

# PARALLEL IMPLEMENTATION AND COMPARISON OF TWO UAV PATH PLANNING ALGORITHMS

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**Abstract:** The development of autonomous Unmanned Aerial Vehicles (UAVs) is of high interest to many governmental and military organizations around the world. An essential aspect of UAV autonomy is the ability for automatic path planning. In this paper, we use the genetic algorithm (GA) and the particle swarm optimization algorithm (PSO) to cope with the complexity of the problem and compute feasible and quasi-optimal trajectories for fixed wing UAVs in a complex 3D environment while considering the dynamic properties of the vehicle. The characteristics of the optimal path are represented in the form of a multi-objective cost function that we developed. The paths produced are composed of line segments, circular arcs and vertical helices. We reduce the execution time of our solutions by using the “single-program, multiple-data” parallel programming paradigm and we achieve real-time performance on standard COTS multi-core CPUs. After achieving a quasi-linear speedup of 7.3 on 8 cores and an execution time of 10 s for both algorithms, we conclude that by using a parallel implementation on standard multicore CPUs, real-time path planning for UAVs is possible. Moreover, our rigorous comparison of the two algorithms shows, with statistical significance, that the GA produces superior trajectories to the PSO.

## 1 INTRODUCTION

The path planner is an element of the UAV control module (Chen et al., 2009). It allows the UAV to autonomously compute the best path from a start point to an end point. Whereas commercial airlines fly constant prescribed trajectories, UAVs in operational areas have to travel constantly changing trajectories that depend on the particular terrain and conditions prevailing at the time of their flight.

In the past, the best path has been associated with the shortest path and deterministic search algorithms were used to find the very shortest path. The definition of the problem has since evolved and the best path is now associated with the path that minimizes the distance travelled, the average altitude, the fuel consumption, the radar exposure, etc. These are a few examples of the factors to be considered and clearly show that the complexity of the problem has grown. To cope with this complexity, researchers have slowly moved from using deterministic algorithms to using non-deterministic algorithms (Masehian and Sedighizadeh, 2007).

In this paper, we use two non-deterministic algorithms to develop an operational path planning module for fixed wing UAVs. Our research work presents three important contributions. Firstly, we propose a comprehensive cost function which includes both the optimization and the feasibility criteria. This allows us to use a generic optimization algorithm (without modification) as the search algorithm. In our case, we use the GA and the PSO, but these could easily be replaced by other algorithms. Secondly, we present a technique to parallelize both the GA and the PSO while minimizing the communication between the processes in order to achieve a near linear speedup and fully exploit the computing power of today’s multicore CPUs. Finally, we offer a statistically significant comparison between the quality of the trajectories generated by our GA-based and PSO-based path planners. Both algorithms have recently been widely used for UAV path planning (Pehlivanoglu, 2011), (Macharet et al., 2010), (Fu and Gao, 2010), (Xia Li et al., 2010), (Bao et al., 2010), (Yangguang Fu et al., 2009) and (Foo et al., 2009). However, to our knowledge, there exists no rigorous comparison between the two algorithms

when applied to this particular problem. The results we present in this paper provide clear insight as to which of the two optimization algorithms is preferable for UAV path planning in complex 3D environments.

## 2 REPRESENTATION

The first step of path planning is to discretize the world space into a representation that will be meaningful to the path planning algorithm. This representation is closely related to a search algorithm and some algorithms will only perform well when coupled with a specific environment representation. An overview of the performance of different representations used with different algorithms is presented in (Sariff and Buniyamin 2006). In our implementation (see Figure 1), we use an approximate cell decomposition of the terrain using a 2D grid where each element of the matrix represents the elevation of the terrain. This representation allows us to use digital elevation maps freely available from the GeoBase (Anon n.d.) repository with no further processing. Our representation of the environment also allows for the definition of cylindrical danger zones (or no-fly zones) to be kept in a separate matrix where each row represents the coordinates and the diameter of the cylinder. Complex no-fly zones can be built by partially juxtaposing multiple cylinders. The trajectories generated by the optimization algorithm are composed of line segments and encoded in a matrix where each row represents the (x, y, z) coordinates of a waypoint. The trajectories are flown at constant speed and can also be represented as a function of time.

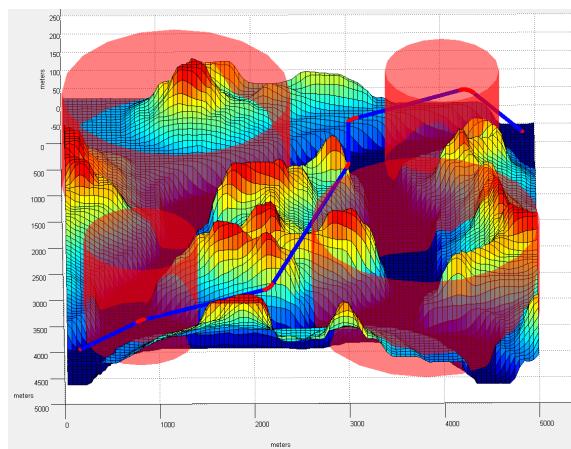


Figure 1: Trajectory in a 3D environment.

## 3 COST FUNCTION

As previously stated, searching for the best path is often associated with searching for the shortest path. This is the case when solving the Traveling Salesperson Problem (TSP), which consists of finding the shortest path that visits all the given cities only once. In the case of UAV path planning, the optimal path is more complex and includes many different characteristics. To take into account these desired characteristics, a cost function is used and the path planning algorithm becomes a search for a path that will minimize the cost function. The cost of a path decreases with the degree to which the desired characteristics are being fulfilled. A path that fulfills all the characteristics to a high degree would result in a low cost. We define our cost function as follows:

$$\begin{aligned} F_{\text{cost}} = & C_{\text{length}} + C_{\text{altitude}} + C_{\text{danger zones}} \\ & + C_{\text{power}} + C_{\text{collision}} \\ & + C_{\text{fuel}} + C_{\text{smoothing}} \end{aligned} \quad (1)$$

where  $C_{\text{length}}$  penalizes longer paths,  $C_{\text{altitude}}$  penalizes paths with a higher average altitude,  $C_{\text{danger zones}}$  penalizes paths going through danger zones,  $C_{\text{power}}$  penalizes paths requiring more power than the maximum available power of the UAV,  $C_{\text{collision}}$  penalizes paths colliding with the ground,  $C_{\text{fuel}}$  penalizes paths requiring more fuel than available in the UAVs and finally,  $C_{\text{smoothing}}$  penalizes paths that cannot be smoothed using circular arcs. All terms are normalized on the interval [0, 1].  $C_{\text{length}}$ ,  $C_{\text{altitude}}$  and  $C_{\text{danger zones}}$  are optimization criteria and are used to improve the quality of the trajectory whereas  $C_{\text{power}}$ ,  $C_{\text{collision}}$ ,  $C_{\text{fuel}}$  and  $C_{\text{smoothing}}$  are feasibility criteria that must be satisfied for the final trajectory to be valid. In order to separate viable and non-viable trajectories, we add a penalty constant to each feasibility constraint not satisfied.

## 4 GENETIC ALGORITHM

The GA is a population based non-deterministic optimization method that was developed by John Holland in the 1960s and first published in 1975 (Holland, 1975). Based on the genetic theory of Darwin evolution, the GA simulates the evolution of a population of solutions to optimize a problem. Similarly to living organisms adapting to their environment over the generations, the solutions in the GA adapt to a fitness function over an iterative process using biology-like operators such as the

crossovers of chromosomes, the mutations of genes and the inversions of genes. In this work, the GA simulates the evolution of a population of trajectories adapting to the cost function defined in the previous section. Our implementation uses stochastic universal sampling as the selection method, single point crossover as the reproduction mechanism and addition, deletion and modification as genetic operators (Yu and Gen, 2010). We also used the concept of elitism when replacing the old generation with the new one in order to improve conversion. The flowchart of the GA is shown in Figure 2 and the different genetic operators used, in Figure 3.

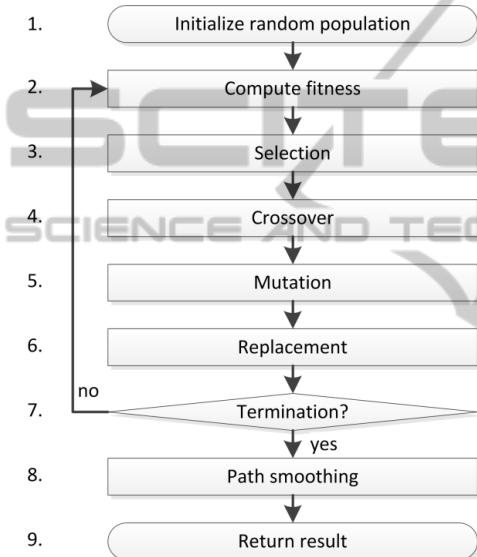


Figure 2: Flow chart of the genetic algorithm.

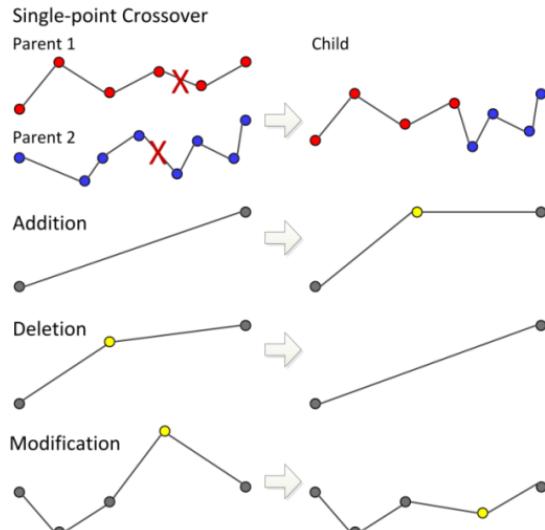


Figure 3: GA operators.

## 5 PARTICLE SWARM OPTIMIZATION

The PSO is a population based non-deterministic optimization method that was proposed by Kennedy and Eberhart in 1995 (Kennedy & Eberhart 1995). The algorithm simulates the movement of a swarm of particles in a multidimensional search space progressing towards an optimal solution. The position of each particle represents a candidate solution (a complete trajectory encoded in a single vector) and is randomly initiated. At every step of the iterative process, the velocity of each particle is individually updated based on the previous velocity of the particle, the best position ever occupied by the particle (personal influence) and the best position ever occupied by any particle of the swarm (social influence). As outlined in (Clerc 2005), the equations used to compute the velocity and position of a single particle at iteration  $t$  are as follows:

$$\mathbf{v}_{t+1} = \omega \mathbf{v}_t + c_1 \mathbf{r}_1 \cdot (\mathbf{b}_t - \mathbf{x}_t) + c_2 \mathbf{r}_2 \cdot (\mathbf{g}_t - \mathbf{x}_t) \quad (2)$$

$$\mathbf{x}_{t+1} = \mathbf{x}_t + \mathbf{v}_{t+1} \quad (3)$$

where variables in bold are vectors;  $\mathbf{v}$  is the velocity of the particle;  $\mathbf{x}$  is its position;  $\mathbf{b}$  is the best position previously occupied by the particle;  $\mathbf{g}$  is the best position previously occupied by any particle of the swarm;  $\mathbf{r}_1$  and  $\mathbf{r}_2$  are vectors of random values between 0 and 1; and  $\omega$ ,  $c_1$  and  $c_2$  are the inertia, the personal influence and the social influence parameters. Still based on (Clerc, 2005), the flow diagram of the PSO is displayed in Figure 4.

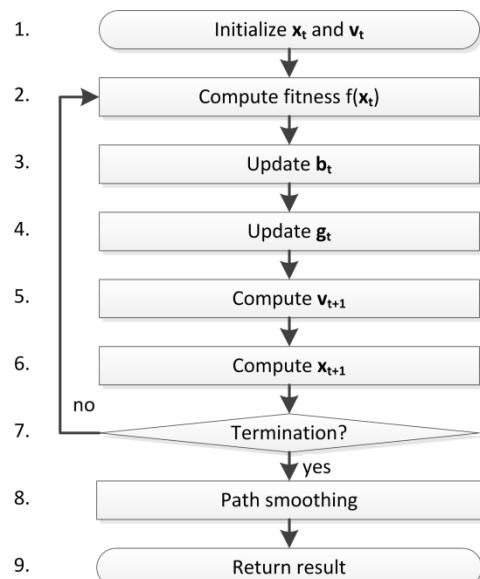


Figure 4: Flowchart of the particle swarm optimization.

## 6 PATH SMOOTHING

Consistent with solutions proposed in the literature (Labonté, 2009), (Hasircioglu et al., 2008), (Anderson et al., 2005), our solution generates a path composed of line segments. This would be sufficient for multi-directional ground robots, but inadequate for a fixed-wing UAV. To remove all discontinuities in the velocity, we smooth the final path by connecting the line segments with simple circular arcs (when the power available is sufficient) or circles on a horizontal plateau (when the power available is not sufficient to fly a simple circular arc) based on (Labonté, 2009), (Anderson et al., 2005), (Bottasso et al., 2008) and as shown on Figure 5. Our final stage module also replaces any line segment requiring more power than available with a vertical helix as in (Labonté, 2009). Although smoothing of the path is performed after the optimization process, the feasibility of this operation is verified in our cost function to ensure the smoothing of the final trajectory is always possible.

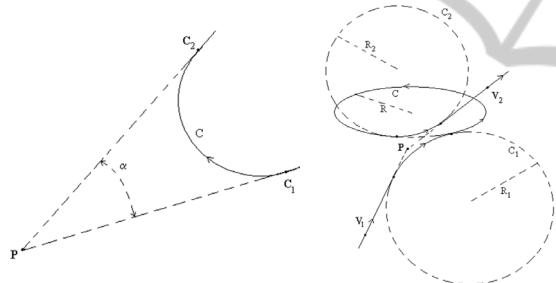


Figure 5: Circular constructions used to smooth the final trajectory and remove all discontinuity in the velocity (left diagram shows a simple circular arc and the right diagram shows a connection using 2 circular arcs and a circle on an horizontal plane).

## 7 PARALLEL IMPLEMENTATION

We have now discussed all the elements required to build a complete path planning module for UAVs. Although the generated trajectories are feasible and nearly optimal, the computation time remains too long for real-time applications. To address this problem, we developed parallel versions of our GA and PSO using the “Single-program, multiple-data” parallel programming paradigm. Our implementation was done in MATLAB. It minimises the communication between the processes and allows full use of today’s multicore CPUs. The

flowchart of our parallel GA is shown in Figure 10. Although drawn for 2 processes, our implementation allows any number of processes. Our parallel version of the PSO is not shown in this paper but follows the same principle. The execution time and the speedup of our parallel GA were measured on a system equipped with two Intel Xeon E5310 quad-core processors using the parameters in Table 1 and are plotted in Figure 6 and Figure 7. The execution time and the speedup of our parallel PSO are not presented here, but are almost identical.

Table 1: Algorithm parameter values.

Parameters	Values
Terrain resolution	500 x 500
Number of waypoints per trajectories	8
Number of gen. (AG) or ite. (PSO)	100, 200 and 300
Number of chromo. (AG) or part (PSO)	128 and 256
Mutation rate (AG)	10 %
Elitism rate (AG)	10 %
$\omega$ (PSO)	0.7298
$c_1$ (PSO)	1.4960
$c_2$ (PSO)	1.4960

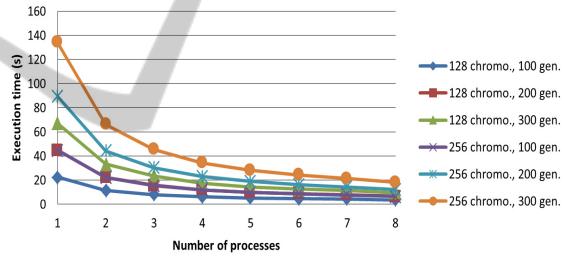


Figure 6: Execution time of our parallel GA for different work sizes.

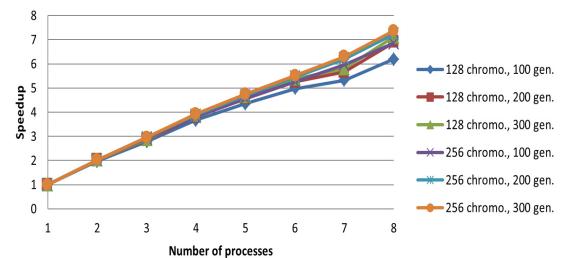


Figure 7: Speedup achieved by our parallel GA for different work sizes.

## 8 COMPARISON OF THE GA AND THE PSO

Finally, we compare the performance of the GA and the PSO using 40 different scenarios from two

fictitious terrain elevation maps and six real terrain elevation maps (see Figure 8 and Figure 9). The digital elevation maps for the six real terrains were taken from the GeoBase repository (Anon n.d.). The average costs of 60 trajectories generated using our parallel GA and parallel PSO are compared using the T-test with 5% significance to conclude that:

- The GA produced trajectories significantly better than those generated by the PSO for 25 of the 40 scenarios;
- the PSO produced trajectories significantly better than those generated by the GA for 3 of the 40 scenarios; and
- the GA and the PSO produced trajectory of similar quality for 12 of the 40 scenarios.

Based on these results, we conclude that the GA is preferable to the PSO when solving the path planning problem for UAVs in a fixed computation time of 10 s on multicore COTS processors.

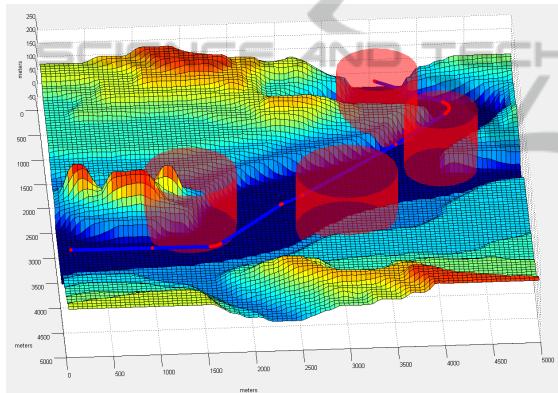


Figure 8: 3D visualisation of the computed path (fictitious map, 25 km<sup>2</sup>, altitude ranging from 0 to 250 m ASL).

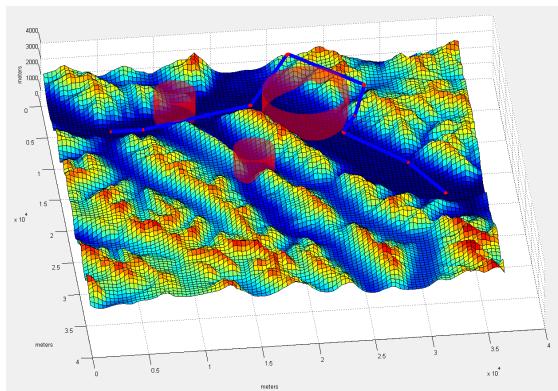


Figure 9: 3D visualisation of the computed path (Banff, Alberta, CA, 1 360 km<sup>2</sup>, 1 290 to 3 079 m ASL).

## 9 CONCLUSIONS

This paper presents a path planning solution for UAVs which considers the dynamic properties of the UAV and the complexity of a real 3D environment. We used two non-deterministic algorithms, the GA and the PSO, to attack this complexity and produce solutions in a relatively short computation time. We further reduced the execution time by developing parallel versions of our algorithms. After achieving a quasi-linear speedup of 7.3 on 8 cores and an execution time of 10 s for both algorithms, we conclude that by using a parallel implementation on standard multicore CPUs, real-time path planning for UAVs is possible. Moreover, our rigorous comparison of the two algorithms shows, with statistical significance, that the GA produces superior trajectories to the PSO.

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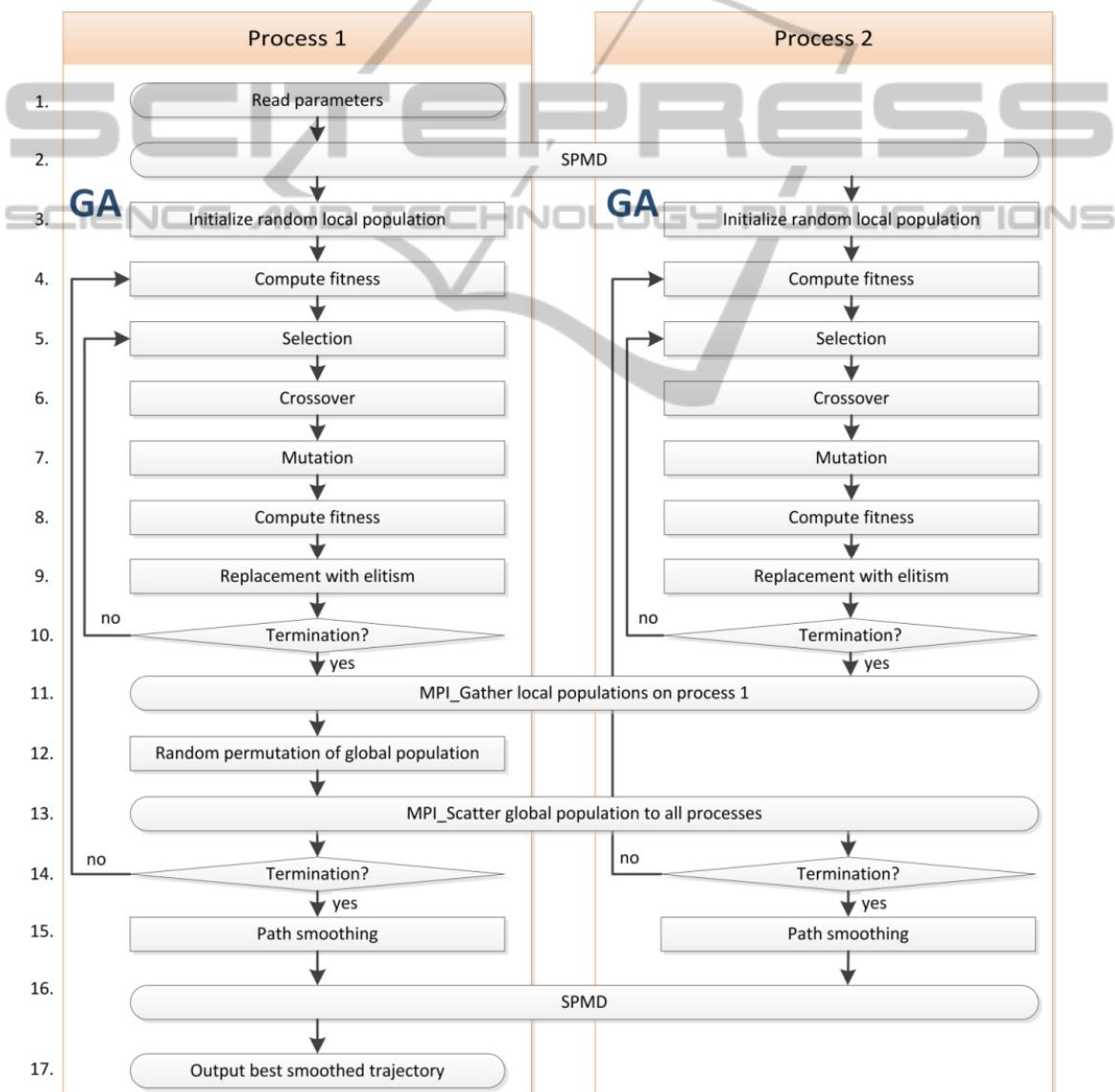


Figure 10: Flowchart of our parallel genetic algorithm.