

A FUZZY LOGIC APPROACH USED IN THE INVERSE KINEMATIC ALGORITHM OF A SPACE ZERO-G FREE FLYING ROBOT

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Abstract: A fuzzy algorithm for the fixed attitude restricted motion problem of free-flying robots is proposed in this paper. One of the main applications is to guide the robotic arm of a space servicing satellite: in such a mission, one of the priorities is to reduce disturbances on the satellite attitude induced by robotic arm movements so as not to perturb the pointing position of the satellite. A robot whose base has both mass and inertia of the same order of magnitude of its robotic arm is considered - in this configuration the disturbance of the satellite attitude is not negligible. Objective is to plan the robot's arm motion in such a way as the end-effector tracks a desired trajectory while disturbances on the base's attitude are minimized. This objective is achieved by taking into account the coupling between the arm and the floating base of the robot in the kinematic inversion of the guiding control, controlling the gain matrix of the subtask introduced in the kinematic inversion equation by means of a fuzzy algorithm. The proposed strategy combines the advantages of the inverse kinematic algorithm and a fuzzy logic approach.

1 INTRODUCTION

The advancement of space robotics is currently recognized by space agencies as a key strategy to reduce costs of space exploration. Robotic systems can advantageously be used during robotic exploration missions, on-orbit servicing operations Internal Vehicular Activities (IVA) and Extra-Vehicular Activities (EVA) substituting astronauts during operations. The use of a floating robot with a dexterous arm is considered to be a viable option for on-orbit servicing (Hirzinger, 2000; Tatsch, 2006; Thronson, 2008).

Hence, controlling autonomous robotic systems is of outmost importance and research is currently focusing on the development of algorithms, which allow performing safe and complex robotic manoeuvres in space. Many space agencies have funded important programs for developing space robotic systems (Hirzinger, 1994; Yoshida, 2003; Roderick, 2004; Marzwell, 2001; Culbertson, 2003; Oda, 2008).

In this paper, we tackle the problem of controlling a platform to be used in space servicing missions. In the framework of this research, a spacecraft equipped with a robotic arm is considered to be a free-flying robot where the spacecraft is the floating base of the robot - no active thrusters are considered in this study. The goal is to plan the robot's arm motion in such a way that the end-effector tracks a desired trajectory while disturbances on the base's attitude are minimized. This problem is known as Fixed Attitude Restricted (FAR) motion problem (Gu, 1993; Sagara, 2008; Boning, 2010, Khaloozadeh, 2010; Rastegaria, 2010). We investigated the problem in which both mass and inertia of the base are comparable to those of the robotic arm - the disturbance produced by the arm on the base can therefore be significant if a non-suitable controller is used. The goal is achieved by taking into account the coupling between the arm and the base of the robot in the kinematic inversion of the guiding control and by combining the advantages of inverse kinematic algorithms and a

Fuzzy Logic approach.

This work follows an experimental phase in which our working group has built a free-floating robot that was tested during the Sixth Student Parabolic Flight Campaign sponsored by the ESA (Menon, 2003; Menon, 2004; Cocuzza, 2004; Menon, 2005).

In Section 2 we introduce the fixed attitude restricted motion problem. In Section 3 the fuzzy algorithm is presented. Section 4 reports the simulation performed to test the algorithm and the main results. Finally, Section 5 draws the conclusion of this work.

2 KINEMATIC CONTROL

The free-floating problem (FFP), which we considered, consists in the description and control of a system in which (i) the position and orientation of the spacecraft respect to an inertial coordinate system are well-known in the initial state, (ii) there are no external forces or torques about the center of mass, hence the conservation of momentum and the equilibrium of forces and moments hold strictly true, (iii) there are no attitude control devices such as reaction wheels or thrusters - internal forces are generated only by joint motors, (iv) the robot acts in a zero-gravity environment. In order to solve the FFP, the linear and angular momentum conservation laws are used. The considered system is nonholonomic, namely the satellite orientation is not only a function of the joint configuration, but also a function of the path taken to reach such an orientation. As a consequence, nonholonomy offers the possibility to perform a reorientation of the satellite using the motion of the only robotic arm (Nenchev, 1988; Nenchev, 1992). This could be useful in docking operations to save fuel and reduce pollution near the target satellite. This kind of manoeuvres can be employed to augment the workspace of the robot too; it allows turning the satellite into a different orientation, bringing back the manipulator into its reference configuration. Another possibility resulting from nonholonomy is that manoeuvres can be sought to reduce attitude variation of the spacecraft.

A closed loop differential kinematic inversion algorithm can be adopted (Sciavicco, 1988; Nenchev, 1992; Siciliano, 1993) and additional subtasks introduced. In our context, n is the number of degrees of freedom of our problem, m_a is the dimension of operating space of the arm and m_b is the dimension of operating space of the base or

spacecraft; for a 3D environment, $m_b=6$. If \dot{q}_a is the velocity vector of the arm joints, it is represented by the following equation:

$$\dot{q}_a = J_{AG}^+(q)(K_p e + \dot{x}_d) + (I - J_{AG}^+ J_{AG}) J_c^T K_c e_c \quad (1)$$

where q is the vector of joint positions (arm and base), J_{AG} is the Analytic Generalized Jacobian (Umetani, 1989; Menon, 2003), J_{AG}^+ is its pseudo-inverse, e is error of the end-effector (the difference between desired and real position), x_d is the desired position and orientation of working space, K_p and K_c are gain matrixes (K_c is positive definite), I is the identity matrix, J_c is the Jacobian associated to the constraint task error, e_c is the error of the constraint task defined as $e_c = q_{bd} - q_b$ where q_b is a generalized position variable of the free floating base of the robot that is constrained to the desired trajectory q_{bd} . The matrix $(I - J_{AG}^+ J_{AG})$ projects the joint velocity contribution into the null space of the generalized Jacobian in order to separate the constraint and end-effector tasks.

Since the aim is to keep fix a rotational angle of the base, the constraint error can be expressed as $e_c = -q_b$. In order to obtain high performance of this algorithm, K_c should be selected properly (Menon, 2005): the variables of interest should be handled in a flexible manner for planning optimal trajectories while taking into account the constraints of the problem; a fuzzy algorithm capable to online adjust the elements of the K_c matrix, and therefore manage the motion of the robot is implemented.

In an experiment performed with a free-floating robot that was tested during the Sixth Student Parabolic Flight Campaign sponsored by the ESA (Menon, 2003; Menon, 2004; Cocuzza, 2004; Menon, 2005) we have proved the real possibility of keeping the robot base stationary during arm operations with a K_c matrix fixed. This work is an improvement of the experimental results: the main purpose of the proposed solution is to handle the K_c matrix during the trajectory evolution and controls any instability that can be induced to the system. Specifically, a Mamdani Fuzzy Inference System (FIS) is developed to control the values of K_c during the evolution of the trajectory of the space robot. The use of fuzzy systems has been extensively used in other works e.g. (Gu, 1993; Antonelli, 2003; Radaideh, 2003; De Santis, 2008; Zou, 2009; Fu, 2009) - in this work we have used this approach to control the motion of a free-floating robot operating in a zero-g environment.

The representation of the robot is obtained by using the reference frame proposed in Menon

(2005): the entire system is modelled as a single robot with a fixed base. To describe the position and orientation of the base, a fictitious arm, which is a sequence of frames and joints linking the inertial reference frame to the base itself, is introduced. Because the free-floating base has six degree of freedoms (DOF), we considered a fictitious arm with three prismatic and three revolute joints, called virtual joints.

3 FUZZY LOGIC ALGORITHM

The correct determination of the K_c matrix of Eq.1 is of fundamental importance to effectively solve the constraint minimization problem for the following reasons: (1) an unstable dynamic response of the robotic system and an increased position error of the end-effector could be caused by selecting too large values of the elements of the K_c matrix; (2) imposed constraints could not be satisfied if elements of the K_c matrix assume too small values.

The proposed fuzzy algorithm selects the elements of the K_c matrix in order to minimize the error e_c (see Eq.1). This algorithm combines the advantages of the inverse kinematic algorithm (see Section 2) with a Fuzzy Logic approach with a hierarchical structure having a conventional differential inverse kinematic algorithm at the bottom layer (Eq.1) and a tuner at an upper-level: at each step the kinematic is inverted using the K_c matrix calculated by fuzzy algorithm in the previous step. This work is related to the top-level tuner using a fuzzy approach: this tuner uses a set of linguistic rules for adjusting the constraint error gain matrix during the kinematic inversion. The performance of this fuzzy tuner is evaluated hereafter on the basis of simulation results. The proposed algorithm takes as input the constraint error $e_c = -q_b$ defined in Section 2.

3.1 Detection of Oscillations

Possible dynamic oscillations of the robotic system are detected by monitoring the oscillation of the joint velocity \dot{q} ; at this purpose a moving average filter is used.

During the calculation of the differential inverse kinematics, for each time step the moving average of the joint velocity vector is calculated, and compared with its actual value. If the moving average is crossed twice by the joint velocity the joint velocity \dot{q} is determined to be oscillating. The number of joints (for the arm) and virtual joints (for the base),

which are oscillating, becomes an input of the fuzzy algorithm.

The crisp inputs of the FIS are the constraint error e_c and the number of oscillating joints. The crisp output is the increment or the decrement of the current K_c elements.

Two linguistic variable are considered: *constraint error* = {zero (Z), positive small (PS), positive (P), positive medium (PM), positive large (PL)} and *oscillation* = {OFF, ON}, where OFF means no oscillations. If the constraint error is greater than 0.1 rad/s, the error is considered PL. The output linguistic variable is the gain increment = {Negative Large (NL), Negative (N), Zero (Z), Positive Small (PS), Positive (P), Positive Large (PL)} that is the increments of K_c elements; the fuzzy sets used for this output linguistic variable are not symmetric. In fact, for a better management of the instability for a more rapid decrement of the K_c the robotic system can react in a better way to the system instability that can be reached during the increment of the K_c .

The membership functions used for the input and output linguistic variable are reported in Fig. 1.

The fuzzy rules used are the follows: (1) if (*constraint error* is Zero) or (*constraint error* is Positive Small) and (*oscillation* is OFF then (*gain increment* is Positive Small); (2) if (*constraint error* is Positive) and (*oscillation* is OFF) then (*gain increment* is Positive); (3) if (*constraint error* is Positive Large) and (*oscillation* is OFF) then (*gain increment* is Positive Large); (4) if (*oscillation* is ON) then (*gain increment* is Negative Large).

The main idea of the algorithm is the following: if the system has no oscillations, the increment of gain matrix is in the same direction of the constraint error: this enable the controller to increment the weight of the constraint that we have added to resolve the FAR motion problem, but when the instability is reached the controller reacts and decrements rapidly the gain matrix.

4 SIMULATIONS

The test bed for the evaluation and comparison of the algorithm presented in this paper is based on a Matlab simulator developed by the authors. This simulator enables the simulation of (i) rigid body motion, (ii) direct and inverse kinematic (iii) differential kinematic, and (iv) control problem. It is possible to build various types of redundant or non-redundant robots with fixed or free-floating base and with revolute or prismatic joints.

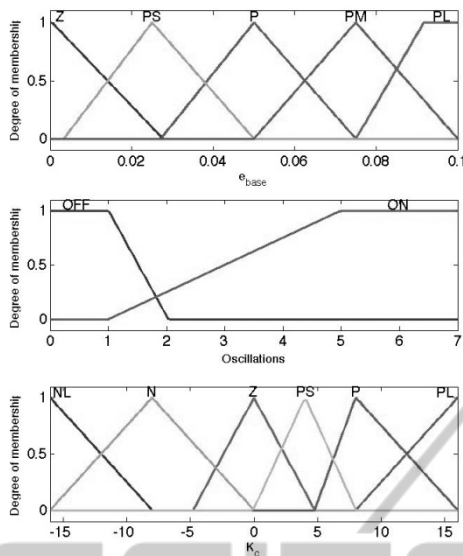


Figure 1: Fuzzy membership input and output functions. From left to right: (a) constraint error; (b) oscillation of joints; (c) output K_c .

The geometrical parameters of the robot, which were selected for the simulation, were those of a robotic prototype tested by the authors during the Sixth Student ESA Parabolic Flight Campaign. This prototype was a free-floating robot with 4 DOFs operating in a 3D zero-g space environment. Table 1 reports the links of the parameters of the simulated robot.

For all links the mass is 4 kg. The mass of the base is 16 kg and its inertia is:

$$I_b = \begin{pmatrix} 0.5760 & 0 & 0 \\ 0 & 0.5760 & 0 \\ 0 & 0 & 0.5760 \end{pmatrix} \text{kgm}^2 \quad (3)$$

With a 4-DOF robotic arm, it is possible to control the position or orientation of the end-effector and keep fixed the rotation of the base about one axis: this means that the K_c becomes a scalar. The end-effector (EE) position and the yaw angle of the base were chosen as desired parameters to be controlled in this study.

Table 1: Parameters of the simulated robot.

Link	Arm length	Arm center of mass	Inertia tensor
7, 8, 9	1 m	0.5 m	$\begin{pmatrix} 0.3358 & 0 & 0 \\ 0 & 0.3358 & 0 \\ 0 & 0 & 0.0450 \end{pmatrix} \text{kgm}^2$
10	0.5 m	0.25 m	$\begin{pmatrix} 0.1892 & 0 & 0 \\ 0 & 0.0450 & 0 \\ 0 & 0 & 0.1892 \end{pmatrix} \text{kgm}^2$

About 1000 random trajectories of the EE were used as input for the kinematic inversion algorithms. To test if the generated trajectories were physically consistent, the calculated trajectories were passed to the robot simulator with a robust control algorithm that control the end-effector position and the yaw angle of the base (Menon, 2005) and compared with the desired input. The fuzzy algorithm uses the same robust controller but it adapts the K_c matrix. A max rotation of 0.4 rad in 10-15 s (the last of simulated trajectories) is considered for the base yaw angle. The integration step time is 0.01 s.

The following parameters were considered to evaluate the performance of the algorithm and reported in Table 2: (i) *EE pos.*: norm of the end-effector position error (difference between the desired and generated trajectory), (ii) maximum (*Max d.*) and mean deviation (*Mean d.*) of the base yaw angle with respect to a zero rotation, (iii) *Oscill.*: mean value of the oscillation occurring during the kinematic inversion (this was considered to be a suitable parameter to evaluate the stability), that is the number of joints that oscillate for each step time divided for the number of steps.

Table 2 reports the main results of the performed simulations with the proposed fuzzy algorithms with respect to the approach of Eq. 1 (called classical approach in this context) with a fixed K_c , where the first column reports the K_c value used as a constant (for the closed loop inverse algorithm) or the starting K_c value for the fuzzy algorithm.

From Table 2 it is possible to note that the mean and maximum deviation from the zero trajectory of the base yaw angle is smaller than the classical approach; in addition, the number of oscillations of the fuzzy algorithm is comparable to the one obtained with a classical approach, with the exception of cases with initial $K_c \geq 1000$, in which the algorithm acts as a system stabilizer. This is a very interesting behaviour and an important result of this algorithm; in fact the algorithm is able to reduce or eliminate large joint oscillations by increasing K_c , enabling the optimization of the fixed attitude restricted motion subtask; this behaviour provides justification of the smaller end-effector position error obtained by using the fuzzy algorithm.

Some examples of trajectories are shown on the left-hand side of Fig. 3, 4 and 5. Each Figure contains a trajectory with (i) orientation of the yaw angle of the base not constrained, (ii) orientation constrained with $K_c=1000$ fixed (Eq.1), (iii) orientation of the proposed fuzzy algorithm; the right panel shows the K_c value selected by the fuzzy algorithm. Fig. 3 reports an example of trajectory in

Table 2: Comparison between closed loop algorithm with fixed and fuzzy-adaptive K_c .

K_c	K_c constant				K_c fuzzy-adaptive			
	EE pos. err. (m)	Yaw max d. (rad)	Yaw mean d. (rad)	Oscill.	EE pos. err. (m)	Yaw max d. (rad)	Yaw mean d. (rad)	Oscill.
10	$2.5 \cdot 10^{-5}$	0.064	0.020	0.0014	$2.6 \cdot 10^{-5}$	0.028	0.005	0.048
100	$9.3 \cdot 10^{-5}$	0.041	0.011	0.0030	$3.0 \cdot 10^{-5}$	0.030	0.006	0.016
500	$2.0 \cdot 10^{-5}$	0.030	0.006	0.0096	$2.7 \cdot 10^{-5}$	0.024	0.004	0.060
1000	0.0013	0.027	0.005	0.0587	$2.8 \cdot 10^{-5}$	0.023	0.004	0.070
5000	0.56	0.233	0.019	0.5439	$2.8 \cdot 10^{-5}$	0.010	0.001	0.110

which the subtask target is reached but the fuzzy algorithm is more effective. Fig. 4 shows an example of trajectory in which the subtask is maintained only with this proposed fuzzy algorithm. The trajectory of Fig. 5 is stable without task optimization but the subtask objective is not reached; if we use a fixed K_c the trajectory is not stable; it is stabilized with the proposed fuzzy algorithm and the subtask objective is reached. As shown in these figures the performance of the fuzzy algorithm is higher than the closed loop inverse algorithm of Eq. 1 with a fixed K_c .

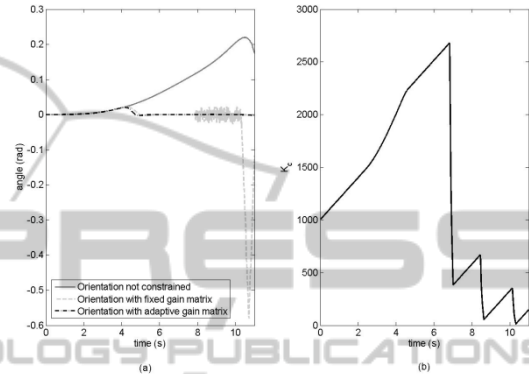


Figure 5: Trajectory example 3. Left: base yaw angle of not constrained, constrained (fixed K_c) and fuzzy-adaptive trajectories. Right: calculated K_c adaptive value.

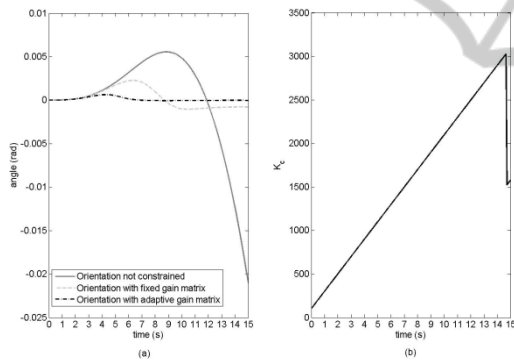


Figure 3: Trajectory example 1. Left: base yaw angle of not constrained, constrained (fixed K_c) and fuzzy-adaptive trajectories. Right: calculated K_c adaptive value.

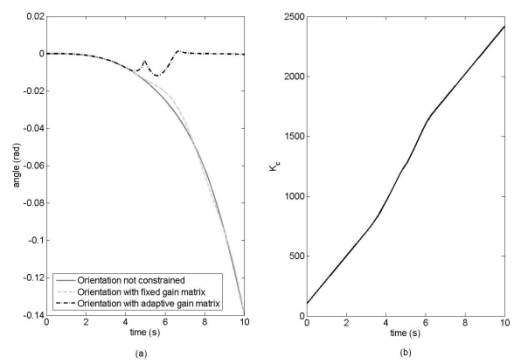


Figure 4: Trajectory example 2. Left: base yaw angle of not constrained, constrained (fixed K_c) and fuzzy-adaptive trajectories. Right: calculated K_c adaptive value.

5 CONCLUSIONS

In this paper is proposed a fuzzy algorithm suitable to control the yaw angle of a free-flying robot operating in a space zero-g environment. The performed simulations, which used parameters of a real robotic platform tested by authors, has shown that the yaw angle obtained with the fuzzy algorithm is smaller than that obtained with a classical approach, while the end-effector position error was comparable. The gain matrix was incremented up to the point in which the system was close to instability; when this condition is reached, the algorithm promptly reacts (possible oscillations may be considered as an indication that the gain matrix is too large) and the fuzzy controller decreases the elements of the gain matrix. In fact, the proposed algorithm acts as a stabilizer for the robot under control. It detected oscillations and reacted to stabilize the system; it behaved as a system control tuner. The proposed method is potentially suitable for solving a large class of control problems and could in principle be applicable to any kind of robot's geometrical constraint.

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