

# AN APPROACH FOR COMBINING SEMANTIC INFORMATION AND PROXIMITY INFORMATION FOR TEXT SUMMARIZATION

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**Keywords:** Latent semantic analysis, Proximity language model, Singular value decomposition, Text summarization.

**Abstract:** This paper develops and evaluates an approach for combining semantic information with proximity information for text summarization. The approach is based on the proximity language model, which incorporates proximity information into the unigram language model. This paper novelly expands the proximity language model to also incorporate semantic information using latent semantic analysis (LSA). We argue that this approach achieves a good balance between syntactic and semantic information. We evaluate the approach using ROUGE scores on the Text Analysis Conference (TAC) 2009 Summarization task, and find that incorporating LSA into PLM gives improvements over the baseline models.

## 1 INTRODUCTION

The challenge of this paper is to generate an informative summary using sentence extraction. Ranking sentences for extraction can be performed by the sentence ranking function, which evaluates each sentence against the document set, and gives a score representing its relevance for the summary. The ranking function that we use is based on the proximity language model, which uses physical proximity information between terms in addition to term frequency information. We further extend this model by performing semantic smoothing using latent semantic analysis (LSA).

## 2 RELATED WORK

Related work for our paper spans three areas: 1) papers that have adapted ranking functions for text summarization; 2) those that employ the proximity language model; and 3) those that use semantic smoothing.

In the first area, (Xie et al., 2004) performs text summarization using a ranking function that is based on various features of the sentence, such as its length and location, while (Carbonell and Goldstein, 1998) employs Maximal Marginal Relevance criterion to select best non-redundant sentences. Finally, (Mihalcea, 2004) uses graph-based ranking function based on the HITS algorithm to assign scores for sentences.

The ranking function that this paper uses extends traditional ranking functions to incorporate the proximity language model (Zhao and Yun, 2009) and semantic smoothing (Steinberger, 2004). The former embeds syntactic information into the ranking function, while the latter embeds semantic information.

The proximity language model (PLM) extends the traditional unigram language model to integrate term proximity information. PLM embeds the proximity information in a probabilistic model using Dirichlet hyperparameters, rather than relying on a linear combination of term frequency and proximity information.

Meanwhile, latent semantic analysis (LSA) can be used to incorporate semantic information. (Landauer et al., 1998) explored using latent semantic analysis for text summarization. In particular, we use ideas in (Steinberger, 2004) to smooth our term importance scores.

## 3 PROXIMITY LANGUAGE MODEL

Proximity language model (PLM) forms the heart of our ranking function, and is based on the unigram language model (Zhao and Yun, 2009).

### 3.1 Unigram Language Model

The unigram language model first considers the vocabulary set,  $V = \{w_1, w_2, \dots, w_{|V|}\}$ , for each word. In the model, both the query  $q$  and the document  $d_i$  are represented as vectors of counts for each word:  $q = (q_1, q_2, \dots, q_{|V|})$  and  $d_i = (d_{i,1}, d_{i,2}, \dots, d_{i,|V|})$  respectively.

Then, a multinomial model is used, with parameters  $\theta_i = \{\theta_{i,1}, \theta_{i,2}, \dots, \theta_{i,|V|}\}$ , with  $\theta_{i,j}$  representing the probability of emission of word  $w_j$  in document  $d_i$ . Using maximum likelihood estimation for the multinomial distribution yields the estimator

$$\hat{\theta}_{i,j} = \frac{n_{i,j}}{n_j} \quad (1)$$

with  $n_{i,j}$  being the occurrence of the word  $w_j$  in document  $d_i$ , and  $n_j$  being the total occurrence of the word in the collection.

### 3.2 Proximity Measure

The unigram language model is a simple model that is based on the bag of words assumption. Under this assumption, the only relevant information for a term is whether or not it occurs in the document; i.e. its position has no bearing on the model.

An intuitive way to extend the unigram language model is to incorporate proximity information. For example, we can give a higher score to a document that contains the query terms in close proximity with each other.

Typically, the distance is defined as the minimum number of words that occur between the query terms in the document. If a query term does not exist in the document, the length of the document is used for the distance.

Proximity score for a term can then be calculated using these term distance. One way uses the average distance among the query terms as the term proximity score. While this approach has advantages in that all of the distances are taken into account, not all information may be equally relevant. For example, suppose that the query is “computer mouse and video games”, and that we are calculating proximity score for the query term “mouse”. In this case, once we have determined that the term “mouse” occurs in close proximity with the term “computer”, its context becomes somewhat clear, and the proximity information between the term “mouse” and other query terms becomes much less relevant.

Thus, another way to calculate term proximity score is to use the minimum distance among the query

terms as the distance, which has shown higher accuracy scores empirically than using the average distance (Zhao and Yun, 2009).

We then perform an exponential transformation on the term distance to convert it to a (0,1) scale. The final proximity score for a term  $q_i$  is given as:

$$Prox(q_i) = 1.5^{-MinDist(q_i, q_j)} \quad (2)$$

### 3.3 Proximity Language Model

We are now ready to incorporate proximity information to the unigram language model. In PLM, proximity information for a term is incorporated as Dirichlet priors  $(u_1, u_2, \dots, u_{|V|})$ , where  $u_i = \lambda Prox(w_i)$ , and  $\lambda$  is the Dirichlet parameter. Dirichlet priors reflect our belief on how much the term proximity structure should affect the term’s emission probability. The maximum likelihood estimator in Equation 1 now becomes

$$\hat{\theta}_{i,j} = \frac{n_{i,j} + \lambda Prox(w_j)}{n_j + \sum_{j=1}^{|V|} \lambda Prox(w_j)} \quad (3)$$

PLM further smoothes this estimator by using a collection language model  $p(\cdot|C)$  to account for unseen words in the document. The corresponding Dirichlet priors  $\{\mu p(w_1|C), \mu p(w_2|C), \dots, \mu p(w_{|V|}|C)\}$  are then applied on Equation 3, yielding us the PLM estimator:

$$\hat{\theta}_{i,j} = \frac{n_{i,j} + \lambda Prox(w_j) + \mu p(w_j|C)}{n_j + \sum_{j=1}^{|V|} \lambda Prox(w_j) + \mu} \quad (4)$$

## 4 SMOOTHED PROXIMITY LANGUAGE MODEL

So far we have expanded the unigram language model with the term proximity information. In addition, we can employ latent semantic analysis (LSA) to smooth the term frequency (Steinberger, 2004). Latent semantic analysis relies on *singular value decomposition*, which extracts latent semantic information from a term frequency matrix (Landauer et al., 1998).

### 4.1 Semantic Smoothing

We first calculate term frequency matrix for each document, with the rows consisting of the terms and the columns consisting of sentences in the document. Each entry  $t_{i,j}$  of the matrix contains the number of occurrences of the word  $w_i$  in document  $d_j$  divided by the total occurrence of the word in the collection.

Traditionally, the term frequency information is further augmented with the inverse document frequency to incorporate word importance; however, in our case, a similar role will be performed by semantic smoothing.

With the term frequency matrix in hand, we perform singular value decomposition, which extracts orthogonal matrices with components in the latent semantic space. A dimension in the latent semantic space can be thought of as a topic for the document; for example, it may take in terms “car” and “truck” as input, and yield us a new dimension that is a linear combination of these two words, which may be interpreted as a “vehicle”.

The output from singular value decomposition consists of the orthogonal matrices  $U$  and  $V$  and the diagonal matrix  $\Sigma$ .  $U$  gives component vectors for each term in the latent semantic space, while  $V$  similarly relates each document to the latent semantic space. Meanwhile,  $\Sigma$  gives us the relative importance of each latent semantic dimension.

We can now refine  $n_{i,j}$ , the number of occurrences of the word  $w_j$  in document  $d_i$ , by exploiting the equation:

$$n_{i,j} = n_i \times p(w_j) \quad (5)$$

where  $n_i$  is the total number of words in document  $d_i$ , and  $p(w_j)$  is the probability of the word  $w_j$  in the collection. Next, we can use results from singular value decomposition to smooth  $p(w_j)$  as in the equation below, where  $d$  represents a dimension in the latent semantic space.

$$p(w_j) = \sum_d p(w_j|d)p(d) \quad (6)$$

We must now estimate  $p(d)$  and  $p(w_j|d)$ , which are needed to calculate  $p(w_j)$ . Relative weights for each dimension are already given in the  $\Sigma$  matrix, and  $p(d)$  can be estimated as

$$p(d) \sim \sigma(d) \quad (7)$$

As for  $p(w_j|d)$ , this can be estimated using a variety of ways. The most obvious is to consider the length of term vector, weighted by the importance of each dimension, as a measure of its influence, which results in the estimation:

$$p(w_j|d) \sim \sqrt{\sum_d (U(j,d)\sigma(d))^2} \quad (8)$$

Now, using the semantically smoothed value for  $n_{i,j}$  gives us the SPLM estimator:

$$\hat{\theta}_{i,j} = \frac{n_i \times p(w_j) + \lambda \text{Prox}(w_j) + \mu p(w_j|C)}{n_j + \sum_{j=1}^{|V|} \lambda \text{Prox}(w_j) + \mu} \quad (9)$$

## 4.2 Ranking Function

The smoothed proximity language model gives us a probability of each word occurring in a document. We can then use these probability values to assign scores for each query-document pair using the KL divergence score as in (Zhao and Yun, 2009). The KL divergence score represents the information loss incurred by using the query instead of the document, and the closer this divergence score is to zero, the closer the document is to the query. In document ranking, we would thus choose documents with the smallest KL divergence scores. The KL divergence is defined as:

$$D_{KL}(\hat{\theta}_q || \hat{\theta}_d) = \sum_i \hat{\theta}_q(i) \log \frac{\hat{\theta}_q(i)}{\hat{\theta}_d(i)} \quad (10)$$

where  $\hat{\theta}_q$  is the estimator for the query, and  $\hat{\theta}_d$  is the estimator for the document. After substitution of the estimators, Equation 10 reduces to

$$\sum_i p(w_i | \hat{\theta}_q) \log \frac{\theta_{q,i}}{\alpha_d p(w_i | D)} + \log \alpha_d \quad (11)$$

where  $\theta_{q,i}$  is the probability of the word  $w_i$  occurring in the query, and

$$\alpha_d = \frac{\mu}{n_i + \sum_{i=1}^{|V|} \lambda \text{Prox}(w_j) + \mu} \quad (12)$$

## 5 TEXT SUMMARIZATION

Ranking functions that rank documents based on a query can be used to rank sentences for text summarization instead. When there is only one document in the collection set, one can use the ranking function in a straightforward manner to extract the most relevant sentences. However, there may be multiple documents to be summarized, as may be the case when generating a summary from multiple news articles.

### 5.1 Summarizing Multiple Documents

There are two approaches to rank sentences in this case: the first is to combine all the documents, and then to compute the sentence relevance score against the combined document; the second is sum the relevance scores between the sentence and each of the documents. We use the latter approach, as it has three advantages. First, it is a scalable approach that can easily admit additional documents. Second, one can easily assign and readjust weights of different documents; for example, more weight may be given to

more reputable sources. Finally, proximity information can be better exploited when a sentence is compared against each document separately.

## 5.2 Selecting Multiple Sentences

While the ranking function gives us the most representative sentence, it provides no information for selecting the best  $k$  sentences when there are multiple sentences to be selected.

There exist many solutions to this problem. The most basic solution is to select the  $k$  top scoring sentences. However, doing so may result in selection of redundant sentences. To help mitigate this problem, one may only select sentences that have less than a certain degree of overlap with every sentence in the summary set (Kumar et al., 2009). More sophisticated approaches, such as the MMR algorithm, formulate the sentence selection problem as a search problem that seeks to maximize an objective function which gives credit for the relevance score, and penalizes for overlap (Carbonell and Goldstein, 1998).

Experiments did not show many differences between these methods, and for our evaluation, we use the aforementioned approach used in (Kumar et al., 2009).

## 6 EXPERIMENTAL SETUP

The Summarization Task in the Text Analysis Conference (TAC) 2009 is an evaluation framework that provides a comparative analysis for computer-generated summaries. Using this framework, accuracy scores for short summaries can be compared among different algorithms. In the task, the challenge is to generate summaries of up to 100 words from a collection of 10 documents across 44 different topics (Gillick et al., 2010). Then, the generated summary is compared against model summaries using ROUGE-2 measures, which gives recall and precision scores based on whether bigrams in the generated summary are also present in the model summary (Lin, 2004).

### 6.1 Methods for Comparison

We compare our approach against methods that only use either PLM or semantic smoothing to see whether employing both yields better results. In addition to LSA, we compare semantic smoothing using latent Dirichlet allocation (LDA) (Blei et al., 2003) and random indexing (RI) (Sahlgren and Karlgren, 2005). We thus consider the following approaches:

- Language Modeling (LM) only.

- Proximity Language Model (PLM).
- LM + latent semantic analysis.
- LM + random indexing.
- LM + latent Dirichlet allocation.
- PLM + latent semantic analysis.
- PLM + random indexing.
- PLM + latent Dirichlet allocation.

Sections 3-4 show the formulas used for the proximity language model and PLM + latent semantic analysis. The formulas used for other methods can be adapted from these formulas, as we show.

#### 6.1.1 Formula for the Language Modeling Approach

Language modeling approach represents the most basic approach among our comparison methods. This approach uses the estimator in Section 3.1, and the KL divergence in Equation 10 can be used in a straightforward manner to derive scores for each sentence.

#### 6.1.2 Formula for the Random Indexing Approach

Random indexing represents another form of semantic smoothing. Thus, employing random indexing instead of LSA will affect equations in Section 4.1.

Running random indexing on the term-document matrix will produce a term-context matrix. We can perform LSA on this matrix, which will yield matrices  $U$  and  $V$  and  $\Sigma$  that we can use in Equations 7-8 in Section 4.1. Using these values will result in a modified estimator in Equation 9. Sentence ranking can then proceed as in Section 4.2. This method follows the random indexing + LSA approach shown in (Sellberg and Jonsson, 2008).

This approach has advantages over LSA in performance due to the fact that the term-context matrix is of a reduced dimension. Computing the term-context matrix takes an order of magnitude less time than LSA, and thus, this approach leads to an improved overall performance compared to regular LSA.

#### 6.1.3 Formula for the Latent Dirichlet Allocation Approach

Latent Dirichlet allocation is yet another form of semantic smoothing. LDA can be used to analyze the term-document matrix and provide latent topic probabilities for each term. The topic probabilities for each term can be substituted for  $p(w_j|d)$  in Equation 6.

A weakness of using LDA in our semantic smoothing framework is that LDA does not provide

topic weights. So instead of using tailored topic weights, we use a constant value of 1 for  $p(d)$  in Equation 6.

The updated  $p(d)$  and  $p(w_j|d)$  values can be used in Equation 9 to yield a modified estimator for the LDA approach. Sentence ranking can then proceed as in Section 4.2.

### 6.1.4 Baseline Model for Comparison

The baseline model that we compare against is the HexTac baseline model provided by NIST, which uses five human sentence extractors to manually select the summary set (Genest et al., 2010). NIST states that results from this model “provides an approximate upper bound on what can be achieved with a purely extractive summarizer”.

## 7 RESULTS

We first compare text summarization results from our model against reference and baseline models to show advantages of the PLM + semantic smoothing approach. We then provide further experiments to show that the PLM + LSA model is robust against parameter variations.

Table 1: Results.

Algorithm	F-score
Language Model (LM)	.0954
Proximity Language Model (PLM)	.0968
LM + latent semantic analysis (LSA)	.0989
LM + latent Dirichlet allocation (LDA)	.0993
LM + random indexing (RI)	.0961
PLM + LSA	.1054
PLM + LDA	.0947
PLM + RI	.1027
HexTac Baseline	.1082

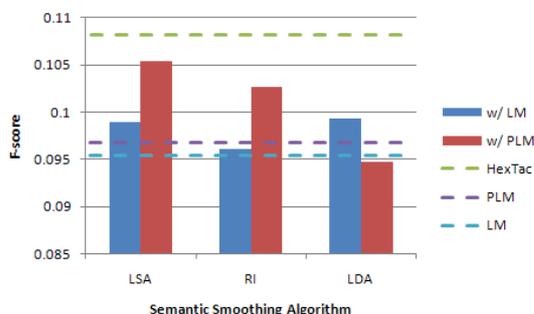


Figure 1: Comparison Results.

In Figure 1, we see that the performance of SPLM is generally better than approaches that only utilize the proximity language model or semantic smoothing. The only exception is the PLM + LDA approach, which may be explained by the fact that LDA does not provide topics weights used in Equation 7.

The results show that SPLM can achieve a score that is close to the HexTac baseline model, which is considered to be an upper bound for extractive algorithms such as ours (Genest et al., 2010).

### 7.1 Robustness Testing Results

We may be wary of the choice of Dirichlet prior parameters  $\lambda$  and  $\mu$  in Equation 9. If our results are too sensitive to these parameters, then this limits applications of the approach in new domains. We varied the values of  $\lambda$  and  $\mu$  from 300 to 8900 to see whether parameter variation would lead to a large change in the F-score. Fortunately, we found these variations to only cause a maximum of 4.8% change in the F-score.

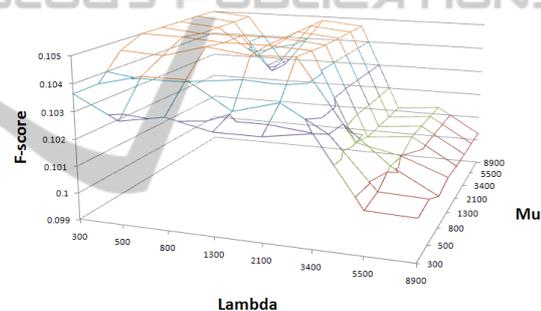


Figure 2: Robustness Testing Results for the PLM + LSA Approach.

## 8 CONCLUSIONS

The key contribution of this paper is in developing an approach for combining semantic information with proximity information for text summarization. The approach is based on the proximity language model, which expands the unigram language model to incorporate proximity information. This paper novelly expands the proximity language model to incorporate semantic information using latent semantic analysis (LSA). The proximity language model considers the physical distance between terms to provide a better ranking, while LSA applies semantic smoothing to term importance. We argue that the presented approach achieves a good balance between syntactic and semantic information.

Upon evaluation of our approach, we find that it yields an improvement on models using just PLM or LSA, and also comes close to what is considered the limit for extractive systems. Moreover, further experiments show that it is robust to parameter variations.

There still remains much room for improvement. For achieving better results, we imagine having a better sentence selection process, assigning variable document weights, and using other forms of topic modeling for better semantic smoothing.

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