

# AUTOLSA: AUTOMATIC DIMENSION REDUCTION OF LSA FOR SINGLE-DOCUMENT SUMMARIZATION

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**Abstract:** The role of text summarization algorithms is increasing in many applications; especially in the domain of information retrieval. In this work, we propose a generic single-document summarizer which is based on using the Latent Semantic Analysis (LSA). Generally in LSA, determining the dimension reduction ratio is usually performed experimentally which is data and document dependent. In this work, we propose a new approach to determine the dimension reduction ratio, DRr, automatically to overcome the manual determination problems. The proposed approach is tested using two benchmark datasets; namely DUC02 and LDC2008T19. The experimental results illustrate that the dimension reduction ratio obtained automatically improves the quality of the text summarization while providing a more optimal value for the DRr.

## 1 INTRODUCTION

Text Summarization is the process of taking one or more information sources and presenting the most important content to a user in a condensed form. This could be achieved in a manner sensitive to needs of the user or application. While there are different types of summarizers suggested in the literature, this work is focused on automatic single-document generic and extractive summaries.

Recently, Latent Semantic Analysis (LSA) has been suggested as one of the promised approaches used for text summarization (Yeh et al., 2005; Ding, 2005; Steinberger and Jezek, 2004; Steinberger and Kristan, 2007; Gong and Liu, 2002). In this context, LSA can be viewed as a way to overcome two major challenges of text summarization, namely (i) sparseness and (ii) high dimensionality. Eventually, the LSA similarity is computed in a lower dimensional space, in which second-order relations among terms and texts are exploited. Moreover, it avoids using humanly constructed dictionaries, knowledge bases,

semantic networks, grammars, syntactic parsers, or morphologies. However, the conceptual representation obtained by LSA is unable to handle polysemy. The problem of polysemy is related to common words having potentially different meanings existing in different documents. In turn, words with different meaning but co-occurring with the proper name may be bound together in the semantic space even though they do not have any relations with one another (Yeh et al., 2005). Yeh et al. (Yeh et al., 2005) suggested an approach for using the LSA with the Text Relationships Map (LSA+TRM) for summarization. The combination between the LSA and the TRM leads to an improvement in the summarization performance. However, in the LSA+TRM, as in LSA in general, determining the dimension reduction ratio is usually performed experimentally, and in turn is data and document dependent. In this work, we propose a new approach to determine the dimension reduction ratio automatically to overcome this problem.

## 2 LSA FOR SUMMARIZATION

Using the LSA for text summarization is performed through four main steps, namely; (1) constructing the word-by-sentence matrix, (2) applying the Singular Value Decomposition (SVD), (3) dimension Reduction (DR), and finally (4) sentence selection for summarization. In the following, we will shed more light on each of these steps.

1. **Constructing the Word-by-sentence Matrix.** If there are  $m$  terms and  $n$  sentences in the document, then the word-by-sentence matrix  $A$  will be  $m \times n$  matrix. The element  $a_{ij}$  in this matrix is defined as:  $a_{ij} = L_{ij} \times G_{ij}$ , where  $a_{ij}$  is the element of word  $w_i$  in sentence  $s_j$ ,  $L_{ij}$  is the local weight for term  $w_i$  in sentence  $s_j$ , and  $G_{ij}$  is the global weight for term  $w_i$  in the whole document. The weighting scheme suggested by the LSA+TRM algorithm, thereon referred to as Original Weighting Scheme (OWT), is given as follows

$$L_{ij} = \log\left(1 + \frac{t_{ij}}{n_j}\right), \quad (1)$$

$$G_{ij} = 1 - E_i \quad (2)$$

$$E_i = -\frac{1}{\log N} \sum_{j=1}^N t_{ij} \times \log t_{ij}, \quad (3)$$

where  $t_{ij}$  is the frequency of word  $w_i$  in sentence  $s_j$ ,  $n_j$  is the number of words in sentence  $s_j$ ,  $E_i$  is the normalized entropy of word  $w_i$ , and  $N$  is the total number of sentences in the document. Steinberger et al. (Steinberger et al., 2007) studied the influence of different weighting schemes on the summarization performance. They observed that the best performing local weight was the binary weight and the best performing global weight was the entropy weight as follows:

$$L_{ij} = \begin{cases} 1 & \text{if } w_i \text{ occurs in sentence } s_j \\ 0 & \text{Otherwise} \end{cases} \quad (4)$$

$$G_{ij} = 1 - \sum_j \frac{P_{ij} \times \log P_{ij}}{\log N}, \quad (5)$$

where  $P_{ij} = t_{ij}/g_i$ ,  $g_i$  is the total number of times that term  $w_i$  occurs in the whole document  $D$ . We refer to this technique as the Modified Weighting Technique (MWT). A comparative study between the two different weighting schemes is conducted to study the effect on the summarization performance. The result shows that the MWT gives its best performance with the high dimension reduction as well as the low dimension reduction. We will focus on using the MWT, since we implemented the LSA to get its benefits in the dimension reduction phase.

1. **Applying the SVD.** The SVD of an  $m \times n$  matrix  $A$  is defined as:  $A = U\Sigma V^T$ , where  $U$  is  $m \times n$  column-orthonormal matrix,  $\Sigma = \text{diag}(\sigma_1, \sigma_2, \dots, \sigma_n)$  is  $n \times n$  diagonal matrix, whose diagonal elements are non-negative singular values sorted in descending order and  $V$  is  $n \times n$  orthonormal matrix. The SVD decomposition can capture interrelationships among terms, therefore that terms and sentences can be clustered on a ‘‘semantic’’ basis rather than on the basis of words only.

2. **Dimension Reduction.** After applying the SVD decomposition, the dimensionality of the matrices is reduced to the  $r$  most important dimensions. The initial Dimension Reduction ratio (DRr) is applied to the singular value matrix  $\Sigma$ . The DRr reflects the number of LSA dimensions, or topics, to be included. If few dimensions are selected, the summary might lose important topics. However, selecting too many dimensions implies including less important topics which act as a noise and affect negatively the performance. Dimension reduction can be useful, not only for reasons of computational efficiency, but also because it can improve the performance of the system. The DRr in most cases is selected manually, which we refer to as Manual Dimensionality Reduction (MDR).

3. **Sentence Selection for Summarization.** In this step the summary is generated by selecting a set of sentences from the original document. The LSA+TRM uses the text relationships map (TRM) for sentence selection through reconstruction the semantic matrix  $A'$  using the new reduced dimensions. The similarity between each pairs of sentences is calculated using the cosine similarity between the semantic sentences representation. If the similarity exceeds a certain threshold,  $Sim_{th}$ , this pair of sentences are semantically related and are linked. The significance of a sentence is measured by counting the number of valid links for each sentence. Yeh et al. (Yeh et al., 2005) use  $Sim_{th} = 1.5 \times N$  to decide whether a link should be considered as a valid semantic link. A global bushy path is then established by arranging the  $k$  bushiest sentences in the order that they appear in the original document. Finally, a designated number of sentences are selected from the global bushy path to generate a summary.

Two main drawbacks of the LSA+TRM are:

1. Determining the DRr manually is data dependent, and is conducted based on an experimental evaluation of ratios from  $0.1 \times N$  to  $0.9 \times N$ . However, datasets usually has different documents with dif-

ferent structures that have different optimal ratios. Therefore, the test should be performed for each document to get the best ratio for each document which is not applicable.

2. The TRM requires a threshold to check the validity of the link between two sentences to calculate the significance of each sentence. Moreover, this threshold is also data dependent.

The main contribution of this paper is to propose a summarizer for tackling the drawbacks of the LSA+TRM.

### 3 AUTOLSA: AUTOMATIC DIMENSION REDUCTION FOR LSA

The algorithm proposed in this work, AutoLSA, enhances the performance of text summarization using the LSA+TRM approach. We used two different datasets in this experimental study, namely, (i) DUC02 dataset<sup>1</sup> and (ii) LDC2008T19 dataset<sup>2</sup>. The DUC02 dataset contains 250 documents and each document attached with two different human summaries. On the other hand we selected 300 documents from the LDC2008T19 dataset attached with their associated human summaries. The Recall, Precision and  $F_1$  measure are used to judge the coverage of both the manual and machine generated summaries. All our experiments are done with Compression Ratios (CR) of 25%, 30% and 40% for both dataset. Moreover, we performed a 5-folds cross-validation across the datasets. We divided each set to subsets of 50 documents selected randomly. In the following, we examine the results of the experiments performed using these datasets as follows:

#### 3.1 The Effect of the Weighting Technique on the Performance

Figure 1 shows the performance of the MWT and OWT using a CR of 40% for both the DUC02 and LDC2008T19 dataset. It is worth noting that we observe similar performance using other values for CR, and these results have been omitted in favor of space. The results illustrate that the MWT demonstrates the best performance on extreme values when applied to the DUC02 dataset (at  $DRr=0.1 \times N$  and  $DRr=0.9 \times N$ ). This is in contract to the performance of OWT using different values of CR, which shows

<sup>1</sup><http://duc.nist.gov>.

<sup>2</sup><http://www ldc.upenn.edu>.

the best performance at average DRrs, namely  $DRr=0.5 \times N$ . While the performance of LDC2008T19 data using the OWT demonstrates the best performance at average values of DRr ( $DRr=0.5 \times N$ ), the performance using the MWT is only better at high values of DRr.

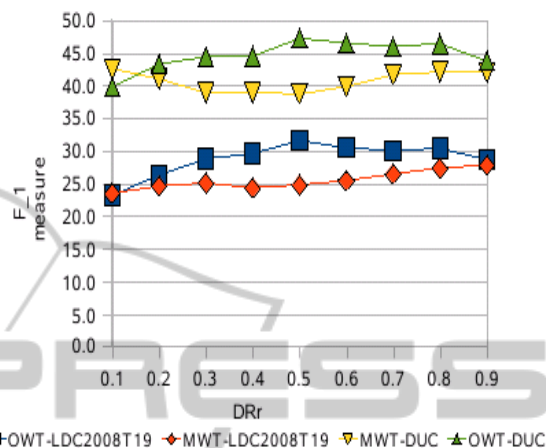


Figure 1:  $F_1$  measure for the LDC2008T19 and DUC02 dataset using MWT and OWT at CR=40%.

#### 3.2 Semantic Similarities Aggregation, SSA, for Sentence Scoring

As mentioned previously, the LSA+TRM algorithm manually selects a threshold,  $Sim_{th}$ , to check the validity of the link between two sentences to calculate the significance of the sentence. Instead of obtaining a threshold, we used the similarities aggregation between the semantic representation of the sentence and all other sentences as indicating significance for that sentence. Accordingly, we relax the requirements of selecting a threshold. We compare the semantic similarities aggregation (SSA) to the performance of the LSA+TRM. For each sub-set we have experimented with  $Sim_{th}$  ranges from  $1.5 \times N$  to  $0.0001 \times N$ , and the optimal threshold value for this sub-set is determined. The experiments show that, the optimal  $Sim_{th}$  differs from one sub-set to another. AutoLSA achieves an  $F_1$  measure of 37.2 and 36.0 on the DUC02 and LDC2008T19 respectively. Using the LSA+TRM achieves a performance of 33.1 for both data sets using a threshold  $Sim_{th}$  of 0.005 and 0.001 for the DUC02 and LDC2008T19 datasets respectively. These results show that using the SSA not only relaxes the requirements to set a threshold for sentence selection, but also contributes positively to the overall performance.

### 3.3 Automatic Dimension Reduction Ratio (ADRr)

Steinberger et al. (Steinberger et al., 2007) proposed a method to calculate the DRr automatically by using the summarization ratio  $DRr = CR/100 \times N$ . Empirical results show that this method is not efficient across different datasets. Alternatively we propose three methods for determining the ADRr namely;(1) 1-dimension only, (2) 1-or-2 dimensions and (3) log of accumulated concepts.

1. First Dimension Only (FDO): The first dimension of the matrix  $\Sigma$  is selected.
2. First Two Dimensions Only (FTDO): The second dimension is retained only if the Accumulated Concepts of the second dimension ( $ACon_2$ ) exceeds a threshold  $C_{AC}$ . In this study we have experimented in this study with the value of  $C_{AC}$  set at 0.3-0.6. Selecting values of  $C_{AC}$  less than 0.3 implies that the summary covers a very limited amount of information, while when it is larger than 0.6, only one dimension is selected.
3. Log of the Accumulated concept (LAC): In this method we define the importance of certain dimension based on the gain accumulated by each concept. The dimension  $i$  is important if

$$\log(X_i) > C_{ADR}, \quad (6)$$

where  $X_i = \frac{ACon_i}{i}$ ,  $ACon_i$  is the accumulated concept that captured at dimension  $i$  and  $C_{ADR}$  is a constant. In this study we investigated the performance of the algorithm using different values for  $C_{ADR}$  ranging from 1.3 to 1.6. Lower values of  $C_{ADR}$  reflect the limitation of the amount of information accepted for the summarization, while values larger than 1.6 limits the selection to the first dimension and causes a saturation in the results.

Table 1 illustrates the average  $F_1$  performance using different values for  $C_{AC}$  and  $C_{ADR}$  with CR=40% on the five-fold cross validation. It is worth noting that the standard variation of the results ranged from 1.1 to 3.0. Experimental results indicate that the optimal value of  $C_{AC}$  and  $C_{ADR}$  are 0.6 and 1.5 respectively. Finally, selecting the first dimension alone has demonstrated the Recall/Precision/ $F_1$  measure values of  $51.5 \pm 1.1/38.2 \pm .4/43.04 \pm 1.3$  and  $59.1 \pm 3.4/20.6 \pm 2.2/28.6 \pm 2.6$  for the DUC02 and LDC2008T19 datasets respectively @CR=40%.

### 3.4 Overall Performance

Table 2 summarizes the average recall, Precision and  $F_1$  measure using the best DRr value for the three

Table 1:  $F_1$  measure for different values of (a) $C_{AC}$  and (b)  $C_{ADR}$  @ CR=40% for DUC02 and LDC2008T19 dataset.

$C_{AC}$	0.3	0.4	0.5	0.6
DUC02	41.6	43.5	44.2	44.3
LDC2008T19	27.5	28.7	28.6	28.7

(a)

$C_{ADR}$	1.3	1.4	1.5	1.6
DUC02	43.2	44.3	44.4	44.4
LDC2008T19	28.2	28.2	28.9	28.9

(b)

Table 2: Recall, Precision and  $F_1$  measure for the (i) MDRr, (ii) FDO, (iii) FTDO with  $C_{AC} = 0.6$  and (iv) LAC using  $C_{ADR} = 1.5$  for (a) DUC02 dataset and (b) LDC2008T19 at different values for CR.

	MDRr	ADRr,		
		FDO	FTDO	LAC
CR=25%				
DRr	0.90	0.05	0.05	0.05
Recall	30.9	32.3	32.4	32.3
Precision	39.9	41.5	41.6	41.5
$F_1$	32.8	34.3	34.3	34.3
CR=30%				
DRr	0.9	0.05	0.05	0.05
Recall	32.6	40.4	39.9	39.9
Precision	36.4	42.2	43.5	43.5
$F_1$	32.8	39.0	39.3	39.3
CR=40%				
DRr	0.90	0.05	0.05	0.05
Recall	43.4	48.7	49.3	49.6
Precision	37.8	41.5	41.9	41.8
$F_1$	39.5	43.8	44.3	44.4

(a)

	MDRr	ADRr,		
		FDO	FTDO	LAC
CR=25%				
DRr	0.90	0.04	0.05	0.05
Recall	41.3	41.0	41.0	41.0
Precision	23.0	22.6	22.6	22.6
$F_1$	28.4	28.0	28.0	28.0
CR=30%				
DRr	0.90	0.04	0.04	0.04
Recall	45.9	47.6	47.4	47.6
Precision	22.2	22.6	22.2	22.6
$F_1$	27.7	28.2	28.1	28.3
CR=40%				
DRr	0.90	0.04	0.05	0.04
Recall	57.0	59.1	59.3	59.4
Precision	20.2	20.6	20.7	20.9
$F_1$	27.8	28.6	28.7	28.9

(b)

ADRr methods and the MDRr. We selected the best parameters for each method. It is worth noting that the standard deviation across the five folds cross validation was limited to the range from 1.0 – 3.7 for all the values.

We note that for the DUC02 dataset both the LAC and the FTDO criteria demonstrate performance better than the optimal MDRr. It is also notable that at low CR, all the methods select only the first dimension and hence produce similar results. Moreover the Recall and  $F_1$  measures improve with the increase of CR, as opposed to the Precision which decreases in this case. In addition, the differential improvement over the MDRr increases with the higher CR. A similar performance can be seen on the LDC2008T19 dataset, where the relative difference is smaller compared to the DUC02 dataset. The Log of the Accumulated concepts is slightly better than the other approaches and produces improved results compared to the MDRr with a huge reduction in the DRr. We selected the best parameters for each method.

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## 4 CONCLUSIONS

In this paper, we have presented the AutoLSA for automatically determining the optimal Automatic Dimension Reduction (ADR) ratio. The suggested approaches produce computationally efficient ADR, while improving the overall performance. This is supported by an empirical evaluation conducted on benchmark datasets from DUC02 and LDC2008T19. The performance on both datasets illustrate the improvement in performance using AutoLSA compared to LSA+TRM with Manual selection of DRr, (MDRr).

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