MODEL-BASED DESIGN OF CODE FOR PLC CONTROLLERS

Krzysztof Sacha

Warsaw University of Technology, Nowowiejska 15/19, 00-665 Warszawa, Poland

Keywords: Automatic program generation, Model verification, Finite state machine, Programmable logic controller.

Abstract: This paper describes a method for model-based development of software for programmable logic controllers (PLC). The method includes modeling of a control algorithm, verifying the algorithm with respect to the requirements, and automatically generating the code in one of the IEC 61131 languages. The modeling language is UML state machine diagram, and the verification tool is UPPAAL model-checking toolbox. The method has good scalability with respect to the number of the modeled objects and the ability to cope with integer values by means of variables and function blocks.

1 INTRODUCTION

This paper describes a method for model-based development of software for programmable logic controllers – PLC. The method includes modeling of a control algorithm, verifying the algorithm, and automatically generating the code for a PLC.

The development cycle is shown in Figure 1. The modeling language is UML state machine diagram (OMG, 2005), which has been widely accepted as a means for specifying the controller at a suitable high level of abstraction. The verification tool is the UPPAAL model-checker (Behrmann et al, 2004). When the verification has been finished, the implementation code can be generated automatically in one of the IEC 61131 languages (IEC, 1993).



Figure 1: Modeling, verification and implementation of the program code.

A formal semantics for a UML state machine is given by a translatable finite state time machine – FSTM (Sacha, 2007, 2008). Modeling a controller in UML, modeling the environment in UPPAAL, and formulating safety requirements in a formal language of CTL formulae are done manually. The tasks of converting the model from UML to UPPAAL and to FSTM, verifying the model, and generating the program code are done automatically.

The unique features of the method described in this paper are the use of UML state machine as a problem modeling tool, and the ability to verify time dependent behavior of the controller. Widely accepted models of timed automata (Alur, Dill, 1996) and timed I/O automata (Kaynar et al, 2006) are used mainly for modeling and verification of time-dependent behavior of state systems. Still another models of time triggered automata (Krcal et al, 2004) and PLC-automata (Dierks, 1997) are used for code generation only.

The paper is organized as follows. Section 2 gives an overview of PLC controller and finite state time machine. Section 3 defines the semantics of UML state machine in FSTM. Section 4 presents a conversion algorithm from FSTM to UPPAAL and explains the verification process. The conversion of finite state time machine into a program code is described in Section 5. A discussion of the results and plans for future work are given in Conclusions.

2 PLC CONTROLLER

PLC is a computerized device that cooperates with its environment through a set of input and output signals. The controller executes in a loop, polling the inputs and computing the values of the outputs.

130 Sacha K. (2009).

Copyright © SciTePress

MODEL-BASED DESIGN OF CODE FOR PLC CONTROLLERS.

In Proceedings of the 6th International Conference on Informatics in Control, Automation and Robotics - Signal Processing, Systems Modeling and Control, pages 130-135 DOI: 10.5220/0002209801300135

The controller counts time using timers. A timer can be activated in a given a set of states. An active timer counts time and expires when it has continued to be active for a predefined period of time. An expired timer is perceived by the controller similarly as an input signal. The execution of a controller can be described in a pseudo-code, which creates a reference model for PLC execution:

```
state = initial_state();
loop_forever {
    input = poll_the_input();
    timers =
    set_timers(active_timers(state));
    state = next_state(state,timers,input);
    output = count_output(state);
    set_the_output(output);
}
```

Board software of a PLC sets the initial state (initial_state), executes the loop (loop_ forever), polls the input signals (poll_the_ input) counts time and sets the expired timers (set_timers), and sets the output signals (set_ the_output). The programmer must only write a code for selecting active timers (active_timers), and calculating the next state of the controller (next state) and of the output (count output).

The semantics of a PLC program is defined by a finite state time machine (Sacha, 2007), which is a tuple $A = (S, \Sigma, \Gamma, \tau, \delta, s_0, \Omega, \omega)$ where

- S is a finite set of *states*,
- Σ is a finite set of *input symbols*,
- Ω is a finite set of *output symbols*,
- Γ is a finite set of variables called *timer symbols*, $\tau: \Gamma \to 2^S \times N^+$ is an injective function, called *timer function* (with two projections $\tau_S: \Gamma \to 2^S$
- and $\tau_{N}: \Gamma \to N^{+}$, respectively), $\delta: S \times \Sigma \times 2^{\Gamma} \to S$ is a partial function, called *transition function*, such that:
 - $[(s, a, T) \in Dom(\delta)] \Leftrightarrow (\forall t \in T) [s \in \tau_S(t)]$
- $s_0 \in S$ is the initial state,
- $\omega: S \to \Omega$ is an output function.

Notation: N^+ is the set of positive integers, $Dom(\delta)$ is the domain of a function δ , card(X) is the cardinality of a set X, and ϕ is an empty set.

Finite state time machine looks much like a Moore automaton with three additional elements: Γ , τ , ε , which add to the model the dimension of time. A timer symbol $t \in \Gamma$ is a variable, which takes values from the set N^+ . The current value of t is interpreted as the duration of a period of time. Timer function τ assigns to each timer a group of states and a constant value. The meaning is such that timer t is enabled,

i.e. counts time, as long as the automaton resides in one of the states from $\tau_S(t)$ and it expires when the current value of *t* exceeds $\tau_N(t)$.

Timer symbols in Γ can be set in an arbitrary order and denoted $t^{l} \dots t^{n}$. The valuation t of timer symbols can be described as a vector of values t. The current value of a timer t^{i} is denoted t^{i} .

The execution of a finite state time machine starts in state s_0 with the values of all timers equal to 0. For a given state s_k and a valuation of timers t_k there exists a set of expired timers, defined as:

$$\Theta(s_k, t_k) = \{ t' \in \Gamma : s_k \in \tau_S(t') \text{ and } t'_k \ge \tau_N(t') \}$$

The machine executes in a state (s_k, t_k) by taking an input symbol a_k and moving to the next state s_{k+l} defined by the transition function:

$$s_{k+1} = \delta(s_k, a_k, \Theta(s_k, t_k))$$
 where $k = 0, 1, \dots$

When the machine enters a state s_{k+l} time advances and the values of timers change reflecting the elapsed time interval:

$$t_{k+l}^{i} = \begin{cases} t_{k}^{i} + 1 & \text{if } s_{k+l} \in \tau_{S}(t^{i}) \text{ and } s_{k} \in \tau_{S}(t^{i}) \\ 0 & \text{otherwise} \end{cases}$$

When the valuation of timers *t* changes, the set Θ of expired timers may change as well. This way a finite state time machine can respond to the flow of time, even if $s_{k+l} = s_k$ and $a_{k+l} = a_k$. Please note that the last argument of δ is a set of expired timers, hence, no conflict exists if several timers expire at the same time instant.

The state space of a PLC as well as of an FSTM can be defined by enumerating all of the elements, eg. $S = \{s_1, s_2, ..., s_n\}$. An alternative way is to allow for using variables and to define the state space as a Cartesian product of a set of enumerated elements and a set of all possible valuations of those variables. This is only a shorthand notation, which does not add any new semantics to the model, and therefore it is not shown in the formal definition.

In the rest of this paper, we will adopt a naming convention of UPPAAL (Behrmann et al, 2004) and refer to the enumerated elements of state as locations. Locations will be shown in graphical models explicitly, as the nodes of a graph, while variables will be referred to by guard expressions and will be assigned values within actions of transitions.

3 UML STATE MACHINE

UML state machine diagram is a graph composed of nodes, which are locations, and edges, which are labeled transitions. A transition can be triggered by a signal received from the outside. A transition which is triggered can fire, if the corresponding guard expression over a set of variables evaluates to true. Firing of a transition can move the machine to a new location, change the values of variables and send a signal. This way, the state space of a UML state machine is a Cartesian product of the set of locations and the set of all possible valuations of variables.

UML allows for nesting of locations. However, a hierarchy of locations can always be flattened. A formal model and an algorithm for flattening the hierarchy were described in detail in (Sacha, 2007) an will not be discussed in the rest of this paper.

Relating this model to a PLC, one can note that a received signal corresponds to a combination of the input signals of the PLC, and a sent signal corresponds to a combination of the output signals. States of an UML state machine and transitions between states correspond to states of a PLC and to the next-state function defined by a program code.

A conversion algorithm of a UML state machine into a FSTM can be described as follows.

- *S* equals to the Cartesian product of the set of all locations of the UML state machine and the valuations of variables used in guard expressions.
- Σ equals to the set of external signals, which trigger transitions in the UML state machine; a signal is a combination of all the input signals of the PLC.
- Γ is a set of timer symbols $t^{l},...,t^{n}$; there is one timer symbol t^{i} for each timed transition (i.e. transition with an *after* clause) in the UML state machine,
- τ is the timer function, which assigns to each timer symbol t^i created for a timed transition T a pair composed of a source state of this transition and the value of the after clause of this transition.
- δ is the transition function δ: S × Σ × 2^Γ → S, such that: $δ(s_1, a, T) = s_2$ if and only if there exists a transition in the UML state machine diagram such that s_1 is the source and s_2 the destination state of this transition, and either *a* is the event that triggers this transition (in this case T = φ), or $T = \{t^i\}$ and t^i is the timer symbol of this timed transition (ie. $δ(s_1, a, T) = s_2$ for all a ∈ Σ).
- s_o is the initial state of the UML state machine.
- Ω equals to the set of combinations of all the output signals of the PLC that are set by the actions of the UML state machine.

 ω is the output function, which assigns to each state $s \in S$ the output symbol $q \in \Omega$, which is set by all transitions to *s*.

Example. Consider a railroad crossing controlled by a PLC. There are a number of railway tracks within the crossing, and a number of trains can approach the crossing simultaneously (one train on a track is allowed). The movement of trains is controlled by a set of semaphores that can prevent trains from entering the crossing. The road traffic is controlled by a gate that can be open or closed. A semaphore can be operated by a controller to display green light, when a train approaches, but not earlier than after the gate has been closed. Opening and closing states of the gate are confirmed to the controller by the input signals: up and down, respectively. Closing the gate must last less than 30 seconds, or else an alarm must sound. The semaphores are red and the gate is *up* in the initial state of the crossing.

An algorithm for the railroad crossing controller is shown in Figure 2. The locations within the graph correspond to states of the crossing with respect to train positions. The transitions bear labels of the type *event / action*, where *event* corresponds to a condition on the input signals or timers, and *action* corresponds to setting the values of variables.



Figure 2: UML model of the railroad crossing controller.

The positions of particular trains are signaled to the controller by short input pulses *approach(i)* and *leave(i)*, i=0,...n-1. The appearance of an *approach*pulse is stored in a vector variable a(i), i=0,...n-1and makes the controller to close the *gate*. When the gate is *down*, the controller uses the stored data to send *green* signals to the appropriate semaphores – the function MOV(a, green) sends a *green*-signal for each train, which approaches the crossing. The controller keeps track of all the trains inside the crossing, and waits until the last train has left. If this is the case, the controller turns the *green* signals off, *opens* the gate and waits until the gate is *up*.

Vector *a* is part of the controller state. This way, there are in fact as many *Entering* and *Inside* states as are the combinations of values in vector *a*. Output signals of the state machine are *open* and *close* to operate the gate, and the signals *green(i)* to operate the semaphores to display *green* or *red*.

FSTM model of the controller has the same set of locations and the same set of variables. It has a single timer symbol *t*, and the timer function $\tau_S(t) = \{Entering\}$ and $\tau_N(t) = 30$. The transition function is defined by the set of all the transitions of the UML state machine. The sets of input and output symbols are the combinations of input and output signals.

4 VERIFICATION

UPPAAL is a toolbox for modeling and verification of real time systems, based on the theory of timed automata. The core part of the toolbox is a modelchecking engine, which enables for verification of properties defined as CTL path formulae.

A timed automaton (Alur, Dill, 1996), as used in UPPAAL, is a finite state machine extended with clock variables that evaluate to positive real numbers and state variables that evaluate to discrete values. State variables are part of the state. All the clock variables progress simultaneously. An automaton may fire a transition in response to an action, which can be thought of as an input symbol, or to a time action related to the expiration of a clock condition. A clock variable can be reset to zero at a transition.

A set of timed automata can be composed into a network over a common sets of clocks, variables and actions. This way a cooperation between a controller and a controlled plant can be modeled.

The use of a dense-time model-checker to verify a discrete-time model may look as an overkill. But in fact it is not, because the environment of the controller works in real-time and must be modeled using a dense-time method.

A conversion algorithm of FSTM into UPPAAL is described in (Sacha, 2008).

Verification. UPPAAL can verify the model with respect to the requirements, expressed formally as CTL formulae. To do this, UPPAAL model-checker evaluates path formulae over the reachability graph of a network of timed automata.

The query language consists of state formulae and path formulae. A state formula is an expression that can be evaluated for a particular state in order to check a property (e.g. a deadlock). Path formulae quantify over paths of execution and ask whether a given state formula φ can be satisfied in any or all the states along any or all the paths.

Path formulae can be classified into three types:

- Reachability properties: E<>φ. (will φ be satisfied in a state of a path?)
- Safety properties: $E[] \varphi$ and $A[] \varphi$. (will φ be satisfied in all the states along a single or along all paths?)
- Liveness properties: A <> φ and ψ --> φ. (will φ eventually be satisfied? will φ respond to ψ?)

Example. Consider again the railroad crossing described in Section 3. A train cannot be stopped instantly. When a train is detected by a train position sensor, a controller has 30 seconds to *close* the gate and display a *green* signal, which allows the train to continue its course. After these 30 seconds, it takes further 20 seconds to reach the crossing. Otherwise, if the *green* signal is not displayed within these 30 seconds, the train must break in order to stop safely before the crossing. Closing the gate must last less than 20 seconds, or else an alarm must sound. The gate can be opened when the position sensor has sent a *leave* signal after the last train has left the crossing.

The environment of the controller consists of a number of trains and a gate. Each of these elements can be modeled in UPPAAL and synchronized with the controller within a network of timed automata.

The template of a train is shown in Figure 3. Actions, which names bear the suffix '?', act like input symbols that enable the associated transitions. Actions, which names bear the suffix '!', act like output symbols that are passed to other automata in order to trigger the respective input symbols. This way the execution of one automaton can control the execution of a other automata.



Figure 3: UPPAAL model of a train.

Time invariant $t \le 30$ of state *Approaches* forces a transition after 30 seconds have passed since the train has entered the state. This models the necessity of breaking the train if *green* has not been displayed in time. Time condition t > 20 at the transition from *On crossing* to *Faraway* reflects the minimum time of passing the crossing by a fast train. Time invariant $t \le 40$ of the state *On crossing* reflects the maximum time of passing by a slow train.

The template is parameterized with the train identifier *id*. A set of *n* trains, e.g. four, can be generated using the values of id = 0 through 3.

A model of the gate is shown in Figure 4. Time invariants $t \le 20$ at states *Closing* and *Opening* reflect time that it takes to close or to open the gate.



Figure 4: UPPAAL model of the gate.

The simple reachability properties can check if a given state is reachable:

- *E*<> *train1.On crossing*: This checks if train 1 can pass the crossing (a similar property can be checked for other trains).
- E<> (train1.On crossing && train2.On crossing && train3.On crossing && train4.On crossing): This checks if all the trains can move through the crossing simultaneously.

The safety properties can check that unsafe states will never happen:

- *A* [] (train1.On crossing or train2.On crossing or train3.On crossing or train4.On crossing) imply gate.Closed: This ensures that each time a train is passing the crossing, the gate is closed.
- A [] (gate.open imply (¬train1.On crossing && ¬train2.On crossing && ¬train3.On crossing && ¬train4.On crossing)): This ensures that each time the gate is open, a train is not on the crossing.

The liveness properties can check consequences of an event, e.g.:

• *train1.Approaches* --> *train1.On crossing*: This ensures that whenever train 1 approaches the crossing, it will eventually pass it.

In our example the liveness condition is not satisfied: Assume that the train 2 approaches when

train 1 is just leaving. The controller does not react to *approach* in state *Leaving*, hence, the transition to *Outside* appears without displaying *green* signal for train 2. The train will stop and can never reach the crossing.

The corrected finite state time machine model of the controller is shown in Figure 5.



Figure 5: The corrected model of the controller.

5 CODE GENERATION

The semantics of a PLC program is defined within the reference model by the semantics of its programming language (IEC, 1993), e.g. ladder diagram or structured text. The behavior of a finite state time machine has been defined in Section 2. By that means a method for translating a high level abstract model of finite state time machine (S, Σ , Γ , τ , δ , s_0 , Ω , ω) into a PLC program can formally be defined in the following steps:

- 1. Mapping of sets Σ , Ω into the input and output signals of PLC. This can be an arbitrary one-to-one mapping (coding of symbols).
- 2. Mapping of the set of locations which define part of state *S* into the values of flip-flops. This can be an arbitrary one-to-one mapping (coding of states). Mapping of the variables which define the other part of the state into the variables within the memory of the PLC.
- 3. Mapping of set Γ into the set of timers. A separate timer with the expiration time equal to τ_N (*t*) is allocated for each timer symbol $t \in \Gamma$.
- 4. Defining the function active_timers consistently with function τ . This function defines the input signals of all timer blocks. The input signal of a timer block allocated for a timer $t \in \Gamma$,

is a Boolean function over the set of flip-flops used for coding of states, such that it is true in state *s* if and only if $s \in \tau_s(t)$.

- 5. Defining function next_state consistently with function δ . This function defines the set and reset signals of flip-flops, which have been used for coding of states. The signal to set (reset) a flip-flop is a Boolean function over the set of flip-flops, input signals of PLC and output signal of timer blocks, such that it is true if and only if this flip-flop is set (reset) in the next state of FSTM.
- 6. Defining function count_output consistently with function ω . This function defines the values of output signals of PLC. The value of an output signal is a Boolean function over the set of flipflops, such that it is true if and only if this output signal is set in the current state of FSTM.

Example. To capture four trains within the crossing, we need four *approach* and four *leave* input signals from trains, plus two *up* and *down* input signals from the gate (Figure 5). There are four *green* signals output to semaphores, two signals *open* and *close* to the gate and a *sound* output signal. Any combination of the input (output) signals corresponds to an input (output) symbol. PLC controller stores the locations as states of its internal flip-flops. At least three flip-flops are needed. A selected coding for states and output signals of the controller is shown in Table 1.

Table 1: The coding of states and output signals.

Ml	M2	М3	a[i]	State	close	open	green(i)	sound
0	0	0	0	Outside	0	0	0	0
0	1	0	a(i)	Entering	1	0	0	0
1	1	0	a(i)	Inside	0	0	a(i)	0
1	0	0	0	Leaving	0	1	0	0
0	1	1		Alarm	1	0	0	1

The program for PLC is a ladder diagram (IEC, 1993) consisting of a sequence of lines, each of which describes a Boolean expression to set or reset a flip-flop or an output signal, to activate a timer, or to call a function block to operate a variable, according to the values of input signals, states of flip-flops, variables and timers. The expressions reflect the coding of locations and implement the functions active_timers, next_state and count_output described in Section 2. An example is shown in Figure 6, which presents the transitions from *Entering* to *Alarm* and from *Entering* to *Inside* (Figure 5). M11 and M13 are auxiliary flip-flops, which mirror the main flip-flops M1 and M3, in order to assure atomicity of the transitions.



Figure 6: A fragment of the ladder diagram program for the railroad crossing controller.

6 CONCLUSIONS

A method is described for the specification, verification and automatic generation of code for PLC controllers. The advantages of the method are intuitive modeling by means of a widely accepted UML state machine, and a potential for automatic verification and implementation of the model.

A tool which implements the steps of the method has been implemented and verified on small scale examples. The verification included experiments in a lab equipped with a few process models and a set of S7 PLC controllers from Siemens.

REFERENCES

- Alur R., Dill D., 1996. Automata-theoretic verification of real-time systems. In Formal Methods for Real-Time Computing, Trends in Software Series, John Wiley.
- Behrmann G., David A., Larsen K.G, 2004. A Tutorial on Uppaal, Aalborg University.
- Dierks, H., 1997. PLC-Automata: A New Class of Implementable Real-Time Automata. LNCS 1231. Springer, Berlin.
- IEC, 1993. Programmable controllers part 3: Programming languages.
- Kaynar D.K., Lynch N.A., Segala R., Vaandrager F.W., 2006. The Theory of Timed I/O Automata. Synthesis Lecture on Computer Science, Morgan & Claypool.
- Krcal P., Mokrushin L., Thiagarajan P.S., Wang Yi. 2004. Timed vs. Time Triggered Automata. LNCS 3170, Springer-Verlag, Heidelberg.
- OMG, 2005. Unified Modelling Language: Superstructure, version 2.0.
- Sacha K., 2007. Translatable Finite State Time Machine. LNCS 4745, Springer, Berlin.
- Sacha K., 2008. Model-Based Implementation of Real-Time Systems. LNCS 5219, Springer, Berlin.