WORD SEGMENTATION BASED ON HIDDEN MARKOV MODEL USING MARKOV CHAIN MONTE CARLO METHOD

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Abstract: It is well-known that Japanese has no word boundary, so that we should think about how to separate each sentence into words by means of morphological analysis or some other word segmentation analysis. It is said, however, that the separation depends on domain specific rules. The author have proposed a sophisticated word separation method based on Conditional Random Fields (CRF). Unfortunately we need a huge amount of test corpus in application domains as well as computation time for learning. In this investigation, we propose a new approach to obtain test corpus based on Markov Chain Monte Carlo (MCMC) method, by which we can obtan efficient Markov model for segmentation.

1 MOTIVATION

Recently there have been a wide variety of research activities targeted for Web page text processing without any knowledge of format, tags and commands. Among others, *text mining* puts an emphasis on the problem how we should analyze various kinds of free texts such as minutes of meetings, daily reports and questionnaire.

When we examine plain text documents, we face to an issue of *word segmentation* in Japanese, Chinese or some other languages. This is because there is no boundary between words, and thus how to discover the boundaries in text or speech is of interest for practical reasons such as morphological analysis. There is no common rule to put space or any other punctuation in Japanese, and when processing the texts, we should start with word segmentation. We should think about this issue as a step of morphological analysis.

There have been many interesting approach to the morphological approach. One is based on local rules and statistics, thus the process is driven by means of rule interpretation. This is quite successful but it is hard to extract rules, to keep the rules consistent and no common procedures to extract. Another approach is based on explicit probabilistic models or stochastic process models. Analyzing texts statistically, we learn how morphemes act, i.e., we extract common patterns in a probabilistic way. Traditionally there have been assume *common* situation for all purposes. Even if we know domain-dependent situation, it is hard to find any useful solution.

In this investigation, we propose an experimental approach for word segmentation in Japanese under domain-dependent situation. We apply *Hidden Markov Model* (HMM) to our issue. Here we need *training corpus* to obtain the HMM model. The more corpus we have, the better rules we get. Clearly it takes much time to huge corpus. To overcome the issue, Baum-Welch (EM) algorithm has been proposed. But the results depend heavily on the corpus. Compared to such conventional discussion, we propose completely different approach to obtain HMM models based on *Markov Chain Monte Carlo* (MCMC) technique. By generating random values which capture similar distribution to the corpus, we can obtain huge amount of training corpus and improve the results.

In section 2, we review morphological analysis to Japanese, and in section 3, we discuss word segmentation problem. In section 4 we review HMM and MCMC approach in section 5. Section 6 contains the model to apply MCMC to segmentation problem, and section 7 contains experimental results. We conclude our work in section 8.

2 MORPHOLOGICAL ANALYSIS AND SEGMENTATION

Documents consist of mainly texts, figures and tables, texts contain many sentences which are sequences of words. A word means a character string separated by space or punctuation, but the problem is not really simple: how can we think about compound words such as "U.S.A.", idioms (a group of words carrying a different meaning when used together) or collocation (the way that some words occur regularly when other words are used) such as "not only...but also". A sentence in natural languages consists of morphemes. A morpheme is a unit of strings carrying minimal meaning. Each sentence can be decomposed into a sequence of morphemes in a form of token (single word), inflection (stemming) and part-of-speech (POS) as noun and verb. The process is called morphological analysis. In this work, by morpheme, we mean a pair of token and part-of-speech attributes.

In morphological analysis, we have dictionary which talks about relationship among morphemes, and grammatical knowledge about morphemes. We divide sentences into word segments, and examine their role (and meaning) as well as the structural relationship. The morphological analysis is one the key steps for syntax and semantic analysis.

We know the fact that, in English, a word describes grammatical roles such as *case* and *plurality* by means of word order or inflection. The difference between "John calls Mary" and "Mary calls John" corresponds to the two interpretation of *who calls whom* over John and Mary. Such kind of language is called *inflectional language*.

On the other hand, in some languages as Japanese and Chinese, grammatical relationship can be described by means of postpositional particles, and such kind of languages is called agglutinative language. For example, "I", "My" and "Me" correspond to " ", "", " " respectively where "" means the first personal pronoun. The differences are 3 postpositional particles "", "" and "" which define subjective, possessive and objective respectively. As for John and Mary, the two sentences "Wł AŁ[", "W AŁ[ł" correspond to the two sentences "John calls Mary" and "Mary calls John" where the positions of "W"(John), "AŁ["(Mary) and ""(call) are exactly same but the difference of postpositional particles. There is another problem, there is no boundary between words in Japanese. Basically, if we get words and relevant postpositional particles, we could specify segmentation. Morphological analysis examines roles of words and determines which parts should be attached to which words. In our case, we put tags between words such as "/Wł/AŁ[/" and "/W/AŁ[ł/". In agglutinative languages, *word segmentation* plays essential role on syntax and semantic analysis.

It is also important for the analysis step to examine *compound words*. For example, we can decompose "Lw" (University Education) into "Lw" (University) and ""(Education) but not "Lw" (University Student) into "Lw" and "". Such segmentation rules depend often on application domains. In this investigation, we propose an experimental and efficient approach of domain dependent word segmentation base don stochastic process. We apply *n*-gram model to Japanese, examine relationship between morphemes by Hidden Markov Model (HMM) for the word segmentation.

3 SEGMENTING WORDS

In a case of inflectional languages, there is no sharp distinction between word segmentation and part-ofspeech (POS) tagging, and we can apply similar techniques to analyze and examine sentences. There have been two major approaches proposed so far, rule-based tagging and probability-based tagging. In the former, we extract characteristic patterns between words or POS tags and between some more ones before/after the words of interests. Then we put them into a form of rules. For example, we may have a rule "this is not a verb if the preceding word is a determiner". By using well-structured rule tables, we can get rather excellent results. The problems arise, how we can extract useful, global, consistent and efficient rules? The process is not trivial and hand-coded, thus we take much time yet not reliable.

On the other hand, in probability-based tagging, we apply some of probabilistic approach (such as naive Bayesian classification) and stochastic process approach to tagging. A *Hidden Markov Model* (HMM) is one of the typical examples where tags are considered as states and words as observation symbols. Given word sequences (sentences), we guess tag sequences by means of *Maximal Likelihood Estimation* (MLE) under a simple Markov Model among states.

These investigation are also really useful for agglutinative languages such as Japanese since we need POS tagging. However, given sentences in the languages, we need word segmentation techniques different from POS tagging: we should examine word boundaries to make every word consistent by using postpositional particles. This is not easy to detect the boundaries, and some approach such as "ChaSen" has been proposed based on HMM.

As for compound words in morphological anal-

ysis, there might be no common rule in both kinds of languages. For instance, "c" (Narita Airport) is a compound word ("c" for Narita, "" for Airport) and considered as one word in usual dictionaries. On the other hand, "" (Miyazaki Airport) is not and we should have two words "" (Miyazaki) and "" (Airport). We see similar situation in English. "Ballpark" describes one concept that means a park for baseball playing, contained in a dictionary as one word. However, "Amusement park" consists of two words "amusement" and "park", contained not as one word but as a derivative of "Amusement".

We take a stochastic approach for segmentation. Our idea is that we extract some knowledge from training data and capture them in probability distribution, then we must have much excellent quality of word segmentation.

4 A HIDDEN MORKOV MODEL

In this investigation, we discuss a *Hidden Markov Model* (HMM) which is an efficient stochastic vehicle. HMM is a probabilistic automata based on a simple Markov model where a label corresponds to a state and an observation symbol to an output at a state. Both state transition and output symbols are described in a probabilistic manner. Formally we say HMM has a model $\mathcal{M} = (Q, O, a, b, \pi)$ where Q, O mean a finite set of states and a finite set of output symbols respectively. A transition from a state *i* to *j* arises with probability a_{ij} but it doesn't depend on any other states. This property is called *simple-Markov*. Generating an output symbol $o_t \in O$ depends only on a current state *i* with probability $b_i(o_t)$ where $\sum_t b_i(o_t) = 1$. An initial state happens to be *i* with probability $\pi(i)$.

In HMM, we can observe an (output) sequence but we don't know on which states we are standing and how state transition arises according to a simple Markov model. This is why we say *hidden*. Given a model \mathcal{M} and an observation sequence $X = \langle x_1, ..., x_{i-1}, x_i, x_{i+1}, ..., x_n \rangle$, we like to guess label sequence $Y = \langle y_0, ..., y_{i-1}, y_i, y_{i+1}, ..., y_n \rangle$ that is most likely to generate an output sequence X in a sense of probability. For this purpose, there have been proposed some techniques of dynamic programming such as *Viterbi* algorithm.

Clearly it is hard to determine definitely $\{a_{ij}\}$, $\{b_i(o_t)\}$ and the initial probability π in a model of HMM. This problem is called a *model calculation* of HMM. Usually we do that by means of some machine learning techniques.

One of the typical approach is *supervised learning*. In this approach, we assume *training data* in advance to calculate the model, but the data should be correctly classified by hands since we should extract typical patterns them by examining them. And, another approach is called *unsupervised learning*. Assume we can't get training data but a mountain of unclassified data except a few. Once we obtain strong similarity between the classified data and unclassified data (such as high correlation), we could extend the training data in a framework of Expectation Maximization (EM) approach.

One of the well-known approach in unsupervised learning is a *Baum-Welch* algorithm. The algorithm has been proposed based on *Expectation Maximization* (EM) approach. That is, the algorithm adjusts the parameters many times to maximize the likelihood for the generation of the output symbols given as unsupervised data. The process goes just same as EM calculation, i.e., we calculate the expect value of the transition probability and the output probability, then we maximize them. We do that until few change happens. Baum-Welch approach is easier to apply for model calculation even if small amount of training data is available. However it often provides us with tremendously imprecise results because the approach depends only on initial values.

On the other hand, we can estimate the model directly under supervised learning. We assume enough training data in advance to calculate the model and examine sequences of both states and output symbols. Then we count their frequencies and consider the relative values as the probabilities. Formally, we consider the relative frequency¹ of transition from *i* to *j* as a_{ij} , the relative frequency of the initial state *i* as $\pi(i)$, and the relative frequency of output symbol o_t at a state *i* as $b_i(o_t)$. The model reflects the situation in training data correctly and we could obtain excellent results. However, we should have enough amount of training data to estimate all the possibilities in HMM which is hard, time-consuming and costly.

We take the direct calculation approach to obtain precise models. But how about training data ? This is the *true goal* of this investigation. We generate training data automatically enough to obtain reliable models.

5 MARKOV CHAIN MONTE CARLO METHOD

A *Monte Carlo Method* is a general framework to generate random numbers. Random numbers based on

¹Precisely we say a_{ij} = (frequency of transition from *i* to *j*)/(all the frequencies of transition from *i*).

uniform distribution or normal gaussian distribution can be generated through many intrinsic functions of software, but it is not easy to obtain random numbers according to any probability density function. Generally we can apply a sophisticated algorithm of *rejection sampling*. However, it is not common to obtain these functions over state space A in advance. If we are given non-parametric information such as frequency and empirical knowledge, we can't utilize general sampling algorithms.

A notion of *Markov Chain Monte Carlo* method (MCMC) is a general framework by which we can generate random numbers approximately according to a given distribution in any form. Generally MCMC is not really efficient so that they have been proposed several algorithms of *Gibbs Sampler* which are efficient and easy to implement.

Let us go inside the detail. Given a state space $A = \{1,..,N\}$, a sequence of random variables $X_1,...,X_n$ of length *n* over *A* and a sequence of states $s_1...s_n$ where $s_i \in A$, we can think about a probability $P(X_1 = s_1,..,X_n = s_n)$. We say the probability is *stationary* if we can determine the value functionally on state sequences. Let us note that we can't always determine the probability even if we get exactly same $s_1...s_n$.

Assume we have stationary probability distribution. Given an initial state s_0 and a sequence starting with s_0 , say, $s_0s_1...s_n$, we say the sequence has Markov Chain property if $P(X_0 = s_0, X_1 = s_1, ..., X_n = s_n) = P(X_{n-1} = s_{n-1}, X_n = s_n)$, that is, a probability $X_n = s_n$ under $X_0 = s_0, X_1 = s_1, ...,$ and $X_{n-1} = s_{n-1}$ depends only on the situation of $X_{n-1} = s_{n-1}$. In this case, when we have a transition probability p_{ij} from a state *i* to *j*, we can say $P(X_n|X_0 = s_0) = p^n P(X_0 = s_0)$. Moreover, under some condition², we can prove the existence of *invariant distribution* $\lim P(X_n)$.

MCMC assumes Markov Chain property for state transition, and generates random numbers approximately along the invariant distribution by using non-parametric information. To do that, we generate X_n from X_{n-1} recursively until we get to stationary situation, and then we obtain desired sets of random numbers.

When generating random numbers, very often we like to generate vectors $x_k = (x_1^{(k)}, ..., x_m^{(k)})$ over $\{1, ..., N\}$, but it takes much time and memory to apply MCMC in a straightforward manner. To generate vectors efficiently, we generate each component $x_i^{(k+1)}$ in an one-by-one manner. *Gibbs Sampler* is an algorithm to utilize a conditional probability $P(x_i^{(k)}|x_1^{(k+1)}, ..., x_{i-1}^{(k+1)}, x_{i+1}^{(k)}, ..., x_m^{(k)})$ in a serial manner.

 2 This is called *Ergodic* conditions, though we skip this issue.

It is possible to show that the result state transitions satisfy Markov Chain property if state transitions at vector level satisfy Markov Chain property.

In this experiment, we generate a random number *s* by using Gibbs Sampler. Given a random variable $x_k = (x_1^{(k)}, ..., x_m^{(k)})$, a set of initial (observation) data *Y* with its distribution function ρ , we generate random numbers as follows:

- 1. Generate *m* randomly between the minimum and the maximum given.
- 2. Generate initial values appropriately: $(x_1^{(0)}, x_2^{(0)}, ..., x_m^{(0)})$
- 3. Generate $x_1^{(1)}$ randomly accoding to the distribution $\rho(x_1|x_2^{(0)},...,x_m^{(0)})$.
- 4. Generate $x_2^{(1)}$ randomly according to the distribution $\rho(x_2|x_1^{(1)}, x_3^{(0)}, ..., x_m^{(0)})$.
- 5. We repeat this process and we obtain $x^{(k)}$.

Let us note $x^{(k)}$ comes to $\lim_{k\to\infty} x^{(k)}$ which is a sample according to the invariant distribution $\rho(s|Y)$. We should repeat the process until we get to stationary situation, but practically we can assume *k* is finite.

6 WORD SEGMENTATION BASED ON MCMC

In this section, let us discuss how to generate training data for word segmentation based on MCMC. Since we calculate a model for a HMM directly by counting frequencies along with state transitions and output generation in HMM, we should generate huge amount of training data based on MCMC.

As an initial set of observation data, we are given a set of sentences in Japanese. We translate each sentence by hand into a sequence of morphemes, each morpheme consists of a word and a tag B (means *Begin*) or I (means *Intermediate*). We apply "Chasen" to obtain sequences of words, and then we examine frequencies of the morphemes. For example, let us examine a sentence: "" (I see a dog) We apply morphological analysis to this sentence and we obtain a sequence:

""("I", pronoun), ""(postpositional particle for subjective), ""("dog", noun), ""(postpositional particle for objective), ""("see", verb)

Then we apply word segmentation with B and I by hand:

"(B)", "(I)", "(B)" "(I)", "(B)"

This is equivalent to the sequence³ below:

| | ||

Now we translate each morpheme into a number in an one-by-one manner and count the frequencies. This is the set of initial observation data *Y*. We generate the distribution ρ from *Y*. Now we start with Gibbs Sampler algorithm. Let *m* be a number which is randomly generated between the minimum and maximum lengths of sentences in the initial set. Given a number *m* of words in each sentence and a set of *m* initial values (all these values are generated randomly), we generate a "sentence" (a sequence of words) $s = (s_1, ..., s_m)$ according to ρ . We repeat this step as many as we need.

Let us note that there exists no special meaning in a "sentence" generated by Gibbs Sampler. However, Y contains word information (such as frequencies) and co-occurrence information over any consecutive words (such as collocation). Thus any sentences generated might contain partially consistent information.

For example, as described later, we examine *Patent Information of Instrument in Japan* for experiments. Applying our process, we get plausible sentences in Instrument field like:

/ /y //// / (/in tank/y is/this/to axis/windtunnel/processed/)

We can calculate a model of HMM by using generated sentences.

7 EXPERIMENTS

In this experiment, let us show the effectiveness of our approach for word segmentation. As initial training data, we examine agriculture-related morphemes and instrument-related morphemes from Patent information (1998 and 1999) in Japan⁴.

7.1 Preliminaries

In this experiment, we examine agriculture-related 859 morphemes (289 distinct words) and instrumentrelated 1030 morphemes (229 distinct words) from Patent information (1998 and 1999) in Japan⁵. Then we have generated 8579 random numbers and 7240 random numbers for agriculture field and instrument field respectively. As test data, we have examined other sets of patent information (agriculture-related 3886 morphemes and instrument-related 3569 morphemes) from Patent information (1998 and 1999). We have examined both training and test data by hands. We also examine morphological analysis by Chasen.

Here we examine 3 kinds of experiments to see how useful MCMC plays. We generate several numbers of morphemes and examine the results by MCMC to see how well word segmentation works. Note that we generate training data from small number of initial data. Then we compare our results with the ones of Baum Welch algorithm. Also we examine the results by *Conditional Random Fields* (CRF).

In our experiment, we evaluate the results to word segmentation based on HMM by means of correctness ratio defined as follows:

 $\frac{\text{The Number of Correct Morphemes}}{\text{The Number of Morphemes}} \times 100(\$)$

7.2 Results

Let us show the segmentation results by HMM with several numbers of training data. Note we calculate the HMM model by using frequency of training data which is generated by Gibbs Sampler.

Let us illustrate the results of segmentation in agriculture data in a table 1. As shown, we get the maximum ratio 74.70% with 6000 morphemes. Also we get the improvement of 3.68% between 5000 and 6000 morphemes. Also we show the results in instrument data in a table 2 where the ratio keeps constant.

Table 1: Ratios in Agriculture Data.

| Morphemes | MCMC (%) | BW (%) |
|-----------|----------|--------|
| 997 | 71.23 | 49.69 |
| 2016 | 71.08 | 48.79 |
| 3019 | 70.84 | 48.81 |
| 4002 | 70.51 | 50.64 |
| 5007 | 71.02 | 50.15 |
| 6004 | 74.70 | 50.59 |
| 7022 | 74.60 | 50.49 |

Let us look closer at incorrectly segmented data in agriculture appeared in 6000 morphemes but not 5000 morphemes. There exist 254 occurrences at 5000 morphemes and 206 occurrences at 6000 morphemes, and we see technical terms such as *housing* and *hole* in agriculture. On the other hand, there arises no occurrences in incorrectly segmented data.

We also show the results by Baum-Welch algorithm in tables 1 and 2. In agriculture case, we get the best result 74.70 % of MCMC approach at 6000

³This means a correct sequence in Japanese: "I", "dog", "see"

⁴We have examined NTCIR-3 PATENT information.

⁵We have examined NTCIR-3 PATENT information.

Table 2: Ratios in Instrument Data.

| Morphemes | MCMC (%) | BW (%) |
|-----------|----------|--------|
| 1004 | 77.95 | 49.23 |
| 2002 | 77.58 | 48.42 |
| 2999 | 77.50 | 50.43 |
| 4010 | 78.17 | 47.69 |
| 4996 | 77.58 | 49.17 |
| 6019 | 77.56 | 50.83 |
| 6999 | 77.61 | 48.98 |



Figure 1: Ratios in Agriculture Data.



Figure 2: Ratios in Instrument Data.

morphemes while 50.64 % of Baum Welch approach at 4000 morphemes, 24.04 % better. Similarly in instrument case, we get 78.17 % of MCMC at 4000 morphemes and 50.83 % of BW at 6000 morphemes, 27.34 % better.

Let us see the results in more detail. We show the morphemes which are incorrectly segmented by BW approach. Generally we can say postpositional particles such as "" and "" appear though they can't be there. On the other hand, we see nouns in MCMC approach which depend on application domain and training data.

Finally let us compare the results with CRF.

Table 3: Incorrect Data in Agriculture.

| MCMC | | |
|----------|-----|-------------------|
| Morpheme | Tag | Incorrect Answers |
| vf | В | 62 |
|) | В | 41 |
| , | В | 37 |
| В | В | 35 |
| | В | 32 |
| | В | 31 |
| | В | 30 |
| | В | 26 |
| | В | 25 |
| | В | 19 |

| | Baum- | Welch |
|----------|-------|-------------------|
| Morpheme | Tag | Incorrect Answers |
| А | В | 190 |
| | В | 91 |
| vf | В | 73 |
| j | В | 66 |
| | в | 59 |
| В | в | 55 |
| Z | В | 42 |
| У | I | 41 |
| ł | В | 41 |
| bh | I | 40 |

Table 4: Incorrect Data in Instrument

| MCMC | | |
|----------|-----|-------------------|
| Morpheme | Tag | Incorrect Answers |
| u | В | 56 |
| х | Ι | 33 |
| q[[| Ι | 31 |
| w | В | 26 |
| | В | 19 |
| а | В | 18 |
| | В | 17 |
| • | Ι | 13 |
| М | Ι | 11 |
| tM | Ι | 11 |

| Baum-Welch | | |
|------------|-----|-------------------|
| Morpheme | Tag | Incorrect Answers |
| | В | 145 |
| | В | 84 |
| | Ι | 59 |
| q[[| Ι | 47 |
| х | Ι | 44 |
| | Ι | 42 |
| В | В | 34 |
| z | В | 32 |
| tM | Ι | 29 |
| ł | В | 29 |

In tables 5 and 6, we show the comparison results where CRF approach requires about 13000 morphemes for training. In agriculture case, we get the best result 74.70 % of MCMC approach at 6000 morphemes, so 21.90 % worse. Similarly in instrument case, we get 78.17 % of MCMC, 19.95 % worse.

Table 5: Comparison in Agriculture.

| Approach | Ratio (%) |
|-------------|-----------|
| MCMC (6000) | 74.70 |
| CRF | 96.60 |

Table 6: Comparison in Instrument.

| Approach | Ratio (%) |
|-------------|-----------|
| MCMC (4000) | 78.17 |
| CRF | 98.12 |

7.3 Discussion

Let us discuss what our results mean. We have examined the segmentation results and shown that the result increases at 6000 morphemes in agriculture data, although there exists no sharp distinction in instrument data. This means we need enough amount of data to obtain reasonable results although they depend on application domains. We can say that MCMC is useful to word segmentation since we have generated enough amount of training data (remember we have about 1000 morphemes in advance).

Compared to Baum Welch approach, we have obtained the better results, say more than 25 % better, whichever the number of training data we have. We can apply word segmentation correctly in MCMC approach, since we put I tag correctly to postpositional particles while we can do that hardly in BW approach.

CRF approach is excellent, say more than 20 % better in our experiments. But we need 13000 morphemes in advance for this purpose, while we have assumed about 1000 morphemes in MCMC approach. Also Gibbs Sampler is much efficient compared to CRF.

8 CONCLUSIONS

In this investigation, we have proposed word segmentation based on HMM. More essentially we have discussed how to generate training data automatically based on MCMC and we have shown the experimental results. Then we have shown superior results and MCMC is really useful for this purpose. In this work, we have just discussed MCMC approach for HMM, but we can generalize the techniques to other stochastic frameworks. Then we could have enhanced ideas depending on new kinds of POS tags.

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