

LINEAR COMPLEXITY STEREO CORRESPONDENCE

From Interpolation to Segment-based Approach

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Abstract: This paper presents the work in progress on the enhancement of a stereo correspondence method based on linear complexity region indexing with an image segmentation method. Such improvement shows itself to achieve better results (compared to its predecessor) when evaluated on Middlebury Stereo Evaluation, keeping the computing complexity $O(n)$ of the algorithmic solution. In spite of the better results, this method still need to solve some issues related to surfaces inclinations. The steps taken to create this improvement, some stereo correspondence results and evaluations are presented.

1 INTRODUCTION

Perception is an important field on MR (Mobile Robotics). This field still has a need of solutions' development, mainly on computer vision (Murray and Little, 2000). The MR perception can be performed by several different kinds of passive and active sensors. This work explores the subfield of PSV (Passive Stereoscopic Vision) for MR.

For a better understanding, PSV's classic processing pipeline is: 1) Calibration; 2) Rectification; 3) Correspondence; 4) Reconstruction; 5) Spatial Information Use. Of course, some applications don't use this whole pipeline, but most of them do. In our case, we are going to assume that we have well defined and working methods for steps 1, 2, 4 and 5. That sets our focus to step 3, the Correspondence issue.

In our application scenario, we seek to build complete 3D maps from the MR environment. We also aim to recognize 3D objects. When using dense correspondence, instead of the sparse one, we will be able to obtain information around solid objects and walls. These "solid" objects allow us to compute complete 3D maps, instead of partial 3D maps or merely 2D maps of the environment. These constraints led us to choose the dense correspondence instead of sparse correspondence.

When the MR is operating, it is preferred to use low cost computing methods for processing all kinds of information. That preference is either related to energy saving or to low time processing.

Based on those premises, this work developed a research on dense correspondence methods. We started by comparing a LM (Linear Complexity Method) (low cost computing) - presented at (Oliveira and Wazlavick, 2005) - with a state-of-the-art method.

1.1 Middlebury Images

For comparison and evaluation purposes, the method used in this work is proposed by (Scharstein and Szeliski, 2002) and (Scharstein and Szeliski, 2003). The authors of this EM (evaluation method) also provide a web-based rank, for comparison with several state-of-the-art methods (Middlebury, 2011). This approach is widely accepted and used when comparing stereo correspondence methods.

This EM has 4 (four) most used stereo image pairs available; each pair has an expected correspondence result and a name. We have used the four images in our evaluations, but only the results for *Teddy* pair will be shown on this paper as illustrative results. The pairs' names are: *Teddy*, *Tsukuba*, *Venus* and *Cones*. The *Teddy* original left

image is shown in Figure 1 and its expected result is depicted in Figure 2.

There are 3 (three) main evaluations performed by this EM: 1) **nonocc** – performs evaluation only on non-occluded areas; 2) **all** – performs evaluation in all areas of the expected result; and 3) **disc** – evaluates only “near image edges” areas.



Figure 1: Left image of the *Teddy* stereo pair.

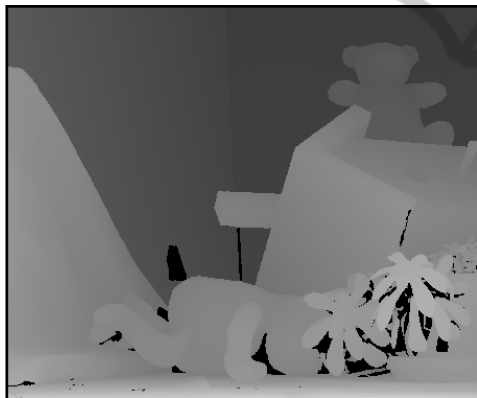


Figure 2: Expected correspondence result for the *Teddy*.

2 THE LINEAR APPROACH

The LM was proposed by Oliveira and Wazlavick, 2005 and performs dense stereoscopic correspondence on linear computing complexity. That means an algorithmic solution on $O(n)$ and plays a role on low computing cost. The above-mentioned method is divided in four basic steps: 1) Region indexing based on intensities; 2) Wrong correspondences elimination; 3) Continuity verification; 4) Disparity map interpolation. The first three steps generate sparse correspondence results and step four generates the dense result by interpolation.

Step 1, region indexing based on intensities, is described in Figure 3. A Kernel is applied to a Region to describe a chain of Selected Points. Also, a Mean Value from the Region is used as reference on a Binary Threshold procedure over the Selected Points. The result is a binary Index number, for finding corresponding regions over the stereo’s epipolar line.

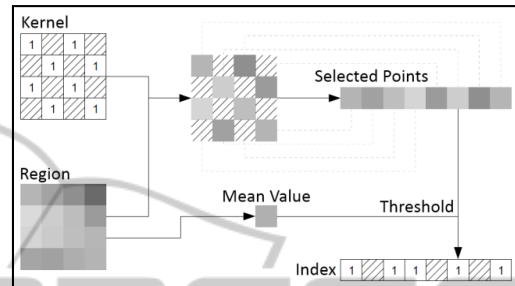


Figure 3: Indexing operation for LM. Image from (Oliveira and Wazlavick, 2005).

When applying this LM to the *Teddy* image, (Scharstein and Szeliski, 2003), we reach the result shown in Figure 4. The obtained result for this LM can be visually compared to the expected result (Figure 2), where both of them showed similar disparities to the same regions. The biggest differences between them (errors) are around the edges of the image’s objects.

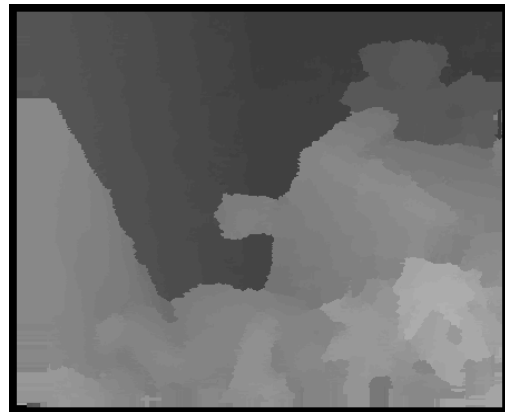


Figure 4: Final result for the linear method on *Teddy*.

We also applied this method to images *Tsukuba*, *Venus* and *Cones* and we submitted all the results taken to EM presented in section 1.1. The EM results can be found in Table 1.

Despite of the similar result presented in Figure 4, the evaluation’s results in Table 1 report a bad correspondence between all of the obtained results against the expected results for all the images.

Table 1: Original linear method evaluation (Closer to 0.0 best. Closer to 100.0 worst). Threshold = 2.

Image	Evaluation		
	nonocc	all	disc
Tsukuba	94.0	93.4	85.6
Venus	99.8	99.8	97.7
Teddy	100.0	99.5	99.9
Cones	99.7	99.4	99.1

2.1 Sparse Evaluation of Steps

After getting bad scores from the LM's final result, we studied the sub-results from each step. As mentioned before, LM steps 1, 2 and 3 resulted in sparse data, but the applied EM does not evaluate sparse results. For that reason, we defined a simple SEM (Sparse Evaluation Method).

We were based on EM's idea and applied a *hit-and-miss* technique with a threshold value as error tolerance. This is applied only to the sparse correspondences found. We can obtain a percentage value from that analysis, and such percentage indicates the proportion of errors on each LM step. We only considered steps 2, 3 and 4, which were called *Indexing*, *Continuity* and *Interpolation*, respectively. The result can be seen in Table 2.

Table 2: LM steps analysis (Closer to 0.0 best. Closer to 100.0 worst). Threshold = 2.

Step	Errors (%)			
	Teddy	Tsukuba	Venus	Cones
<i>Indexing</i>	7.50	5.32	20.59	3.81
<i>Continuity</i>	7.87	6.08	23.05	4.99
<i>Interpolation</i>	11.08	6.85	25.37	9.27

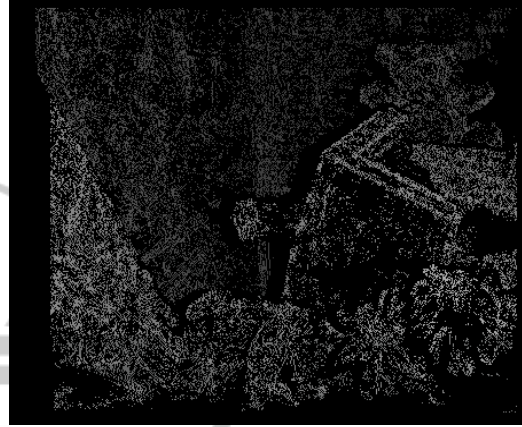
As the results indicate (Table 2), each step on the process adds more error to the final result. Improving each step by getting lower errors or using earlier steps (with less accumulated error) should be done for obtaining consistent information of the environment. Figure 5 shows the *Indexing* step result.

2.2 Segment-based Step

As pointed in the previous section, the improvement of LM results could be performed by enhancing each individual step. For this reason, we have studied the use of a method based on Klaus et al, 2006. We propose to change the interpolation step for a segment-based expansion of those found correspondences.

ISP (Image segmentation process) is a pixel grouping process, where two or more pixels (or even

sets of pixels) are grouped while both of them satisfy two basic conditions: 1) they are connected spatially, and 2) they are said to be similar by some similarity measure. In the end of this process, we have sets of pixels which should indicate objects (or pieces of objects) in images.


 Figure 5: *Indexing* Sparse results on *Teddy*.

We used the regions identified by the ISP as "safe regions with fixed disparity". The disparity value for each region is determined by a *winner-takes-all* process, where n_d is the number of occurrences of a d disparity, R_x is an x given region identified by the ISP and D is the set of identified sparse correspondences of LM's step 2.

$$n_d = |R_x \cap (d \in D)| \quad (1)$$

The process is described by Equation (1). The disparity with most occurrences in a given region will be assigned for that whole region.

2.3 Image Segmentation Method

The image segmentation can be achieved by using any image segmentation algorithm. Of course, better results would be taken with better algorithms. Our definition of a better segmentation algorithm is that which is able to find the proper objects boundaries in images, but the best algorithms are usually the most computational intense solutions. In our problem, we intend to keep one of the main advantages of the LM, the low cost computing.

The only way of keeping that linear computing time is by using a linear segmentation method. For that reason, we chose the CSC (*Color Structure Code*) approach (Rehrmann and Priese, 1997). That approach obtains robust results while processing color images with a performance of $n \cdot 4$ times operations on the worst case. That preserves our constraint: $O(n)$.

An example of result obtained with CSC method when applied to *Teddy* left image is shown in Figure 6. The only parameter in this method is a threshold, fixed on 24 for all our experiments.

3 RESULTS

We applied the suggested approach to the same 4 (four) images studied in Table 1. Those results were evaluated through the same criteria as in Table 1. Figure 7 shows the resulting image for the *Teddy* image, while Table 3 contains the evaluation results for the experiment.



Figure 6: Result of CSC method applied to *Teddy* image.

This approach has improved the original's method score on (Middlebury, 2011). One of the main contributions for that accomplishment is the edge preserving of the objects on images. That enhance on edges is derived directly from the image segmentation algorithm.

Table 3: Proposed method evaluation (Closer to 0.0 best. Closer to 100.0 worst). Threshold = 2.

Image	Evaluation		
	nonocc	all	disc
Tsukuba	4.17	4.68	15.3
Venus	4.13	4.54	12.8
Teddy	14.1	17.6	23.9
Cones	8.44	15.4	15.7

On the other hand. Even after getting quite higher scores, there are still some problems to be solved. As shown in Figure 7, there are several small regions in black color. Those regions are called *unsolved regions* and that is either because of small faults on segmentation algorithm (black dots on Figure 6) or because of an inexistence of intersection

between a sparse correspondence (Figure 5) and an image segment (Figure 6).

4 CONCLUSIONS

The proposed method is able to improve the LM's score on (Scharstein and Szeliski, 2002) evaluation's method. That is significant improvement, since it went from a very low score to a higher one. That improvement was also enough to get this method ahead of at least 10 other correspondence approaches that are ranked at (Middlebury, 2011).



Figure 7: Result of the proposed method when applied to *Teddy* image.

We also have several improvements to study. For example: the occurrence of inclination of some objects along Z axis. Small inclinations would result in smaller errors, while big inclinations would end in bigger errors. Other points we are studying are: 1) the development of a color-based indexation, instead of intensity-based (for better indexing results); and 2) fixing the *unsolved regions*, detailed in the previous section.

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