

HOW TO TRANSMIT MESSAGES VIA WSN IN A HOSTILE ENVIRONMENT *

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Abstract: In this paper we present a scheme for secure message transmission in WSN in the presence of an adversary. We assume that the adversary can easily find *some random* nodes. However it is much harder for it to find all of them (or even a concrete subset) quickly. Security of the proposed scheme is based on this practical assumption. The protocol can be easily combined with various routing schemes as a security layer preserving all merits of the underlying protocol for the price of reasonable communicational and storage overhead.

1 INTRODUCTION

In this paper we present and analyze a protocol for secure messages transmission in a radio network of weak devices. Proposed method provides confidentiality of transmitted message. It can be combined with other security methods in order to ensure authentication, anonymity or other aspects of security. It may be considered as an additional security layer.

The network we have in mind is a multi-hop sensor network used for security purposes – such as a network used for intrusion detection, protection of industrial installations, or a military system used in a battlefield. In this type of systems it is not possible to use very advanced general purpose security mechanisms due to many reasons including limited computational power, short range of communication, small memory of devices and their cost. The nodes of the networks can be seized by an adversary. Since the devices have to be of low cost, we have to assume that the adversary can retrieve all secret keys installed inside a captured device. On the other hand, providing security, in particular confidentiality of processed data may be a key-issue in many vital applications mentioned.

One of a few possible methods of improving message confidentiality in such settings is splitting the message into pieces. A simple solution is, for example, to use secret sharing and send the shares via disjoint paths. However, in this solution the adversary has to capture only a single node on each path to

recover the message, as long as no complex methods like onion encoding are used.

Main contribution of this paper is a secure message transmission algorithm consisting of specific message partitioning and routing algorithm. The solution is based on a following paradigm: the adversary has to capture a very specific subsets of nodes in order to break confidentiality.

1.1 Previous and Related Work

There is a long list of papers presenting solutions based only on symmetric methods, and in particular key predistribution e.g. (REN, ; Cichoń et al., 2009; Du et al., 2005). The main goal of these protocols is to establish encrypted channels in the target environment between devices. The keys used are symmetric keys shared by communicating devices. We would like to stress that solution proposed below can be efficiently combined with key-predistribution scheme, including extensions like key-evolution protocols (Klonowski et al., 2007; Ren et al., 2006) providing forward or backward security. However, methods based only on key predistribution schemes does not solve problems stated in our paper. Some other notable security mechanisms in similar models were presented in (Chan and Perrig, 2005; Eschenauer and Gligor, 2002).

Proposed construction resembles in some sense DUO-onions / Hydra-Onions described in (Iwanik et al., 2004) (i.e. choosing several nodes in each intermediate step), however goals, as well as requirements of those protocols are completely different. There

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are also many other security protocols based on dividing protected content into parts – one of the most important example is Rivest’s Chaffing and Winnowing (Rivest, 1998) or (Iwanik et al., 2004). However, to the best of our knowledge they cannot be used directly to solve issues discussed in our paper.

2 MODEL

Network Model. We consider a multi-hop radio network. It can be seen as a communication channel consisting of consecutive layers L_1, \dots, L_l .

Each layer is a set of nodes. For the sake of simplicity we assume that each layer contains n nodes labeled from 1 to n and layers are disjoint. Each pair of nodes in consecutive layers shares a (symmetric) secret key used to encrypt messages exchanged between them. This forms a secure channel between pairs of nodes. Thus, each node keeps $2n$ cryptographic keys.

Each packet broadcasted by a node from layer L_i is received by all nodes in layer L_{i+1} . Each packet consists of a header and encrypted data. Header is a short encrypted data that allows a node to quickly check whether it is the proper receiver of the message.

Starting from this point, we assume that any message sent between layers is encrypted and can be read only by the party having access to cryptographic keys stored in the memory of the sender or the receiver. For the sake of clarity, this fact is not reflected in the notation and the description of the protocol.

Note that most of assumptions can be significantly relaxed in a straightforward manner. Indeed, proposed scheme can be used not only in structured networks but also in a various kinds of ad hoc networks.

Model of the Adversary. The aim of the adversary is to get the encrypted message transmitted through the network. If the adversary is successful we say that the message is *corrupted* (seized).

We assume that the adversary can capture some subset of nodes and is able to retrieve all cryptographic keys, and data from them. Moreover we assume that the adversary can eavesdrop communication in the whole network.

3 PROTOCOL

We describe transmission of a message M according to our protocol. At each layer of the network there is a subset of l nodes (*transmitting nodes*) responsible for M . The l ($2 \leq l \leq n$) is called *forking parameter*. It

governs security/communication trade-off – for small l communication overhead is smaller but it is easier to seize the message. The transmitting nodes are chosen pseudo-randomly as described in **Routing** paragraph.

3.1 Protocol Overview - Single Message

The protocol uses the standard XOR-based secret sharing procedure: in order to split a message M into l parts: first $l - 1$ parts M_1, \dots, M_{l-1} are chosen independently at random. The part M_l is computed as $M_l = M \otimes M_1 \otimes \dots \otimes M_{l-1}$ (\otimes denotes bitwise XOR operation). It is obvious that M can be retrieved only having all M_i for $1 \leq i \leq l$. Moreover, any nontrivial subset of these parts does not reveal any information about M .

Initialization. The *source node* decides to transmit the message M (represented in the Fig. 1 as M_0). In the first step it partitions M^0 into l parts $M_{1,1}^0, \dots, M_{l,l}^0$ (the upper index denotes the layer number, the lower index – the message part number). Then it randomly chooses l receivers in the layer L_1 and sends each part of the message to one of them.

The receiver of the j th part in the layer L_1 partitions its part $M_j^1 = M_j^0$ into l parts $M_{j,1}^1, \dots, M_{j,l}^1$ (the first lower index denotes part of the message, the second - part of the part of the message) and sends them to l nodes in the group L_2 . The receivers in L_2 are assigned in such a way that all senders from L_1 send their parts to the same set of l nodes from L_2 .

Message Partitioning. For $i < n$ and $j \leq l$, the j th transmitting node in the layer L_{i+1} collects l parts $M_{1,j}^i, \dots, M_{l,j}^i$ from l nodes from the layer L_i and combines them to obtain $M_j^{i+1} := M_{1,j}^i \otimes \dots \otimes M_{l,j}^i$ and again splits M_j^{i+1} into another l parts $M_{j,1}^{i+1}, \dots, M_{j,l}^{i+1}$ that are sent to the nodes in L_{i+2} .

Routing. As mentioned before we want each transmitting node from one layer to send parts of its message to exactly the same l nodes from the following layer. As shown in Fig. 1 each packet exchanged between layers contains not only a message part but also a pseudo random number r generated by its sender. Each receiver combines all received random numbers and basing on the result deterministically selects l *transmitting nodes* in the following layer. Then it generates its own pseudo random number and attaches it to each packet it sends to the receivers in the next layer. This way all l receivers get the same set of pseudo random values and can independently determine the same set of l receivers in the following layer.

Sink. From the last layer all parts are sent to a sink representing the receiver of the original message. Note that: $M_{1,j}^i \otimes \dots \otimes M_{l,j}^i = M_j^{i+1} = M_{j,1}^{i+1} \otimes \dots \otimes M_{j,l}^{i+1}$ Message parts are repartitioned on each level so that it is not possible to reconstruct the original message capturing some parts on each layer – all parts from at least one layer is necessary.

The idea of the protocol is described in Fig. 1.

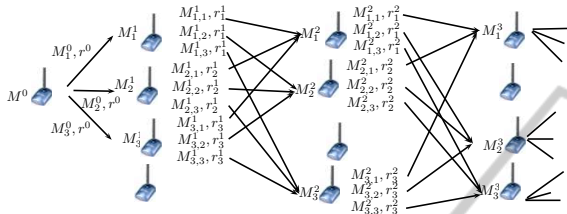


Figure 1: Exemplary protocol execution for one message and $l = 3$.

Note that this protocol may be used with various other methods - for example with Message Authentication Codes (MAC) to make the change of the message more difficult or secret sharing scheme (Shamir, 1979) for robustness.

4 SECURITY ANALYSIS

In this section we discuss security aspects of the proposed scheme in some realistic scenarios. We assume that adversary can capture at most K nodes. Our analysis is based on the following observations:

1. The adversary is able to learn the plaintext, if he controls all transmitting nodes for this plaintext in at least one layer.
2. Information gained by the adversary from nodes in one layer does not help to corrupt the message by attacking another layer.

Since our protocol is based on one-time-pad encoding offering unconditional security, the analysis boils down in fact to combinatorial questions.

First, we discuss the case, wherein a single message is transmitted through the channel.

Nonadaptive Attack. In this subsection we consider a scenario, wherein the adversary chooses the nodes to be corrupted **before** the transmission. Let us assume that the adversary knows the partition into n -node layers and corrupts arbitrary k_i nodes in the i th layer (provided that $\sum_i k_i \leq K$). First note that if $k_i < l$ the adversary does not learn anything from the i th layer. On the other extreme, if $k_i = n$ for at least one layer, the adversary breaks each message for sure. Thus, the interesting case is that $n > K \geq l$.

Below we investigate, which strategy of assigning the numbers k_1, k_2, \dots, k_t maximizes adversary's chances of corrupting the message (equivalently, at some layer all l nodes transmitting a message are under adversary's control). Let $p_{l,n}(k_1, k_2, \dots, k_t)$ be the probability that the adversary will corrupt the message provided that he controls k_i nodes in the i th layer. It can be proved that the function $p_{l,n}$ is maximized if the value k_1 is maximized. I.e the adversary chooses all K nodes from a single layer. More precisely one can prove following theorem

Theorem 4.1. *Let $n > K \geq l$ be the number of corrupted nodes and k_i be the number of corrupted nodes in the i th layer for $i = 1, \dots, t$. The strategy of putting all corrupted nodes in exactly one layer maximizes probability of the adversary for corrupting the message.*

The above theorem is intuitive, however the formal proof is non-trivial.

By Theorem 4.1 we get immediately the following corollary:

Corollary 4.1. *In the system with splitting parameter l , with n nodes in each layer, and the adversary capable to corrupt K nodes, the probability that the adversary corrupts a transmitted message is 0 if $K < l$, $\binom{K}{l} / \binom{n}{l}$ if $l \leq K < n$, and 1 if $K \geq n$.*

Random Choice of Captured Nodes. Now we assume that an adversary has access to exactly K nodes randomly chosen out of all $L = n \cdot t$ nodes. We believe that such a model is very realistic for most of ad hoc wireless sensor networks. Indeed, collecting small devices distributed over a large area in restricted time significantly reduces possibility of collecting devices that belongs to a particular layer.

Lemma 4.1. *Let us assume that an adversary has access to K nodes chosen at random out of $L = n \cdot t$ nodes in total. Let us assume that a single message is transmitted through the network with splitting parameter l . Then the probability that the adversary collects all l transmitting node from at least one layer is*

$$S_n = \sum_{i=1}^t (-1)^{i+1} \binom{t}{i} \frac{\binom{Kl}{l}}{L^l} < \frac{1}{2} \left(\left(1 + \frac{1}{t}\right)^t - \left(1 - \frac{1}{t}\right)^t \right).$$

In the last inequality we assumed without significant limitation of generality that t is an odd number. Standard proof is skipped. Fig. 2 shows obtained estimations for small number of captured nodes.

Nodes Chosen After the Transmission. Let us consider a scenario wherein the adversary can observe the traffic, localize transmitting devices and, after transmission, capture K devices. Obviously, as long as $K < l$ it is not able to corrupt any message.

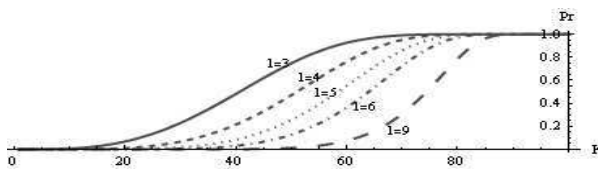


Figure 2: A bound on probability that an adversary collects all l parts from one layer for $L = 100$, $t = 10$, and $l = 3, 4, 5, 6, 9$ respectively for $t \cdot l < K < L/t$.

Otherwise, in the case of a **single** transmitted message, the strategy of the adversary is trivial - it chooses l transmitting nodes from any layer.

The situation is much more complicated when the adversary can observe simultaneous transmission of many, say N messages and then capture some nodes. The number of message pieces transmitted through different nodes is not the same. The adversary may increase his chances by choosing the nodes with relatively many transmissions going through.

Since it is optimal to attack one layer, we consider a single layer. To corrupt one of N messages the adversary must collect all l pieces of this message. Assume that the adversary is able to corrupt K nodes. Let S_K be a family of all subsets of all n nodes of cardinality K . If subset $S \in S_K$ contains all transmitting nodes of exactly x messages, we say that x messages go through S . Let $MAX_{n,K}$ be a random variable denoting the number of messages corrupted by the adversary if he controls K out of n nodes chosen in the optimal way. Of course, the adversary does not know the optimal subset of nodes to attack, but we wish to check what would be adversary's advantage with this knowledge granted for free.

Theorem 4.2.

$$\Pr \left[MAX_{n,K} \geq Np + \frac{1}{3} \log \left(\binom{n}{K} N \right) \left(1 + \sqrt{\frac{18Np}{\log \left(\binom{n}{K} N \right)} + 1} \right) \right] \leq \frac{1}{N}.$$

In particular, for realistic settings and large (compared to the number of devices) number N of sent messages we get the following bound:

Corollary 4.2. For $\log \left(\binom{n}{K} N \right) < Np$ following relation holds: $\Pr \left[MAX_{n,K} \geq Np + 1.5 \sqrt{N \log \left(\binom{n}{K} N \right) p} \right] \leq \frac{1}{N}$.

Proof. Due to space limitations we skip proofs.

Practical meaning of this bound is that the advantage of the adversary given the possibility to choose nodes after transmission is not significantly greater than if the adversary would choose nodes at random. Indeed, in general for fixed n, K, l we have $MAX_{n,K} = N \cdot p + o(N)$ w.h.p.

5 CONCLUSIONS

The main proposal of this paper is to couple security mechanisms for security related application of sensor networks (or just networks with confidential information) with mechanisms that are based on physical difficulty to *find* devices located at random. We believe that from practical point of view this is a crucial mechanism and it can/should be exploited when constructing communication protocols in some specific networks (like military networks). The protocol presented is just an example of such an approach.

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