
1CRN	46	408.53	5.559
1ZDD	34	-1050.85	3.846

We compared the results of MODE-P algorithm with other approaches in the literature.

Table 2 shows the results achieved by our proposed approach (MODE-P) when compared with the ones provides by Cutello et al. (2006) for *Met-enkephalin* peptide.

Table 2: Results for *Met-Enkephalin* peptide.

Algorithm	Energy (kcal mol ⁻¹)	RMSD (Å)	RMSD _{Cα} (Å)
MODE-P	-33.11	3.144	1.814
I-PAES (Cutello et al., 2006)	-20,56	3.605	1.740

Table 3 reports the comparison of MODE-P versus other approaches for 1CRN and Table 4 compares MODE-P with others two approaches for 1ZDD. The RMSD_{C α} values do not appear in these tables because such measures have been omitted in the considered literature.

Table 3: Results for 1CRN protein.

Algorithm	Energy (kcal mol ⁻¹)	RMSD _{Cα} (Å)
MODE-P	408.53	5.559
I-PAES (Cutello et al., 2006)	701.25	4.43
Dandekar and Argos (1996)	–	5.4
NSGA2 (with high-level operators) (Cutello et al., 2006)	–	6.447
NSGA2 (with low-level operators) (Cutello et al., 2006)	–	10.34

The results show that MODE-P is competi-

tive when compared with the literature. For *Met-enkephalin* e 1CRN, MODE-P proved to be a good optimizer considering the potential energy values. Its values are smaller than those in the literature, associate with good RMSD values. In particular case of *Met-enkephalin*, for instance, potential energy and RMSD_{all-atoms} values obtained by MODE-P are better than the comparison approach. For 1ZDD the values in terms of energy and RMSD were competitive to others approaches.

Table 4: Results for 1ZDD protein.

Algorithm	Energy (kcal mol ⁻¹)	RMSD _{Cα} (Å)
MODE-P	-1050.85	3.846
I-PAES (Cutello et al., 2006)	-1052.09	2.27
GA (Dorn et al., 2011)	-983.27	3.92

5 CONCLUSIONS AND FUTURE WORKS

This paper has presented a multi-objective evolutionary algorithm for PSP problem with *ab initio* approach. The evaluation of the conformation of a protein is estimated using energy values of local and non-local interactions in order to compose the potential energy.

The results obtained suggest that MODE-P can predict small proteins structures with competitive values compared with other works in literature. The innovative way for choosing the best individual in a multi-objective differential evolution proved to be a good option to be used during the evolutionary process.

As future work we intend to expand MODE-P to deal with medium size proteins and investigate alternative methods for decision maker.

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