

# TEXTURE REPRESENTATION AND RETRIEVAL BASED ON MULTIPLE STRATEGIES

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**Abstract:** We propose an approach based on the fusion of multiple search strategies to content-based texture retrieval. Given the complexity of images and users' needs, there is no model or system which is the best than all the others in all cases and situations. Therefore, the basic idea of multiple search strategies is to use several models, several representations, several search strategies, several queries, etc. and then fuse (merge) the results returned by each model, representation, strategy or query in a unique list by using appropriate fusion models. Doing so, search effectiveness (relevance) should be improved without necessarily altering, in an important way, search efficiency. We consider the case of homogeneous textures. Texture is represented by three (3) models/viewpoints. We consider also the special case of invariance and use both multiple representations and multiple queries to address this difficult problem. Benchmarking carried out on two (2) image databases show that retrieval relevance (effectiveness) is improved in a very appreciable way with the fused model.

## 1 INTRODUCTION

Content-based image retrieval (CBIR) from image databases has become a very active research areas in the last years and many approaches have been proposed and various results and systems have been carried out since then (Datta et al., 2008). In visual CBIR, content representation and similarity matching are fundamental issues. Content representation can be seen as a model which captures as much as possible the relevant visual information contained in images. Similarity can be defined as a mapping function between the set or vector of parameters representing the content of images and a positive real value chosen to quantify the degree of visual resemblance between the compared images. More recently, researchers have paid more attention to other approaches including, in particular, relevance feedback-based image retrieval (Zhou and Huang, 2003) which allows integration of user judgments of relevance in the retrieval loop, and semantics-based image retrieval ((Lu et al., 2000), (Sun and Ozawa, 2003)) which is a tentative to use semantic features through learning and users' annotations on images. These approaches allow generally a noticeable improvement in search relevance even if they can be criticized at least on the fact that an important effort is asked to users to give relevance judgments or to perform annotations on images.

One approach, which still a pure visual CBIR, has not received enough attention. This approach is data fusion (Belkin et al., 1993), (Lee, 1997), (Wu and Crestani, 2002). Results fusion is a subpart of data fusion. In CBIR, among the rare works dealing explicitly with data fusion, we cite (Berretti, 2004), (French et al., 2003). In (Berretti, 2004), a data fusion model working on distributed collections of images is proposed based on a normalization procedure of similarities among the various image collections. In (French et al., 2003), a results fusion model working on a centralized image collection is proposed based on multiple representations, called viewpoints or channels, of both the query and the images in the database. They used four channels: the original color images, their corresponding grey-level images and their negatives. Results merging coming from different channels is shown to improve performance in a very important way. Note that results fusion differs from a feature integration/combination approach since in the former approach we use multiple representations for the same feature while in the latter approach we use multiple features but with one representation for each feature.

The work presented in this paper explores the idea of results fusion and applies it in the case of textures retrieval. Texture content is represented by two different models: the autoregressive model and a perceptual model based on a set of perceptual features such

as coarseness and contrast. The perceptual model is considered in two viewpoints: the original image's viewpoint and the autocovariance function viewpoint. Computational measures are based on these two viewpoints. So we have a total of three models/viewpoints (called representations). We consider also the special case of invariance, we introduce multiple queries, along with multiple representations, to address this problem. Benchmarking presented at the end of the paper shows how a multiple representations, multiple queries and results fusion can improve in very interesting way the search effectiveness (relevance) without, necessarily, altering, in an important way, search efficiency.

The rest of this paper is organized as follows: In section 2, we present the multiple representation models considered in this paper and we discuss briefly their capacity to model textures; We also show the benefits from using multiple representations and present the results fusion models used to fuse results returned by different representations; In section 3, we consider the special problem of invariance and we introduce multiple queries along with multiple representations to address this difficult problem; In section 4, benchmarking over 2 image databases using the recall graph is presented and discussed; And finally, in section 5, a conclusion is given and further investigations related to this work are briefly discussed.

## 2 MULTIPLE REPRESENTATIONS AND RESULTS FUSION

### 2.1 Multiple Representations

To represent content of textures, we use two different models, the autoregressive model and a perceptual model based on a set of perceptual features (Abbadeni et al., 2000). The autoregressive used is a causal simultaneous AR model with a non-symmetric half-plan (NSHP) neighborhood with four neighbors. The perceptual model is considered with two viewpoints: the original image's viewpoint and the autocovariance function (associated with original images) viewpoint. Each of the viewpoints of the perceptual model used is based on four perceptual features, namely coarseness, directionality, contrast and busyness. So we have a total of three content representations, each having a vector of parameters of size four for a total of twelve parameters.

The set of features of the perceptual model have a perceptual meaning by construction. The set of

features derived from the autoregressive model have no perceptual meaning by construction. A perceptual interpretation of the set of features derived from the autoregressive model was proposed by (Abbadeni, 2005a). This perceptual interpretation consists in considering those features as a measure of the randomness/regularity of the texture.

#### 2.1.1 The Autoregressive Model

The autoregressive model is characterized, in particular, by a forecasting property that allows to predict the grey-level value of a pixel of interest in an image by using the grey-level values of pixels in its neighborhood. The autoregressive model, when used to model a textured image, allow to estimate a set of parameters (their number corresponds to the number of neighbors considered), each one corresponds to the contribution of its corresponding pixel in the forecasting of the pixel of interest (the total of contributions of all pixels in an image is close to 100%).

The simultaneous (2D) autoregressive model (SAR) model is defined as follows:

$$(X_s - \mu) = a_s W_s + \sum_{r \in \Omega^+} a_r (X_{s+r} - \mu) \quad (1)$$

where  $s$  corresponds to position  $(i, j)$  on rows and columns,  $X_s$  is the grey-level at position  $s$ ,  $\Omega^+$  is the neighborhood on rows and columns of  $X_s$  (excluding  $X_s$  itself),  $\Omega = \Omega^+ \cup \{s\}$ ,  $\mu$  is the local grey-level average in the neighborhood  $\Omega$  and  $[a_s, a_r, r \in \Omega^+]$  are the parameters of the model to be estimated.  $W_s$  is a Gaussian white noise, a stationary signal made of non-correlated random variables, defined as follows:

$$\begin{cases} E[W_s] = 0 \\ E[W_s W_{s+r}] = \begin{cases} 1 & \text{if } r = (0,0) \\ 0 & \text{otherwise} \end{cases} \\ E[W_s X_{s+r}] = \begin{cases} a_s & \text{if } r = (0,0) \\ 0 & \text{otherwise} \end{cases} \end{cases} \quad (2)$$

Neighborhood  $\Omega$  can be defined in different ways. We use causal neighborhoods. The causality constraint implies that pixels are ordered in a sequential way (from top to bottom and from left to right). There are two causal neighborhoods: quarter-plan (QP) neighborhood and non-symmetric half-plan (NSHP) neighborhood.

One of the popular methods that can be used to estimate the set of parameters  $[a_s, a_r, r \in \Omega^+]$  is the well-known least squares error (LSE) method. Estimation error  $E_s$  (corresponding to  $W_s$  in equation(1)) of  $X_s$  is given by:

$$E_s = \frac{1}{a_s} \sum_{r \in \Omega} b_r (X_{s+r} - \mu) \quad (3)$$

where  $b_0 = 1$  and  $b_r = -a_r \forall r \neq 0$ .

The quadratic error in all the image is given by:

$$E = \sum_{s \in I} \left( \frac{1}{a_s} \sum_{r \in \Omega} b_r (X_{s+r} - \mu) \right)^2 \quad (4)$$

where coefficients  $[a_s, b_r, r \in \Omega^+]$  are estimated so that  $E$  is minimal, this implies:

$$\frac{\partial E}{\partial b_r} = 0 \quad (5)$$

$$\frac{\partial E}{\partial a_s} = 0 \quad (6)$$

By developing equations (5) and (6), we obtain the following equations (Frankot and Chellappa, 1997), (Kashyap and Chellappa, 1983):

$$\left( \sum_s Z(s) Z^T(s) \right) A = \sum_s Z(s) (X_s - \mu) \quad (7)$$

$$a_s^2 = \frac{1}{N^2} \sum_s ((X_s - \mu) - A^T Z(s))^2 \quad (8)$$

where  $Z(s)$  is equivalent to  $[X(s+r) - \mu, r \in \Omega^+]$  and  $A$  is the vector of parameters  $[b_r, r \in \Omega^+]$ .

Note that in equation (7),  $Z(s) Z^T(s)$  corresponds to the covariances matrix computed in the considered neighborhood. This means that parameters  $[a_r, r \in \Omega^+]$  are estimated based on the covariances matrix. The system of equations represented by (7) is a linear one. Resolving this system allows to obtain parameters  $[a_r, r \in \Omega^+]$ . The  $LU$  decomposition method was used to resolve this system. Resolving equation (8) allows to obtain the noise parameter  $a_s$ .

### 2.1.2 The Perceptual Model

The perceptual model, which is perceptual by construction, is based on a set of three computational measures that simulate three perceptual features: coarseness, contrast, and directionality. Coarseness was estimated as an average of the number of extrema; Contrast was estimated as a combination of the average amplitude of the gradient, the percentage of pixels having the amplitude superior to a certain threshold and coarseness itself; Directionality was estimated as the average number of pixels having the dominant orientation(s).

**Coarseness.** Coarseness, denoted  $C_s$ , is estimated as the average number of maxima in the autocovariance function. In fact, a coarse texture will have a small number of maxima and a fine texture will have

a large number of maxima. The estimation equation of coarseness is as follows:

$$C_s = \frac{1}{\frac{1}{2} \times \left( \frac{\sum_{i=0}^{n-1} \sum_{j=0}^{m-1} \text{Max}(i,j)}{n} + \frac{\sum_{j=0}^{m-1} \sum_{i=0}^{n-1} \text{Max}(i,j)}{m} \right)} \quad (9)$$

where  $\text{Max}(i, j) = 1$  if pixel  $(i, j)$  is a maximum (a maximum line or column) and  $\text{Max}(i, j) = 0$  if pixel  $(i, j)$  is not a maximum.

**Contrast.** Contrast, denoted  $C_t$ , was estimated using the following equation :

$$C_t = \frac{M_a \times N_t \times C_s^{\frac{1}{\alpha}}}{n \times m} \quad (10)$$

where  $M_a$  represents the average amplitude,  $\frac{N_t}{n \times m}$  represents percentage of pixels having an amplitude superior than threshold  $t$ , and  $C_s$  is the computational measure of coarseness ( $\frac{1}{\alpha}$  is a parameter used to make  $C_s$  significant against the quantity  $\frac{M_a \times N_t}{n \times m}$ ). Note also the presence of coarseness in the estimation of contrast since coarseness plays an important role to determine if an image is well contrasted or not. In fact, an image with a high degree of coarseness tends to be perceived as being more contrasted than an image with a fine coarseness.

**Directionality.** The degree of directionality is related to the visibility of the dominant orientation(s) in an image. Directionality was estimated as the number of pixels  $N_{\Theta_d}$  having dominant orientation(s)  $\Theta_d$ . Let  $\Theta_d(i, j) = 1$  if pixel  $(i, j)$  has a dominant orientation  $\Theta_d$  and  $\Theta_d(i, j) = 0$  if pixel  $(i, j)$  does not have a dominant orientation  $\Theta_d$ . The degree of directionality  $N_{\Theta_d}$  of an image can be expressed by the following equation:

$$N_{\Theta_d} = \frac{\sum_{i=0}^{n-1} \sum_{j=0}^{m-1} \Theta_d(i, j)}{(n \times m) - N_{\Theta_{nd}}} \quad (11)$$

where  $N_{\Theta_{nd}}$  denotes the number of non-oriented pixels. The more  $N_{\Theta_d}$  is large, the more the image is directional. The more  $N_{\Theta_{nd}}$  is small, the more the image is non-directional.

The computational measures proposed for each perceptual textural feature were evaluated by conducting a set of experimentations taking into account human judgments and using a psychometric method. The Spearman coefficient of rank-correlation was used to evaluate the correlation between human judgements and computational rankings. Experimental results show very strong correspondence between the proposed computational measures and human rankings. Values of Spearman coefficient of rank-correlation  $r_s$  found are as follows: for coarseness,  $r_s = 0.913$ ; for directionality,  $r_s = 0.841$ ; and

for contrast,  $r_s = 0.755$ . Compared to related works ((Amadasun and King, 1989) and (Tamura et al., 1978)), these perceptual features have more stronger correlation with human judgements.

## 2.2 Similarity Matching

The similarity measure used is based on the Gower coefficient of similarity denoted  $GS$  (Gower, 1971), (Abbadeni, 2005b), (Abbadeni, 2003). The non-weighted similarity measure can be defined as follows:

$$GS_{ij} = \frac{\sum_{k=1}^n S_{ij}^{(k)}}{\sum_{k=1}^n \delta_{ij}^{(k)}} \quad (12)$$

Where  $S_{ij}^{(k)}$  is the partial similarity between images  $i$  and  $j$  according to feature  $k$ ,  $\delta_{ij}^{(k)}$  represents the ability to compare two images  $i$  and  $j$  on feature  $k$  ( $\delta_{ij}^{(k)} = 1$  if images  $i$  and  $j$  can be compared on feature  $k$  and  $\delta_{ij}^{(k)} = 0$  if not.  $\sum_{k=1}^n \delta_{ij}^{(k)} = n$  if images  $i$  and  $j$  can be compared on all features  $k, k = 1..n$ ).

Quantity  $S_{ij}^{(k)}$  is defined as follows:

$$S_{ij}^{(k)} = 1 - \frac{|x_{ik} - x_{jk}|}{R_k} \quad (13)$$

Where  $R_k$  represents a normalization factor.  $R_k$  is computed on the database considered for experiments and is defined as follows:

$$R_k = \text{Max}(x_{ik}) - \text{Min}(x_{ik}) \quad (14)$$

The weighed version of the similarity measure can be defined as follows:

$$GS_{ij} = \frac{\sum_{k=1}^n w_k S_{ij}^{(k)}}{\sum_{k=1}^n w_k \delta_{ij}^{(k)}} \quad (15)$$

Where  $w_k$  corresponds to the weight associated with feature  $k$ . As mentioned,  $w_k$  can be either the inverse of variance of feature  $k$  or the Spearman coefficient of rank-correlation.

For more details and motivations behind the use of Gower coefficient of similarity as a similarity matching measure, we refer the reader to (Abbadeni, 2003).

## 2.3 Fusion of Results Returned by Multiple Representations

It has been reported in the literature on the subject of data fusion, in the IR field, that different representations of the same query or the images in the

database, or different search strategies for the same query, etc. return different search results. Results fusion is then the merging of the different results lists returned by the different models, representations or queries to form a unique fused (merged) list which is, hopefully, more effective (relevant) than the separated lists (Belkin et al., 1993), (Lee, 1997). Given several list results returned by different representations, there are three important phenomena that can be observed (Vogt and Cottrell, 1999), (Lee, 1997). Generally, results fusion models found in literature exploit one or several effects from these three important effects:

- Skimming effect: Each model retrieve a subset of the relevant images and intersection between them is rather low. A relevant image is retrieved, often, by only one model. In this case, results fusion must consider images that are ranked in top positions in different lists.
- Chorus effect: Different models retrieve approximately the same results but with different ranks and similarity values. In this case, a relevant image is ranked by several models in top positions (not necessarily the same position). The fact that several models retrieve an image is a more convincing evidence or proof that this image is relevant to the query compared to the case where this image is retrieved by only one representation. Results fusion, in this case, must take in consideration all the representations used.
- Dark horse effect: Exceptionally, even a good model can return some irrelevant images for a given query. Generally, different models did not return the same irrelevant images. Results fusion, in this case, must consider all the representations and use appropriate techniques to eliminate irrelevant images.

We have used and experimented three basic results fusion models that are denoted **FusMAX** (or **MAX**), **FusCL** (or **CL**) and **FusComb** (or **Comb**) defined respectively as follows:

$$FusMAX_{ij} = \text{MAX}(GS_{M_{ij}^k}) \quad (16)$$

$$FusCL_{ij} = \frac{\sum_{k=1}^K GS_{M_{ij}^k}}{K} \quad (17)$$

$$FusComb_{ij} = \prod_{k=1}^K GS_{M_{ij}^k} \quad (18)$$

where  $GS$  represents the Gower-based similarity score returned for each image,  $M^k$  represents model/viewpoint  $k$ ,  $K$  represents the number of models/viewpoints used,  $i$  represents a given query,  $j$  represents images that are found similar to query  $i$

according to model  $M^k$  and  $GS_{M_{ij}^k}$  is the similarity value between query  $i$  and image  $j$  when using model/viewpoint  $M^k$ . These fusion models use only the values of the similarity function returned by the considered model/viewpoint. Ranks can be also used. We have used them as weights. In fact, more an image is ranked at top positions, more is its weight in the fusion models. Thus, we can define a weighted version for each of the **FusCL**, **FusMAX** and **FusComb** models. In such weighted models, each image  $j$  is weighted with its rank in the list of results returned for query  $i$  using model  $M^k$ .

Fusion models **FusCL** and **FusComb**, both non-weighted and weighted, exploit the chorus effect since these models give more importance to images that are retrieved and ranked in top positions by different models/viewpoints. They also exploit the dark horse effect since an irrelevant image that is ranked in top positions by one model/viewpoint is not ranked at top positions in the fused list given that this irrelevant image is not ranked at top positions by the other models/viewpoints.

The **FusMAX** model exploits the skimming effect, to some extent, since this model takes images that are classified in top positions in different results lists but it re-ranks them according to similarity values.

Generally, when the chorus effect exists in an important way between different lists, the gain that we can obtain by exploiting the skimming effect becomes low and *vice-versa* (Vogt and Cottrell, 1999).

### 3 MULTIPLE QUERIES FOR THE CASE OF INVARIANCE

#### 3.1 Multiple Queries

Invariant image retrieval is the ability to retrieve all relevant images to a query even if some of them have been transformed according to different geometric and photometric transformations such as rotation, scaling, illumination, viewpoint change and contrast change as well as non-rigid transformations (Zhang and Tan, 2002), (Lazebnik et al., 2004), (Abbadeni and Alhichri, 2008).

We propose to use both multiple representations and multiple queries to address this difficult problem. We use multiple models/viewpoints to represent the textural content of images. We used the same models as the general case (autoregressive model, perceptual model with two viewpoints). These models are not necessarily invariant with respect to geometric and

photometric transformations. At the query level, we use multiple queries to represent a user's need. We use appropriate results fusion models to merge results returned by each model/viewpoint and then by each query. Therefore, results fusion, in the case of invariance, is performed in two successive levels: The first level consists in merging results returned by different representations for the same query (similar to the general retrieval case); 2. The second level consists in merging results returned by multiple queries.

Results fusion returned for different queries allows to consider the fact that relevant images to a given query image can be located in disjoint regions in the space of features (French et al., 2003). The use of only one query image, especially in the case of invariance, will not retrieve, certainly, all the relevant images depending on the degree of variance in the considered database. With this approach, there is computation overhead since we use several queries for the same user's need. However, the size of the vector of parameters does not change for images in the database. Only a user's need is represented with several queries, and thus with several vector of parameters. Thus, efficiency is not altered in an important way.

##### 3.1.1 Multiple Queries Fusion

We can use the same fusion models as in the case of multiple representations fusion. However, those models did not give good results in experimental results since the chorus and dark horse effects are not very significant in the case of invariance. In fact, when using multiple queries, each with a different orientation, scale, or contrast for example, the results returned for each query contain, actually, a small number of common images since the content representation models are not invariant. Models that can be used, in this case, are those who are able to take, from each results list (for each query), the best results. This effect is known as the skimming effect in the information retrieval community (Vogt and Cottrell, 1999). The **MAX** model defined previously exploits to some extent the skimming effect as we explained previously; therefore it can be used in the case of invariance.

Another fusion model, exploiting also the skimming effect, is a model known as the round robin (**RR**) model in the literature (Belkin et al., 1993), (Berretti, 2004). The **RR** technique makes use of the rank of an image in the returned results list rather than the value of the similarity function. The **RR** technique consists simply in taking images that are ranked in the first position in each list (corresponding to each query) and give them all the same first position in the fused list, then taking images that

are ranked in the second position in each list (corresponding to each query) and give them all the same second position in the fused list and so on. We can stop this process after a threshold of the similarity value and/or the rank or after having retrieved a certain number of images. Obviously, if we find the same image in different lists, which may occur occasionally, only one image is considered. Note that the **RR** technique exploits the skimming effect in a more effective way than the **MAX** model does.

## 4 EXPERIMENTAL RESULTS AND BENCHMARKING

### 4.1 The General Case

#### 4.1.1 Experimental Results

We have conducted a large experimentation on Brodatz database (Brodatz, 1966). Figure 1 gives a sample of images from Brodatz database. This database contains 1008 128x128 images (112 classes; 9 images per class).



Figure 1: Sample of images from Brodatz database.

Experimental results show that: 1. The autoregressive model in its non-weighted NSHP version perform better than the other versions of the autoregressive model, 2. The weighted version, using Spearman coefficients of rank-correlation, of the perceptual model based on original images performs better than the other versions of this model; 3. And, finally, the weighted version, using the inverse of variances, of the perceptual model based on the autocovariance function performs better than the other versions of this model. For results merging, the **FusCL**

model gives the best results compared to the **FusMAX** model and gives similar results compared to **FusComb** model. So, in the following, we will show results for only these best models.

#### 4.1.2 Evaluation

Recall is a common standard to benchmark search relevance in information retrieval systems in general. Recall, which can be defined as the number of relevant and retrieved images divided by the number of relevant images,

measures the ability of a model to retrieve all relevant images.

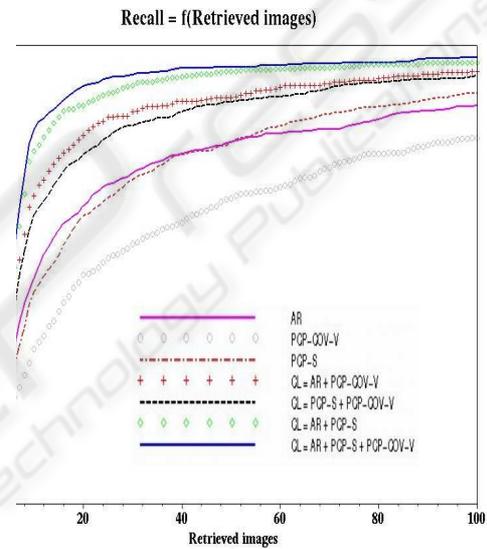


Figure 2: Recall graph: Recall = f(Retrieved images).

Figure 2 shows the recall graph. From this figure, we can point out that the overall performance of the different models is as follows (in a decreasing order): **CL**, **AR + PCP-S**, **AR + PC-COV-V**, **PCP-S + PCP-COV-V**, **AR**, **PCP-S** and **PCP-COV-V**. The fused model **CL** (using all of the three basic representations) gives the best results. The fusion two by two also gives better results than the separated models. The perceptual model using the original image's viewpoint (**PCP-S**) performs better than the perceptual model using the autocovariance function viewpoint (**PCP-COV-V**), but when these two viewpoints are fused, the resulting model (**PCP-S + PCP-COV-V**) performs better than each of them taken separately. The autoregressive model (**AR**) performs better than the perceptual model (**PCP-COV-V**) based on the autocovariance function viewpoint and have a quite similar performance compared to the perceptual model based on the original image's viewpoints (**PCP-S**).

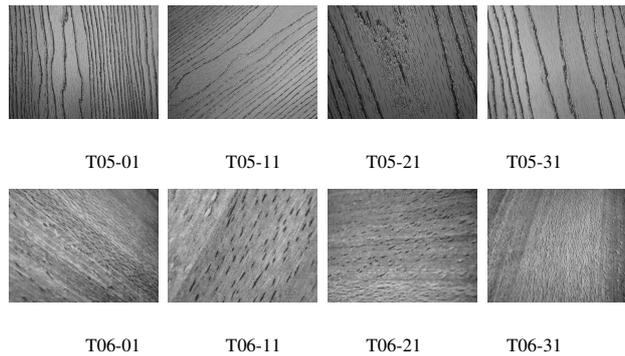


Figure 3: Sample of images from the Ponce's group texture database.

When comparing retrieval performance in terms of recall rate with other works, we can point out the following remarks (see table 1):

- If we consider only 83 classes, our fused model performs better than most of the known works including pure CBIR approaches such as Gabor filters (Manjunath and Ma, 1996), MRSAR (Manjunath and Ma, 1996), (Liu and Picard, 1996) and Wold model (Liu and Picard, 1996), and relevance feedback-based approaches such as MARS (Rui et al., 1997) and RBF-based retrieval (Muneesawang and Guan, 2004). Note that for table 1, we give the retrieval rate at the position that corresponds to the number of relevant images for each class. Note that in our approach no relevance feedback from users is used.

- If we consider all of the 112 classes, including highly non-homogeneous images, our model performs better than some and less than some other models. We must mention again that considering the 29 highly non-homogeneous classes may lead to incorrect conclusions since these classes contain images that are not visually similar.

Table 1: Average recall rate for different models. We showed the recall rates given by authors of the corresponding model.

Model	Recall rate
FusCL (112 classes)	.687
FusCL (83 classes)	.819
MRSAR	.74
Gabor	.74
WOLD	.75
RBF	.737
MARS	.671

## 4.2 The Case of Invariance

### 4.2.1 Experimental Results

For experimental results and benchmarking, we have used an image database coming from Ponce's group at UIUC<sup>1</sup>. A sample from this database is given in figure 3. We considered 22 classes; each class contains 640x480 40 images per class for a total of 880 images. Within each class there is a high degree of variance between images in orientation, scale, contrast as well as non-rigid deformations. In experimental results, the **AR**, with an NSHP neighborhood, weighted with the inverse of each feature's variance gave the best results among the different versions of the **AR** models. Both the **PCP** and the **PCP-COV** models in their weighted version using the Spearman coefficient of rank-correlation gave the best results among the different versions of the perceptual model.

### 4.2.2 Evaluation

Benchmarking we have done, based on the recall measure, concerns both the use of one query as well as the use of multiple queries:

- When considering one query, we have considered the best version of each separated model/viewpoint. Then we have fused these multiple models/viewpoints, using the **CL** results fusion model, for the same query.
- When considering multiple queries, based on the fused models/viewpoints for each query, we have fused the results of 4 queries using the **MAX** model and the **RR** model as described earlier in this paper. Query images were selected randomly and correspond to images 1, 11, 21 and 31 from each class.

<sup>1</sup>[http://www-cvr.ai.uiuc.edu/ponce\\_grp/data/texture\\_database](http://www-cvr.ai.uiuc.edu/ponce_grp/data/texture_database)

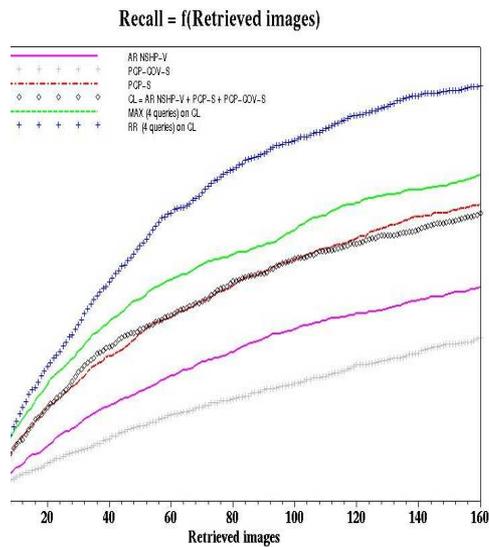


Figure 4: Average recall graph for different separated models (1 query) and fused model (4 queries).

Table 2: Average recall rate at positions 40, 80, 120, and 160 according to different separated and fused models.

Model	P40	P80	P120	P160
AR NSHP-V	.219	.34	.426	.485
PCP-S	.331	.489	.593	.67
pcp-COV-S	.145	.234	.31	.37
MAX (4 Queries)	.408	.557	.674	.735
RR (4 Queries)	.495	.747	.867	.932

Fig. 4 shows the average recall graph for different models, both separated and fused, by considering one query and multiple queries. This figure shows that the PCP model weighted with Spearman coefficients performs better than the other separated models. Fusing different models/viewpoints for the same query does not achieve an important improvement in performance since two of the three models/viewpoints consider, namely the **AR NSHP-V** and the **PCP-COV** model, have rather poor performance in the case of invariance as explained earlier in this paper.

Fusing multiple queries using both the **MAX** and **RR** models allow improvement in performance. While the **MAX** model allows an average improvement in performance, the **RR** model allows a significant improvement in performance measured in terms of recall. Remember that both the **MAX** and the **RR** models exploit the skimming effect while the **CL** model exploits both the chorus and dark horse effects. Thus, in the case of invariance, the skimming effect, is more important than both the chorus and dark horse effects.

These conclusions can be also drawn by examining table 2, which gives the average retrieval rate at positions 40, 80, 120 and 160 across all the database according to a selection of separated and fused models.

## 5 CONCLUSIONS

We presented in this paper a data fusion approach to content-based image retrieval in which results returned by multiple models/viewpoints and multiple queries are fused. This approach was employed in both the general image retrieval case and in the special case of invariant image retrieval. We have considered the case of textures. Texture content are represented by two different content representation models: the autoregressive model and a perceptual model based on a set of perceptual features such as coarseness, directionality, etc. Two viewpoints of this perceptual model were considered: the original images and the autocovariance function.

In the case of invariance, since these models/viewpoints used were not invariant with respect to geometric and photometric transformations, we used also multiple queries. Thus we used multiple representations and multiple queries in the case of invariance.

Experimental results and benchmarking showed the following results: 1. In the general case of image retrieval, the fusion of multiple representations allowed a very significant improvement in retrieval relevance compared to single representations. Fusion models able to exploit the chorus effect and the dark horse effect are more appropriate in the general case of image retrieval. 2. In the case of invariance, fusing multiple representations achieved a low improvement in search relevance while multiple queries fusion achieved a significant improvement in search relevance. Fusion models able to exploit the skimming effect are more appropriate in the case of invariance.

Further research related to the work presented in this paper concerns mainly the investigation of the possibility to define more representations. In the case of invariance, the choice of appropriate queries is an open question. In this paper, we have chosen multiple queries in a random way. We believe that, if this choice can be done using some procedure taking into account user's needs, search relevance can be further improved.

## REFERENCES

- Abbadeni N. Information Retrieval From Visual Databases Using Multiple Representations and Multiple Queries. ACM SAC'09, March 2009.
- Datta R., Joshi D., Li J., and Wang J.Z. Image Retrieval: Ideas, Influences, and Trends of the New Age. ACM Transactions on Computing Surveys, 40(2), 60 pages, 2008.
- Abbadeni, N. and Alhichri, H. Low-level invariant image retrieval based on results fusion. Proceedings of the IEEE ICME, Hannover-Germany, June 2008.
- Muneesawang P, Guan L. An interactive approach for CBIR using a network of radial basis functions. IEEE Transactions on Multimedia, 6(5):703-716, October 2004.
- Abbadeni N. Perceptual meaning of the estimated parameters of the autoregressive Model. IEEE ICIP, Genova, Italy, 2005.
- Abbadeni N. Multiple representations, similarity matching, and results fusion for CBIR. ACM/Springer Multimedia Systems Journal, 10:(5): 444-456, 2005.
- Abbadeni N. A new similarity matching measure: application to texture-based image retrieval. Proceedings of the 3<sup>rd</sup> International Workshop on Texture Analysis and Synthesis (held in conjunction with IEEE ICCV), Nice, France, October 2003.
- Abbadeni N, Ziou D, Wang S. Computational measures corresponding to perceptual textural features. Proceedings of the 7<sup>th</sup> IEEE International Conference on Image Processing, Vancouver, BC, September 10-13 2000.
- Amadasun M, King R. Textural features corresponding to textural properties. IEEE Transactions on Systems, Man and Cybernetics, 19(5):1264-1274, September/October 1989.
- Belkin NJ, Cool C, Croft WB, Callan JP. The effect of multiple query representation on information retrieval performance. Proceedings of the 16th International ACM SIGIR Conference, pp. 339-346, 1993.
- Berretti S, Del Bimbo A, Pala P. Merging results for distributed content-based image retrieval, Multimedia Tools and Applications, 24:215-232, 2004.
- Brodatz P. Textures: A Photographic Album for Artists and Designers. Dover, New York, 1966.
- Frankot R. T. and Chellappa R. Lognormal random-field models and their applications to radar image synthesis. IEEE Transactions on Geoscience and Remote Sensing, 25(2), March 1987.
- French JC, Chapin AC, Martin WN. An application of multiple viewpoints to content-based image retrieval, Proceeding of the ACM/IEEE Joint Conference on Digital Libraries, pp. 128-130, May 2003.
- Gower JC. A general coefficient of similarity and some of its properties. Biometrics Journal, 27:857-874, December 1971.
- Kashyap R. L. and Chellappa R. Estimation and choice of neighbors in spatial interaction models of images. IEEE Transactions on Information Theory, 29(1):60-72, 1983.
- Lazebnik S., Schmid C. and Ponce J. A Sparse Texture Representation Using Local Affine Regions. Beckman CVR Technical Report, No. 2004-01, University of Illinois at Urbana Champaign (UIUC) (also submitted to IEEE PAMI), 2004.
- Lee JH. Analysis of multiple evidence combination. Proceedings of the ACM SIGIR Conference, pp. 267-276, Philadelphia, PA, USA, 1997.
- Liu F, Picard RW. Periodicity, directionality and randomness: Wold features for image modeling and retrieval. IEEE Transactions on Pattern Analysis and Machine Intelligence, 18(7):722-733, July 1996.
- Lu Y, Hu C, Zhu X, Zhang H, Yang Q. A unified framework for semantics and feature based relevance feedback in image retrieval systems. Proceedings of the 8<sup>th</sup> ACM International Conference on Multimedia, pp. 31-37, Marina Del Rey, CA, 2000.
- Manjunath BS, Ma WY. Texture features for browsing and retrieval of image data. IEEE Transactions on Pattern Analysis and Machine Intelligence, special issue on Digital Libraries, 18(8):837-842, August 1996.
- Rui Y, Huang TS, Mehrota S. A Relevance feedback architecture for multimedia information retrieval systems. IEEE Workshop on Content-based Access of Image and Video Libraries, pp. 82-89, 1997.
- Sun Y, Ozawa S. Semantic-meaningful content-based image retrieval in wavelet domain. Proceedings of the 5<sup>th</sup> ACM International Workshop on Multimedia Information Retrieval (held in conjunction with ACM Multimedia), pp. 122-129, Berkeley, CA, November 2003.
- Tamura H, Mori S, Yamawaki T. Textural features corresponding to visual perception. IEEE Transactions on Systems, Man and Cybernetics, 8(6):460-472, June 1978.
- Vogt CC, Cottrell GW. Fusion via a linear combination of scores. Information Retrieval Journal, 1:151-173, 1999.
- Wu S. and Crestani F. Data Fusion with Estimated Weights. Proceedings of the International ACM Conference on Knowledge and Information Management (CKIM), pp. 648-651, McLean, Virginia, USA, november 4-9, 2002.
- Zhang J. and Tan T. Brief Review of Invariant Texture Analysis Methods. *Pattern Recognition*, 35:735-747, 2002.
- Zhou XS, Huang TS. Relevance feedback for image retrieval: a comprehensive review. ACM Multimedia Systems Journal, 8(6):536-544, 2003.