SIMULATION STUDY OF TISSUE TYPE DIFFERENTIATION USING NON-NEGATIVE MATRIX FACTORIZATION

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Abstract: Finding the brain tumor tissue-specific magnetic resonance spectra and their corresponding spatial distribution is a typical Blind Source Separation (BSS) problem. Non-negative Matrix Factorization (NMF), which only requires non-negativity constraints, has become popular because of its advantages compared to other BSS methods. A variety of algorithms based on traditional NMF have been recently proposed. This study focuses on the performance comparison of several NMF implementations, including some newly released methods, in brain glioma tissue differentiation using simulated magnetic resonance spectroscopic imaging (MRSI) signals. Experimental results demonstrate the possibility of finding typical tissue types and their distributions using NMF algorithms. The (accelerated) hierarchical alternating least squares algorithm was found to be the most accurate.

1 INTRODUCTION

Automatic tissue type differentiation in brain tumor patients is of utmost importance in guiding therapy and determining prognosis. Magnetic resonance spectroscopic imaging (MRSI) (Brown et al., 1982), which produces localized spectra, is used as a noninvasive tool for additional clinical diagnosis of brain tumors; see Figure 1. Given an $m \times n$ matrix X which represents the observed spectra from MRSI data, each column containing a spectrum from one voxel, previous studies (Su et al., 2008) demonstrated that X can be approximately described as a linear combination of constituent specta of different tissue types. The model is

$$X = WH + N \tag{1}$$

W is a $m \times r$ matrix, with each column representing a recovered spectrum for each tissue type. Each row of the $r \times n$ matrix H contains the linear combination weights (interpreted here as abundances or concentrations) of all constituent tissue spectra. N stands for additive measurement noise.



Figure 1: Left: anatomic image of a glioma patient's brain overlaid with the MRSI grid. Right: the spectral profile from the blue voxel from the tumor area.

Blind Source Separation (BSS) is one of the main approaches to perform such factorization. One of the algorithms, non-negative matrix factorization (NMF) (Lee et al., 1999), has attracted much

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attention in recent years because it does not require the constituent spectra to be orthogonal or independent. The mathematical formulation of the basic NMF problem is

$$\min_{W,H} f(W,H) = \frac{1}{2} ||X - WH||_F^2$$
subject to $\forall ij, W_{ii}, H_{ii} \ge 0$
(2)

In this paper, we designed a simulation study aiming to evaluate the accuracy of several popular NMF implementations in solving the brain glioma tissue type differentiation problem. The algorithms' performance was investigated specifically in terms of their accuracy to estimate tissue-specific spectra and their spatial distribution.

2 NMF ALGORITHMS

In this section we describe several NMF algorithms that will be compared in Section 4.

 Multiplicative update method using Euclidean distance measure (mu) (Lee et al., 2001):

This algorithm is used most commonly in solving the NMF problem. It uses the Euclidean distance as a measure to construct the cost function $||X - WH||^2$. The cost function is minimized using the update rule:

$$H_{kj} \leftarrow H_{kj} \frac{(W^T X)_{kj}}{(W^T W H)_{kj}}$$
$$W_{ik} \leftarrow W_{ik} \frac{(X H^T)_{ik}}{(W H H^T)_{ik}}$$
(3)

$$\forall i, j, k$$

• Alternating least squares (als) (Berry et al., 2007): This algorithm alternately solves unconstrained least squares subproblems for *W* and *H* (see Eq. 4) and sets the negative elements to zero.

$$W \leftarrow \arg\min || X - WH ||_F^2$$

$$H \leftarrow \arg\min || X - WH ||_F^2 \qquad (4)$$

Alternating non-negative least squares using projected gradients (cjlin) (Lin, 2007): In this implementation, non-negatively constrained least squares subproblems are solved alternatively for W and H using the projected gradient method. Consider the following standard form of boundconstrained optimization problems:

$$\min_{x \in \mathbb{R}^n} f(x)$$
subject to: $l_i \le x_i \le u_i, \quad i = 1,...,n$
(5)

Projected gradient methods are iterative and update the current solution x^k to the following x^{k+1} by the rule:

$$x^{k+1} = P[x^k - \alpha^k \nabla f(x^k)] \tag{6}$$

where α^k is the step size and

$$P[x_i] = \begin{cases} x_i & \text{if } l_i < x_i < u_i \\ u_i & \text{if } x_i \ge u_i \\ l_i & \text{if } x \le l_i \end{cases}$$

Hierarchical alternating least squares (hals) (Cichocki et al., 2007; Cichocki et al., 2009): hals sequentially estimates one column of W and/or one row of H while fixing all the other ones, that is:

$$W_{k} \leftarrow \arg \min_{W_{k} \ge 0} ||X - WH||_{F}^{2} =$$

$$\arg \min_{W_{k} \ge 0} ||X - W_{-k}H_{-k} - W_{k}H_{k}||_{F}^{2} \qquad (7)$$

$$H_{k} \leftarrow \arg \min_{H_{k} \ge 0} ||X - WH||_{F}^{2} =$$

$$\arg \min_{H_{k} \ge 0} ||X - W_{-k}H_{-k} - W_{k}H_{k}||_{F}^{2}$$

where $W_{:k}$, W_{-k} , $H_{k:}$, H_{-k} denote, respectively, the *k*th column of *W*, the matrix *W* without the *k*th column, the *k*th row of *H*, and the matrix *H* without the *k*th row.

• Accelerated multiplicative update method (amu) and Accelerated HALS (ahals) (Gillis, 2011): These two more efficient methods are developed based on the **mu** and **hals** methods. Computational cost is reduced by updating Wseveral times before updating H (and vice versa), instead of updating W and H alternately. An inner loop stopping criterion is utilized for each $W^{(l)}$, defined as the iterate after l updates of Wusing Eq. 3 for **amu** or Eq. 7 for **ahals** (while His being kept fixed):

$$\|W^{(l+1)} - W^{(l)}\|_{F} \le \delta \|W^{(1)} - W^{(0)}\|_{F}$$
 (8)

where δ is a small constant, equal to 0.01 in the implementation.

3 EXPERIMENT & RESULTS

3.1 Simulated Spatial Distribution

In order to construct a realistic MRSI grid Containing spectra from normal tissue, as well as tumor tissue and necrosis, we simulated an MRSI grid in which these 3 tissue types are contained. Table 1 shows the simulated distribution of brain tissues. Each table cell represents a voxel. C, N, and T denote respectively control tissue type (i.e., normal tissue), tumor tissue and necrotic tissue. In the voxels at the interface between tissues, there is usually a mixture of different tissue types. Therefore, decimals are placed into the table to represent concentration of mixed tissues. For instance, 0.8C+0.2T denotes the tissue type in a voxel composed of approximately 80% normal and 20% tumor tissue.

3.2 Simulated MRSI Signals

In our study, the simulated signals are linear combinations of 9 metabolite profiles (two simulated lipid profiles and seven metabolite profiles measured in vitro), i.e., creatine (Cre), glutamate (Glu), myoinositol (Myo), phosphocholine (PCh), N-acetyl-aspartate (NAA), alanine (Ala), lactate (Lac), lipid at 1.3ppm (Lip1), and lipid at 0.9ppm (Lip2). These components are significant biomarkers for normal brain tissue, tumor tissue, and necrosis tissue in pathology (Howe et al., 2003). To choose proper parameters for amplitude, damping, phase and frequency for the simulated signals, we rely on a parameter extraction procedure (Poullet et al., 2006).

In order to emulate the variability within an MRSI grid, 4dB white Gaussian noise, which is in

agreement with our *in vivo* signals, is added to the spectrum of each voxel.

The generated time domain signals, each having 2048 points, are Fourier transformed into the frequency domain, then truncated to the frequency range of interest, 0.25 - 4.2 ppm.

The simulated tissue-specific spectra with noise are shown in the first row of Figure 2 (in blue) and are compared with spectra from a clinical *in vivo* case as shown in the second row of Figure 2. The simulated pure spectra are in red.

3.3 Tissue Type Differentiation using NMF Algorithms

Several NMF algorithms listed in section 2 are applied to the simulated grid described in section 3.1; see Table 1. The number of brain tissue types is set to be 3, indicating normal tissue, tumor tissue and necrotic tissue. The recovered constituent spectra and their corresponding spatial distributions show the variability of tissue type differentiation using each of the described NMF algorithms; see Figure 3. After scaling and normalization, we notice that similar spectra with important peaks, which are biomarkers for discrimination of different tissue types (NAA, Cho, Lac/Lip), are obtained for each tissue type with all methods. The corresponding abundance maps clearly show the location of each tissue type.

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C			С	С	C	C	C	0.8C +0.2T	0.3C +0.7T	Т	Т	0.6T +0.4N	Т
C		C	С	С	С	С	C	0.8C +0.2T	0.3C +0.7T	Т	Т	0.3T +0.7N	0.5T +0.5N
C		C	С	С	С	C	C	0.8C +0.2T	0.3C +0.7T	Т	0.3T +0.7N	0.2T +0.8N	0.3T +0.7N
C		7)	С	С	C	C	C	0.8C +0.2T	0.3C +0.7T	Т	0.1T +0.9N	Ν	0.3T +0.7N
C		C	С	С	С	C	С	0.8C +0.2T	0.3C +0.7T	Т	0.1T +0.9N	Ν	0.4T +0.6N
C		C	С	С	С	С	С	0.8C +0.2T	0.3C +0.7T	0.5C +0.5T	Т	0.5T +0.5N	0.5T +0.5N
C		r)	С	С	С	С	С	С	0.8C +0.2T	0.8C +0.2T	0.5C +0.5T	0.3C +0.7T	0.5C +0.5T
C		C	С	C	С	С	С	С	С	С	0.8C +0.2T	0.8C +0.2T	0.8C +0.2T
C	C (7	С	С	С	С	C	С	С	С	С	С	С

Table 1: Simulated tissue-specific spatial distribution. C denotes control tissue type, i.e., normal tissue. T denotes tumor tissue. N denotes necrotic tissue.



Figure 2: Spectra with SNR of 4dB from different voxels. The first row shows simulated spectra from normal tissue, tumor tissue and necrotic tissue, respectively. Simulated noiseless spectra are shown with thick red lines. For comparison, the last row contains *in vivo* spectra from the three different tissue types.



Figure 3: Simulation results of normalized recovered spectra (left column) and their corresponding spatial distribution (right column) averaged over successful runs among 500 runs with different initializations using several NMF algorithms: (a) mu; (b) cjlin; (c) als; (d) hals; (e) amu; (f) ahals. The color bars show scales for the distribution of concentration.

3.4 Validation of Spectral Separation and Abundance Estimates

In order to evaluate the accuracy of the algorithms listed in section 2, averaged results from 500 runs

(results with convergence problems were excluded, i.e. 8 out of 500 runs for **mu**, 9 out of 500 runs for **als**) for each algorithm were calculated, with different starting values. For every run, all the methods take the same initial value. Specifically,

correlation coefficients R between constituent spectra estimated by NMF and simulated spectra are computed. The closer R to 1, the better the similarity between spectra generated using NMF and the simulated spectra, thus the better the performance. Furthermore, we compute the error rate of the corresponding spatial distribution for each tissue type:

$$Error Rate = \frac{\sum (h_e - h_s)^2}{\sum h_s^2} \cdot 100\%$$
(9)

where h_e is the estimated abundance map from NMF and h_s is the original distribution (see Table 1) When the value of the error is lower, the accuracy of the estimated spatial distribution is higher.

Algorithms were adjusted to make sure they all detect convergence according to the same stopping criterion, namely the condition that $||W^{(r+1)} - W^{(t)}||$ or $||H^{(r+1)} - H^{(t)}||$ (i.e., the difference of recovered sources or the recovered abundance maps in subsequent iterations) drops below a certain tolerance level, set to 10^{-4} for all the methods.

Results are shown in Figure 4. Overall, hals gives the best result for all tissue types, especially the error rate calculated by hals for tumor is significantly lower than for other methods. Results of **ahals** were also investigated but not shown here since they are identical to hals.



Figure 4: Accuracy evaluation. (a) correlation coefficient; (b) error rate.

4 DISCUSSION & CONCLUSION

In this simulation study, we aimed at comparing the performance of several NMF algorithms on spectra with a high noise level. Spectral distortions due to, e.g., magnetic field inhomogeneity and the chemical shift displacement effect may lead to more signal variability and to the violation of the model in Eq.1. We chose not to include such non-linear factors of variability in the simulations because those would obscure the reasons for differences between methods. Nevertheless, in vivo signals need to be reprocessed and significantly distorted signals need to be excluded before spectral separation using NMF.

Among the tested NMF implementations, Lee and Seung's algorithm mu (Lee et al., 2001) was the most commonly used one in the past. Comparisons between various NMF algorithms have already been presented in the literature (Kim et al., 2007). But previous comparisons between algorithms were mostly focused on evaluating computational efficiency and divergence problems (Kim et al., 2007; Cichocki et al., 2009), which are indicated by the cost function $||X - WH||_{F}^{2}$. However, the accuracy of estimated tissue type profiles and the corresponding spatial location is much more important in the clinical diagnosis than computational speed since the computing time of all the methods is affordable for the dimensions of the considered MRSI grids. Instead of evaluating the results only visually, we follow (Croitor Sava et al., 2010) who calculated correlation coefficients between the obtained tissue sources and reference tissue models. Our error rate is calculated between the estimated spatial information and the simulated spatial information. In this way, the accuracy of the estimated spatial distribution of each tissue type can be evaluated.

Overall, our results show that (a)hals gives the best results in the simulation study, which confirms the argumentation in (Gillis, 2011) that (a)hals has remarkable performances. Especially the error for tumor tissue shows a significant decrease compared to all other methods. It demonstrates that the very recent NMF algorithms hals and ahals can be suitable for solving brain tissue type differentiation problems using MRSI signals. In another study, we further validate the feasibility of utilizing NMF algorithms for brain tumor tissue differentiation using *in vivo* MRSI signals.

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