

# OPTICAL SECURE COMMUNICATION SYSTEM BASED ON CHAOS SYNCHRONIZATION

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Abstract: We propose a secure optical communication system based on the principles of generalized and complete synchronization of chaotic oscillations. Both a transmitter and a receiver are composed by two chaotic external-cavity semiconductor lasers which are coupled in a master-slave configuration to provide generalized synchronization, while the master lasers in the transmitter and in the receiver are completely synchronized via an optical fiber. A message is added to the slave laser in the transmitter and sent to the receiver to be compared with the output of the receiver slave laser. The system is robust to a small mismatch of the laser parameters or of the coupling between the master and slave lasers, unavoidable in a real system, and can even enable a good communication up to a 5 Gb/s transmission rate using the chaos masking encryption, when the master lasers in the transmitter and in the receiver are coupled bidirectionally.

## 1 INTRODUCTION

Due to their high relaxation oscillation frequencies (10 GHz and beyond) and direct comparability with existing optical fiber communication technology, semiconductor lasers have attracted much attention from researchers working in optical communications (Shore et al., 2008), especially after successive experiments with the Athens' fiber networks (Argyris et al., 2005). In these lasers, high dimensional chaotic signals with a large information entropy are generated by means of delayed feedback (Mirasso et al., 1996; Ruiz-Oliveras and Pisarchik, 2006). The system performance largely depends on the quality of chaos synchronization, i.e. the synchronization error should be minimized. Depending on the particular application of chaotic optical communication, different encoding and decoding schemes, such as chaos masking, chaos shift keying, and chaos modulation were implemented (Tang et al., 2006). The majority of these schemes are based on complete synchronization (CS) and use only a single channel for both the laser coupling and the signal transmission. A drawback of such schemes is that CS asks for identical systems, very easy to obtain in theory but difficult in practice.

A secure communication system based on the concept of generalized synchronization (GS) (Afraimovich et al., 1986) and its combination with CS was originally suggested by Murali and Lakshma-

nan (Murali and Lakshmanan, 1998). Since they used a single communication channel, the signal itself created a synchronization error that reduced the communication quality. A different approach (Terry and Van-Wiggeren, 2001) consisted of two identical pairs of chaotic systems (master and slave); one pair in the transmitter and the other pair in the receiver. A binary message was encrypted in the coupling strength between master and slave in the transmitter and was recovered by analyzing the error dynamics in the receiver; in fact, this method was a modification of a chaos shift keying with an important innovation, it used two channels: one to provide CS between the transmitter and the receiver master systems, and the other channel to compare the two slave trajectories. However, in the chaos shift keying schemes a binary bit message inherently produces a synchronization error, hence limiting the communication rate with the synchronization time because the transmitter and the receiver are not continuously synchronized.

## 2 COMMUNICATION SCHEME AND LASER MODEL

We propose a new two-channel optical secure communication system shown in Figure 1, which utilizes two pairs of unidirectionally coupled external cavity

semiconductor lasers, one pair in the transmitter, and the other in the receiver; each consisting of a master laser (ML) and a slave laser (SL), not necessarily identical, but coupled enough to exhibit GS, while the master lasers in the transmitter and in the receiver should be identical (or near identical) and completely synchronized. This scheme is completely symmetric, the optical paths between the master and slave lasers in the transmitter and in the recorder are the same, this provides close similarity between their GS functions. Such a similarity cannot be obtained if only one master laser is coupled with two slave lasers, one in the transmitter and one in the receiver (Yamamoto et al., 2007; Annovazzi-Lodi et al., 2008), giving difficulties for long distance communication.

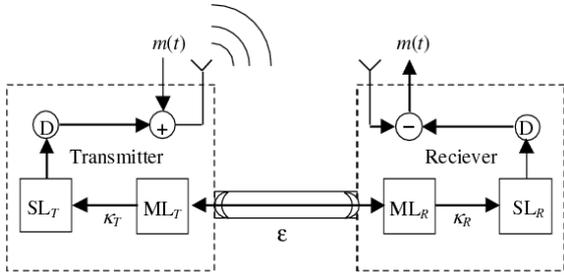


Figure 1: Two-channel optical chaotic communication using chaos masking encryption scheme.  $ML_T$ ,  $SL_T$  and  $ML_R$ ,  $SL_R$  are the master and slave lasers in the transmitter and in the receiver, respectively,  $\kappa_T$  and  $\kappa_R$  are the coupling strengths between the lasers in the transmitter and in the receiver,  $\epsilon$  is the coupling strength between the master lasers, and  $D$  are the photodetectors.

The external cavity semiconductor lasers can be modeled by the following equations based on the well-known Lang-Kobayashi approach (Mirasso et al., 1996; Lang and Kobayashi, 1980):

$$\begin{aligned} \dot{E}_{M,T,R}(t) = & \frac{1}{2}(1 + i\alpha) \left[ G_{M,T,R}(t) - \frac{1}{\tau_p} \right] E_{M,T,R}(t) + \\ & \gamma_{M,T,R} E_{M,T,R}(t - \tau_{M,T,R}) \exp(-i\phi_{M,T,R}) + \\ & \epsilon E_{M,R,T}(t) + \sqrt{2\beta N_{M,T,R}(t)} \xi_{M,T,R}(t), \end{aligned} \quad (1)$$

$$\begin{aligned} \dot{E}_{S,T,R}(t) = & \frac{1}{2}(1 + i\alpha) \left[ G_{S,T,R}(t) - \frac{1}{\tau_p} \right] E_{S,T,R}(t) + \\ & \gamma_{S,T,R} E_{S,T,R}(t - \tau_{S,T,R}) \exp(-i\phi_{S,T,R}) + \\ & \kappa_{T,R} E_{M,T,R}(t) + \sqrt{2\beta N_{S,T,R}(t)} \xi_{S,T,R}(t), \end{aligned} \quad (2)$$

$$\dot{N}_{M,S}(t) = \frac{I}{q} - \frac{N_{M,S}(t)}{\tau_n} - G_{M,S}(t) |E_{M,S}(t)|^2, \quad (3)$$

$$G_{M,S}(t) = g \frac{N_{M,S}(t) - N_0}{1 + \rho |E_{M,S}(t)|^2}, \quad (4)$$

where the subscripts  $M$  and  $S$  stand for ML and SL,  $T$  and  $R$  stand for transmitter and receiver,  $E_{M,S}(t)$

is the slow varying electric complex field ( $P_{M,S} = |E_{M,S}(t)|^2$  being the laser output power),  $N_{M,S}(t)$  is the carrier density,  $\alpha = 3$  is the linewidth enhancement factor,  $\tau_p = 2$  ps and  $\tau_n = 2$  ns are the photon and carrier lifetimes respectively,  $\gamma_{M,S}$  is the feedback parameter ( $\gamma_{M,T,R} = 25$  ns<sup>-1</sup> and  $\gamma_{S,T,R} = 20$  ns<sup>-1</sup>),  $\tau_{M,S}$  is the external cavity round-trip time ( $\tau_{M,T,R} = 1$  ns and  $\tau_{S,T,R} = 0.5$  ns),  $\phi_{M,S} = \omega\tau_{M,S}$  is the initial phase,  $\omega = 1.2 \times 10^3$  ps<sup>-1</sup> is the angular frequency for all lasers,  $\beta = 1.1$  ps<sup>-1</sup> is the spontaneous emission rate,  $\xi_{M,S}(t)$  is Gaussian white noise of zero mean and unity intensity (Heil et al., 2001),  $I = 29$  mA is the pump current,  $q = 1.602 \times 10^{-19}$  C is the electronic charge,  $g = 1.5 \times 10^{-8}$  ps<sup>-1</sup> is the gain parameter,  $N_0 = 1.5 \times 10^8$  is the carrier density at transparency,  $\rho = 10^{-7}$  is the gain saturation coefficient, and  $\chi = \eta_{ex} \sqrt{1 - R} / (\tau_c \sqrt{R})$  is the coupling parameter ( $\chi = \kappa_T, \kappa_R, \epsilon$ ) (Mirasso, 2000) varied in the simulations ( $R = 0.3$  being the facet laser power reflectivity and  $\tau_c = 6.6$  ps being the internal cavity round-trip time, and  $\eta_{ex}$  accounts for losses different than those introduced by the laser facet).  $\chi = 100$  ns<sup>-1</sup> corresponds to the case when approximately 42.8% of the laser output power is injected into the other laser. For the case of unidirectional coupling,  $\epsilon$  appears only in  $ML_R$ .

## 2.1 Chaos Synchronization and Information Transmission

To quantitatively measure synchronization, we calculate the normalized cross correlation  $C$  between the output powers of two coupled lasers ( $i$  and  $j$ )

$$C(t) = \frac{\langle P_i(t') P_j(t' - t) - \overline{P_i} \overline{P_j} \rangle_{t'}}{\sigma_i \sigma_j}, \quad (5)$$

where  $\langle \dots \rangle$  stands for time average,  $\overline{P_i}$ ,  $\overline{P_j}$  and  $\sigma_i$ ,  $\sigma_j$  are the mean and standard deviations of the laser powers, respectively. Since in this paper we only take into consideration isochronous synchronization, we only calculate  $C(0)$ . CS can be quantitatively characterized with the mean synchronization error

$$\langle e \rangle = P_i - P_j. \quad (6)$$

Figure 2 shows  $C$  and  $\langle e \rangle$  when Eqs. (5) and (6) are used for our system;  $C_M$ ,  $\langle e_M \rangle$  are calculated for  $ML_R$  and  $ML_T$  [Fig. 2(a)],  $C_T$ ,  $\langle e_T \rangle$  for  $ML_T$  and  $SL_T$ ,  $C_R$ ,  $\langle e_R \rangle$  for  $ML_R$  and  $SL_R$  [Fig. 2(b)], and  $C_S$ ,  $\langle e_S \rangle$  for  $SL_R$  and  $SL_T$  [Figure 2(c)], as functions of the coupling strengths for unidirectional and bidirectional coupling between  $ML_T$  and  $ML_R$ . The qualitative behavior is similar in both cases, however for bidirectional coupling a much smaller  $\epsilon$  is required

to obtain CS between the masters [Figure 2(a)] and between the slave [Figure 2(c)] lasers. Another advantage of bidirectional coupling, very important for security purposes, is that the transmitter has feedback information about the receiver's behavior, so that if someone tried to enter the synchronization channel in order to obtain part (or all) of the laser light, the feedback signal would be modified. If a hacker was able to connect with the synchronization channel, he would use a part of the laser power to synchronize his own laser, this would reduce the power entering to the authorized receiver and hence the power returning to the transmitter that could be easily identified.

Since ML and SL are not identical, we obtain GS characterized by a relatively small cross-correlation ( $C \approx 0.8$ ) and a high mean error ( $\langle e \rangle \approx 0.4$ ) for even very strong coupling ( $\kappa = 100 \text{ ns}^{-1}$ ) [Figure 2(b)]. These characteristics indicate a large difference between the laser dynamics preventing a non-authorized person, even when he has access to both channels, to read the message without knowing the function  $H$ . The same curves were obtained for both the transmitter and the receiver, since we supposed that their ML and SL were coupled with the same coupling strengths, i.e.  $\kappa_T = \kappa_R$ . From Figures 2(b) and 2(c), one can see that CS between the master and slave lasers is not needed to obtain CS between  $SL_T$  and  $SL_R$ , proved even a relatively small coupling strength ( $\kappa \approx 50 \text{ ns}^{-1}$ ) allows for an excellent correlation.

One way to quantitatively characterize the performance of a communication system is Q-factor, given by

$$Q = \frac{\langle P_1 \rangle - \langle P_0 \rangle}{\sigma_1 + \sigma_0}, \quad (7)$$

where  $\langle P_1 \rangle$  and  $\langle P_0 \rangle$  are the average optical powers of bits "1" and "0", respectively, while  $\sigma_1$  and  $\sigma_0$  are the corresponding standard deviations. We prove the benefits of our system with three encoding methods: (i) chaos modulation, where the message is encrypted by modulating the transmitter's chaotic carrier according to the expression  $(1 + m(t))E_S \exp(i\phi_S)$  resembling the type of amplitude modulation (AM), (ii) chaos shift keying, where the message is added to the pump current of  $SL_T$  in Eq. (2),  $I + m(t)$ , inevitably producing an error in synchronization between the slave lasers, and (iii) chaos masking, where the message, completely independent of the electric field, is added to the chaotic carrier as  $E_S \exp(i\phi_S) + m(t) \exp(i\phi_m)$  ( $\phi_m$  being the message phase). In all these methods, the message amplitude is set to a 2% of the  $SL_T$  amplitude and the length of the encoded message is a  $10^4$  random bit sequence. The decoded message is filtered with a 5th order Butterworth low-pass filter and

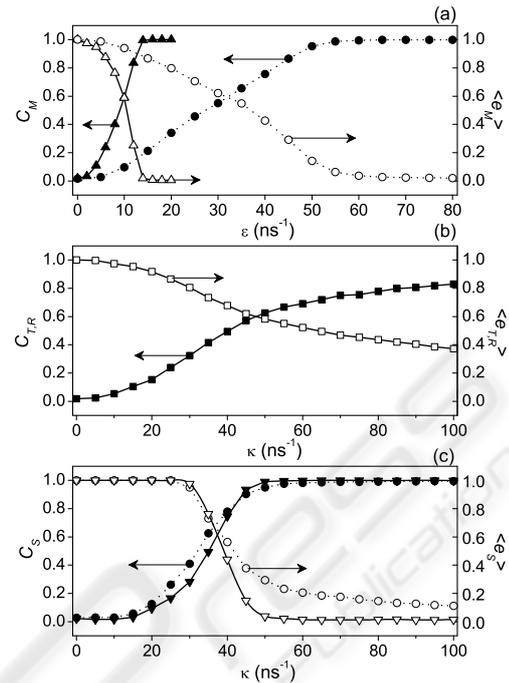


Figure 2: Cross-correlation (filled signs) and mean synchronization error (clean signs) between (a)  $ML_T$  and  $ML_R$ , (b)  $ML_T$  and  $SL_T$ , and (c)  $SL_T$  and  $SL_R$ , when  $ML_T$  and  $ML_R$  are coupled unidirectionally (dots) ( $\epsilon = 80 \text{ ns}^{-1}$ ) and bidirectionally (triangles) ( $\epsilon = 16 \text{ ns}^{-1}$ ) as functions of their coupling parameter. All cross-correlations are calculated in the absence of a message.

the eye diagrams from the extracted codes are constructed to evaluate the transmission quality.

For the chaos modulation method, a very low Q-factor is obtained and hence the information transmission is hardly possible. In Figure 3 we plot the values of the Q-factor as a function of the coupling parameter  $\kappa = \kappa_T = \kappa_R$  for chaos shift keying [Figure 3(a)] and chaos masking [Figure 3(b)]. We use  $\epsilon = 80 \text{ ns}^{-1}$  for unidirectionally coupled and  $\epsilon = 16 \text{ ns}^{-1}$  for bidirectionally coupled  $ML_T$  and  $ML_R$ . Note, that 5 Gb/s good signal transmission is only possible for chaos masking in the case of bidirectional coupling.

Finally, we consider the case when the transmitter and the receiver systems are not exactly identical, i.e. either  $\kappa_T \neq \kappa_R$  or laser parameters exhibit a small mismatch. Therefore,  $SL_R$  and  $SL_T$  are partially synchronized by a certain function. Now, GS between ML and SL in the transmitter and in the receiver is characterized by two different functional dependences, that causes a small difference between  $C_T$  and  $C_R$ ,  $\delta C = C_T - C_R$ , and we are interested in how the mismatch  $\delta C$  affects communication quality. Keeping all laser parameters identical and  $\kappa_T = 80 \text{ ns}^{-1}$  for which  $C_T = 0.7781$  [Figure 2(b)], we vary  $\kappa_R$  ( $60 \text{ ns}^{-1} \leq \kappa_R \leq 100 \text{ ns}^{-1}$ ) giving as a result the variation

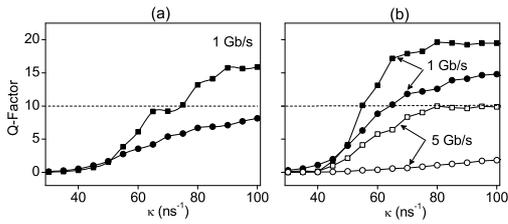


Figure 3: Q-factor as a function of coupling parameter between ML and SL for (a) chaos shift keying and (b) chaos masking for 1 Gb/s (filled signs) and 5 Gb/s (open signs) signal transmission when master lasers are coupled unidirectionally (dots) and bidirectionally (squares) for (a) chaos shift keying and (b) chaos masking. The communication quality is good above the dashed line. For chaos shift keying the 5 Gb/s transmission is not possible.

of  $C_R$  ( $-0.04 \leq C_R \leq 0.04$ ). Figures 4(a-c) show  $\langle e_S \rangle$  (in %) and  $Q$  as functions of  $\delta C$  for 1 Gb/s and 5 Gb/s transmission; Fig. 4(a) was obtained with chaos shift keying and Figs. 4(b) with chaos masking for bidirectionally coupled master lasers with  $\varepsilon = 16 \text{ ns}^{-1}$ . The loss of synchronization between slaves due to the chaos shift keying results in the displacement of the maximum  $Q$  and minimum  $\langle e_S \rangle$  from  $\delta C = 0$  in Figure 4(a). With the same  $\varepsilon$  Figure 4(c) represents the results for chaos masking for unidirectional coupling, clearly not as efficient as bidirectional coupling. The communication quality for chaos shift keying with unidirectional coupling is not sufficient ( $Q < 10$ ) [Figure 3(a)]. Although chaos masking allows a 1 Gb/s communication with unidirectional coupling, the error is relatively high ( $\langle e_S \rangle > 15\%$ ) [Figure 4(c)].

We now also consider what happens when the master lasers are not completely identical, keeping  $\kappa_R = \kappa_T$ . In this case, the most critical parameter for synchronization is the injection current. Figures 4(d-f) show how a small mismatch  $\delta I = I_T - I_R$  ( $I_T$  and  $I_R$  being the injection currents of the master lasers in the transmitter and in the receiver) affects  $\langle e_M \rangle$  and  $Q$ . One can see that when the master lasers are coupled bidirectionally, the system is more robust to a parameter mismatch, i.e. the 1 Gb/s transmission can be realized in a much larger region of  $\delta C$  or  $\delta I$ , and even a 5 Gb/s rate can be obtained but only for chaotic masking and only when the slave lasers and the master lasers are completely synchronized, i.e. when the identity conditions,  $\delta C \approx 0$  and  $\delta I \approx 0$ , are fulfilled. Figure 4(d) shows that chaos key shifting even for 1 Gb/s is not as efficient as chaos masking.

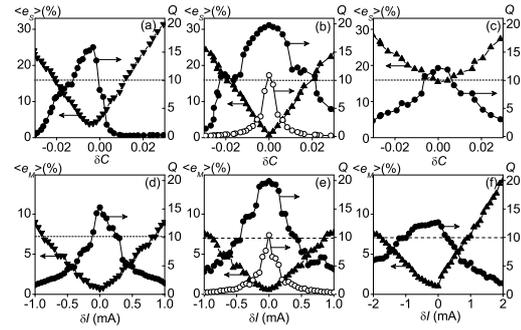


Figure 4: Mean synchronization error (triangles) and Q-factor (dots) as functions of mismatch of (a-c) correlations  $\delta C$  and (e-f) injection currents  $\delta I$  of master lasers for chaos shift keying (left-hand column) and chaos masking (middle and right-hand columns) when the master lasers are coupled either bidirectionally (left-hand and middle columns) or unidirectionally (right-hand column). 1 Gb/s and 5 Gb/s transmission are shown by the closed and open dots, respectively.  $\kappa_T = 80 \text{ ns}^{-1}$ ,  $\varepsilon = 16 \text{ ns}^{-1}$  for bidirectionally and  $\varepsilon = 80 \text{ ns}^{-1}$  for unidirectionally coupling, and  $I_T = 29 \text{ mA}$ . The communication quality is good above the dashed lines.

### 3 CONCLUSIONS

We have introduced an efficient optical chaotic communication system which uses the combination of complete and generalized synchronizations. The system contains two channels, one for synchronization and the other for information transmission, and consists of two pairs of external cavity semiconductor lasers each coupled in GS configuration, while the master lasers in the transmitter and in the receiver are completely synchronized. The ability of this system for high-quality communication is demonstrated through numerical simulations with the Lang-Kobayashi model. We have shown that bidirectional coupling between the master lasers provides much better communication quality (up to 5 Gb/s) than unidirectional coupling and makes the system more robust to a mismatch between the ML parameters or the coupling strengths between ML and SL. In the case of bidirectional coupling, the two coupled lasers influence to each other so that the identity requirements for complete synchronization are not as strong as in the case of unidirectional coupling that allows more tolerances. The efficiency of this system is very clear when the encryption method is chaos masking, it can also be used for other methods although the results are not so spectacular.

## ACKNOWLEDGEMENTS

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