

COMPARATIVE PERFORMANCE ANALYSIS OF SUPPORT VECTOR MACHINES CLASSIFICATION APPLIED TO LUNG EMPHYSEMA IN HRCT IMAGES

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Abstract: High-resolution computed tomography (HRCT) became an essential tool in detection, characterization and follow-up of lung diseases. In this paper we focus on lung emphysema, a long-term and progressive disease characterized by the destruction of lung tissue. The lung patterns are represented by different features vectors, extracted from statistical texture analysis methods (spatial gray level dependence, gray level run-length method and gray level difference method). Support vector machine (SVM) was trained to discriminate regions of healthy lung tissue from emphysematous regions. The SVM model optimization was performed in the training dataset through a cross validation methodology, along a grid search. Three usual kernel functions were tested in each of the features sets. This study highlights the importance of the kernel choice and parameters tuning to obtain models that allow high level performance of the SVM classifier.

1 INTRODUCTION

HRCT scans are very accurate in diagnosis of lung diseases. However, the interpretation of HRCT images, in the presence of patterns associated with lung diseases is a time-consuming task and requires experience. The latest generations of CT scanners allow the acquisition of a large number of images per patient examination. The use of computerized image analysis methods can be of great help in

radiologist services improving precision, consistence and earlier diagnosis.

Emphysema is a chronic lung disease that affects severely person's everyday life. The principal factor risk is cigarette smoking, although genetic conditions, air pollution, chemical fumes or dust also can cause emphysema. This disease is defined as "a permanent, abnormal enlargement of airspaces distal to the terminal bronchiole, accompanied by the destruction of the walls of the involved airspaces"

(Verschakelen, 2007). The diagnosis of emphysema in HRCT images is based on the detection of regions of very low attenuation that contrast with healthy lung. Figure 1 shows examples of a region of a healthy lung and a region of emphysema.

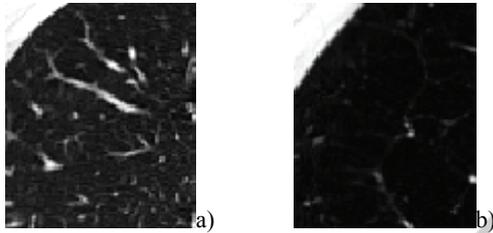


Figure 1: Visual aspects of lung tissue pattern in CT images: a) Healthy and b) emphysema.

In this work feature extraction is based on statistical approach to describe lung tissue texture. Classification of each region of interest (ROI) in classes of lung pattern disease was performed using SVM algorithm.

SVM has emerged as an efficient technique for solving classification problems. SVM has its origin on statistical learning theory and structural risk minimization (Vapnik, 1995) (Burges, 1998). A comparative study was performed by Meyer (Meyer, 2005) between SVM and other popular classifiers. The results showed that SVM classifiers are among the best. In Depeursinge et al. (Depeursinge, 2010b) five common classifiers were compared in their ability to discriminate six lung tissue patterns in HRCT. The results of this study showed that SVM constitutes the best trade-off between the error rate and the capability of generalization. However, performance of SVM strongly depends on user kernel choice and parameters selection. In training phase the SVM model optimization must be carefully done. No optimal parameter selection can lead to significant reduction in classification performance. This fact constitutes the main limitation of the use of SVM. In this work we carried out a comparative performance analysis of different kernel functions in classification ROIs of normal lung and ROIs of emphysema, under SVM model parameters variations, using features vectors extracted from three different methods.

The remainder of the paper is organized as follows. Section 2 briefly describes the feature extraction methods. Section 3 presents the theory of SVM classification algorithm. The dataset used and optimization methodology of the classifier is described in section 4. In section 5 results are presented and discussed and final conclusions are drawn in section 6.

2 FEATURES EXTRACTION

Texture analysis is fundamental in medical images interpretation. In this study each texture pattern is described by their statistical properties, organized in a n -dimensional feature vector. The next paragraphs briefly review the principles of the methods used to describe ROIs texture.

In Spatial Gray Level Dependence Method (SGLDM) the second-order distribution of pixels gray levels are explored. Each entry of the co-occurrence matrix $C(i,j|d,\theta)$ represents the number of times a pair of gray level values (i,j) occur at distance d , in the direction θ . For each distance and orientation (d, θ) a matrix is computed and a set of six textural measures was extracted. In Gray Level Run-Length Method (GLRLM) texture is based on run-length primitives, which corresponds to a set of consecutive pixels with the same gray level in a given direction. These primitives can be characterized by their length, direction and gray level. The run-length descriptors are extracted from the run-length matrix, where each element of $M(a,r|\theta)$ represents the number of runs with pixels of gray level intensity a and length r along the orientation θ . The Gray Level Difference Method (GLDM) is a technique of texture analysis based on the occurrence of absolute difference in gray levels of pairs of pixels, in a certain distance and direction. The result is a histogram $H(k|d,\theta)$ which gives the probability of the occurrence of the difference gray level value k between two pixels distant (d,θ) . The features extracted from the methods used are listed in Appendix. A brief description can be found in (Vasconcelos, 2010).

3 SUPPORT VECTOR MACHINE CLASSIFICATION

In this section we outline the basic theory of SVM and their application on lung data classification.

3.1 Linear SVM

Consider the training data represented by the pairs $\{\mathbf{x}_i, y_i\}, i = 1, \dots, n, \mathbf{x}_i \in \mathcal{R}^m, y_i \in \{+1, -1\}$, where the vector \mathbf{x}_i is the texture descriptors extracted from lung parenchyma regions and y_i the class label associated by the radiologist to the training case i . The label +1 is associated with emphysema class and -1 with normal class. When

data is linearly separable exists a vector $\mathbf{w} \in \mathbb{R}^m$ and a scalar $b \in \mathbb{R}$, that satisfy the conditions

$$y_i(\mathbf{w} \cdot \mathbf{x}_i + b) - 1 \geq 0, \forall i = 1 \dots n \quad (1)$$

The objective of the SVM classifier is to build an optimal hyperplane that separates the two classes in such a way that the distance (also called margin) from the hyperplane H to the nearest training data points, in each of the classes, is as large as possible, see Figure 2.

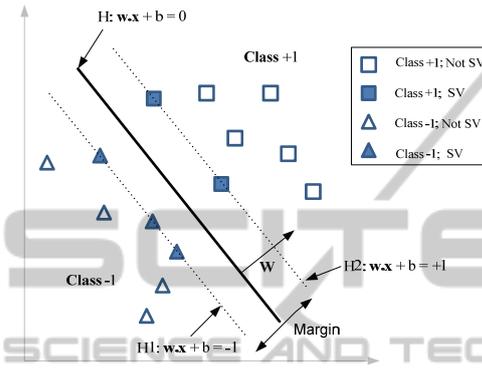


Figure 2: Optimal separating hyperplane in SVM linearly separable case.

The distance between the hyperplanes H1 e H2 is $2/\|\mathbf{w}\|$. The maximization of this margin leads to

$$\text{minimize } \frac{1}{2} \|\mathbf{w}\|^2 \quad (2)$$

subject to the equality constrains of Equation (1). A convenient way to solve constrained minimization problems is using a Lagrangian formulation, which leads to the following optimization problem:

$$L_p = \frac{1}{2} \|\mathbf{w}\|^2 - \sum_{i=1}^n \alpha_i (y_i(\mathbf{w} \cdot \mathbf{x}_i + b) - 1) \quad (3)$$

This equation should be minimized with respect to primal variables \mathbf{w} and b and maximized with respect to dual variables α to obtain the dual formulation:

$$L_d = \sum_{i=1}^n \alpha_i \frac{1}{2} \sum_{i=1}^n \sum_{j=1}^n \alpha_i \alpha_j y_i y_j (x_i \cdot x_j) \quad (4)$$

$$\text{Subject to } \sum_{i=1}^n \alpha_i y_i$$

$$\alpha_i \geq 0, \forall i = 1 \dots n$$

In dual formulation the problem optimization is done using only the dot product of data training and respective classes. The training of SVM now involves the maximization of Equation (4) in respect

to α . The points with $\alpha_i \neq 0$ are called Support Vectors (SVs) and lie on one of the parallel hyperplane H1 or H2 (Figure 2). In the case of a two class classification problem, the decision rule becomes

$$f(\mathbf{x}) = \text{sgn}\left(\sum_{i=1}^n \alpha_i y_i (\mathbf{x} \cdot \mathbf{x}_i) + b\right) \quad (5)$$

This SVM formulation is called hard margin, since no training errors are allowed. All the training samples satisfy the inequality $y_i f(\mathbf{x}_i) \geq 1$.

3.2 The NonLinear Case

In some cases, a linear hyperplane is unable to separate the classes appropriately. The SVM strategy is to map the input data into a high dimensional feature space by a mapping $\Phi: \mathbb{R}^m \rightarrow H$, in order to improve the separability between classes. This method is known as nonlinear SVM. In the feature space the decision function becomes:

$$f(\mathbf{x}) = \text{sgn}\left(\sum_{i=1}^n \alpha_i y_i K(\mathbf{x}, \mathbf{x}_i) + b\right) \quad (6)$$

There are several kernels functions $K(\mathbf{x}, \mathbf{x}_i) = \Phi(\mathbf{x}) \cdot \Phi(\mathbf{x}_i)$ that can be used to solve nonlinear problems. Some of the most common choices are:

- Linear:

$$K(\mathbf{x}, \mathbf{x}_i) = \mathbf{x} \cdot \mathbf{x}_i \quad (7)$$

- Gaussian Radial Basis Function (RBF):

$$K(\mathbf{x}, \mathbf{x}_i) = \exp(-\|\mathbf{x} - \mathbf{x}_i\|^2 / 2\sigma^2) \quad (8)$$

- Polynomial:

$$K(\mathbf{x}, \mathbf{x}_i) = (\gamma(\mathbf{x} \cdot \mathbf{x}_i) + \delta)^d \quad (9)$$

$$\text{with } \gamma > 0, \delta > 0, d > 0$$

3.3 The Inseparable Case

When information classes, obtained from CT data are not totally separable by linear boundaries, the SVM formulation is called soft margin. In this case slack variables are introduced to relax the constraints of Equation (1) that becomes:

$$y_i(\mathbf{w} \cdot \mathbf{x}_i + b) \geq 1 - \xi_i \quad (10)$$

$$\text{subject to } \xi_i \geq 0, \forall i = 1 \dots n$$

The optimization problem is formulated in this situation as

$$\text{minimize } \frac{1}{2} \|\mathbf{w}\|^2 + C \sum_{i=1}^n \xi_i \quad (11)$$

The regularization parameter C is a trade-off between the maximization of de margin (first part of Equation 11) and minimization of training errors. The optimization process is similar to the separable case except the constraints that become $0 \leq \alpha_i \leq C$.

4 METHODOLOGY

4.1 Dataset and Features Definitions

In this study part of a dataset that is being organized in collaboration with Radiology Department of Coimbra University Hospital. The dataset contain examples of representative patterns associated with normal and lung disease tissue. The visualization of CT images, selection and characterization of the ROIs by radiologists, is done with a user friendly software, developed by the authors for this propose (Vasconcelos, 2009). HRCT images were acquired using multidetector row scanner from General Electric Healthcare (LightSpeed VCT 64), with a slice thickness of 1.3 mm. Each image is stored in 512x512 pixels with 16-bit gray level, using DICOM (Digital Imaging and COmmunications in Medicine) standard. Each image was displayed using a lung window with a centre of -700 Hounsfield Units (HU) and a width of 1500 HU.

From 290 scans of 82 patients (#55 male and #27 female) with an average age of 65 ± 15 years, radiologists outlined #185 ROIs of emphysema, including different types and severities of emphysema and #105 of normal ROIs. From each scan only one ROI was obtained.

In a previous study we evaluated the importance of a set of parameters in the classification accuracy of lung CT images, such the size of the ROIs, the quantization level and features used to characterize each texture ROI (Vasconcelos, 2010). These results are the starting point for some options taken in the study described in this paper.

Each ROI is characterized as an n -dimensional feature vector obtained from SGLDM, GLRLM and GLDM. The four directions $\{0^\circ, 45^\circ, 90^\circ, 135^\circ\}$ are considered for the three methods. In GLDM the six features are obtained over an intersample of 1 to 4 pixels, resulting in a 96-dimensional feature vector. Using SGLDM the intersample used was 1 and 2

resulting in a set of 48 features. The 44-dimensional feature vector obtained with GLRLM results from the eleven features extracted over the four directions. For standardization reasons all ROIs were quantified to 32 gray levels, despite the fact the best performance for GLDM's features were obtained for a quantization levels of 64 gray levels (only 0.7% better). The minimum and maximum HU value is calculated for all ROIs of the dataset and each ROI is quantized according to this value. All features were independently normalized to zero mean and unit variation.

4.2 Classifier Evaluation

The dataset (#290 ROIs) was divided in train and test set, 70% for training and 30% for testing. Then, ROIs of train and test sets are split in smaller ROIs of 40x40 pixels (#980 in train set and #331 in test set).

The search for the optimal parameters is carried out using a grid search methodology. Initially a coarse search is done. For every point of the search space a k -fold cross validation (CV) is performed. The parameters that allow the best mean CV accuracy were selected and a fine grid search is carried out around the selected parameters, for refinement. The final classifier model is built using all training data and the optimal parameters previously obtained. Model is evaluated in test patterns. The accuracy (the number of correctly classified samples divided by the total samples in the test set); sensibility (the number of samples correctly classified as positive divided by the total number of positive samples in the test set) and specificity (the number of samples correctly classified as negative divided by the total number of negative samples in the test set) are computed.

5 EXPERIMENTS AND RESULTS

The SVM kernel functions tested were linear (equation 7), RBF (equation 8), and polynomial (equation 9, considering $\gamma = 1, \delta = 1$ and $d = 3$). The classification was performed using SVM classifier available in bioinformatics toolbox of MATLAB (MATLAB, 2009).

The parameter adjustment methodology was performed for the regularization parameter C for linear and polynomial kernels and (C, σ) for RBF kernel. First, we evaluate the parameters values using a coarse grid in $C=2^{-5}, 2^{-4.5}, 2^{15}$ and $\sigma=2^{-2}, 2^{-1.5}, \dots, 2^7$ and then focus the search in a finer grid. If

the pair (2^c , 2^s) generates the lowest cross validation error, a finer search is performed around them with a step of 0.25 upward and downward. Figure 3 and 4 depicts graphics contours of CV accuracy and number of SV, after a 10-fold cross validation, for RBF Kernel and features extracted with GLDM.

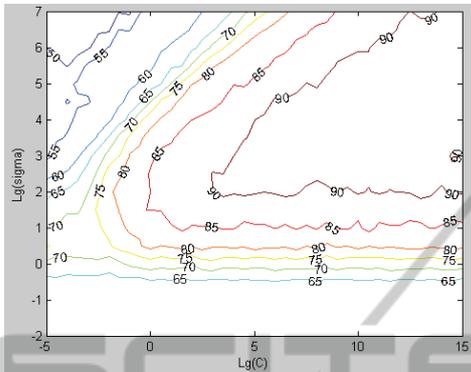


Figure 3: CV accuracy (%) obtained along the search space for finding (C, σ) parameters. GLDM features and RBF kernel were considered.

A heuristic analysis of the curves of Figure 3 allows a good understanding of the parameters space and a way of reduce search space. Variations in accuracy results are of the order of 45%. The worst accuracy was 41.5%, obtained in grid coordinates ($C=2^{-4}$, $\sigma=2^7$) and the best accuracy was 92.8% obtained at ($C=2^5$, $\sigma=2^{2.5}$). The number of SV varied between 152 and 785. A similar methodology was performed for all the kernels and features sets.

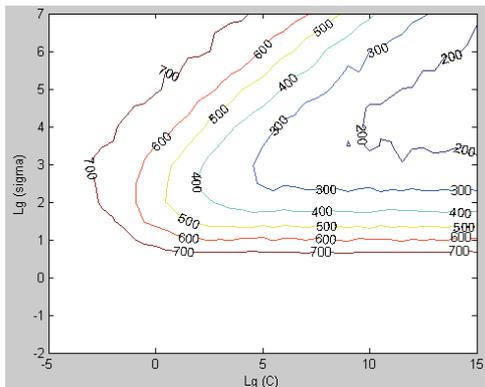


Figure 4: Number of SV obtained along the search space for finding (C, σ) parameters. GLDM features and RBF kernel were considered.

Table 1 illustrates the results obtained for the parameters that best handled the classification problem. The highest classification accuracy (Acc), sensibility (Sen) and specificity (Sp) was achieved with RBF kernel, for all the features extraction

methods. However, the parameter tuning must be carefully done to obtain the optimal parameters. According to the experiments, the polynomial kernel originated the SVM models that achieved the worst metrics. The large values of the regularization parameter C, that correspond to a high penalization to misclassified samples, can compromise the performance of the model because correspond to an overfitting situation. However, more experiments are necessary since this kernel function was used with the parameters γ , δ and d fixed. The adjustment of these parameters might lead to better results.

Table 1: Results obtained for the three sets of features and kernels.

Method	Kernel	N° SV	Lg(C); Lg(σ)	Acc CV (%)	Acc (%)	Sen (%)	Sp (%)
SGLDM	Linear	117	4.25	95.3	89.8	91.3	88.1
	RBF	130	5.25; 2.5	99.0	94.3	96.5	91.8
	Poly	231	11	96.3	87.7	89.6	85.5
GLRLM	Linear	45	3.50	98.4	96.1	99.4	92.5
	RBF	73	9; 4.5	98.9	96.4	99.4	93.1
	Poly	54	13	98.5	92.5	93.1	91.8
GLDM	Linear	203	3	87.0	81.9	76.9	87.4
	RBF	355	5; 2.75	93.1	88.6	85.0	92.5
	Poly	266	12	90.1	80.2	75.4	85.3

An interesting characteristic of SVM is that the optimization problem leads to a sparse solution, in the sense that only SV points of the feature space have $\alpha_i \neq 0$ (in Equation 6). This fact is very attractive from the computational point of view, specially for large datasets. Analyzing Table 1, we can conclude that GLRLM features led to the best results in all the metrics, with the less number of SV. With this feature set, linear kernel is also a good option, allowing results very similar to RBF kernel.

6 CONCLUSIONS

In this paper a comparative performance analysis in discrimination of lung emphysema pattern in HRCT images from healthy pattern was presented. Three common kernel functions were tested with different statistical features sets. A grid search was carried out in order to get the optimal parameters which influence the model performance. From presented study, it's clear that the kernel choice and parameters tuning is crucial to maximize the SVM performance. In the three features sets tested, the RBF kernel achieved the highest performances. The polynomial kernel was not the ideal function for

these classifications propose. However, more tests will be done with the adjustment of the kernel parameters.

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APPENDIX

Table 2: Textural Features extracted from each method.

Spatial Gray Level Dependence Method (SGLDM)	Gray Level Run-Length Method (GLRLM)	Gray Level Difference Method (GLDM)
	Short Run Emphasis	
	Long Run Emphasis	
Angular Second Moment	Gray Level Non-Uniformity	Angular Second Moment
Entropy	Run Length Non-Uniformity	Entropy
Inverse Difference Moment	Run Percentage	Inverse Difference Moment
Correlation	Low Gray Level Run Emphasis	Correlation
Variance	High Gray Level Run Emphasis	Variance
Contrast	Short Run Low Gray Level Emphasis	Contrast
	Short Run High Gray Level Emphasis	
	Long Run Low Gray Level Emphasis	
	Long Run High Gray Level Emphasis	