

# ESTIMATING SOFTWARE DEVELOPMENT EFFORT USING TABU SEARCH

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**Abstract:** Some studies have been recently carried out to investigate the use of search-based techniques in estimating software development effort and the results reported seem to be promising. Tabu Search is a meta-heuristic approach successfully used to address several optimization problems. In this paper, we report on an empirical analysis carried out exploiting Tabu Search on two publicly available datasets, i.e., Desharnais and NASA. On these datasets, the exploited Tabu Search settings provided estimates comparable with those achieved with some widely used estimation techniques, thus suggesting for further investigations on this topic.

## 1 INTRODUCTION

Effort estimation is a critical basic activity for planning and monitoring software project development and for delivering the product on time and within budget. Several methods have been proposed in order to estimate software development effort. Many of them determine the prediction exploiting some relevant factors of the software project, named cost drivers. These methods, named data-driven, exploit data from past projects, consisting of both factor values that are related to effort and the actual effort to develop the projects, in order to estimate the effort for a new project under development (Shepperd and Schofield, 2000). In this class, we can find some widely used techniques, such as Linear and Stepwise Regression, Classification and Regression Tree, and Case-Based Reasoning (Briand and Wieczorek, 2002).

In the last years, some attempts have been made to apply search-based approaches to estimate software development effort. Indeed, effort estimation can be formulated as an optimization problem (Harman, 2007), where we have to search for the most accurate estimate, i.e. the one that minimizes the difference with the actual effort. In particular, some researchers have analyzed the use of Genetic Programming in estimating software development effort (Burgess and Lefley, 2001) (Lefley and Shepperd, 2003), reporting results that encourage further investigations in this context.

Genetic Programming is a search-based approach inspired by evolutionary biology to address optimization problems. There exist other search-based techniques that have been found to be very effective and robust in solving numerous optimization problems. In particular, Tabu Search has been successfully applied for software testing (Diaz *et al.*, 2008), for object replication in distributed web server (Mahmood and Homeed, 2005) and for Software-Hardware Partitioning (Lanying and Shi, 2008). In this paper, we report on an empirical study carried out to analyze the effectiveness of Tabu Search for effort estimation. In particular, the specific contributions of the paper are:

- the definition and the analysis of a Tabu Search algorithm for effort estimation;
- the comparison of the proposed approach with widely used estimation methods.

To this aim we employed two publicly available datasets, i.e., Desharnais (Desharnais, 1989) and NASA (Bailey and Basili, 1981), widely used in the context of effort estimation.

The remainder of the paper is organized as follows. Section 2 provides a brief description of the Tabu Search algorithm conceived for estimating software development effort. Section 3 summarizes the empirical analysis we performed to assess the effectiveness of the algorithm. Related work is presented in Section 4. Final remarks and future work conclude the paper.

## 2 THE ESTIMATION METHOD

Tabu Search (TS) is an optimization method proposed originally by Glover to overcome some limitations of Local Search (Glover and Laguna, 1997). It is a meta-heuristic relying on adaptive memory and responsive exploration of the search space. To build a TS algorithm we have to perform the following steps:

- define a representation of possible solutions;
- define the neighbourhood;
- choose an objective function to evaluate solutions;
- define the Tabu list, the aspiration criteria, and the termination criteria.

In the context of effort estimation, a solution consists of a model described by an equation that combines several factors:

$$\text{Effort} = c_1 op_1 f_1 op_2 \dots op_{2n-2} c_n op_{2n-1} f_n op_{2n} C$$

where  $f_i$  and  $c_i$  represent the values of the  $i^{\text{th}}$  factor and its coefficient, respectively,  $C$  represents a constant, while  $op_i$  represents the  $i^{\text{th}}$  operator. Although a variety of operators could be considered, only the set  $\{+, -, *\}$  was took into account for our analysis.

The search space of TS is represented by all the possible equations that can be generated assigning the values for  $c_i$ ,  $C$ ,  $op_i$  providing positive *Effort* values. The initial solution is randomly generated. Starting from the current solution, at each iteration the method applies local transformations (i.e., moves), defining a set of neighboring solutions in the search space. Each neighbour of a given solution  $S$  is defined as a solution obtained by a random variation of it. In particular, a move consists of three steps:

1. change each coefficient  $c_i$  of  $S$  with probability  $\frac{1}{2}$ . The new coefficient is calculated as follow:

$$c'_i = f(c_i, r)$$

where  $f \in \{+, -, *, /\}$  and  $r$  is randomly chosen in the range  $[0,1]$ ;

2. change the constant factor  $C$  of  $S$  with probability  $\frac{1}{2}$  in the same way coefficients are changed;
3. change each arithmetic operator  $op_i$  of  $S$  with probability  $\frac{1}{2}$ .

At each iteration the neighbouring solutions are compared to select the best one which will be used in the next iteration to explore a new neighbourhood. Moreover, if the best neighbouring solution is better than the current best solution, the latter is replaced.

The comparison between solutions is performed by exploiting an objective function able to evaluate the accuracy of the estimation model. A number of accuracy measures are usually taken into account to compare effort estimation models. All are based on the residual, i.e. the difference between the predicted and actual effort. Among them we used as objective function the MMRE (Conte *et al.*, 1986), whose definition is reported in the next section. In particular, the goal of TS is to minimize the MMRE value.

To avoid loops and to guide the search far from already visited portions of the search space; the moves recently applied are marked as tabu and stored in a Tabu list. Since only a fixed and fairly limited quantity of information is usually recorded in the Tabu list (Gendreau, 2002), we prohibit the use of a tabu move for ten iterations. In order to allow one to revoke a tabu move, we employed the most commonly used aspiration criterion, namely we permit a tabu move if it results in a solution with an objective function value (i.e., the MMRE value) better than the one of the current best solution.

The search is stopped after a fixed number of iterations or after some number of iterations that do not provide an improvement in the objective function value.

## 3 EMPIRICAL ANALISYS

The goals of our empirical analysis were:

- 1) analyzing the effectiveness of TS in estimating software development effort;
- 2) comparing the accuracy of TS with the one of widely and successfully employed estimation methods.

To evaluate the accuracy of the estimates we employed some widely used summary measures (Conte *et al.*, 1986), namely: the Mean and Median of *Magnitude of Relative Error* (MMRE and MdMRE), and Pred(25). According to (Conte, 1986), a good effort prediction model should have a  $\text{MMRE} \leq 0.25$  and  $\text{Pred}(25) \geq 0.75$ , meaning that at least 75% of the predicted values should fall within 25% of their actual values.

To address the second research goal, we compared TS with Manual Stepwise Regression (MSWR) (Kitchenham and Mendes, 2004) and Case-Based Reasoning (CBR) (Shepperd and Schofield, 2000), that are widely used estimation techniques.

SWR is a statistical technique that allows us to build a prediction model representing the relationship between independent and dependent variables. The estimation model is obtained by adding, at each stage, the independent variable with the highest association to the dependent variable, taking into account all variables currently in the model. SWR aims to find the set of independent variables that best explains the variation in the dependent variable.

To select the variables to be added in the model a Manual SWR (MSWR) can be applied, using the technique proposed by Kitchenham (1998). The idea underlying this procedure is to select the important independent variables, and then to use linear regression to obtain the final model.

CBR is a branch of Artificial Intelligence where knowledge of similar past cases is used to solve new cases. The idea is to predict the effort of a new project by considering similar projects previously developed. We applied CBR by employing ANGEL (Shepperd and Schofield, 2000). ANGEL implements the Euclidean distance as similarity function and uses features normalised between 0 and 1. We used 1, 2, and 3 analogies employing as adaptation strategies the mean of  $k$  analogies (*simple average*), the *inverse distance weighted mean* and the *inverse rank weighted mean* (Shepperd and Schofield, 2000). We used the feature subset selection of ANGEL in order to let the tool to automatically choose, among all the variables, the ones to employ as set of key features in the analogy based estimation.

To have a better visual insight on the effectiveness of the estimation models, we compared the prediction accuracies taking into account both the summary statistics and the boxplots of absolute residuals, where residuals are calculated as (EFreal – EFpred). Boxplots are widely employed in exploratory data analysis since they provide a quick visual representation to summarize the data, using five values: median, upper and lower quartiles, minimum and maximum values, and outliers (Kitchenham *et al.*, 2001). In development effort estimation, boxplots are used to visually represent the amount of the error for a given prediction technique. In particular, we used boxplot to graphically render the spread of the absolute residuals.

In order to verify whether the estimates obtained with TS are characterized by significantly better accuracy than the considered benchmarks we statistically analyzed the absolute residuals, as suggested in (Kitchenham *et al.*, 2001). Since (i) the

absolute residuals for all the analyzed estimation methods were not normally distributed, and (ii) the data was naturally paired, we decided to use the Wilcoxon test (Royston, 1982). The achieved results were intended as statistically significant at  $\alpha = 0.05$ .

We performed the empirical analysis by exploiting two datasets: the Desharnais (Desharnais, 1989) dataset, containing 81 observations, and the NASA (Bailey and Basili, 1981) dataset, with 18 observations. Despite of these datasets are quite old, they have been widely and recently used to evaluate and compare estimation methods (see e.g., (Burgess and Lefley, 2001) (Shepperd and Schofield, 2000)). As for Desharnais dataset, in our analysis we did not consider the length of the code as made in (Burgess and Lefley, 2001), and categorical variables (i.e., Language and YearEnd). We excluded four projects that had missing values, as done by Shepperd and Schofield (2000). The NASA dataset consists of two independent variables, i.e. Developed Lines (DL) of code and Methodology (Me). The descriptive statistics of the selected factors for the two datasets are shown in Tables 1 and 2.

Table 1: Descriptive statistics of Desharnais dataset.

Variable	Min	Max	Mean	Std.Dev.
TeamExp	0.00	4.00	2.30	1.33
ManagerExp	0.00	7.00	2.65	1.52
Entities	7.00	387.00	120.55	86.11
Transactions	9.00	886.00	177.47	146.08
AdjustedFPs	73.00	1127.00	298.01	182.26
RawFPs	62.00	1116.00	282.39	186.36
Envergue	5.00	52.00	27.45	10.53
EFH (m/h)	546.00	23490.00	4903.95	4188.19

Table 2: Descriptive statistics of NASA dataset.

Variable	Min	Max	Mean	Std. Dev.
Me	19.00	35.00	27.78	5.39
DL	2.10	100.80	35.26	35.10
EFH (m/m)	5.00	138.30	49.47	45.73

We exploited some parameter settings to find suitable values for moves and iterations numbers. Concerning the number of moves, we executed TS using four different values, i.e. 100, 500, 1000, and 2000. The best results in terms of MMRE and Pred(25) were achieved with 1000 moves for Desharnais dataset and 100 moves for NASA dataset. We also executed the algorithm with different numbers of iterations, and the best results were achieved using 3000 and 500 iterations on Desharnais and NASA, respectively. We did not consider number of moves greater than 2000 for Desharnais dataset and 100 for NASA dataset since we noted a decreasing in the performance. Moreover, note that for NASA dataset, having a

number of factors and observations less than the Desharnais dataset, the best results were obtained with fewer moves. This aspect should be further investigated in the future using other datasets to verify whether some thresholds could be identified in the choice of moves number. A similar consideration can be made for the number of iterations.

The validation process was performed using a hold-out validation on Desharnais and a 3-fold cross validation for NASA, since it is quite small (Briand and Wieczorek, 2002). In particular, we randomly split the Desharnais dataset into a training set of 59 observations and a test set of 18 observations. NASA dataset was partitioned into 3 randomly test sets of equal size and then for each test set we used the remaining 12 observations as training set.

Table 3 and Table 4 provide the results for the summary measures MMRE, MdMRE, and Pred(25). As we can see the thresholds provided in (Conte, 1986) are not satisfied for TS on Desharnais, since Pred(25) value is less than 0.75 and MMRE and MdMRE values are greater than 0.25. On the other hand, the estimates obtained on NASA provided MMRE and MdMRE values less than 0.25 and a Pred(25) value very close to 0.75.

To have an insight on the results and understand the actual effectiveness of TS on these datasets, it is important to compare TS estimation accuracy with that of widely used techniques, such as MSWR and CBR (reported in Tables 3 and 4). Only the best results obtained for CBR are reported.

Table 3: MMRE, MdMRE, and Pred(25) on Desharnais.

	MMRE	PRED(25)	MdMRE
TS	0.45	0.39	0.43
CBR	0.48	0.55	0.22
MSWR	0.39	0.22	0.38

Table 4: MMRE, MdMRE, and Pred(25) on NASA.

	MMRE	PRED(25)	MdMRE
TS	0.21	0.72	0.19
CBR	0.24	0.56	0.20
MSWR	0.20	0.72	0.19

Table 5: Results of Wilcoxon tests.

	TS vs MSWR	TS vs CBR
Desharnais	p-value = 0.41	p-value = 0.16
NASA	p-value= 0.80	p-value = 0.17

As for Desharnais, we can see that TS provided a better Pred(25) value and slightly worse MMRE and MdMRE values with respect to MSWR. As for CBR, TS achieved a slightly better MMRE value but worse MdMRE and Pred(25) values. Regarding the

NASA dataset, the best results were achieved using MSWR and TS, while the worse results were obtained with CBR. In particular, TS and MSWR provided comparable results.

The analysis of the boxplots in Figures 1 and 2 suggests that TS has a median very close to the median of MSWR and CBR. With regards to Desharnais dataset, even if the boxplot of MSWR is less skewed than those of CBR and TS, it has more outliers. Furthermore, the boxes and the tails of TS and CBR are quite similar. As for NASA dataset, the tails of TS boxplot are less skewed and the outliers of TS are more close to the box. In the other cases, the box length and tails of boxplots are similar. Summarizing, we can deduce that boxplot of TS is slightly better than the boxplots of CBR and MSWR for NASA dataset.

To get a better understanding, we also tested the statistical significance of the results by comparing paired absolute residuals with the Wilcoxon test (see Table 5). We can observe that for both datasets, there is no statistical significant difference between the absolute residuals obtained with TS and CBR and TS and MSWR (the results were intended as statistically significant at  $\alpha = 0.05$ ). Thus, we can conclude that for the performed analysis TS has comparable performances with respect to two widely used estimation techniques.

However, further analysis could be carried out to identify a better setting of the features of the TS algorithm. Indeed, for example other operators could be used for the prediction model, as well as other measures could be exploited as objective function instead or together with MMRE.

It is interesting to compare our results with the one of Burgess and Lefley (2001) that assessed the use of Genetic Programming (GP) for estimating software development effort exploiting on the Desharnais dataset. The settings they used were: an initial population of 1000, 500 generations, 10 executions (i.e., run), and a fitness function designed to minimize MMRE. The proposed GP did not outperform Linear Regression (LR), CBR (with  $k=2$  and  $k=5$  analogies), and Artificial Neural Networks (ANN) in terms of summary measures MMRE and Pred(25). However, no statistical tests were carried out by the authors to verify whether there was significant difference between the results. As for GP, they obtained an MMRE value which is close to the one we obtained with TS, and a Pred(25) value which is worse than the one obtained with TS.

So, our analysis confirms their results on the potentially effectiveness of search-based techniques for effort estimation by suggesting also the

usefulness of TS. Moreover, it confirms the need for further investigations to verify if a better set up of the algorithms could improve the accuracy of the estimations.

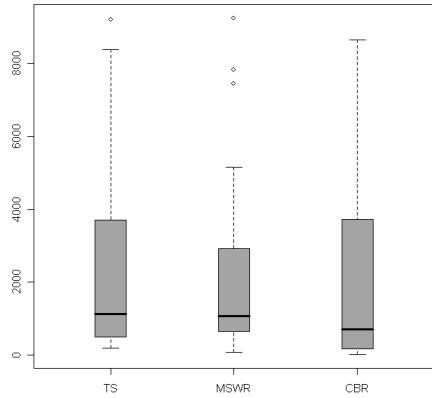


Figure 1: The boxplots of absolute residuals, Desharnais dataset.

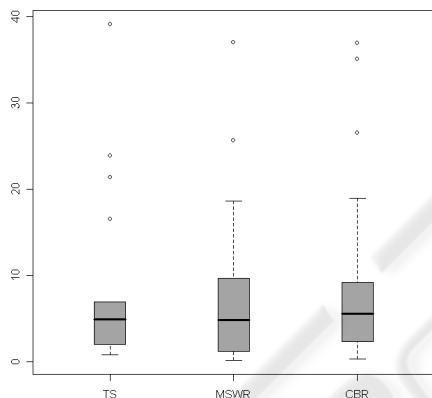


Figure 2: The boxplots of absolute residuals, NASA dataset.

## 4 RELATED WORK

Besides, the work of Burgess and Lefley (2001) whose results have been reported in Section 3, some empirical investigations have been performed to assess the effectiveness of genetic algorithms in estimating software development effort. In particular, Dolado (2000) employed an evolutionary approach in order to automatically derive equations alternative to multiple linear regression. The aim was to compare the linear equations with those obtained automatically. The proposed algorithm was run a minimum of 15 times and each run had an initial population of 25 equations. Even if in each run the number of generation varied, the best results were obtained with three to five generations (as

reported in the literature, usually more generations are used) and by using the Mean Squared Error (MSE) (Conte *et al.*, 1986), as fitness function. As dataset, 46 projects developed by academic students were exploited through a hold-out validation. It is worth noting that the main goal of Dolado work was not the assessment of evolutionary algorithms but the validation of the component-based method for software sizing. However, he observed that the investigated algorithm provided similar or better values than regression equations.

Successively, Lefley and Shepperd (2003) also assessed the effectiveness of an evolutionary approach and compared it with several estimation techniques such as LR, ANN, and CBR. As for genetic algorithm setting, they applied the same choice of Burgess and Lefley (2001), while a different dataset was exploited. This dataset is referred as “Finnish Dataset” and included 407 observations and 90 features, obtained from many organizations. After a data analysis, a training set of 149 observations and a test set of 15 observations were obtained applying a hold-out validation and used in the empirical analysis. Even if the results revealed that there was not a method that provides better estimations than the others, the evolutionary approach performed consistently well.

An evolutionary computation method, named Grammar Guided Genetic Programming (GGGP), was proposed by Shan *et al.* (2002) to fit models, with the aim of improving the estimation of the software development effort. Data of software projects from IBSG database was used to build the estimation models using GGGP and LR. The fitness function was designed to minimize the Mean Squared Error (MSE), an initial population of 1000 was chosen, the maximum number of generations was 200, and the number of executions was 5. The results revealed that GPPP performed better than Linear Regression in terms of MMRE and Pred(25).

## 5 CONCLUSIONS AND FUTURE WORKS

Our analysis has shown that Tabu Search can be effective as other widely used estimation techniques. The study can be seen as a starting point for further investigations to be carried out (possibly with other datasets) by taking into account several different configuration settings of TS. These configurations could be based on:

- several objective functions possibly not em-

ployed in the previous works. Indeed, such a choice could influence the achieved results (Harman, 2007), particularly when the measure used by the algorithm to optimise the estimates is the same used to evaluate the accuracy of them (Burgess and Lefley, 2001). Moreover, we could consider a multi-objective optimisation given by a combination of Pred(25) and MMRE.

■other operators and moves to better explore the solution space.

We will also replicate the study employing data from other companies in order to mitigate possible external validity threats (Briand and Wust, 2001).

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