

IDENTIFICATION OF AREAS WITH SIMILAR WIND PATTERNS USING SOFM

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Abstract: In this paper it is shown a process to demarcate areas with analogous wind conditions. For this purpose a dispersion graph between wind directions will be traced for all stations placed in the studied zone. These distributions will be compared among themselves using the centroids extracted with SOFM algorithm. This information will be used to build a matrix, letting us work with all relations simultaneously. By permutation of elements in this matrix it is possible to group related stations.

1 INTRODUCTION

Clustering is a method of unsupervised learning, and a common technique for statistical data analysis used, the majority of times, in data mining, machine learning, pattern recognition, image analysis, bioinformatics or dimension reduction. However, in many such problems, there is a little prior information (e.g., statistical models) available about the data, and the decision-maker must make as few assumptions about the data as possible. It is under restrictions that clustering method is particularly appropriate for the exploration of interrelationships among the data points to make an assessment (perhaps preliminary) of their structure.

This method is used when to compile and classify by hand is expensive, and the characterization of the patterns change with time. On the other hand, lets to find useful characterization to build classifiers, and the discovery of class and subclass that to reveal the nature of the problem structure.

There are many clustering techniques; the most widely used are hierarchical clustering and dynamic clustering (Xiaozhe, 2006). The first are the called clustering tree and is one of the most widely used clustering approaches due to the great visualization power it offers. Hierarchical clustering produces a nested hierarchy of similar groups of objects, according to a pairwise distance matrix of the objects. One of the advantages of this method is its generality, since the user does not need to provide any parameters such as the number of cluster.

However, its application is limited to only small datasets, due to its quadratic computational complexity. The second is the well knows k -means. While the algorithm is perhaps the most commonly used clustering algorithm in the literature, it does have several shortcomings, including the fact that the number of clusters must be specified in advance. Both of these clustering approaches, however, require that the length of each time series is identical due to the Euclidean distance calculation requirement, and are unable to deal effectively with long time series due to poor scalability. As in supervised classification methods, there is not clustering technique that is universally applicable.

The demarcation of different zones with connected wind patterns could have an important contribution to prediction models based on data acquired in meteorological stations placed in the studied area. When these models are based on the statistical learning of data (Neural Networks, ARMAX, Genetic Fuzzy Learning...), the inclusion of not correlated or erroneous stations can destabilize the process of obtaining the desired knowledge.

In this article, we will use the self-organizing feature map (SOFM) clustering analysis technique to classify zones with similar wind patterns. The main reason of to apply this algorithm is the capability of the learning by example held in SOFM model (Kun-Lin, 2007). One time that this first clustering has been realized, we propose a new method based on Genetic Algorithms for to optimize the final classification of the study zone.

2 AREA AND WIND DATA

In this work the daily mean wind speed and direction of 88 met stations, from 2005 to 2008 have been used. The map of the region and the location of these stations are depicted in Fig. 1. These stations are distributed over 87000 Km² and they are orientated to measure agriculture variables (*Red de Información Agroclimática*). In this way, wind records have not enough reliability because, despite of the most of them are located in open zones, the anemometer height is 1,5 m and is highly affected by obstacles and ground effects. (This fact add value to this study because this kind of meteorological records are more frequent than the good ones, and is interesting to build a structure that allows to use them in order to the wind resource evaluation.)

3 METHOD FOR EXPLORATORY DATA ANALYSIS

There exist several methods for quickly producing and visualizing simple summaries of data sets. A main goal in the field of exploratory data analysis is to extract useful information out of large and usually high-dimensional data sets. In the past, clustering large datasets has been a domain of classical statistical methods. More recently a new approach, Kohonen's Self Organizing Feature Map (SOFM) has been proposed in order to classify high dimensional datasets, while having no analogous traditional method for unsupervised data analysis (Varfis, 1992).

As new approaches from the field of connectionism were presented, those were compared to classical methods and similarities among them were said to be found. In particular the Kohonen algorithm was said to be similar to the k-means method, as it is stated, that the SOFM method is closely related or a partitioning method of the k-means type (Murtagh, 1995). The SOFMs aren't identical to k-means type and in some cases outperform a variety of classical statistical approaches.

3.1 The Self-organizing Map Algorithm

Kohonen's Self-Organizing Feature Maps represent one very well known and widely used Neural Network Model which employs unsupervised

learning. This means that the result is formed by the properties inherent to the data itself; there is no master who tells what is true or false. So no previous knowledge about the structure of the data is needed to be able to use the algorithm.

Self-organizing feature maps (SOFM) learn to classify input vectors according to how they are grouped in the input space. They differ from competitive layers in that neighboring neurons in the self-organizing map learn to recognize neighboring sections of the input space. Thus, self-organizing maps learn both the distribution (as do competitive layers) and topology of the input vectors they are trained on.

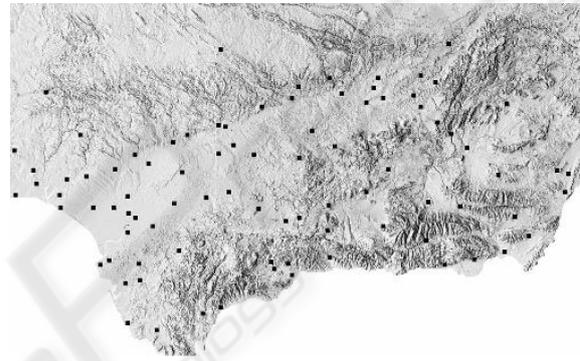


Figure 1: Map showing the location of meteorological stations.

The basic SOM consists of M neurons located on a regular low dimensional grid, usually 1 or 2 dimensional. The lattice of the grid is hexagonal, rectangular or random, see Fig. 2.

The neurons represent the inputs with reference vectors m_i , the components of which correspond to synaptic weights. One reference vector is associated with each neuron called unit in a more abstract setting. The unit, indexed with c , whose reference vector is nearest to the input x is the winner of the competition:

$$c = c(x) = \arg \min_i \{ \|x - m_i\|^2 \} \quad (1)$$

Usually Euclidean metric is used, although other choices are possible as well.

The winning unit and its neighbours adapt to represent the input even better by modifying their reference vectors towards the current input. The amount the units learn will be governed by a neighbourhood kernel h , which is decreasing function of the distance of the units from the winning unit on the map lattice. If the locations of units i and j on the map grid are denoted by the

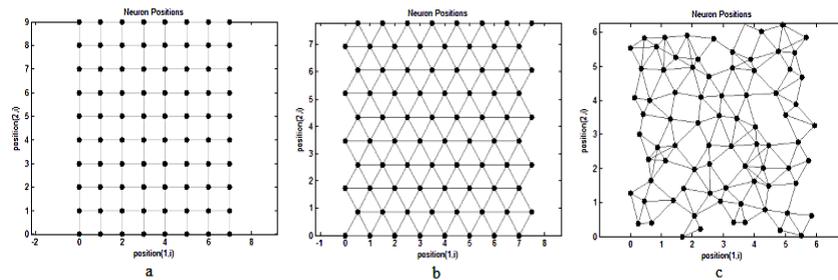


Figure 2: Topologies for the original neuron locations: (a) rectangular lattice, (b) hexagonal lattice, (c) random lattice.

two-dimensional vectors r_i and r_j , respectively, then $h_{ij}(t) = h(\|r_i - r_j\|; t)$, where t denotes time.

During the learning process at time t the reference vectors are changed iteratively according to the following adaptation rule, where $x(t)$ is the input at time t and $c = c(x(t))$ is the index of the winning unit:

$$m_i(t+1) = m_i(t) + h_{ci}(t)[x(t) - m_i(t)] \quad (2)$$

In practice the neighbourhood kernel is chosen to be wide in the beginning of the learning process to guarantee global ordering of the map, and both its width and height decrease slowly during learning.

The learning process, consisting of winner selection by equation 1 and adaptation of the synaptic weights by equation 2, can be modelled with a neural network structure in which the neurons are coupled by inhibitory connections.

The main properties of such self-organizing maps can be stated as (Ritter, 1989):

- The distance relationships between the input data are preserved by their images in the map as faithfully as possible. While some distortion is unavoidable, the mapping preserves the most important neighbourhood relationships between the data items, i.e., the topology of their distribution.
- The map allocates different numbers of nodes to inputs based on their occurrence frequencies. If different input vectors appear with different frequencies, the more frequent one will be mapped to larger domains at the expense of the less frequent ones.

4 PROPOSED PROCEDURE FOR TO CLUSTER STATIONS USING SELF-ORGANIZING FEATURE MAPS (SOFM)

The following procedure has been executed to demarcate areas with similar wind patterns:

4.1 Characterization of Stations

To characterize the measurement stations, wind directions (WD) of all them have been chosen for two random days to yield a vector of dimension 2×88 . Once we have obtained this vector the SOFM algorithm has been carried out. The SOFM module in MATLAB 7.7.0 has been used to be our tool of analysis. The configurations parameters related to the implementation of SOFM by MATLAB 7.7.0 software were as follows: size of layer dimension, [2 5]; network topology, 'hextop'; distance function, 'linkdist'. With these parameters we perform the training of the network to obtain the weights of the network. Figure 3 shows the scatter plot of this vector together with the initial weights of the network and the final weights of the network after training.

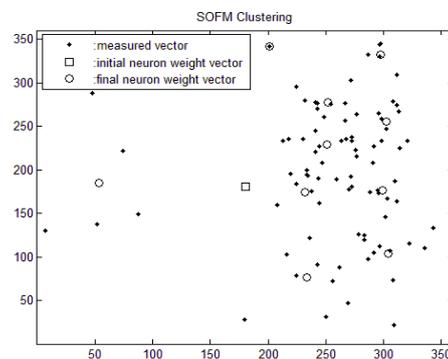


Figure 3: SOFM Training.

Once the network has been trained we come back to choose two random days and is simulated with the obtained network configuration. The following are make a note of what cluster each station belongs. This process is repeated 373 times with what a matrix of size (88x373) is obtained to end. After this matrix is obtained, it is possible to determine how many times two stations have been inserted en the same cluster.

4.2 Matrix of Similarities

Once all stations are characterized by the position of the weights of the network it is possible to establish a parameter which indicates the degree of similarity (DS) between two distributions. We propose (3) the calculation of the mean distance between each neuron, C , and the nearest one belonging to the distribution of the other station, C'_i . Thus, the lower is the value of DS , the higher is the similarity of both distributions.

$$DS_{ij} = \frac{\sum |C_n^i - C_n^j|}{n} \quad (3)$$

Calculating this parameter for all possible pairs of stations, the matrix DS (composed of DS_{ij}) can be constructed. This matrix contains the relations among all the wind patterns measured at the stations, and it can be represented as figure 4 shows, grouped by provinces. The order of grouping of the provinces is *Almería* (Alm), *Cádiz* (Cad), *Córdoba* (Cor), *Granada* (Gra), *Huelva* (Hue), *Jaen* (Jae), *Málaga* (Mal), and *Sevilla* (Sev). The dark pixels are associated to a low value of DS ; therefore, they connect stations with similar patterns. Thus, the white cross observed over *Málaga* (Mal) stations indicates that the most of them have not relations with other stations, even if they are placed in the same province. On the contrary, *Huelva* (Hue) shows strong relations among the stations installed in the area. *Córdoba* (Cor) presents the same pattern in almost all the province, but this pattern is repeated in *Sevilla* (Sev), as it is possible to infer from the dark areas connecting these provinces. This fact indicates that the classification of the stations according to their provinces is not the best in order to visualize the areas with a similar wind patterns.

The actual order of the matrix comes from alphabetical and administrative criteria, but these considerations have not relation with the concerned problem, the wind classification. If the stations were grouped according to the relations among them, by

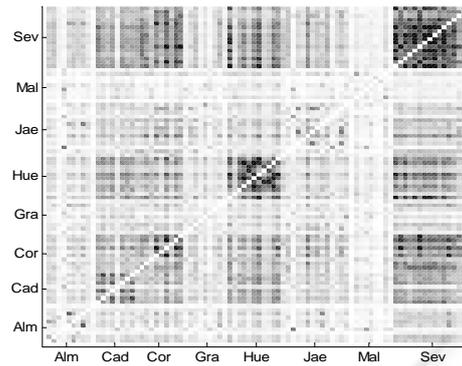


Figure 4: Representation, greyscale, of the matrix composed of the values of DS for each pair of stations.

permutation of rows and columns of the matrix, the relations and clusters could be clarified.

5 GENETIC ALGORITHMS

Genetic algorithms (GAs) have been recognized as powerful approaches to solving optimization problems. They are search algorithms based on natural genetic and selection combining the concept of survival of the fittest with a structured interchanges, but aleatory of the information. These concepts involve the preservation of the characteristics of the best exponents of a generation in the next generation; moreover introducing aleatory changes in the new generation composition by means of crossing over and mutation operations (Lorena, 1997). One of the main advantages of GA in opposite to the traditional search methods is that this aleatory component prevents getting stuck into a local maximum from which you can not escape to reach a global maximum. Other advantage is its utility of real time applications, in spite of not providing the optimal solution to the problem it provides almost the better solution in a shorter time, including complex problems to solve by traditional methods.

5.1 Ordering the Matrix DS with Genetic Algorithms

Although the permutation of rows and columns to put in order the DS matrix seems to be a simple problem; the reality proves that this process could be compared with a Rubik cube, since the order in a part of the matrix could involve the disorder in other one.

The result (or objective) of the recombination of

rows and columns must be a matrix in which the stations with similar winds patterns and relations will be neighbours, that is, the nearby elements of the obtained matrix must be as similar as possible. Figures 5a and 5b present two possible recombination of the matrix represented in figure 4, being the second one closer to the objective explained before. To evaluate this idea of order, the parameter p is proposed in equation 4, where p_0 , a and b are constants related to the scale of the problem. In this case $p_0 = 25000$, $a = 100$ and $b = 415$.

$$p = \frac{1}{p_0} \cdot \sum_{j=1}^{88} \sum_{k=-3}^{k=3} \sum_{i=1}^{88} F_{ij} \cdot (A_{ijk} + B_{ijk}) \quad (4)$$

$$F_{ij} = 1 - \frac{|i - j|}{88}$$

$$A_{ijk} = \frac{a}{a + (DS_{ij} + DS_{i(j+k)})}$$

$$B_{ijk} = \frac{|DS_{ij} - DS_{i(j+k)}|}{b}$$

Each column, j , which represents a station, is compared with the six closer columns indexed by $j+k=j-3, \dots, j, \dots, j+3$, calculating two factors with their i -th elements, A_{ijk} and B_{ijk} . The resulting value of $A_{ijk} + B_{ijk}$ is low when the sum of the elements is high and the difference low. That is, nearby stations with high similarities among them and with analogous relations with the rest of the stations will contribute with low values to the final result of p . The sum of all these values, covering all the columns, gives an objective measurement of the similarities among the nearby columns and, therefore, an evaluation of the global order of the matrix. For example the value of p for the matrix shown in figure 4 is 0.902. As it was expected, figures 5a and 5b obtain lower values because they have been ordered in some sense. Especially the combination represented in 5b presents a very low value of p ($p=0.843$) which indicates a high degree of similarity (or order).

Now the problem of ordering the matrix of similarities has been reduced to find a combination of stations with a minimum value of p . We propose to solve this minimization problem using Genetic Algorithms (GA). Each matrix of similarities can be characterized by a vector of 88 elements containing the position of the stations. This vector could be considered as a genome which defines univocally the associated matrix. Furthermore, using the value of p calculated with these matrixes, a population of

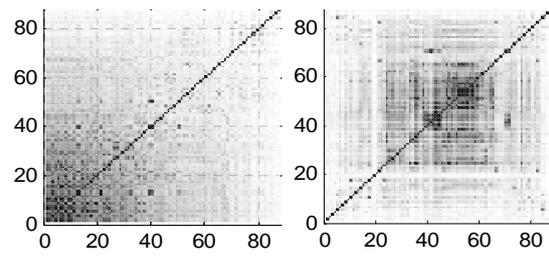


Figure 5: a) Ordination of stations from sparsely related to highly related ($p=0.854$). 5b) Ordination according to subjective criteria of permutation ($p=0.843$).

these vectors could be tested and ranked. In these conditions, GA could improve this population using evolutive operators as crossover, mutation, migration, etc., in order to obtain the minimum value of p (Goldberg, 1989).

As it has been introduced upper, the vectors used as genome of the matrixes contain 88 elements. These elements are non repeated integer numbers between 1 and 88, and each of them is associated to one of the used stations. The positions of this numbers in the vector define the position of the stations in the matrix and, thus, the value of p for this combination can be calculated. Because of the properties of the genome used in this work, the evolutive operator selected to produce the new generations is the Recombination. Recombination permutes one or more elements of the genome, thus, the resulting vector is composed of 88 non repeated integers again; avoiding the repetitions, decimals and values out of range given by other operators.

6 RESULTS

The matrix selected by the GA as best combination of stations, after 1000 generations and a population of 10^5 individuals is represented in figure 6. This

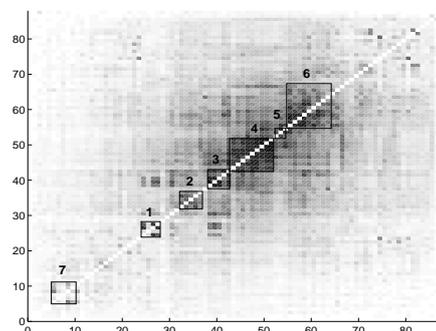


Figure 6: Representation, greyscale, of the matrix obtained after applying the Genetic Algorithm where the main clusters have been selected with numbered squares.

figure depicted the main clusters with squares and the value of p associated to this matrix is 0.805.

Once we have selected the clusters are represented in the study area. This is shown in figure 7 where it follows the same colour code. Tables 1 and 2 shows the information of the stations that have been selected as cluster belongs.

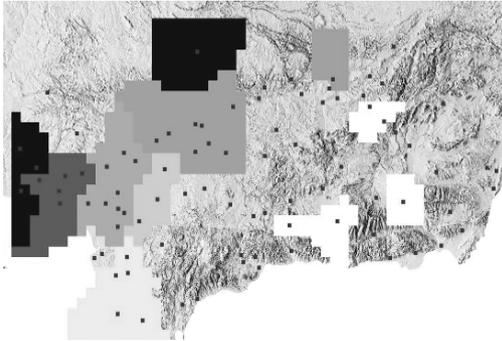


Figure 7: Representation of study zone and the clusters selected.

Table 1: Names selected stations in the clusters 1, 2, 3 and 4.

Cluster 1 ■	Cluster 2 ■	Cluster 3 ■	Cluster 4 ■
- Puebla Guzmán - Bélmez - Gibraleón - Lepe	- Conil - Jerez - Puerto Santa Mª - Vejer - Basurta	- Moguer - Cebollar - Tojalillo - Niebla - Palma del Condado	- Sanlúcar la Mayor - Guillena - Almonte - Rinconada - Aznalcázar - Puebla del Río - Lebrija - Puebla del Río II - Isla Mayor

Table 2: Names selected stations in the clusters 5, 6 and 7.

Cluster 5 ■	Cluster 6 ■	Cluster 7 ■
- Tomejil - Los Molares - Las Cabezas de San Juan	- La Luisiana - Palma del Río - Écija - Hornachuelos - Lora del Río - Santaella - Córdoba - Villanueva - Linares	- Huesa - Padul - Zafarraya - Fiñana - San José de los Propios

7 CONCLUSIONS

The results obtained demonstrate that the proposed method is able to demarcate areas with analogous wind patterns, even if the data acquired is affected by low quality instruments or locations. In the same way, erroneous stations, or stations not representative of the wind climate in their zone, will be identified since they will not be included in any cluster. So, this tool could be useful in two aspects:

- In first steps of wind resource assessment, when a preliminary description of the wind climate in a zone is needed. Then, using the information given by this matrix, it is possible to associate the location of the target area with an expected wind pattern.
- When a wind methodology, as Measure-Correlate-Predict or the ones used in wind temporal forecasting, needs support stations to complete or extend the database used. In this situation is very important to exclude stations with errors or not representative of the studied area because it could lead to important differences between results and reality.

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