

THROTTLING DDoS ATTACKS USING DISCRETE LOGARITHM PROBLEM

Avinash Darapureddi, Radhesh Mohandas and Alwyn R. Pais

Information Security Lab, Department of Computer Engineering, NITK, Surathkal, Karnataka, India

Keywords: Distributed denial of service, Application of discrete logarithm problem, Source throttling, CPU stamps, Application level attacks.

Abstract: Amongst all the security issues that the internet world is facing, Distributed Denial of Service attack (DDoS) receives special mention. In a typical DDoS attack, an attacker runs a malicious code on compromised systems to generate enormous number of requests to a single web server. The flood of incoming requests makes the victim web server resources to wear out completely within a short period of time; thereby causing denial of service to the legitimate users. In this paper we propose a solution to trim down the impact of DDoS attacks by throttling the client's CPU i.e., to make clients pay a stamp fee which is collected in terms of resource usage such as CPU cycles. Our proposed solution makes use of the discrete logarithm problem to generate the CPU stamps.

1 INTRODUCTION

Distributed Denial of Service (DDoS) attacks have been increasing in recent times. Application level DDoS attacks are the worst of such attacks and even companies such as Microsoft, Yahoo are not immune to them. In the present day web applications the client sends a request for a resource to a web server with just one click, but the latter has to process lots of data to respond to that request which is an order of higher magnitude. This computation difference favours the attacker to tie up the web server by flooding requests with group of compromised systems.

In this paper we propose a solution to trim down the impact of DDoS attacks by throttling the client's CPU i.e., to make client pay a stamp fee which is collected in terms of resource usage such as CPU cycles. Our proposed solution makes use of the Discrete Logarithm Problem (DLP) (Darrel. Hankerson and Vanstone, 2004) to generate the CPU stamps and re-compute the same on change of request, everytime. We propose to use DLP, as it is mathematically complex to solve this on current day non-quantum computers in polynomial time.

Rest of the paper is organized as follows. Section 2 presents related work. Working of the proposed solution is shown in Section 3. Section 4 will discuss about algorithms. Implementation results and comparison with integer factorization are shown in Section 5 and we conclude the paper in Section 6.

2 RELATED WORK

(Saraiah and et al, 2009) have proposed a solution to reduce the impact of a DDoS attacks on a web server by throttling the clients CPU using integer factorization to generate CPU stamps. The protocol flow of the proposed solution is as follows. A client sends a request to web server for a webpage. The server starts a session and retrieves primes from pre-computed primes based on the server time and the client IP address and sends the product integer along with a JavaScript. The client will commit its resources and factors the integer into its prime factors and sends to the server. The server will verify whether the product of prime factors sent by the client are equal to the original integer sent by the server and decides to processes or drop the request.

(Tuomas Aura and Leiwo, 2000) had showed how stateless authentication protocols and the client puzzles can be used to prevent DoS attacks that exhaust the server resources. The summary of the solution is as follows. Initially, server asks the client to solve a puzzle by committing its resources. Based on the commitment of the client in solving the puzzle, the server allocates the resources to the client.

(Wang and Reiter, 2003) proposed a puzzle mechanism called puzzle auction. In this, the auction lets each client determine the difficulty of the puzzle it solves and allocates server resources first to the client that solves the difficult puzzle when the server is busy.

(Back, 2002) proposed a solution using Hashcash in May 1997. It was originally proposed as a mechanism to throttle systematic abuse of un-metered internet resources such as email, and anonymous remailers. In his paper Hashcash was used as a CPU cost-function to compute a token which can be used as a proof-of-work.

(Dwork and Naor, 1992) presented a computational technique for combating junk mail, in particular and controlling access to a shared resource. The main idea is that a user is required to compute a moderately hard, but not intractable, function in order to gain access to the resource, thus preventing frivolous use.

All these mechanisms make the attacker to pay the CPU stamp fee. However there are some drawbacks in the proposed solution in (Saraiah and et al, 2009). We come up with a solution to overcome this drawback with less overhead on the server and with more throttling effect.

3 PROPOSED SOLUTION

3.1 Definitions

In our solution we use the DLP, on which many cryptosystems are built. Before going into details, we present definitions to be used in our solution.

Let p be an odd prime, $Z_p = \{0, 1, \dots, p - 1\}$ a finite field, Z_p^* the set of integers which are relatively prime to p i.e., $Z_p^* = \{a \in Z_p | \gcd(a, p) = 1\} \Rightarrow Z_p^* = \{1, \dots, p - 1\}$. Let α be a generator of Z_p^* i.e., $Z_p^* = \{\alpha^0 \text{ mod } p, \alpha^1 \text{ mod } p, \dots, \alpha^{p-1} \text{ mod } p\}$ and β be a non zero integer in Z_p such that

$$\beta \equiv \alpha^x \text{ mod } p \tag{1}$$

The problem of finding x in equation(1) is called Discrete Logarithm Problem. It can be denoted as

$$x = \log_{\alpha} \beta \tag{2}$$

For example let $p = 11, Z_p^* = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$, $\alpha = 2$ a generator. Given $\beta = 9$ in equation(1); $9 \equiv 2^x \text{ mod } 11$. By exhaustive search in Table 1 the value of x is 6. When p is small it is easy to find x , but when p is large then table will be large and then it is hard to find x . It is easy to find out β when α, x, p are given but it is hard to find out x when α, β, p are given.

Table 1: Exhaustive search into exponent table.

x	0	1	2	3	4	5	6	7	8	9	10
$\alpha^x \text{ mod } p$	1	2	4	8	5	10	9	7	3	6	1

3.1.1 Threshold Value

In Figure 1 dark horizontal line indicates the Threshold value, at which the server can handle maximum number of requests without straining its resources. And the curve below the Threshold value indicates normal flow of traffic and other curve denotes the abnormal flow of traffic. Our solution is invoked when number of requests arriving at the server are more than the Threshold value.

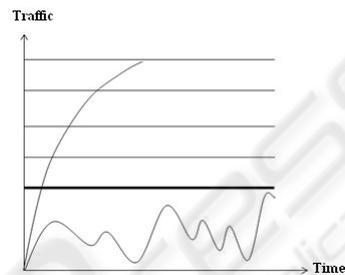


Figure 1: Threshold Value.

3.2 Proposed Solution

Notations. We make use of the following notations throughout this paper.

p : An odd prime.

Z_p : A finite field.

Z_p^* : The set of integers which are relatively prime to p i.e., $Z_p^* = \{1, \dots, p - 1\}$.

α : A generator of Z_p^* .

β : An integer in finite field other than zero and one i.e., $\{\beta \in Z_p | \beta \neq 0 \text{ or } 1\}$

$pdigits$: Number of digits in prime p

x : value computed using equation(2).

The flow of operations is as follows

1. Client sends a request to the web server for a resource.
2. Server starts a session and sends (p, α, β) values along with the JavaScript.
3. Client computes x and sends (p, α, β, x) values to the server.
4. The server verifies whether (p, α, β) values sent by the client are same as the values sent by the server to the client in step 2 and then verifies whether $\beta \equiv \alpha^x \text{ mod } p$. If not equivalent server drops the request otherwise processes it.

3.2.1 Description of Solution

Based on the server load the server varies $pdigits$ value from 2 to 8. In our solution, we pre-computed primes such that $(p-1)/2$ is also a prime this is to overcome Pohlig-Hellman attack (Darrel. Hankerson and Vanstone, 2004). One generator for each field is pre-computed and stored. The values (p, α) are retrieved from pre-computed primes and generators based on the server load and server time since last bootup. β is a random value between 2 to $(p-1)$. The server sends (p, α, β) values to the client and makes client to compute x .

An attacker with a malicious client will not send x values to the server. Hence, all such requests are dropped by the server. Alternately a progressive attacker can modify his malicious client to read the JavaScript and to compute x values. In that case the client has to pay resources and consequently the attack rate drops down drastically. Moreover, if the attack deepens, the server increases $pdigits$ which results in throttling of malicious clients.

3.2.2 Efficient Pre-computation of Generators

The standard algorithm to generate α is to pick a random g from Z_p^* and find if it is a generator. The algorithm is as follows

1. Picks a random number g between 1 and p to be a potential generator.
2. Checks to see if $g^{(p-1)/2} \bmod p = 1$. If yes go back to step 1.
3. Compute $g^2 \bmod p, g^3 \bmod p$, until either
 - (a) The answer is 1 (go back to step 1)
 - (b) The power is $(p-1)/2$ (we've found a generator)
4. Return the generator found in step 3.

This approach will lead to a pre-computation time of around 36 hours for the whole space of primes smaller than 8-digits.

We improvised this by making use of boolean array and not computing directly the step 2 of above algorithm as it is a costly operation (consumes more CPU cycles).

1. Take a boolean array $isNotGenerator[]$ of size p and initialize to false and $isNotGenerator[0] = true$
2. Picks a random number g between 1 and p to be a potential generator.
3. If $isNotGenerator[g] = true$ then $g \leftarrow (g + 1) \bmod p$.

4. $answer \leftarrow g, count \leftarrow 2$
5. Compute $isNotGenerator[answer] = true; answer = (answer * g) \bmod p$; and increment $count$ by 1 until either
 - (a) The $answer$ is 1 (go back to step 3)
 - (b) The $count \doteq (p-1)/2$ (we've found a generator)
6. Return the generator found in step 5.

And were able to finish this computation in just 10 hours.

4 ALGORITHM

Before we discuss the algorithm, different scenarios in which the attacker actively fine tunes his malicious client to launch distributed attack on the web server and the countermeasures to overcome these attacks are presented.

Scenario 1. In this scenario when the attacker observes that server is sending same (p, α, β) values for all the requests. He computes x once and appends this value to every request to perform a replay attack. Suppose, if the attacker observes that server is sending same p, α and different β for all the requests. He computes the exponent table (which is used for exhaustive search like Table 1) once and then searches to find x and as a result avoids expensive computation. To counter these two kinds of attack we will generate p dynamically based on the server time (difference of server current time and the server last boot up time in milliseconds) and this difference is sufficiently random as varies for every millisecond. So the prime value generated will be unique for each request.

Scenario 2. The Table 2 shows the total number of primes (NP) in each digit whose $(p-1)/2$ is also a prime from 2 to 8. Suppose, if all these pre-computed primes are saved in an array in a sequential manner then the attacker might try to guess the value of p from its previous values. This prediction can be done if he maintains pre-computed primes and uses the same algorithm that we use to generate p , as the $server_time$ varies by 1 for every millisecond, so he can retrieve nearest primes from the pre-computed primes and guessing attack can be done. To overcome this prediction and to optimize the storage space, a random combination of primes and its corresponding generators are selected. The number of primes so selected is given in Table 2. The primes are selected

in a random manner and the value of nP of each digit is unknown, so the prediction of next prime is impossible to an attacker. We change this combination every half an hour to prevent the attacker from tabulating the combination for further use.

Table 2: Total Number of primes, primes whose $(p-1)/2$ also a prime and selected primes in each digit.

Digits	2	3	4	5	6	7	8
Total no of primes(TNP)	21	143	1061	8363	68906	586081	5096876
No of primes whose $(p-1)/2$ also a prime(NP)	5	18	90	555	3654	26333	198911
No of primes selected in random(nP)	5	10	70	300	2000	9000	10000

The Generation algorithm takes in four arguments. *servertime*, *pdigits*, *selectedPrimes* array (which contains a randomly chosen combination from the total set of primes), *selectedGenerators* array (which contains corresponding generators of primes selected) and nP which denotes number of primes for each digit in the *selectedPrimes* array. The algorithm used for generation of p dynamically overcomes the attacks discussed in *scenario1* and *scenario2*.

Algorithm Generate (p,α,β)

1. $mapvalue \leftarrow servertime \bmod nP$
2. $p = selectedPrimes[pdigits][mapvalue]$
3. $\alpha = selectedGenerators[pdigits][mapvalue]$
4. $\beta = RandomNumber(2,p-1)$

Scenario 3. In this scenario the attacker satisfies the equation (1) but the (p,α,β) values sent by the attacker are not the same as the values sent by the server. The attacker changes the original values which is a repudiation attack. To overcome this attack the server makes use of session variables to store (p,α,β) values on the server side for verification. This is the only storage cost at the server end and reasonable for the present day memory on the server. These numbers take 12 bytes and current server can handle 3K requests per second. For a 60 seconds timeout the state table goes up to 2.1MB which is tolerable.

Scenario 4. In this scenario the attacker sends genuine (p,α,β) values and instead of finding x he will send random value between 2 to $p-1$ i.e., he will send $(p,\alpha,\beta,random\ value)$. To counter this attack the server will verify whether values sent by the client are satisfying equation(1) or not. The probability of such request going through is $1/(p-2)$ which becomes small when p is greater

than 100. The probability of that the chosen random value is x for 3-digit primes is 0.00272 and for 4-digit number 0.00023 and this probability becomes small when p increases.

Scenario 5. For each field one generator is pre-computed and stored on server side when same prime encounters the generator sent will be same only β changes in this case. At this scenario the attacker computes the exponent table once and uses it when the same prime encounters. In this case the attacker have to save all the values of $\alpha^x \bmod p$ where x varies from 1 to $(p-1)$. From Table 2 number of 8 digit primes(NP) are 198911 which requires a storage space of around 2MB and to save all the values of *beta* the storage space required is 2MB for each 8-digit prime. So the total storage space required is around 389GB. As this much storage space is not available in all the compromised systems involved in attack, this type of attack is not practical with the current hardware technology.

Algorithm used for verification takes in four arguments p,β,α and x values sent by the client. The verification algorithm overcomes the attacks discussed in *Scenario 3* and *Scenario 4*.

Algorithm Verification

1. check whether p,α,β are genuine using session variables saved on the server side.
2. If p,α,β are genuine then do the following
 - (a) If $\beta \equiv \alpha^x \bmod p$
 - i. Process Request
 - (b) Else Drop Request
3. Else Drop Request

5 IMPLEMENTATION

To test our proposed solution we have used the following setup

Server Configuration. Intel Xeon Quad CPU, processor speed 3.60 GHz each, 4 GB RAM, Win 2003 server.

Client Configuration. Intel core2 Duo CPU with processor speed 3.00 GHz and 2.99 GHz, 2 GB RAM, Windows XP professional operating system.

5.1 Results

To show the effectiveness of our solution we have used the same web applications as in (Saraiah and

et al, 2009) and modified them to include our solution i.e., we have used websites with solution and without solution. We have modified the HTML page of website with solution such that the page consists of JavaScript which makes the client browser to find x when p, α, β are given. When a request comes to the server then server retrieves the number of requests per second from Windows performance counters and when it crosses Threshold value the server starts sending p, α, β values to all the clients using cookies in each response. The client responds with p, α, β, x values, in which x is found using the JavaScript in the static page. The server makes use of verification algorithm and if the conditions are satisfied by the client, the server will respond with actual page and p, α, β values in the session variables are modified with new values.

We have measured the time taken by different web browsers(in milliseconds) to find out x value when p, α, β values are given and tabulated those readings in Table 3 . CCB in the Table 3 represents the custom command line browser built using C#.NET, which an attacker may build.

Table 3: Time taken(in milliseconds) by different browsers to find x .

pdigits	IE	Mozilla	Opera	Chrome	CCB
2	0.92	0.57	0.31	0.78	0.03
3	1.84	1.25	1.13	0.94	0.014
4	10.2	3.89	3.72	2.75	0.214
5	82.37	74.35	45.23	39.64	1.128
6	1013.9	672.89	682.82	543.28	14.428
7	7084.62	5407.38	5907.93	5108.6	145.0675
8	30894.57	26175.07	28907.87	24106.81	1559.611

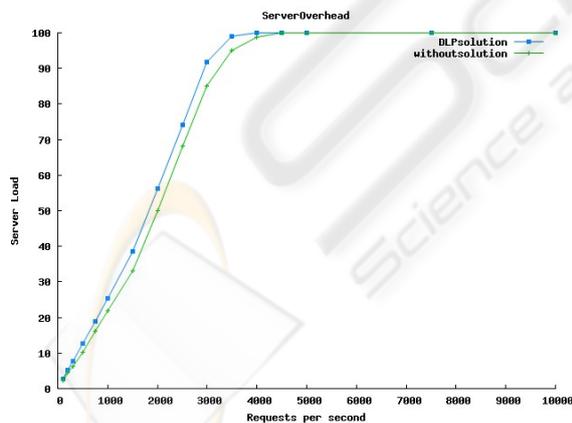


Figure 2: Server Overhead with and without solution.

Figure 2 shows the overhead on the server when the solution is used and when the solution is not used. We can observe from the Figure 2 overhead is very less when our solution is used.

Figure 3 shows the server load relief. We sent a good traffic(which computes x) of 1000 requests per second using client1 and bad traffic(which will not

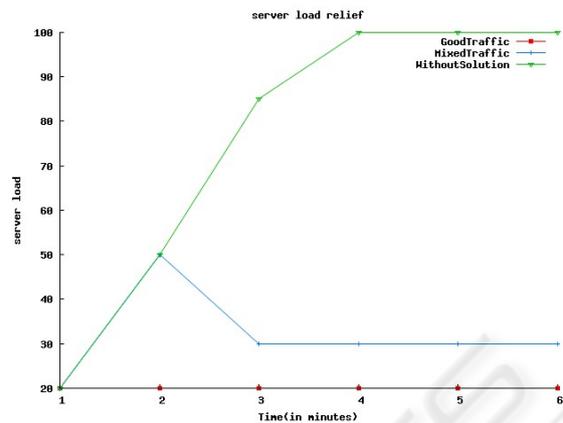


Figure 3: Server Load Relief.

compute x) i.e., attack traffic of about 2000 requests per second through client2. As a result server load crosses Threshold value and our solution is invoked and server starts sending the p, β value to the clients. The server drops the bad traffic. We can observe in the Figure 3 the sever load falls down once solution is invoked.

5.2 Comparison with Integer Factorization

In this section first we present some drawbacks of solution proposed in (Saraiah and et al, 2009) and then we show how our solution is more efficient than the proposed solution in (Saraiah and et al, 2009).

5.2.1 Drawbacks of Solution using Integer Factorization

As discussed in the (Saraiah and et al, 2009) the generation of p and q are based on server time since last boot up and client IP address respectively. In this case when the requests are coming from single client. p varies upon each subsequent request but q will not vary as there is no change in the IP address. To make q vary upon every subsequent request selected primes array must be refreshed for every millisecond which is not possible. And this selected primes array is refreshed at periodic intervals say 15 minutes. During this period of time, the attacker can find p by $p = N/q$ and avoid the integer factorization computation.

5.2.2 Comparison on the Client Side

From Table 4 and Table 3 we can observe that client latency in case of DLP solution is significantly more than Integer Factorization(IF) for the same number of digits. This is a direct result of the fact that DLP is a harder problem than IF in terms of computation.

Table 4: Latency in milliseconds of browsers to calculate factors.

Ndigits	IE	Mozilla	Opera	Chrome	CCB
5	0	0.2	0	0.2	0
6	0	0.2	0	0.2	0
7	0	0.2	0	0.4	0
8	0	1.8	0	2.2	0.01
9	6	1.8	3	2.2	0.05
10	34	16	22	18	0.05
11	44	23	28	25	0.07
12	265	134	147	147	0.43
13	318	163	169	173	5.60
14	2512	1269	1347	1398	6.62
15	4975	2475	2659	2866	44.6
16	49820	25069	19859	28173	67.5

5.2.3 Comparison on the Server Side

The overhead on the server is less in our solution than IF. In our solution the parameter for selection of prime is server time since last bootup, where as in solution using IF is server time since bootup and client IP address. As there is no overhead of reading client IP address (which takes around 1.896163 milliseconds) in our solution, the overhead on server is low. The following Table 5 shows the time taken(in milliseconds) by the server for generation and verification algorithms in solutions using IF and DLP. This is average across 1000 requests per second for varying server load.

Table 5: Time taken (in milliseconds) for generation and verification algorithms.

	IF	DLP
Generation Algorithm	1.945352	0.037941
Verification Algorithm	0.000634	0.077118
Overall Time taken	1.945986	0.115059

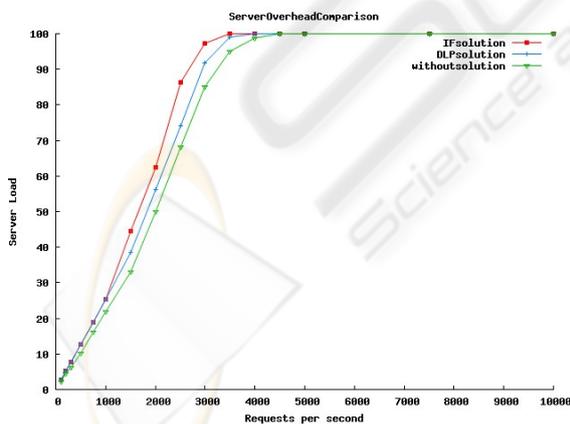


Figure 4: Server Overhead Comparison.

Figure 4 shows the overhead on the server due to solutions using IF and DLP. From the Figure 4 we can observe that overhead on the server is less in our solution than the proposed solution in (Saraiah and et al, 2009).

5.3 Limitations

In this section we present some limitations of our proposed solution.

- When JavaScript is not enabled in the browser then our solution will not work but now-a-days most of the web sites require JavaScript to be enabled.
- Our solution does not block a particular IP address from which an attacker is sending bad traffic(attack traffic). But this problem can be solved easily by using a inexpensive hardware device.
- Our solution will not work if *pdigits* value is more than 8 because the browsers only support up to 16 digit numbers(In JavaScript the function used for finding *x* needs multiplication, if *pdigits* value is 8 then max value will be a 16 digit number). But as we see from the Table 3 this is sufficient to impose the maximum tolerable latency on a human user.
- Latency is not fine tunable as we saw in Table 3 that the difference of latency from 6-digit prime to 7-digit prime is more.

6 CONCLUSIONS

In this paper we proposed a solution which will throttle clients and contains DDoS attack at the application level. We have come up with a algorithm to find a generator faster than the standard random pick and try algorithm. And came up with a strategy to differentiate between good traffic and bad traffic and to drop the latter during DDoS attacks. Our proposed solution is more efficient, having 94% less overhead on the server than the proposed solution in (Saraiah and et al, 2009). Though we have developed this solution for a web server, the same can be effectively be applied to any server by making the client pay a stamp before using up the server resources.

REFERENCES

Back, A. (2002). Hashcash - a denial of service countermeasure.

Darrel. Hankerson, A. M. and Vanstone, S. (2004). *Guide to Elliptic Curve Cryptography*. Springer, NewYork.

Dwork, C. and Naor, M. (1992). Pricing via processing or combatting junk mail. In *In Advances in Cryptology - Proc. CRYPTO 98*. Springer-Verlag: volume 740 of LNCS, pages 139147, Santa Barbara, CA USA.

Saraiah and et al (2009). Throttling ddos attacks. In *Proceedings of SECRYPT 2009 International Conference on Security and Cryptography*.

- Tuomas Aura, P. N. and Leiwo, J. (2000). Dos-resistant authentication with client puzzles. In *Revised Papers from the 8th International Workshop on Security Protocols*. Vol. 2133, Pages: 170 - 177.
- Wang, X. and Reiter, M. K. (2003). Defending against denial-of-service attacks with puzzle auctions. In *Proceedings of the 2003 IEEE Symposium on Security and Privacy*. Page: 78.



SciTeP Press
Science and Technology Publications