

# REAL-TIME FPGA-BASED IMAGE RECTIFICATION SYSTEM

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**Keywords:** Image rectification, Pipeline hardware design, VHDL, FPGA.

**Abstract:** Image rectification is the process of transforming stereo-images as if they were captured using a canonical stereo-system. Computationally intensive tasks, like dense stereo matching, are greatly simplified if performed on rectified images. We developed an efficient pipeline hardware machine which performs real-time image rectification. The design was implemented using VHDL, thus allowing portability on many hardware platforms. The architecture was highly optimized, both in terms of time and resources needed. To increase its flexibility, the design was described based on generics (configuration parameters), which allow reconfiguring different characteristics and behaviour, such as: image size, number of precision bits, memory cache complexity. We also analyze the performance of the implemented solution on a VirtexE600 FPGA device.

## 1 INTRODUCTION

The process of generating dense disparity maps using stereo-images is a computationally intensive task. It involves finding for every pixel in one image, the correspondent pixel in the other image(s). Correct corresponding point is defined as the pixel representing the same physical point in the scene. Normally this is a 2-D search problem, but it can be reduced to a 1-D search problem if the images were captured using a canonical stereo-system, almost impossible to obtain in practice. However it is possible to apply a rectification process over the images, which will make them appear as if they were captured using a canonical configuration. The rectified images can be thought of as captured by a new stereo-system, obtained by rotating the original cameras around their optical centers.

Image rectification consists in transforming the images so that the epipolar lines are aligned horizontally or vertically.

The rectification process can be divided in two major steps:

1. offline calculation of rectification matrices for each camera – performed once for a given calibrated stereo-system;

2. online image rectification from sequence to sequence.

As the second phase is time consuming, a need to be performed by additional hardware is encountered. In this purpose, current paper introduces a pipeline oriented hardware architecture, which was implemented in a FPGA module and performs online image rectification. The hardware architecture is described using VHDL, the image resolution can be dynamically set using generics (configuration parameters) and the entire module is technology independent though it can be ported on any FPGA device. In this context we are able to take advantage of the great speed technology that appears on market, processing time being strictly dependent on it.

## 2 RELATED WORK

Most of the previously stereovision hardware machines that appeared in literature had as purpose other tasks which involved image rectification as a pre-processing step. Moreover they don't really mention any details about the rectification method used within this step, nor specific description about

the hardware design. However, Fusiello, Trucco and Verri (1997) and Fusiello (1998b) present a rectification process based on constraints imposed on the rectified images: principal point in position (0,0), equal focal lengths, unchanged optical centers. A similar method was presented later (Fusiello, Trucco and Verri, 1998a), (Fusiello, Trucco and Verri, 2000). It has the same principles as the previous one, but the constraints differ a little.

A general purpose reconfigurable computer, the PARTS system (Woodfill and Herzen, 1997), consists of 16 tightly coupled Xilinx 4025 FPGAs and 16 1MB SRAMs. Used for the task of stereovision, the system achieves a performance of 42 fps at computing 24 disparities on 320x240 pixel images.

The team from Tyzx developed a hardware system for stereo depth computation implemented in ASIC (Woodfill, Gordon and Buck, 2004). The design is based on a highly parallel pipelined architecture. It uses a pair of two stereo cameras which connect directly to the board, though the latency is reduced and the PCI Bus and memory are not burdened with image data. Each camera is calibrated to define basic imager and lens parameters, which are used to rectify the images.

Jia et al (2004) introduce a miniature stereovision system which generates high-resolution disparity maps using a trinocular system attached to a hardware module implemented in FPGA. Its frequency is 60 MHz, reaching up to 30 fps. The depth is calculated using 64 disparity levels and 256 disparity levels with interpolation. Epipolar rectification is used in order to simplify the stereo correspondence.

### 3 IMAGE RECTIFICATION METHODOLOGY

The idea behind image rectification consists in calculating a rectification matrix, for each camera, based on the Perspective Projection Matrices characterizing both original ( $\mathbf{P}_o$ ) and defined canonical ( $\mathbf{P}_c$ ) stereo systems. Knowing the point coordinates in the original image ( $\bar{\mathbf{i}}_o$ ) and the optical centre ( $\mathbf{c}$ ) of the camera, its correspondent point in World Reference Frame (WRF) is:

$$\mathbf{w} = \mathbf{c} + \mathbf{Q}_o^{-1} \cdot \bar{\mathbf{i}}_o \quad (1)$$

where:

$$\bar{\mathbf{i}}_o = [u_o, v_o, S_o]^T \quad \mathbf{w} = [X, Y, Z]^T \quad \mathbf{P}_o = [\mathbf{Q}_o | \mathbf{q}_o]$$

Considering the projection formula from WRF onto the rectified image (obtained without moving

the optical centre of the camera), the new position of the image point becomes:

$$\bar{\mathbf{i}}_r = \mathbf{P}_c \cdot \begin{bmatrix} \mathbf{w} \\ 1 \end{bmatrix} = [\mathbf{Q}_c | \mathbf{q}_c] \cdot \begin{bmatrix} \mathbf{w} \\ 1 \end{bmatrix} = \mathbf{Q}_c \cdot (\mathbf{c} + \mathbf{Q}_o^{-1} \cdot \bar{\mathbf{i}}_o) + \mathbf{q}_c \Rightarrow \quad (2)$$

$$\bar{\mathbf{i}}_r = \mathbf{Q}_c \cdot \mathbf{c} + \mathbf{q}_c + \mathbf{Q}_c \cdot \mathbf{Q}_o^{-1} \cdot \bar{\mathbf{i}}_o$$

where:

$$\bar{\mathbf{i}}_r = [u_r, v_r, S_r]^T$$

$$\mathbf{Q}_c \cdot \mathbf{c} + \mathbf{q}_c = 0 \quad - \text{optical centre is projected in (0,0)}$$

In this way the corresponding position in rectified image can be calculated for each pixel from original image:

$$\bar{\mathbf{i}}_r = \mathbf{Q}_c \cdot \mathbf{Q}_o^{-1} \cdot \bar{\mathbf{i}}_o = \mathbf{T} \cdot \bar{\mathbf{i}}_o \quad (3)$$

where:

$$\mathbf{T} = \mathbf{Q}_c \cdot \mathbf{Q}_o^{-1} \quad - \text{rectification matrix}$$

It has to be stated that rectifying an image is not a simple product between the rectification matrix and the vector representing the current pixel coordinates in the image. Practically the image coordinates are integer values and the elements of the rectifying matrix are real numbers. The approximation of the corresponding points coordinates could distort the rectified image. So for each integer coordinate of the rectified image the corresponding point onto the original image is computed using the inverse of the rectifying matrix:

$$u_o = t_{11} * u_r + t_{12} * v_r + t_{13} \quad (4)$$

$$v_o = t_{21} * u_r + t_{22} * v_r + t_{23} \quad (5)$$

where:

$$\bar{\mathbf{i}}_o = (u_o, v_o, 1)^T \quad - \text{point coordinates in original image}$$

$$\bar{\mathbf{i}}_r = (u_r, v_r, 1)^T \quad - \text{point coordinates in rectified image}$$

$$\mathbf{T}^{-1} = \begin{bmatrix} t_{11} & t_{12} & t_{13} \\ t_{21} & t_{22} & t_{23} \\ t_{31} & t_{23} & t_{33} \end{bmatrix}$$

Such a point will have real coordinates and will be situated between four pixels (fig. 1). In order to maintain clarity, a bilinear interpolation of the four neighbouring pixels' intensities will give the resulting intensity in the rectified image:

$$u_o = u + d_u \quad (6)$$

$$v_o = v + d_v \quad (7)$$

$$\mathbf{I}_r(u_r, v_r) = \mathbf{I}_o(u, v) * (1 - d_u) * (1 - d_v) + \mathbf{I}_o(u + 1, v) * d_u * (1 - d_v) + \mathbf{I}_o(u, v + 1) * (1 - d_u) * d_v + \mathbf{I}_o(u + 1, v + 1) * d_u * d_v \quad (8)$$

where:

$$\mathbf{I}_r \quad - \text{rectified image intensity bitmap}$$

$$\mathbf{I}_o \quad - \text{original image intensity bitmap}$$

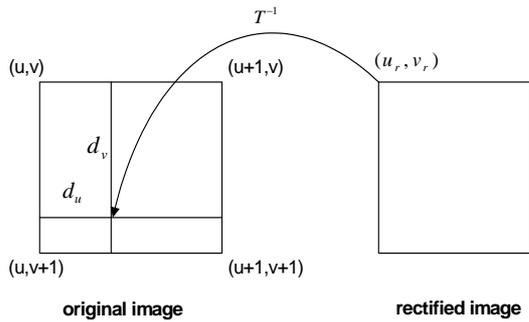


Figure 1: Image rectification methodology.

## 4 HARDWARE DESIGN

There are some issues to be discussed before giving any details about the hardware architecture. First of all the entire architecture was described using VHDL. For that reason, some features could be described using generics: image dimension, image area to be rectified, precision. The inverse of rectification matrix is also given using generics. The design can be optimized in matters of speed and resources to be used inside the FPGA device. Using generics, one can choose for a complex design handling more situations, giving greater precision in results, or choose for a simpler design which would need fewer resources, but would handle less situations or even worse precision.

The input consists in the original image and the output will be the rectified image. Practically, the process consists in parsing the rectified image pixel by pixel and applying the equations (4), (5) and (8) in order to determine their intensity. The hardware architecture was divided in three major parts (fig. 2):

- coordinate generator and 2-D transformation block;
- source image reader;
- interpolator.

### 4.1 Communication Protocol

Each of the three blocks is an independent pipeline module. They communicate using a very simple one-way communication protocol called DFLOW (Data FLOW – fig. 3).

The handshaking is simple: when source has valid data, it outputs the data onto the DATA bus and enables the WEN signal; when destination is ready to receive data it sets the RDY signal high; when both RDY and WEN are set, data transfers

take place on each clock cycle. In this way, continuous transfer is possible.

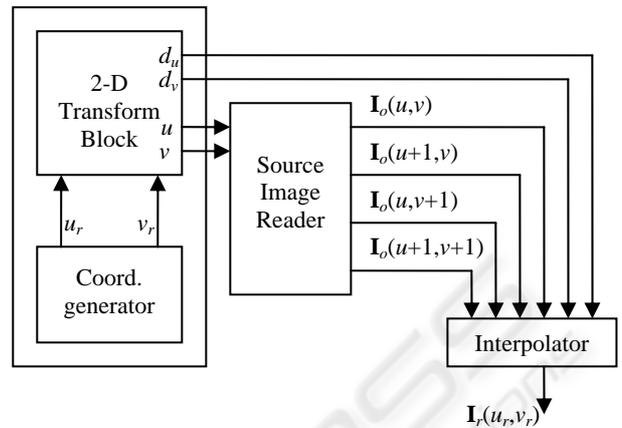


Figure 2: Image rectification hardware architecture.

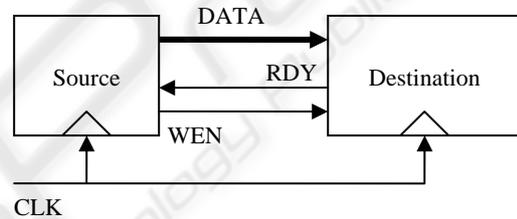


Figure 3: DFLOW communication protocol.

### 4.2 Coordinate Generator and 2-D Transformation Block

This part of the architecture has as purpose the calculation of  $u$ ,  $v$ ,  $d_u$  and  $d_v$  using formulas (4) and (5). As the relations are similar, the same hardware unit can be duplicated to perform all operations. We will discuss further how to implement relation (4).

It can be noticed that only adders and multipliers should be involved, but multipliers are slow and complex modules. Another observation is that  $u_r$  and  $v_r$  are increasing by 1 and rectification matrix elements are real number constants, though it is possible to perform multiplication by using repeated sums, on each clock cycle and storing the temporary result in a buffer (see fig. 4).

Any unit of the module, which is driven by a clock signal, contains a register on the output. Such a measurement was taken in order to insert fast stages in the pipeline. As the entire architecture was designed to work with integers, generics like  $t_{11}$ ,  $t_{12}$ ,  $t_{13}$  had to be shifted to the left with a certain number of precision bits. This number varies depending on the stage of the pipeline architecture. For example,

in the first stage where  $t_{11}$  and  $t_{12}$  are summed repeatedly for a certain number of times, more precision bits are needed than the stage where  $t_{13}$  is added. The idea is to use only  $k$  precision bits when calculating  $u_r * t_{11}$  and  $v_r * t_{12}$  and only  $l$  (smaller than  $k$ ) precision bits when performing the rest of the sums. In this way a lot of FPGA resources will be saved for other purposes. It can be proved that for  $f$  precision bits wanted in the final result,  $k$  and  $l$  should respect the following relations, so as to obtain the optimal solution in terms of resources required:

$$l = f + 4 \tag{9}$$

$$k = f + 2 + \log_2(W + H) \tag{10}$$

where:

$W, H$  – image weight and height

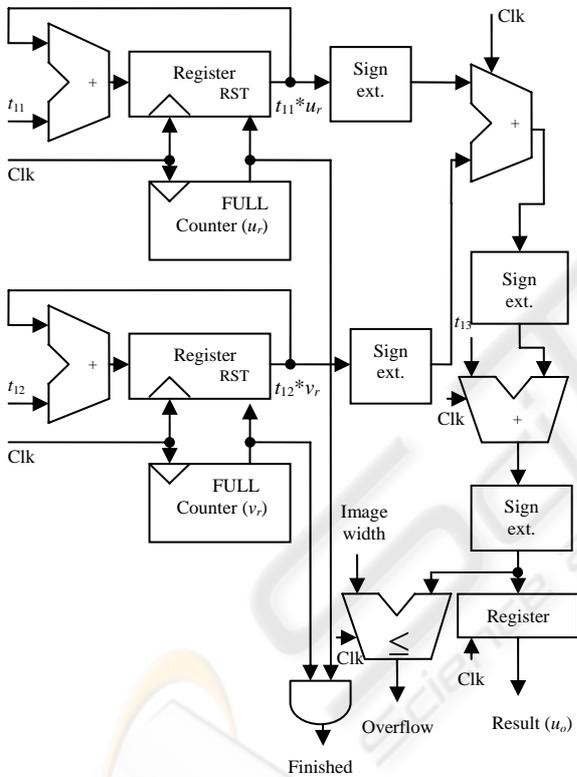


Figure 4: Coordinate generator and 2-D transformation block.

The design in figure 4 is configured using a set of generics:

- $t_{11}, t_{12}, t_{13}$  – first row of rectification matrix;
- $i$  – number of bits to represent the integer part of the result;
- $f$  – number of bits to represent the fractional part of the result;
- image width.

The output lines are:

- Finished – is asserted when the entire image was rectified;
- Overflow – is asserted when the resulting position in the original image is outside;
- Result – represents the result data bus; it is represented using  $i + f$  bits.

### 4.3 Source Image Reader

The large amount of storage space needed for memorizing the acquired frames in a stereo vision system well exceeds the capabilities of internal BRAM units. The solution is to use external memories, which, in most cases, are either SRAM or SDRAM. The former has the advantage of simplified access, while the latter has a higher capacity. Since many of the FPGA-PCI boards present on the market today provide SDRAM modules for external storage, we designed a component that can efficiently fetch the pixels to be used as the input for the interpolator.

The input of the image reader component consists of a stream of pairs of pixels coordinates in the image space. For each such pair of coordinates, the image reader should provide as output a tuple of 4 pixel intensities, corresponding to a 2x2 window whose top-left corner is located at these coordinates in the image that is stored inside the external storage.

The difficulty of the task resides not in fetching the pixel values, but rather doing this in an efficient manner. It can be noticed that while the window sweeps the image, it usually does so by moving in successive partially overlapping positions. Even more conveniently, data is stored inside the SDRAM in 32-bit words, that is, 4 successive pixels are accessible by performing one read operation. As a consequence, it is possible to build an efficient cache that can both provide pixels at a much higher rate and can also significantly reduce the memory load.

The cache will store a window of 2x2 32-bit words (16 pixels) from the image. The operations performed by the cache will be:

- read a 32 bit word into one of the positions of the cache;
- shift the cache in one of the 8 possible directions;
- send the contents of a 2x2 pixel window over the output port.

The phases of the computation performed inside the image reader module are described in what follows (fig. 5):

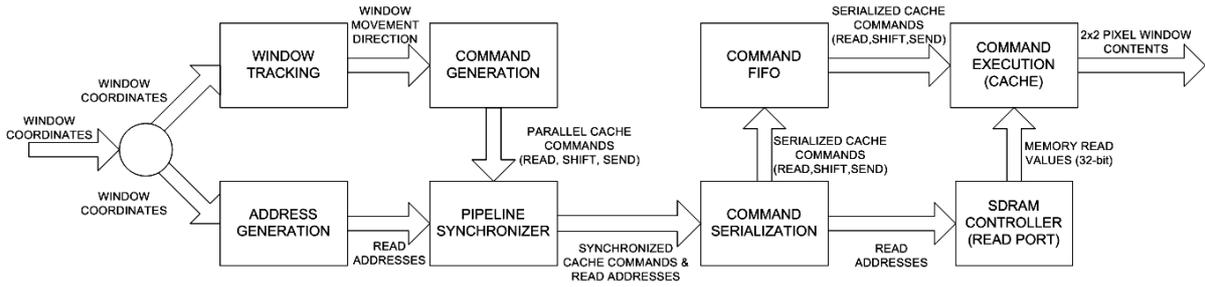


Figure 5: Flow Diagram for Image Reader module.

Window tracking involves detecting the direction in which the 2x2 pixel window moves relative to its previous position. It is a two stage pipeline process, in which the difference between the new and old coordinates is computed on a per-axis basis. Differences corresponding to -1, 0 and +1 are detected and encoded using a direction encoder, described in table 1.

Table 1: Direction encoding.

RST	U-	U0	U+	V-	V0	V+	DIR
1	X	X	X	X	X	X	NEW
0	0	1	0	0	1	0	SAME
0	0	0	1	0	1	0	0 <sup>0</sup>
0	0	0	1	1	0	0	45 <sup>0</sup>
0	0	1	0	1	0	0	90 <sup>0</sup>
0	1	0	0	1	0	0	135 <sup>0</sup>
0	1	0	0	0	1	0	180 <sup>0</sup>
0	1	0	0	0	0	1	225 <sup>0</sup>
0	0	1	0	0	0	1	270 <sup>0</sup>
0	0	0	1	0	0	1	315 <sup>0</sup>
0	Otherwise						NEW

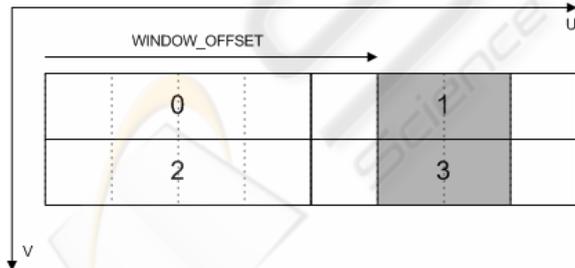


Figure 6: The internal structure of the cache.

Based on the coordinates of the window and the movement direction provided by the window tracker pipeline, command generation block has the task to create the set of parallelized commands that should be carried out by the cache in order to make available all the pixels inside the window. The output of the command generator will be:

- read – a vector of 4 bits, read(*i*) being set if it is necessary to perform a read operation

for word number *i* in the cache (word numbering inside the cache is depicted in figure 6);

- shift – one of the 8 shift directions or SHIFT\_NONE if no shift needs to be carried out;
- offset – the offset of the 2x2 pixel window inside the cache. This will be needed for carrying out the sending operation.

At most 4 read operations may result after the command generation phase, corresponding to the 4 32-bit word positions in the cache. The addresses for the 4 words can be immediately derived from the coordinates of the 2x2 pixel window, by obtaining the byte address ( $v \times img\_width + u$ ) and rounding it down to the nearest 32-bit word (fig. 7).

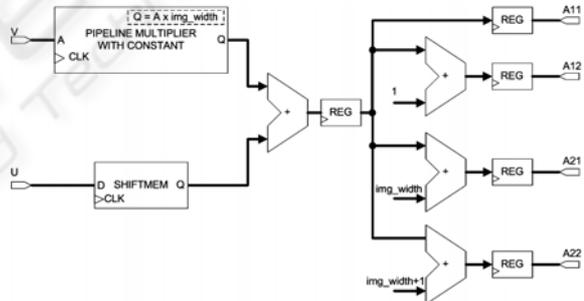


Figure 7: Read addresses computation.

Based on this observation, it is possible to compute the addresses in parallel with the window tracking and command generation phase, thus reducing the overall pipeline length. As address computation involves the use of one constant-argument pipeline multiplier, we developed a highly optimized component based on Booth's Algorithm.

The Address Generation branch and Window Tracking + Command Generation branch (fig. 5) might not have the same number of stages. For that reason, a Pipeline Synchronizer based on DFLOW handshaking protocol was introduced.

Some of the commands may not be executed in parallel by the cache. This problem is solved using a

Command Serialization unit. The following constraints must be met:

- only one read may be performed per clock cycle;
- cache shifting must take place before or in the same clock cycle as the first read operation;
- send operation must be performed after the last read for current window position is completed and before or in the same clock cycle as the first read or shift for the next window position takes place.

Due to the fact not all commands will involve a read operation from memory, using a Command FIFO unit will allow them to be executed while SDRAM Controller performs readings for other commands. The result is a speedup in the process.

The final stage of the image reader pipeline is the cache. Its function is to process the serialized commands coming from the Command Serialization unit through the Command FIFO together with the data values coming from the SDRAM Controller. The control logic will always schedule the shift operation in the first clock cycle after a command is loaded (if there is no pending send command), since it is always possible to execute it. Read operations are scheduled as soon as the data from SDRAM Controller becomes available. Send operations are scheduled last, after the last read operation has been completed. Send operations will actually be executed some time after the last read operation, when the output becomes ready. However, in order to ensure continuous operation of the cache, a send command may be pending while another command is being loaded into the input buffers, allowing the sending of data to be overlapped with the arrival of the next command. Nevertheless, if the sending operation continues to remain pending because the destination is not ready to receive data, the next command will not start execution. The cached data is kept in registers which are capable of executing the shift and read operations. The input of each of the four 32-bit registers is connected, through a multiplexer, to each of the other 3 registers and to the data buffer. This is, the most expensive part of the image reader component both in terms of resources and propagation delay. Further optimizations can be carried out by noticing that, in applications like image rectification, the cache will not be performing shift operations in all of the 8 directions, though some of the logic may be eliminated. Boolean generics, for each window movement direction, were introduced in the VHDL description, to allow flexible design configuration.

#### 4.4 Bilinear Interpolator

This is the final stage of the image rectification architecture. It performs the bilinear interpolation of the four neighboring intensities from the original image, according to  $d_u, d_v$  offsets.

This part includes a set of adders and multiplication modules. We modified formula (8) in such a way that the number of multiplication units decrease to minimum possible. The reason is that a multiplication module requires a lot of pipeline stages. The more consecutive multipliers we have, the greater the number of pipeline stages we get. An optimized solution is presented in what follows.

Consider the following bilinear interpolation formula:

$$P = a*(1-d_u)*(1-d_v) + b*d_u*(1-d_v) + c*(1-d_u)*d_v + d*d_u*d_v \tag{11}$$

This could be written as:

$$P_1 = a*(1-d_u) + b*d_u = a + (b-a)*d_u \tag{12}$$

$$P_2 = c*(1-d_v) + d*d_v = c + (d-c)*d_v \tag{13}$$

$$P = P_1*(1-d_v) + P_2*d_v = P_1 + (P_2-P_1)*d_v \tag{14}$$

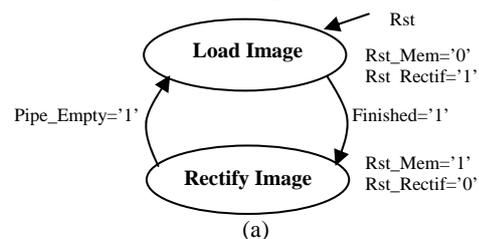
As formulas (12) and (13) can be performed in parallel, the interpolation process was optimized to only two consecutive multiplication stages. Also, the number of needed resources was reduced because the number of multiplication units decreased from 8 to 3.

#### 4.5 Top-level of the Architecture

The entire rectification process was designed to have two major phases:

1. image load into memory;
2. image transformation.

First phase consists in loading the image from the software module into the SDRAM through the PCI bus. For that reason, a counter generating the address for the SDRAM is used. Communication with memory is performed using the DFLOW protocol. Second phase is designated for rectifying the image in memory. The Address Generator module is disabled and the Image Transformation module is put at work. A description of the top-level control unit and dataflow is presented in figure 8.



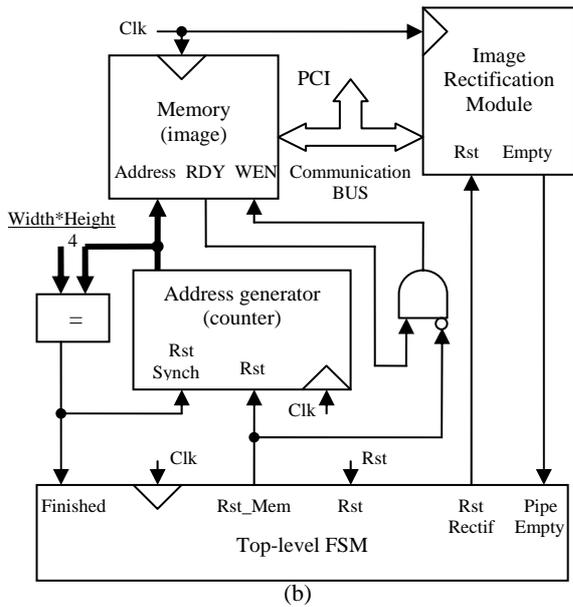


Figure 8: Top-level view of Image Rectification System: a) control unit; b) dataflow.

### 5 EXPERIMENTAL RESULTS

The hardware design was tested using a Strathnuey board equipped with a Ballyderl DIME module containing a Virtex FPGA (model V600EFG680) and 128MB SDRAM. The images (640x512 pixels) were sent from PC through the PCI bus and the rectified images were read back into the PC, registering a total time of 17.5 ms (57 fps). Such amount of time is due to the fact the PCI communication between PC and FPGA-PCI board is very slow. Practically, the design working at a frequency of 80 MHz, waits until the image download and upload through PCI is performed. On the other hand, the time required only for rectifying the image (no upload and download) is about 4.5 ms (222 fps). Download time can be eliminated if images will be captured directly from camera and not through PCI.

The resulting images were tested against those obtained with a software reference implementation. The similitude between both solutions can be seen in figure 9 (dark patterns on the margins represent pixels from the rectified image with correspondents outside the original image).

We performed several tests concerning chip area usage statistics. For example, by reducing the number of possible window movement directions, the amount of chip area and operating frequency can be improved. In the case of the image rectification

task, the image is swept using successive lines. This implies that the window movement direction can take at most 3 values of the 8 possible ones. The improvement in performance is shown in figure 10. Chip area improvement is the most significant, from around 11% down to around 7%.

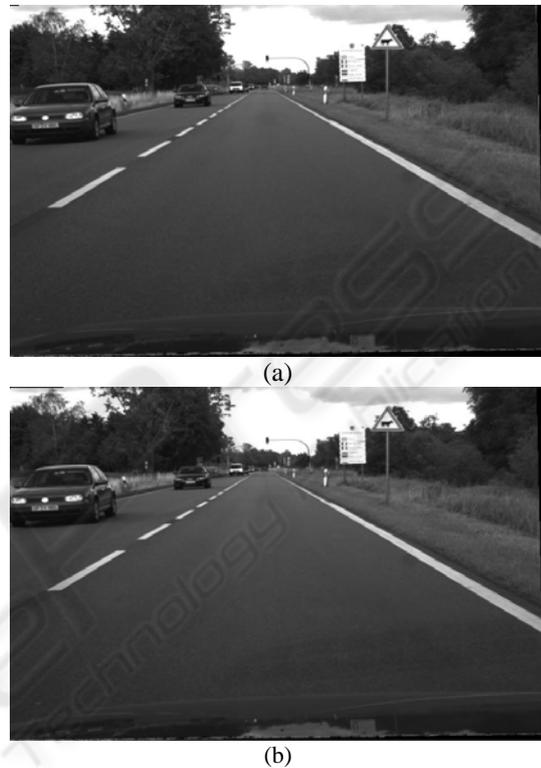


Figure 9: Rectified images: a) hardware results; b) software results.

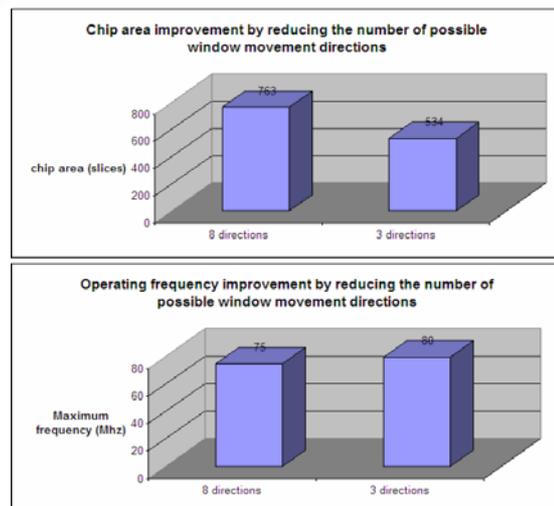


Figure 10: Performance can be improved by removing unused window movement directions.

To test the performance of the Image Reader design, different image rotation matrices have been

used. Figure 11 shows the variation of the throughput (megapixels/second) as a function of the rotation angle, measured at a 75 MHz frequency (memory controller operating at the same frequency).

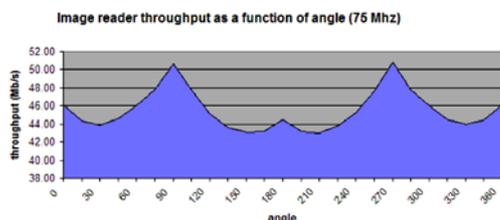


Figure 11: The throughput of the image reader as a function of image rotation angle at a frequency of 75 MHz.

The variation of the throughput is 14% of the maximum value, with a minimum of 43 Mb/s (obtained at  $150^{\circ}$  and  $210^{\circ}$ ) and a maximum of 50.6 Mb/s (for  $90^{\circ}$  and  $270^{\circ}$ ). It can also be noticed that the performance for a  $0^{\circ}$  angle is less than the one obtained at  $90^{\circ}$ . The reason is that, in the first case, when a cache miss is found, two read operations (corresponding to words 1 and 3 of the cache) are requested at once by the Command Generator and the cache must stall for one clock cycle, to perform the second read. In the second case, a miss will usually generate one read operation (words 2 and 3), and will not stall the pipeline (with the exception being the situation in which the window is in the middle of the cache - offset 3 - in which both words 2 and 3 will require reading).

## 6 CONCLUSIONS AND FUTURE WORK

A flexible and scalable solution has been developed for the problem of image rectification, providing real-time results with configurable parameters such as: image resolution, number of precision bits to be used in calculus. The possible window movement directions can be freely configured as to reduce chip area usage and increase accepted clock frequency.

Image quality results proved to be very close to the ones obtained using a reference software implementation. The description was made independent of the underlying technology, though it can be ported easily on other platforms.

The processing time is very small, but the transfer of images through the PCI bus proved to be the weakest part (tests were performed with a slow FPGA from VirtexE family). A solution to eliminate

such inconvenience would be to link the camera directly to the FPGA board and implement, inside the chip, an architecture which knows the communication protocol with the camera. In this way, only resulting images will have to be transferred through the PCI, thus saving a lot of time.

An alternative solution to be investigated in the future consists in replacing the Coordinate Generator and 2-D Transformation blocks with a lookup table containing (with sub-pixel precision) the position in original image, of each pixel from rectified image. In this case the memory workload will increase inefficiently, though several SDRAM/SRAM modules would be needed to avoid such inconvenience. On the other hand, a lookup table based system might be used for more complex processes, like image rectification combined with image un-distortion or ground plane stereo-correction, which require extremely complex operations, difficult to be implemented in a fast pipeline fashion.

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