## A HIERARCHICAL HANDWRITTEN OFFLINE SIGNATURE RECOGNITION SYSTEM

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- Keywords: Signature Recognition, Hierarchical Classifier, Classification, Clustering, Naïve Bayes, Feature Selection, Learning Curve.
- Abstract: This paper presents an original approach for solving the problem of offline handwritten signature recognition, and a new hierarchical, data-partitioning based solution for the recognition module. Our approach tackles the problem we encountered with an earlier version of our system when we attempted to increase the number of classes in the dataset: as the complexity of the dataset increased, the recognition rate dropped unacceptably for the problem considered. The new approach employs a data partitioning strategy to generate smaller sub-problems, for which the induced classification model should attain better performance. Each sub-problem is then submitted to a learning method, to induce a classification model in a similar fashion with our initial approach. We have performed several experiments and analyzed the behavior of the system by increasing the number of instances, classes and data partition. Overall, the classifier performs in a hierarchical way: a top level for data partitioning via clustering and a bottom level for classification sub-model induction, via the Naïve Bayes classifier. Preliminary results indicate that this is a viable strategy for dealing with signature recognition problems having a large number of persons.

### **1 INTRODUCTION**

The verification and recognition of signatures in an offline signature recognition system is performed on data extracted from signatures. The signatures are written on paper. After gathering the signatures, several pre-processing techniques are required. The individual signatures are normalized to fit a standard format. Because the data acquired is usually noisy (either due to the scanning process or because of the pens used in writing) a filter may be applied. Then, a number of static features are extracted from the images and the signature dataset is created. An instance in the dataset consists of an individual signature; the attributes of an instance are the features extracted from the signature, while the class is the owner of the signature. This dataset is used to train a classifier such as to obtain a classification model, which is able to determine the owner of a new signature fed to the system.

Several different learning approaches have been investigated by the scientific community for signature recognition and verification systems. In (Prasad and Amaresh, 2003) the Euclidean distance in the feature space is employed in conjunction with an Artificial Neural Networks classifier to obtain a false acceptance rate of 13.33% on forged signatures. The Hidden Markov Model has been implemented by (Ozgunduz, 2005), obtaining a 75% score on Type I error. In (Justino, 2000), the Support Vector Machines yields a classification ratio of 95% and the Artificial Neural Networks obtains an accuracy of 75%. Another system based on the Hidden Markov Model may be found in Justino & Yacoubi, 2000.

Perhaps one of the most widely employed classification methods in signature verification and recognition systems is the Artificial Neural Networks (ANN) learner. This is why, in our approach, we have also focused on this method for the classification module. Also, initial performance evaluations on several learners have indicated that the Naïve Bayes (NB) classifier yields the most promising results, therefore, it has been chosen as the most appropriate learner in our approach.

The rest of paper is organized as follows. In section 2 we introduce some theoretical employed by our proposed system. Section 3 presents a

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theoretical aspects related to techniques and algorithms model for offline signature recognition. The first part of section 4 reviews the main implementation aspects and previous evaluation results obtained by the offline signature recognition system we have proposed in (Bărbănțan et al., 2009). In the second part of section 4 we propose a new approach for the classification module of the recognition system and discuss the results of an initial experimental analysis on this novel methodology. We conclude the paper with a series of remarks and proposals for future development.

## 2 THEORETICAL BACKGROUND

This section presents the theoretical aspects of the methods employed in the system. Details about how the methods are implemented and their usage are presented throughout the paper.

## 2.1 Feature Selection

Feature selection is one of the most important preprocessing steps in pattern recognition and data mining. It is an effective dimensionality reduction technique and an essential pre-processing method for removing irrelevant and/or redundant features, which are known to have a negative influence on the classification accuracy of most classifiers.

Some of the widely used techniques in feature selection are: the wrapper method (Kohavi and John, 1994), the Correlation-based Feature Selection (Hall, 2000) and Ranker (Witten and Frank, 2005) filters. *Correlation based Feature Selection* 

This filter evaluates the worth of a subset of features by considering the individual predictive ability of each feature along with the degree of redundancy between them; subsets of features that are highly correlated with the class while having low inter-correlation are preferred. They are independent of any classifier. Moreover, the comparative evaluations performed in (Hall, 2000) have shown that it achieves a comparable performance to the wrapper approach in terms of classification accuracy, while requiring a smaller amount of time to generate the attribute subset.

*The Ranker Filter.* The Ranker filter orders individual attributes according to an individual score, such as the information gain. Ranker not only ranks attributes but can also perform attribute selection by removing the lower-ranking ones.

*Wrapper Methods.* Wrapper methods employ performance evaluations on a learning algorithm in order to estimate the worth of a given attribute subset. Although much slower than filters wrappers have been shown to achieve significant performance improvements in classification (Kohavi and John, 1994).

#### 2.2 Learning Curve

The learning curve is often used as a method assessing for the variation of the classifier performance with respect to the variation of the training set size. The basic technique starts from a small size training set and progressively increases the number of instances until the entire available training set is considered. The convergence criterion is obtaining a stable, smooth curve, with constant accuracy.

## 2.3 Clustering

Unlike classification, clustering does not attempt to assign a concept label to an instance, but it partitions the given dataset into clusters containing very similar instances inside the same cluster, while dissimilar individuals are spread among clusters. The goal is to maximize intra-cluster similarity while minimizing inter-cluster similarity.

The similarity between objects when forming clusters is determined by using a distance measure. Among the best known are the Euclidean, Manhattan and the Minkowski distances (Han and Kamber, 2006) for numeric attributes, and the overlap metric for nominal (and binary) attributes.

The clustering techniques are traditionally grouped into four categories (Halkidi and Batistakis, 2001): partitional clustering, hierarchical clustering, density-based clustering and grid-based clustering.

Perhaps the best known clustering technique is k-Means – a partitional approach. It is an iterative technique which performs several steps to reach the final clusters. The algorithm takes as input k, the number of clusters to be created. Initially, the k cluster centres (centroids) are selected at random from the dataset. In each step, the instances are distributed into the appropriate clusters, by computing the distance between the instance and each cluster centroid. The instance is then assigned to the closest cluster. After all instances have been distributed into the current clusters, the cluster centroids are recomputed and a new iteration begins. The algorithm terminates when no more reassignments occur. The advantages of this method include computational efficiency, fast implementation, while the disadvantages refer to the random initialization of the k cluster centers (centroids) and the requirement of specifying k (i.e., k is not a result of data-specific properties) (Saitta et. al., 2007).

## 3 A MODEL FOR OFFLINE SIGNATURE RECOGNITION

This section presents a theoretical model for our offline signature recognition. The model contains the flow of the data acquisition process and a model for tuning the classification module.

#### 3.1 Data Acquisition Process

The flow of the data collection process follows the diagram in Figure 1.



Figure 1: Data collection flow diagram.

*Collection of Data*. The signatures are initially laid down on white sheets of paper. Following a scanning and cropping stage, the standard format images of the signatures are obtained.

*Pre-processing.* To remove the noise which may be introduced during the scanning process, a filter is employed. The images are then binarized, as the interest is in the distribution of the pixels and not their colour intensity.

Because of the different pens used in writing and because of the scanning process, the signatures do not have the same widths, so normalization step is required (Azar, 1997).

*Feature Extraction.* A number of static features are extracted from the one-pixel width signature image, to create a signature instance. Each signature

instance is stored in the signature database to create the signature dataset.

# 3.2 Classification and Recognition Module

The classification and recognition module performs the actual recognition task. Several steps have to be considered in order to reach a robust working system. These steps are presented in Figure 2.



Figure 2: Classification and recognition diagram.

*Performance.* The main factor in establishing the performance of the system is the classification accuracy. Since the recognition problem has a uniform cost (i.e. we are equally interested in identifying all signatures correctly), an error-based metric such as the accuracy is appropriate. *Tuning* 

Several tuning steps have to be considered, the most important being dataset tuning and algorithm tuning. Dataset tuning refers to finding the optimal number of training instances per class, such that the accuracy of the induced classification model remains at a high level as the diversity of the data (i.e. the number of classes) increases. This is achieved by analyzing the learning curve built on the available data.

Algorithm tuning establishes which learning method is more appropriate and which are the best parameter settings for it. Of course this step must take advantage of previous work performed in the field. *The Classification Model.* The working classification model is induced from the tuned dataset, using the learning algorithm and the appropriate parameters determined in the algorithm tuning phase. When a new signature instance arrives in the system, it is assigned a label (a person name) by the classification model.

## 4 A PROPOSED SYSTEM FOR OFFLINE SIGNATURE RECOGNITION

In this section we review the main implementation aspects and previous evaluation results obtained by the offline signature recognition system we have previously proposed in (Bărbănțan et al., 2009). In the second part of this section we propose a new approach for the classification module of the recognition system and discuss the results of an initial experimental analysis on this novel methodology.

#### 4.1 Data Collection

The data has been collected from 84 individuals belonging to different age groups. Each individual has provided approximately 20 signatures. The signatures are initially collected on a white A4 sheet of paper, using either pens or pencils. Each sheet of paper contains 10-20 signatures. The scanning process is performed at a resolution of 150 dpi. Each signature is cropped into a 400x400 pixel frame. Signatures that do not fit this format are discarded. The individual signatures are then saved as 256 color bitmaps.

The first pre-processing step performed, as the diagram in Figure 1 shows, is image enhancement: the noise introduced by scanning is removed using a median filter. Then, the image is binarized and skeletonization method is applied, using Hilditch's algorithm (Azar, 1997).

*Extracted Features.* We have employed a set of global static features extracted from the signature image, all having numerical values. Some of the employed features can be found in similar systems, (Justino, 2000), (McCabe, 2008), (Amaresh and Prasad), and we also proposed two new features.

The 25 features considered in our system, have been grouped into 5 categories, as shown in Table 1. The first category of features contains the two new introduced features which are distance based: Topbottom Euclidean distance and Left-right Euclidean distance. They measure the Euclidean distance from the leftmost and rightmost pixel and from the top to the bottom pixel. By using feature selection method, these attributes are selected as being relevant.

Table 1: The extracted features grouped into categories. \* represents the original features proposed.

Attribute	Number	Category
categories	of	name
C	attributes	
1. Features obtained	6+2*	Border
from the extreme		features
points		10
2. Features extracted	6	Concentratio
from the histogram		n features
3. Features related to	4	Number
the number of pixels		features
4. Features obtained	4	Position
with respect to the	11:	features
pixel position		11
5. Features having as	3	Angle
result an angular	0	features
value		

The content of the categories is the following:

- Border Features = {Width, Height, Left-right, Top-bottom, Area, Aspect ratio, Signature area, Width/Area}
- Concentration Features = {Maximum value of horizontal and vertical histogram, Number of local maximum of horizontal and vertical histogram, Top heaviness, Horizontal dispersion}
- Number Features = {Number, Edge points, Cross points, Mask feature}
- Position Features = {Sum of X and Y positions, Horizontal and vertical centre of the signature}
- Angle Features = {Inclination, Baseline slant angle, Curvature}

Dataset Structure. Following a cleaning stage, in which we removed the signature images which were too noisy, we have ended up with a dataset containing 1548 instances, labelled into 84 classes. For the tuning and evaluation activities we have employed several strategies: either repeated 80-20 percentage splits, or 10-fold cross validation.

#### 4.2 Classification

For the classification module we have considered two Bayesian classifiers and the Multilayer Perceptron (MLP). The two Bayesian classifiers used are the Naïve Bayes and the BayesNet.

#### 4.2.1 Feature Selection

Since we have employed a large set of features coming from different sources, and also added two new features, we have performed feature selection to find the optimal subset of features, by eliminating the irrelevant and redundant features. We have applied the following strategy: the attributes are first ordered by their importance with respect to the class by using the Ranker filter. Then two other methods were used: the CFS filter and the wrapper method, whose results are combined such that the most promising subset is obtained. We employed the implementations found in Weka (Witen and Frank, 2005) for the three methods, with their default parameters.

*Ranker Filter.* We have employed the information gain evaluator to measure the importance of each attribute for the class. The ranking of the attributes was used when combining the results of the other two methods.

*CFS Filter.* The CFS filter removes the attributes which are weakly correlated with the class and/or strongly correlated with other attributes. With the CFS filter 15 attributes are selected as being relevant, from the

total set of 25 attributes.

*Wrapper Method.* For the wrapper approach we have employed a specialization of the 3-tuple wrapper: <generation, evaluation, validation>, using the Naïve Bayes (NB) classifier in the evaluation function. MLP has not been considered because its performance on preliminary evaluations was 5% below that of NB, and previous work (Vidrighin et al., 2008) suggests that feature selection does not affect the initial ranking of classifiers, meaning that the best classifier on the initial set of features yields the highest performance on the reduced set as well. The wrapper method selected a subset of 18 attributes as best describing the instances.

The subset of attributes selected by the CFS filter and the one generated by the Wrapper method has a number of 12 common attributes. One of the two features introduced by us was selected as being relevant by both of the methods.

After selecting the common attributes, some of the remaining attributes were added to the subset in the order generated by ranker. In the end a subset of 23 attributes was obtained as being the most representative.

#### 4.2.2 Learning Curve Analysis

Having generated the dataset, we wanted to evaluate the way the number of instances influences the classification accuracy of our system. That is why we performed several learning curve experiments. We started with a maximum of 20 instances/class and observed that the learning curve had still an ascending aspect. Therefore, we decided to collect more instances from each class. We estimated that 25 instances per class were needed. When evaluating the performance in the new context, we noticed the classification accuracy decreased while increasing the number of classes. Besides the lower accuracy, another problem is that, in a real application, it is unfeasible to collect such a large number of sample signatures from a person for authentication. These drawbacks indicate that a different approach should be considered.

#### 4.3 A New Approach for the Classification Module

Our previous work reported a stable learning curve, for the accuracy value as a function of number of instances/class. However, stability is obtained for a lower accuracy value which suggests the need of a different approach.



#### 4.3.1 Preliminary Investigations

Figure 3: Learning curve with increasing number of classes and 20 instances/class.

We have restarted the experiments with 84 classes, 20 instances per class. The approach this time was to identify the optimal pair <number of instances per class, number of classes per dataset> in terms of accuracy. From the analysis of the learning curve it resulted that between 50 and 55 classes the curve is stable and the accuracy is acceptable, while after 55

classes the performance degradation becomes unacceptable.

In the attempt to evaluate the minimum optimal number of instances/class, we run an experiment on a 55 class dataset. The learning curve obtained is presented in Figure 4. It emphasizes a minimum number of 11 instances/class for an acceptable accuracy. Moreover, the curve becomes stable (with a less steep slope), that is why our expectations are that the optimum number of instances per class to be found in the interval [11,20].



Figure 4: Learning curve with increasing number of instances/class and 55 classes.

This suggests that we should find a technique which has to consider fewer classes in training a classification model.

Because speed is also an issue in signature recognition systems and because we cannot collect a large number of reference signatures from the same person, we have performed a series of experiments with 11 up to 16 instances per class, to determine the best number of training instances/class. We have varied the number of classes between 5 and 84, using a 5 class increment.

As shown in Figure 5, the performance of the NB classifier degrades as the number of classes increases, just like in the case of the 20 instances/class learning curve in Figure 3. This suggests that we need to employ a data partitioning criterion in the training phase, and build classification sub-models on smaller datasets (with fewer classes). Also, a number of 11 or 14 instances per class seem to yield high accuracies.



Figure 5: Clustering using different number of instances/class and 84 classes.

# 4.3.2 A Hierarchical, Data-partitioning based Approach

The new approach we propose employs a hierarchical strategy: first split the initial dataset in several subsets via a clustering method, and subsequently supply each subset to the NB classifier, for building classification sub-models (Figure 6).



Figure 6: Generic training process of the hierarchical classifier.

When a new instance arrives and needs to be classified, the hierarchical classifier first clusters the instance to find the best classification sub-model for it. It then feeds the instance to that classification sub-model, which assigns the class label to the instance (Figure 7).



Figure 7: Generic classification process for the hierarchical classifier.

Clustering is a technique that groups similar instances together. For the purpose of our recognition system, we are interested that the instances from a single class are gathered (as much as possible) by the same cluster. Since the approximate number of clusters can be estimated apriori from the total number of classes and the approximate number of classes we want in each classification sub-model (which follows from careful analysis of the diagram in Figure 5), we have decided to employ k-Means as clustering method.

In the attempt to develop a working functional classification module, we have performed a series of evaluations meant to help establish optimal settings for a number of parameters in our new system, the most important being the optimal number of clusters (i.e. classification sub-models) and the optimal number of instances per class.

For these investigations we have employed the SimpleKMeans implementation from the Weka framework of the k-Means clusterer.

Because the available data contains classes which do not have exactly 20 instances (due to the initial data cleaning), we have removed these classes to obtain a dataset with a uniform distribution. Therefore, the next experiments were conducted on a dataset having 76 classes, each with exactly 20 instances.

The purpose of our next experiments is to determine the optimal number of clusters to use, such as to obtain acceptable sizes for the training subsets, while preserving a good cluster purity.

Therefore, we performed clustering experiments with versions of the training set containing 11, 14, 16, 18 and 20 instances per class. For each experiment, we have varied the number of clusters between 1 (no clustering at all) and 9. A first observation can be made on the speed of the clustering process: as we increased the number of clusters, the speed was dramatically reduced. While for k=2 the results were almost instantaneous on all datasets considered, it took the algorithm 2 days to complete the clustering process for k=9.



Figure 8: Performance analysis of the sub-models induced from clustering with 1-9 clusters, on the datasets having 11, 14, 16, 18 and 20 instances per class.

The next step in training the hybrid classifier is to form the classification sub-problems – generate the reduced training sets for each cluster – and feed them to the NB classifier. Although this step is not yet connected with the clustering step, we have performed initial evaluations to assess the performance of the NB classifier on these reduced training sets (containing fewer, but very similar classes). When performing clustering, for some classes not all the instances fall in the same cluster, so the clusters are not pure. To solve this issue, when forming the training subsets, we have placed all the instances in one class inside the subset corresponding to the cluster with the largest number of instances from that class.

These subsets were then fed to NB classifiers and we evaluated the classification accuracy of the submodels induced, using a 10-fold cross-validation loop. The results are presented in Figure 8.

The results indicate that none of the evaluated dataset settings (i.e. number of instances per class) outperforms all the others for all types of partitioning (i.e. number of clusters evaluated). However, most of them seem to have several local maxima. Figure 9 clearly shows the existence of partitioning intervals in which different pairs of settings perform the best.



Figure 9: Curves representing the local maxima when partitioning into clusters.

Therefore, a maximum can be selected. In doing so we must also consider the cluster purity - to be discussed shortly. The performance slopes in Figure 9 indicate that either 14 or 20 instances/class should be considered, for a 6-9 cluster partitioning. However, the number of clusters should be adjusted for each dataset, current evaluations indicating a 1/10 ratio on the number of clusters/classes.



Figure 10: Curves representing the impurity of clusters for different number of instances/class and 76 classes.

We expect that the way the instances are grouped into clusters affects the performance of the entire system. We define impurity as the number of instances that do not belong to the cluster containing the largest number of instances from the given class. We have performed an analysis of the impurity of the clusters. The results are presented in Figure 10.

Generally, as we increase the number of instances per class the impurity of the clusters increases also. The cluster impurity affects the second step in the training process, i.e. inducing the sub-models for classification. A small cluster impurity is thus preferable.

As a consequence, when tuning the number of instances per class to use for training and the number of clusters in which the classes should be split into, a trade-off between the accuracy and the impurity has to be made. The analyses of the results indicate as optimal the values in Table 2. These values are particular for this dataset. However, they indicate that we can achieve the same performance if we decrease the size of the classification sub-problems when the number of available instances per class is relatively small (we achieved the same performance with 14 instances per class and 8 clusters as with 20 instances per class and 7 clusters). This suggests that, as the number of classes increases, we might have to consider a 2-stage clustering process, such as obtain relatively small sub-classification to problems. Also, we need to consider the time aspect. The speed of building the models for 7 and 8 clusters is significantly better than the speed of building a 9-cluster model.

Table 2: Optimal number of instances per class and the corresponding number of clusters.

Number of instances/class	14	20
Optimal number of clusters	8	7
Minimum number of	4	4
classes/cluster		
Maximum number of	17	20
classes/cluster		
Mean number of classes/cluster	9.5	10.85
Accuracy	~91%	~91%

## 5 CONCLUSIONS AND FUTURE WORK

This paper presents a new method for classifying handwritten signatures using a hierarchical datapartitioning based approach. The new method tackles the problem we encountered with an earlier version of our system when we attempted to increase the number of classes in the dataset: as the complexity of the dataset increased, the recognition dropped unacceptably for the problem rate considered - from 98.53 on a 5-class problem to 84.37 on an 84-class problem. The new method combines a clustering mechanism and a Bayesian classifier. Various experiments were performed in order to determine the optimal number of clusters to divide a given dataset and the number of instances to use from each class.

Preliminary results yield an accuracy of more than 91%, with the entire set of attributes, without using feature selection. We consider that feature selection will further boost the classification accuracy. We also managed to improve the classification time by using a smaller number of instances per class (14).

The results have also shown that peak performances are obtained on a 14 instances/class dataset using 8 clusters and a 20 instances/class dataset using 7 clusters.

Our current work focuses on connecting the two steps of the training process, and addressing the classification stage. Also, for generalizing the scope of the system, during the training process several issues need to be considered.

The first is that the classes are not split uniformly into clusters (instances from the same class are distributed among at most 4 clusters). At present, we solve this issue by adding all the instances to the cluster having the maximum number of instances from that particular class. However, on a global model, such situations should have a specific approach. A possible solution is to distribute all the instances of a class to all clusters which contain a number of instances above a threshold from that class. We need to investigate how this approach influences the complexity, the performance and the time of the induced sub-models, as it may produce the necessity of an additional clustering step.

A second issue which needs addressing is the time required for the SimpleKMeans method to split the dataset into clusters. We experimentally observed that the clustering time increases with the number of clusters. As for 2-5 clusters it takes several minutes to build the clusters, for values like 8 or 9 clusters, the time required is of up to 2-3 days.

Moreover, as the number of classes increases, we might need to introduce additional clustering steps. We are currently evaluating a methodology for automatically establishing the parameters of the hierarchical structure: number of clustering levels, number of clusters per level, optimal size (in terms of number of classes) of the training subset submitted to the Naïve Bayes classifiers.

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