HAND GESTURE RECOGNITION THROUGH ON-LINE SKELETONIZATION
Application of Continuous Skeleton to Real-time Shape Analysis

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Abstract: New method for palm shape analysis and hand gesture recognition with help of continuous skeletons is presented in the paper. Continuous skeleton makes possible to develop fast and simple methods for palm shape analysis and measure a lot of its features. In particular it is possible to develop efficient methods for segmentation and analysis of the object topological structure, measuring relative location of object parts and measuring width of the object in arbitrary place. Applying to palm shape analysis skeleton provides a way to determine number of visible fingers, estimate their thickness and location, and perform efficient palm shape comparison with the sample. Moreover proposed approach allows measuring all mentioned features regardless of palm orientation in the frame. And efficient algorithms for skeleton construction allow performing shape analysis with high speed in real-time applications.

1 INTRODUCTION

At the present time gesture recognition problem is subjected to active research due to its practical importance. Potential applications of gesture recognition technologies include human-computer interaction (Dhawale et al., 2006), virtual reality applications (Aguiar et al., 2009), sign language recognition (Burger et al., 2007) and other (Mitra and Acharya, 2007; Garg et al., 2009).

A lot of different approaches for hand gesture recognition exist. Some of these methods require several cameras or special equipment (Schlattman and Klein, 2007; Wang and Popović, 2009). There are methods which maximize the likelihood of hand to be in certain pose by input image (Liu et al., 2008), but such methods are computationally expensive. Another group of methods work in real-time without special equipment (Burger et al., 2007; Dhawale et al., 2006). However, the range of possible configurations of hand that can be successfully detected with such methods is limited due to scarce feature extraction mechanism.

In this paper application of continuous skeleton to real-time hand shape analysis is presented. Similar approach was used in (Mestetskiy, 2007) for shape comparison of flexible objects. Palm silhouette boundary is approximated as a polygon, and its skeleton is constructed with help of Voronoi diagram of line segments. Simple and efficient pruning algorithm helps to get rid of unimportant skeleton edges.

Hand silhouette skeletonization provides rich feature generation mechanism and allows performing complex shape analysis, determining topology of the hand (number and shape of visible fingers), estimating relative location of palm parts and measuring width of silhouette in arbitrary place. Moreover such analysis can be performed regardless of palm orientation in the frame. In addition computationally efficient skeletonization and pruning algorithms are suitable for usage in real-time applications.

The text of the paper is organized in a following way. Review of the literature on the topic is given in Section 2. The notion of the continuous skeleton is given in Section 3. Application of skeleton analysis for palm shape recognition is presented in Section 4. Experiments are described in Section 5. And Section 6 completes the paper and states the conclusions of

the research and future works.

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2 RELATED WORK

The topic of gesture recognition is subjected to active research, and a lot of different approaches to the problem exist. Some of them are not widely used due to requirement of complex experimental setup (Schlattman and Klein, 2007) or expensive equipment such as instrumented gloves (Aguiar et al., 2009).

Among more available techniques color markers could be used for hand tracking and gesture recognition. And there are a lot of methods which use only image of hand obtained from the camera. Good review of vision based method is presented in paper (Garg et al., 2009).

In (Wang and Popović, 2009) special colored glove is used for hand pose estimation. The advantage of this approach is high range of successfully estimated poses. Shortcomings include requirement to wear the glove and increased requirement to the image quality. Also pose estimation involved computationally expensive search in the database of available poses, that's why parallel algorithm shows only 10fps on modern computer.

In papers similar to (Liu et al., 2008) hand pose estimation is performed by the search in multidimensional space of all possible hand configurations. However such approaches are computationally expensive and can hardly be used in real-time applications.

Also bare hand tracking could be performed by preliminary segmenting skin and non-skin regions in the image and further analysis of regions corresponding to hand. For example, in papers (Burger et al., 2007) and (Dhawale et al., 2006) macro features (such as size, position and Hu invariants) of palm silhouette are used for hand gesture recognition. These methods work fast but the set of detected gestures is poor and the methods provide no way to evaluate location of fingers.

The most promising approach to shape analysis is computation and analysis of skeleton of palm silhouette. In particular such approach is described in (Beristain and Grana, 2010). In that paper skeleton of palm silhouette is constructed and simple greedy algorithm for skeleton comparison is used to classify hand gestures into 3 classes. But the paper did not cover finger detection and tracking as well as measurement of different silhouette features. In addition their skeletonization algorithm operates with discrete boundary and requires development of complex pruning methods given the fact that such methods not always provide acceptable result.

3 CONTINUOUS SKELETON

Methods considered in the paper are based on the notion of the skeleton of a figure. The skeleton is a set of points which are equidistant from two or more figure borders.

In the literature there are two approaches of describing and constructing a skeleton: discrete and continuous approaches. In the discrete case skeleton is described as the set of pixels, and it is constructed with help of pixel-based processing of the original image. In the continuous case skeleton is described as a union of points and curves. The advantage of continuous approach is the fact that it is easier to perform further processing on continuous skeleton in comparison to discrete one. In this paper continuous approach is used and all necessary definitions are given below. Details about continuous skeletons and the process of skeletonization could be found in (Mestetskiy, 2010), (Mestetskiy and Semenov, 2008) and (Siddiqi and Pizer, 2008).

Maximum inscribed circle is the closed circle C that is completely lying inside the figure F, and any other circle C' within the figure does not contain C: $\forall C' \subset F, C' \neq C : C \not\subset C'$.

Skeleton of polygonal shape is the locus of centers of maximum inscribed circles. Also radius of inscribed circle is associated with each point of the skeleton, and such association between skeleton points and radii is called radial function.

It can be proved that the skeleton of the polygon consists of finite set of line segments and arcs of the parabolas (Mestetskiy, 2010). So the skeleton could be considered as a planar graph. And such skeleton representation is called *axial graph*. Below in the article we use both graph and curve properties of skeleton, so terms axial graph and skeleton will be used interchangeably.

Degrees of vertices in axial graph can be from 0 to 3. Each edge of this graph can be line segment or arc of the parabola. Radius of maximum inscribed circle is associated with each vertex of the graph and any internal point of the edges.

The process of skeleton construction from binary image is showed on the figure 1. Low resolution image is chosen as an example: palm size is 36 pixels and fingers' widths are about 5-6 pixels. Continuous skeleton construction from binary image is described in details in the book (Mestetskiy, 2009), but briefly algorithm consists of the following steps:
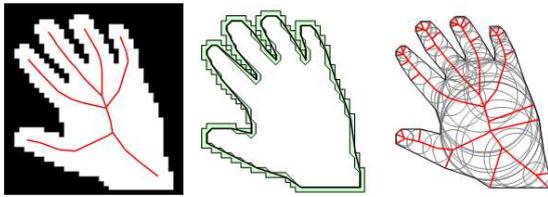
Figure 1: The process of skeleton construction. *Left*. Source binary image and resultant skeleton. *Middle*. Boundary corridor and minimal perimeter polygon. *Right*. Skeleton before pruning.

1. **Construction of Boundary Corridor of the Binary Image.** For initial binary image (figure 1, left) boundary corridor is calculated based on boundary tracing. Boundary corridor consists of two sequences of pixels: black sequence and white sequence. White sequence corresponds to internal boundary of the corridor and black to external. On the middle part of the figure 1 corridor is drawn in gray color.

2. **Construction of Minimal Perimeter Polygon Inside the Boundary Corridor.** Closed path of minimal perimeter is constructed inside the boundary corridor. Such path will be closed contour without self-intersections. Physical model of the path is a rubber thread stretched along the boundary corridor. Minimal perimeter polygon is shown on the middle part of fig. 1.

3. **Skeleton Construction.** Skeleton is constructed for the minimal perimeter polygon. On the right part of the figure 1 skeleton and maximum inscribed circles at the vertices of the axial graph are drawn.

4. **Skeleton Regularization.** When skeleton is constructed it is subjected to pruning. Pruning is performed by sequential cutting of certain terminal edges of the skeleton. Cutting criteria is based upon the following principle. Initial polygon could be represented as a union of all inscribed circles with the centers at the skeleton points. When skeleton edge is removed associated circles are removed too. Union of the remaining circles forms a figure which is called silhouette of the remaining skeleton part. This silhouette is a subset of the initial polygon and it is situated inside it. If Hausdorff distance of this silhouette and initial polygon is less than the threshold then skeleton edge is cut, otherwise - not. In the example on the figure 1 threshold is equal to 2 pixels.

In the rest of the article by skeleton we mean pruned skeleton. Moreover due to the fact that parabolic edges are usually short, they are approximately treated as line segments.

In the axial graph length of each edge is determined as Euclidean length of the corresponding skeleton segment. Lengths of the edges naturally generate distance on the axial graph, in such a way that distance between two vertices can be calculated as the total length of the edges in the shortest path between these vertices.

4 PALM SHAPE ANALYSIS

4.1 Skeleton Branch and its Properties

Here we introduce the notion of *skeleton branch* which is a part of skeleton treated as a continuous curve.

Consider a continuous piecewise-smooth curve without self-intersections $\vec{s}(\bullet) : s(l) = \{x(l), y(l)\}, l \in [0, L]$, and let l be natural parameter of the curve (i.e. arc length along the curve). Let each point of the curve $\vec{s}(\bullet)$ be a point of the skeleton. In such case we will call the curve $\vec{s}(\bullet)$ as *skeleton branch*, which connects points $r(0)$ and $r(L)$ of the skeleton

Radial function $R(x, y)$ is known for each point P of the skeleton, and its value is equal to the radius of maximum inscribed circle with the center at point P. Let's define *radial function along the branch* $\vec{s}(\bullet)$ as $R_s(l) = R(\vec{s}(l)), l \in [0, L]$.

Theorem. For any skeleton branch $\vec{s}(\bullet)$ of the skeleton of polygonal shape radial function along the segment $R_s(l)$ is continuous and piecewise smooth function.

The proof of the theorem is based on the fact that the skeleton of polygonal shape is union of finite number of line segments and arcs of parabolas, and radial function $R(x, y)$ along each such piece of the skeleton is linear or quadratic function of coordinates (Mestetskiy, 2010). So if we consider union of such segments and consider natural parametrization along them, value of radial function will be smooth along each segment and continuous at the junctions of segments.

4.2 Linear Approximation of the Radial Function

It is inconvenient to work numerically with values of radial function along the branch due to presence of parabolic arcs in the skeleton. So we replace the initial skeleton to its approximation without parabolic arcs.

Let's replace all parabolic arcs in the initial skeleton by line segments and call the new graph as *linearly approximated skeleton*.

For each point of linearly approximated skeleton let's introduce *linearly approximated radial function* $\tilde{R}(x, y)$ in the following way. $\tilde{R}(x, y)$ is equal to $R(x, y)$ for the vertices of the initial skeleton, and inside the edges of approximated skeleton $\tilde{R}(x, y)$ changes linearly from one end of the edge to another.

Similarly to the source skeleton, let's consider skeleton branches and *approximated radial function along the branch* $\tilde{R}_s(x, y)$ for the approximated skeleton. It can be proven that such approximated radial function is continuous and piecewise linear function of its parameter.

4.3 Calculation of Approximated Radial Function

Let's consider two vertices A and B of the initial skeleton and simple path P in the axial graph between these vertices. Path P uniquely defines skeleton branch $\vec{s}(\bullet)$ and approximated skeleton branch $\tilde{s}(\bullet)$. Approximated radial function along the branch $\tilde{s}(\bullet)$ could be easily calculated in the following way.

Denote vertices in the path P as $V_0 = A, V_1, \ldots, V_{n-1}, V_n = B$.

Denote the values of the radial function in these vertices as $R(V_i) = R_i$.

Let L_i be the length along the graph between vertices A and V_i, that is $L_i = \sum_{k=0}^{i-1} |V_k V_{k+1}|$

In such notion approximated radial function along segment $\tilde{R}_{\tilde{s}}(l)$ could be calculated as:

$$\tilde{R}_{\tilde{s}}(l) = \begin{cases} R_i & l = L_i; \\ \alpha R_i + (1 - \alpha) R_{i+1} & l = \alpha L_i + (1 - \alpha) L_{i+1}, \\ & \alpha \in (0, 1) \end{cases}$$

4.4 Fingers Detection

Fingers detection is performed by analysis of skeleton branches which ends in the dangling vertices. The algorithm is described below.

Let A be an arbitrary dangling vertex of the axial graph. Let B be the nearest (in terms of the distance along the graph) to the A vertex of the axial graph which degree is equal to 3.

Consider approximated skeleton branch $\tilde{s}(\bullet)$ generated by the shortest path P between vertices A and B, and consider approximated radial function $\tilde{R}_{\tilde{s}}(l)$ along the branch $\tilde{s}(\bullet)$.

Samples of the function $\tilde{R}_{\tilde{s}}(l)$ for two different skeleton branches of palm silhouette from left part of figure 3 are shown on figure 2. Left part of figure 2 depicts $\tilde{R}_{\tilde{s}}(l)$ for skeleton branch corresponding to finger, and the right plot corresponds to non-finger

skeleton branch which starts from dangling vertex in the bottom part of the palm.
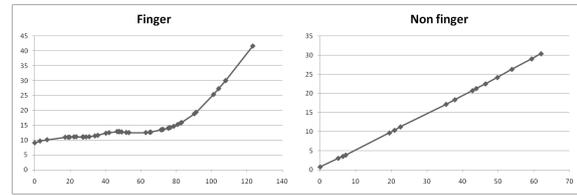

Figure 2: Radial function for finger and non finger.

As it can be seen from the plots, there are distinctive features associated with the length of the segment and radial function values which can be used to distinguish segments of the axial graph corresponding to fingers from others. These distinctive features were used to classify segments of the axial graph as fingers or non fingers.

Here we use notation from the previous subsection ($V_0 \ldots, V_n$, $R_0 \ldots, R_n$ and $L_0 \ldots, L_n$), and introduce values D_i which are discrete derivatives of R_i by L_i. In the corner points let $D_0 = 0$, $D_n = +\infty$, and in the rest points let D_i be calculated by the formula:

$$D_i = \frac{R_{i+1} - R_{i-1}}{L_{i+1} - L_{i-1}}, \quad i = 1, \ldots, n-1$$

We use R_i, L_i and D_i to estimate the position of point C - point of articulation of finger and metacarpus. Given point C different features of the skeleton branch, such as length, average width, distance to the center of the palm, could be measured. And all these values are used for fingers classification.

Search of point C is performed from the assumption that at the end of the finger one of the following conditions should be satisfied:

- R should increase in 2 - 2.5 times in comparison with the beginning of the finger

- Radius starts to increase significantly, i.e. discrete derivatives D_i are greater than the threshold

When the point C is found for the segment AB, we calculate length of segments AB and AC as well as width of segment AC. Width is calculated as the value of radial function at predefined point of AC or as average value of the radial function on the AC. We classify AB as a finger if all the following conditions are met:

- $|AC|/|AB| \geq 0.35$

- Width of AC lies in specified range

- Length of AB should be greater than the threshold, i.e. finger should not be short

Result of the work of the described algorithm is shown in the figure 3. Big blue circle is the circle of

maximal radius inscribed in the palm. The center of
this circle is considered as palm center. And small or-
ange circles correspond to fingertips and articulations
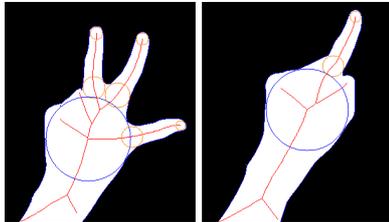of fingers and metacarpus.

Figure 3: Fingers detection samples.

4.5 Gesture Recognition

Gesture recognition is performed by calculating rela-
tive movement of fingers and the palm, and by calcu-
lating absolute movement of the palm as a whole. Us-
ing these values several gestures are recognized and
used in the demo-software. The list of the gestures is
following:

- One finger is seen (fig. 3, right). The finger and
  the palm are moving as a whole. This gesture is
  used for cursor movement and object dragging in
  the demo.

- Two fingers are seen, and their fingertips are mov-
  ing along the straight line (fig. 5). This gesture is
  used for object zooming.

- Three fingers are seen and form a triangle with
  approximately constant lengths of the sides (fig.
  3, left). This gesture is used for object rotation.

- Big and pointing fingers form a ring for a short
  period of time (fig. 4, right). This gesture is used
  for object grabbing.

- All five fingers are seen and spread wide apart for
  a short period of time (fig. 1). This gesture is used
  for object releasing.

Gestures with 1,2,3 and 5 fingers are detected eas-
ily with help of the algorithm from subsection 4.4.
Circles with the centers in the dangling vertices of
skeleton branches corresponding to fingers are treated
as fingertip positions. These circles along with de-
tected junction points of fingers and metacarpus are
drawn orange in figure 3.

Metacarpus movement detection and palm scale
measurement is performed using position and radius
of inscribed circle which radius is maximal among all
inscribed circles and center is at the vertex of axial
graph with degree 3. This circle is shown in blue at
the figure 3.
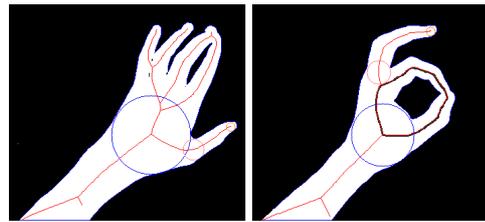
Ring gesture is detected by finding cycles in the

Figure 4: Cycles in skeleton. Cycle on the left corresponds
to non-ring gesture and cycle on the right corresponds to
ring gesture.

axial graph. It should be noted that only cycles which
contain vertices near the center of the palm (blue cir-
cle) are treated as valid cycles (see figure 4), because
only such cycles are formed from ring between big
and pointing fingers. Such classification of cycles is
possible due to the fact that coordinates of each vertex
is known in the axial graph. Moreover to detect ring
gesture, we do not need to analyze contours of palm
silhouette and should only use axial graph.

Five fingers and ring gestures are detected as dy-
namic gestures, that is when the gesture observed
is measured, and gesture counts only if it has been ob-
served for predefined time interval. Dynamic gesture
recognition is possible due to fast frame processing.

5 EXPERIMENTS

Software system was developed to demonstrate and
evaluate proposed gesture recognition method. This
system allows movement, zoom and rotation of sev-
eral objects on the screen of computer, and all the con-
trol is performed by means of gestures.

The following scheme of experimental setup was
used. Conventional consumer web-cam (Logitech
9000) was situated above the homogenous dark sur-
face.

In order to obtain palm silhouette per-pixel skin
detection is performed on the image obtained from
the web-cam (Vezhnevets et al., 2003; Phung et al.,
2005).

Continuous skeleton is constructed for the ob-
tained palm silhouette. And the skeleton was ana-
lyzed by algorithms described in the section 4. As
a result, gestures mentioned in the subsection 4.5 was
detected and used for object movement, zoom and ro-
tation. Figure 5 shows screen shot of the developed
software.

Effective algorithms for skeleton construction and
pruning make it possible to use the system in real-
time application. For example, single threaded im-
plementation of frame processing (including skin re-
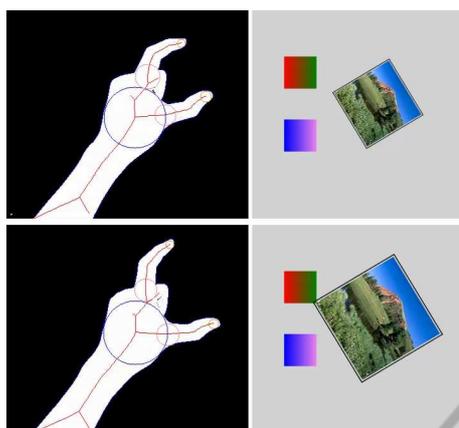gions segmentation, skeleton construction, pruning,

Figure 5: Sample screen shots of the software for experiments. This image demonstrates gesture which was used for object scaling.

gesture recognition and drawing of the result) takes about 22 ms per frame on 2.4Ghz Intel Core 2 Quad CPU, which gives 45fps.

6 CONCLUSIONS

Method of the palm shape analysis by the continuous skeleton is considered in the paper. This method allows wide range of palm silhouette features to be measured, which is hard or even impossible to measure with other approaches. Moreover high processing speed makes this method suitable for real-time applications.

We are going to extend considered approach by adding the second camera to the setup. Image obtained from the second camera will be subjected to similar processing, and obtain pairs of coordinates of each finger will be used for calculation of 3d positions of hand and fingers. For occlusion handling and estimation of exact hand pose we are going to use hand model.

In addition, we are going to apply the method for development of convenient and fast systems for human-computer interaction and virtual reality applications (Aguiar et al., 2009).

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