

# SPATIAL RECONSTRUCTION OF LOCALLY SYMMETRIC OBJECTS BASED ON STEREO MATE IMAGES

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**Abstract:** Restoration of spatial objects characteristics with locally symmetric elements is proposed in this paper. An approach based on the model of a spatial flexible object defined as a family of spheres with the centres on a graph with a tree-like structure is proposed. A method of real time identification of such objects using the stereo mate images of their silhouettes is introduced. Image processing comprises construction of continuous skeletons of silhouettes. Application to real time gesture recognition is considered.

## 1 INTRODUCTION

Reconstruction of spatial objects using several two-dimensional images is a well-known problem and has many real life applications. The essence of our approach is that two-dimensional images are considered to be a binary image and represent only silhouettes of a spatial object. Such statement of the problem, in particular, arises in recognition of gestures by means of standard inexpensive equipment. We suppose the initial data are low resolution (480×640) images received from standard WEB-cameras. In 3D pose estimation of object, such as human hand or body, texture is less important and much of the information can be extracted from the silhouettes alone. Recognition of a gesture requires reconstruction of the spatial form of such a complex and variable object as a human palm or body. The relevance of such statement of a problem is caused by the fact that the range of potential users of gesture recognition systems includes a great number of people (disabled, hard of hearing, etc.) not capable of obtaining expensive equipment but still deeply needing real-time gesture understanding systems. There are works devoted to creation of deaf alphabet understanding software (Burger and Caplier, 2007) as well as to developing gesture-driven computer systems (Keshkin, 2005).

The lack of texture details makes it impossible to analyse images at texture level and apply well known object reconstruction methods based on automatic identification of matching points on stereo mate images. Obviously, the boundary points are the only points that may be reliably identified on the silhouette images. The problem is that the boundary points of a silhouette on one of the stereo mate images have, as a rule, no matching points on the boundary of the silhouette on the other image. Thus, it is impossible to directly identify the matching points on the stereo mate silhouette images.

One can still try to identify the matching points making some assumptions on the nature of the original object. As far as gesture recognition deals with images of a human palm or body we propose to approximately represent these objects as a union of several "cylindrical" elements having local axial symmetry and solve the problem using a well known notion of a planar image skeleton. Such objects are also called "generalised cylinders" or "tubular objects". To be more precise a cylindrical element is a spatial body formed by a family of spheres with the centres on some curve. Such objects are called spatial fat curves. We are interested in objects that can be represented as a union of several fat curves. Such locally symmetric objects can be used as models for the description of a human palm or body.

It is natural that the accuracy of such description of a human body or palm that uses generalized cylinders is very low. Therefore, the proposed approach cannot be used for the high-precision reconstruction of shape and surface of 3D objects, as, for instance, in (German Cheung Baker, 2003). But for the recognition of gestures or poses the high accuracy of the description of shapes and surfaces is not required. It is sufficient to recognise only substantial changes in the shape of these objects, which characterise gestures. This approach makes it possible to obtain solution of the problem with the use of simple and inexpensive equipment under the normal conditions.

## 2 THE PROPOSED METHOD

The proposed approach is based on the revealing the of symmetry axes of the locally symmetric objects. Although, these axes are invisible on the stereo mate images, they still can be calculated for each image by processing a silhouette presented on it.

We assume that the observed object does not have occlusion. This means that all elements of the object, for example, the fingers of a palm are visible in the silhouette image. For objects with occlusions it is intended to use a sequential segmentation of initial grey scaled image to reveal overlapped parts.

Considering the silhouettes of stereo mate images as projections of the spatial fat curves onto the corresponding planes, we can expect that the projections of the axes of the fat curves coincide with the middle axes of the silhouettes.

In reality, the silhouette of a sphere is an ellipsis. For the simplified case, when a radius of a sphere is constant, there is a precise method of restoration based on one silhouette image analysis (Caglioti, 2006). For the images which we deal with, the difference between this ellipsis and a circle is so small, that it can be neglected.

We shall consider some (invisible) points which are not the boundary points of the silhouettes as the common matching points of stereo mate images. Such reference points are provided by middle axes of the silhouettes constituting its skeleton.

Implementation of the proposed approach poses several problems. First we need to build the skeletons of the silhouettes in a way that allows identification of the points of different skeletons. Then we have to restore the spatial form of the whole object using the results of the identification of the pair of skeletons. It is worth mentioning that all calculations should be performed in the framework

of the computer vision system in real time which requires processing of several stereo mate images per second. This demands developing highly efficient computational algorithms.

The notion of a flat flexible object is introduced in (Mestetskiy, 2007) and an effective method of comparing flexible objects on the basis of a boundary-skeletal model is proposed. In the present paper, we propose a generalisation of the notion of a flat flexible object to the spatial case.

We define spatial flexible object as a set of spheres of various sizes with centres on a spatial tree. Stereo mate image processing allows reconstructing the spatial structure of the object.

Reconstructing spatial characteristics of the object allows monitoring the displacement dynamics of the elements constituting the object, as well as the changes in the object's shape. Applied to the human palm or body this allows tracking their gestures or movements.

Implementation of the proposed approach includes solving of several subtasks.

### 2.1 Silhouette Acquisition

It is assumed that there is a pair of video cameras which allows receiving synchronized images of an object. An example of such stereo mate images is presented on fig.1. In our experiments the standard web-cameras connected to the desktop computer were used. Each image is separately segmented, then a silhouette is extracted and represented as a binary raster image. There are different ways of segmentation. All of them depend on specific applications. One can note that in gestures recognition the requirements to the quality of silhouette images are not very demanding. Figure 2 shows the result of palm segmentation obtained using the background subtraction method. In this example a simple method of background subtraction and thresholding was used.

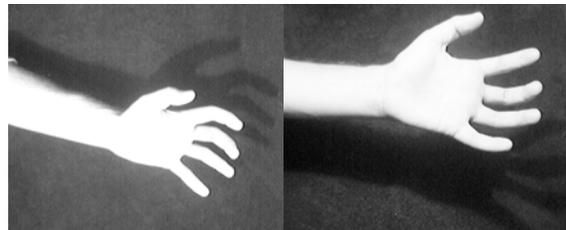


Figure 1: The palm stereo mate.

### 2.2 Continuous Skeleton

Construction of the silhouette skeletons (fig. 3) is

carried out by a method described in (Mestetskiy, 2008). A skeleton represents a geometric locus of the centres of the circles inscribed in a silhouette. The main advantage of the skeleton method used is that the skeleton is represented as a graph with edges as continuous lines. As we show later, this feature allows successfully resolving the problem of identification of skeleton points on different images. Additionally, the method has the advantage of high computing efficiency which allows solving the problem in real time in the framework of computer vision system.



Figure 2: The silhouettes received from two cameras.

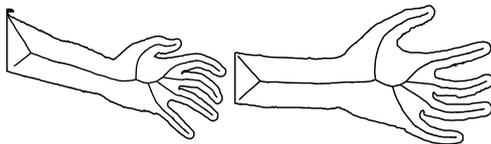


Figure 3: Skeletons of obtained silhouettes.

### 2.3 Camera Calibration

Each point in the space is characterised by the coordinates in a fixed orthogonal system which we call a laboratory system. At the same time each camera has its own orthogonal coordinate system, with the centre located in the centre of the camera, z axis is directed along the optical axis of the camera and the two others are parallel to the coordinate axes of the image. This camera model is called central projection and despite its simplicity it often constitutes an acceptable approximation to the process of image acquisition. Camera calibration process implies the problem of determining the camera location in a certain laboratory coordinate system and adjusting its internal parameters.

Another calibration method is based directly on processing the stereo mate images, which requires the identification of 5-8 points depending on the method chosen (Brückner, 2008). The most complicated part of this approach is allocation and identification of the distinguishable points on the images. Solving this problem with traditional methods require a large amount of computations and is inevitably accompanied by plenty of errors. Thus, such approach is unacceptable when the problem needs to be solved in real time and with the use of

web-cameras. The quality of obtained images, due to their low resolution, does not allow reliably detecting and identifying required number of points on the stereo mate images. However, for locally symmetric objects the use of skeletons makes this problem essentially simpler. The skeleton nodes can be used as the reference points. Thus, the problem is reduced to identification of the nodes of two stereo mate image skeletons.

### 2.4 Identification of the Reference Points on the Skeleton

We assume that the projection of the axes of a locally symmetric object approximately coincides with a skeleton of the silhouette and this allows to calculate these axes. Let  $C$  be a point on one of the stereo mate images. There is a straight line in the space which is projected in this point. The image of this straight line on the other picture is a so called epipolar line of the point  $C$ . For a given point on a skeleton its stereo mate coincides with the point of intersection of the other skeleton and the epipolar line of this point. (fig. 4).

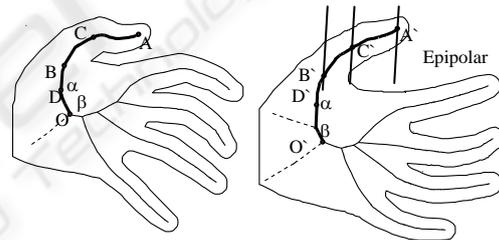


Figure 4: Stereo mate points found on skeletons.

### 2.5 Spatial Object Reconstruction

Having constructed axes on the basis of identification of stereo mate points, it is possible to calculate a spatial structure of a skeleton of the object. Then, using the information on the width of the object, with respect to the middle axes, we restore a surface of the spatial object.

## 3 SKELETON POINTS IDENTIFICATION

We describe our method of model construction for a human palm example. We will consider stereo mate images of a human palm (fig. 1) and the corresponding axial graphs (fig. 4). Obviously, fingers are locally symmetric objects. We assume

that the projection of a spatial axis of a finger coincides with a skeleton of a finger silhouette (fig. 4, curves  $AB$  and  $A'B'$ ).

Experiments show that the centres of the big circles on both silhouettes (points  $O$  and  $O'$ ) are the stereo mates with sufficient accuracy. Hence, it can be assumed that the set of stereo mate points on the sub-tree  $OA$  of the axial graph of the silhouette coincides with the sub-tree  $O'A'$  of the other silhouette's axial graph. This allows constructing a curve in the space.

If we consider the curve  $OA$  as a continuous mapping  $f: [0,1] \rightarrow R^2$ , and the curve  $O'A'$  as  $g: [0,1] \rightarrow R^2$ , the problem reduces to finding a mapping  $w: [0,1] \rightarrow [0,1]$  which maps each point  $f(t)$  into its stereo mate  $g(w(t))$ . (fig 5). Obviously, there are restrictions imposed on  $w$ : the mapping should be monotonous and continuous.

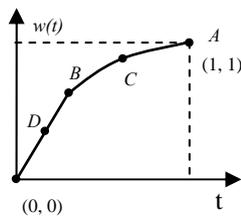


Figure 5: Dependence  $w(t)$ .

Let  $C$  be a point on one of the stereo mate images. For a given point  $C = f(t)$  on the curve  $OA$ , its stereo mate  $C' = g(w(t))$  is located at the intersection of the curve  $O'A'$  and the epipolar of  $C$ . Thus, using the epipolar lines, it is possible to identify the stereo mate points on axial graphs and determine the spatial arrangement of the axes of the fat lines.

However, the difficulty arises when the intersection angle  $\theta(t)$  of the curve  $O'A'$  and the epipolar line is small, and therefore  $C'$  is defined with great inaccuracy. We can avoid this, by imposing the following restriction  $\theta(t) > \theta_{min}$ . The value of  $w(t)$  can be calculated only if  $\theta(t) > \theta_{min}$ . In order to determine  $w(t)$  when  $\theta(t) \leq \theta_{min}$  we interpolate using already obtained values of  $w$ . The application of the linear interpolation is quite comprehensible to our problem.

In figure 5, restriction  $\theta(t) > \theta_{min}$  is violated on curve  $OB$ , thus this curve is a segment.

Based on identification of the skeleton points we obtain complete spatial configuration of the axes of the given locally symmetric object. In many cases, this representation is enough to handle the problems of gesture recognition. However, the method of skeletal representation contains not only the information on the mid-axes of an object, but also the information on the width of an object, since the radii of inscribed circles with the centres on the mid-axes are known. This information on the width of the object makes it possible to visualise a constructed spatial model.

#### 4 VISUALIZATION

Having constructed spatial axes and calculated the sizes of spheres with the centres on these axes, we can reconstruct a spatial image of the object. For each point  $\gamma$  of the spatial axial graph we define a corresponding sphere in the following way: let  $Q$  be a point of the axial graph of one of the silhouettes which is the image of  $\gamma$ . There exists a corresponding maximal sized circle  $S$  with the centre in  $Q$  which is inscribed in the silhouette. The given circle is the image of a sphere  $S_r$  with the centre in  $\gamma$  and radius  $r$ . Let's choose an arbitrary point  $P \in S, P = (u, v)$ . It determines a ray  $l$  which starts in the centre of the first camera and is tangent to the sphere  $S_r$ . Then  $r$  is a distance between the point  $\gamma$  and the ray  $l$ .

Thus, the sphere radius can be calculated. The model of the object is a surface enveloping the set of these spheres. An example of a human palm model visualization obtained from the stereo mate images is presented on fig. 6.

One can see from this example that the visualization is not quite realistic, since in the model not only the fingers are described as the fat curves, but also a palm part between the fingers and a wrist is considered as a fat curve. This fault of visualization can be easily eliminated because the spatial position of the fingers makes it possible to calculate the plane where this palm part is located and slightly flatten the sphere towards this plane. The result of such an improvement is presented on fig. (7).



Figure 6: Spatial model visualization.

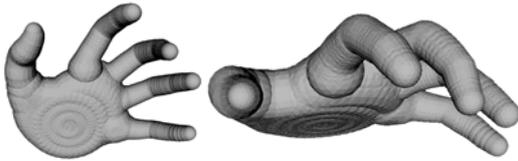


Figure 7: Corrected spatial model.

## 5 EXPERIMENTAL RESULTS

Experiments with the reconstruction of the spatial model of a human body were conducted with dolls of a size of 30 cm. The only purpose of using the dolls was to simplify the process of taking photos in the laboratory conditions. The results can easily be extrapolated for a case of a real human body. Figure 7 shows the initial stereo mate images, their silhouettes and the resulting spatial objects.

The experimental estimation of the accuracy of restoration of human body shape can be obtained with the use of "Kung-Fu Girl" data, presented by Graphics-Optics-Vision group at the Max-Planck Institute for Informatics (MPII). These data consist of synthetic scenes (size  $240 \times 320$ ) obtained from the virtual cameras, for which the precise values of the calibration parameters are known. The results of the experiments are shown on figure 9. Visual analysis shows that the accuracy of restoration of body shape and surface is very poor. But, this accuracy looks like completely sufficient for restoring poses and gestures. We intend to investigate the formal quantitative criterion of accuracy and the methods for its calculation.

The performance of the algorithm implemented on Intel Pentium IV, Core 2 Duo, 2800 Mhz, 1Gb RAM computer is more than 5 frames per second. This makes it possible to use the proposed method as a real time tool in the framework of the computer vision systems.

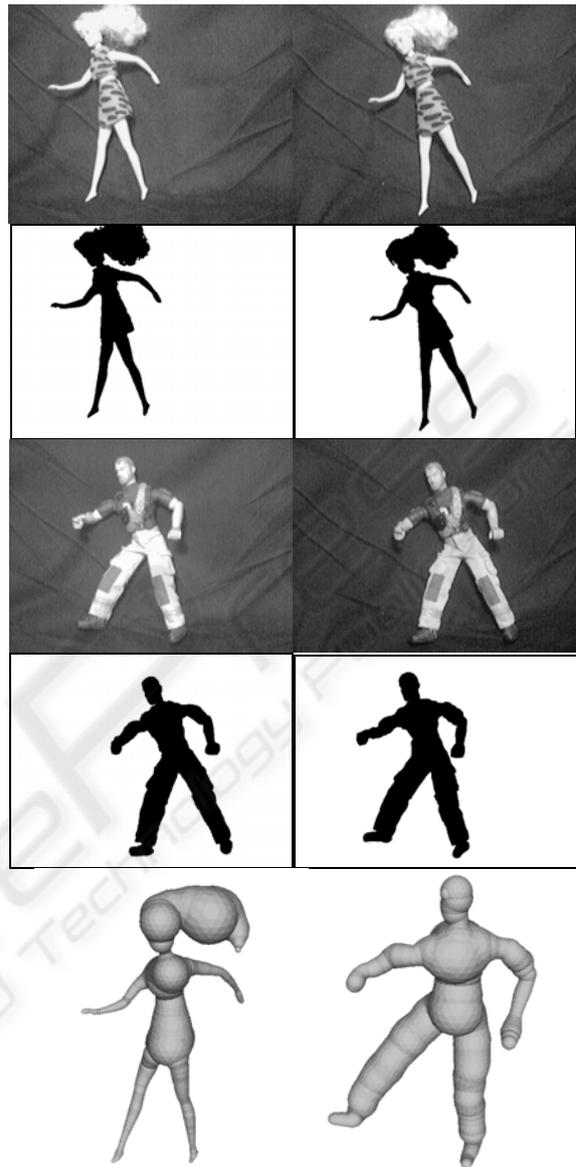


Figure 8: Stereo mate of initial images, their silhouettes and the received spatial objects.

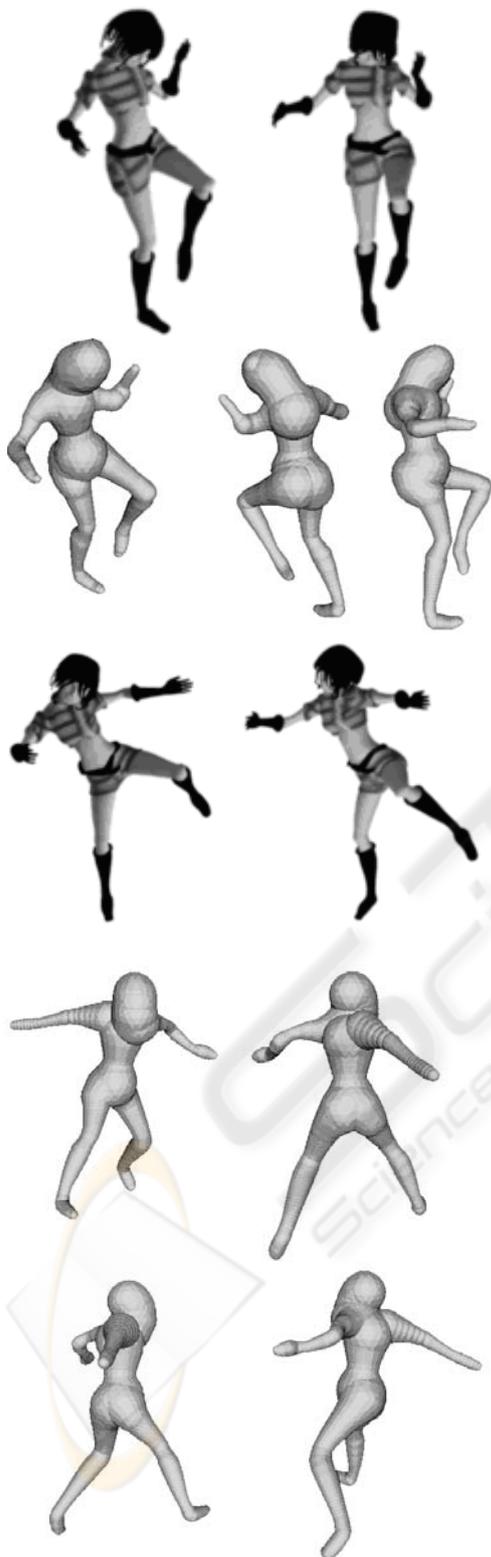


Figure 9: Stereo mate of initial images and received spatial objects for “Kungfu girl”.

## ACKNOWLEDGEMENTS

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