

A SYSTEMATIC APPROACH TO MULTIPLE DATASETS VISUALIZATION OF SCALAR VOLUME DATA

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Abstract: Many applications require simultaneous display of multiple datasets, representing multiple samples, or multiple conditions, or multiple simulation times, in the same visualization. Such multiple dataset visualization (MDV) has to handle and render massive amounts of data concurrently. We analyze the performance of two widely used techniques, namely, isosurface extraction and texture-based rendering for visualization of multiple sets of the scalar volume data. Preliminary tests performed using up to 25 sets of moderate-size (256^3) data show that the calculated times for the generation and rendering of polygons representing isosurface, and for the mapping of a series of textured slices increase non-uniformly with increasing the number of individual datasets. Both techniques are found to no longer be interactive with the frame-rates dropping below one for six or more datasets. To improve the MDV frame-rate, we propose a scheme based on the combination of hardware-assisted texture mapping and general clipping. In essence, it exploits the 3D surface texture mapping by rendering only the externally visible surfaces of all volume datasets at a given instant, with dynamic clipping enabled to explore the interior of the data. The calculated frame-rates remain above one and are substantially higher than those with the other two techniques.

1 INTRODUCTION

Visualization of three-dimensional scalar data has been studied extensively over last two decades. Tremendous challenge is often imposed by the size of the volume data: Either the dataset is too massive to exhaustively visualize or there are multiple datasets to be visualized simultaneously. In this paper, we have focused on the latter case, that is, *multiple datasets visualization* (MDV) by which we mean that more than one datasets of a given type are concurrently rendered in the same visualization. Although multiple datasets have previously been visualized/analyzed in many occasions (Schulze and Forberg, 2004; Crutcher et al., 1996; Abrams and Shaffer, 1996), there exists a little work, if not at all, towards addressing MDV in a systematic way.

We believe that there is no need to over emphasize on the importance of MDV. It is not always possible to make an inference based on single dataset so one needs to compare several datasets in some effective way. So visualization should be able to handle, multiple datasets at the same time, representing multiple cases of interest so

that important relationships and differences among these cases can be better understood.

Examples of multiple datasets, which require simultaneous visual analysis, are abundant. Here, we consider 3D charge density distributions in real material systems, which are investigated on routine basis by parallel quantum mechanical simulations (Codes, 2005). The resulting multiple charge density datasets of interest may represent different samples, or different temperatures or different pressures or different simulation times. One might be interested in comparing the charge distribution for different (say four) types of vacancy defects in a given crystal, say, Mg-, Si-, O1- and O2-defects in an important Earth forming mineral MgSiO_3 perovskite. Or the interest might be in investigating the effect of pressure by displaying multiple datasets corresponding to different pressure conditions (say Mg-defect at eight different pressures) at the same time. Or one might need to visualize together ten different datasets as a function of temperature. Or, if one is interested to look at outputs taken at different times of simulation together, the number of datasets can be arbitrarily large.

Two natural approaches to the *multiple dataset visualization* appear to be a) an extension of the standard visualization methods to handle multiple datasets and b) a parallel processing (using multiple CPUs and/or multiple display screens) of visualization to permit real-time navigation through multiple datasets. In this paper, we adopt the first approach because it enables one to perform MDV with easily available resources such as PC desktops. A large number of 3D scalar visualization techniques currently exist, and their performance is often justified for *single dataset visualization* (SDV) (Meibner et al. 2000). Common examples include the isosurface extraction (Lorenson and Cline, 1987), raycasting (Levoy 1990), splatting (Westover, 1990), shear-warp (Lacroute and Levoy, 1994) and texture mapping (Cabral et al, 1994). Some of these approaches are considered here in the context of the simultaneous visualization of multiple datasets.

It is natural for one to expect that all standard volume visualization techniques are equally applicable to the case of visualization of multiple datasets. However, this expectation is true to a great extent but not entirely. MDV involves simultaneous processing of more than one datasets. This means that the visualization process should become slower by a factor of N or higher for N number of datasets in comparison with single dataset, due mainly to the increased amount of data. The need for larger memory space (which may eventually result in a substantial swapping) and bigger display area (which involves the processing of more pixels) can further slow down the process. One other major issue is that MDV is no longer guaranteed to be interactive. Our preliminary performance tests show that the SDV techniques studied here become increasingly slow as the number of datasets increases. Even for the data size of 256^3 , the frame-rate is less than 1 for six or higher sets thereby indicating the loss of interactivity in MDV.

Interactivity plays a crucial role in any volume visualization and even more so in MDV because it gives the user with immediate visual feedback. The user often needs to repeat visualization process several times, in part or full, to explore a given dataset from various prospects. For instance, the user might need to extract a series of isosurfaces corresponding to different reference (or threshold) scalar values. In the case of clipping, one might need to examine many clipped views at different locations, orientations and sizes. Even the direct volume rendering, although no information is thrown away, poses the difficulty of interpreting the cloudy representation of the volume data. So the extraction of a more complete information requires several of interaction modes like navigation, changes

of transfer functions, region of interest mode, rotation, scaling, and some more sophisticated classification modes be supported in a given visualization.

In this paper, we analyze the performance of two standard volume visualization techniques, namely, isosurface extraction and texture-based volume rendering in the case of multiple datasets. Doing so requires handling of massive amounts of data, which introduces several issues related to memory, resolution and interactivity. Our current focus is to deal with the interactivity issue (by calculating the frame-rate), which arises even in the case of multiple datasets of moderate sizes, e.g., 256^3 . This size of data is very common for today's many scientific and engineering applications. Also, this size can be handled by the texture mapping support of the today's general-purpose graphics hardware. As an effective solution to improving the interactivity, we have adopted a MDV scheme based on 3D surface texture mapping and general clipping. We limit the maximum number of individual datasets to be visualized together to 25 in this study.

2 RELATED WORK

Several visualization methods are available for volumetric scalar datasets. Indirect methods extract an intermediate geometric representation of the surfaces from the volume data and render those surfaces via conventional surface rendering methods, e.g., isosurfaces (Lorenson and Cline, 1987). On the other hand, direct methods render the data without generating an intermediate representation and as such, they are more general and flexible, e.g., texture-based rendering (Cabral et al. 1994, Wilson et al. 1994). In addition to supporting direct volume rendering, texture mapping has also been used in conjunction with clipping (Weiskopf et al. 2003). Both the strengths and weaknesses of all these techniques have been assessed in a wide variety of single dataset (Meibner et al. 2000).

To the best of our knowledge, no systematic analysis and practical evaluation of the current volume visualization methods have yet been reported in the case of multiple datasets. We choose to examine the isosurface- and texture-based visualization methods for MDV for several reasons: First, the former is an indirect method whereas the latter is a direct method. Second, the former is software-based approach whereas the latter is the hardware-assisted approach. Third, isosurface is so widely used whereas texture mapping is faster than the most volume visualization techniques.

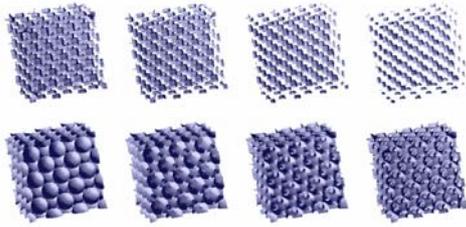


Figure 1: Isosurfaces for eight sets of the electronic charge density data for MgO at different compressions (compression increasing from the lower left to the upper right). The structures represent the charge distribution around O ion sites.

Due to recent advances of commodity graphics hardware, texture-based rendering is able to achieve acceptable frame-rates with high image quality (Wilson et al. 1994; 2002; Weiler et al. 2000; Cullip and Newman, 2003). Clipping combined with texture-based rendering can exploit advanced fragment operations supported by graphics hardware. For example, Van Gelder and Kim (1996) have used clip planes. Techniques for volume clipping with complex geometries, which are based on the depth structure and voxelization of the clip geometry and also involve subsequent shading of the clipped surfaces, have been proposed (Weiskopf et al. 2002; 2003). In the volume clipping based on stencil tests, stencil buffer entries are set at only those positions where the clip plane is covered by an inside part of the clip geometry (Westermann and Ertl, 1998). There are also techniques, which have exploited isosurface clipping (Forguson, 1992) and interactive clipping combined with dual-resolution texture-based volume rendering (Khanduja and Karki, 2005).

3 MDV WITH ISOSURFACE

An isosurface is the 3D surface representing the locations of a constant scalar value within a volume. Common approaches for generating isosurfaces include the Marching Cubes algorithm for generating isosurface polygons on a voxel-by-voxel basis (Lorenson and Cline, 1987), the Dividing Cubes approach of subdividing threshold voxels into smaller cubes at the resolution of pixels (Cline et al, 1988), and raytracing with an analytic isosurface intersection computation (Parker et al. 1998). We use the Marching Cubes algorithm to extract isosurfaces corresponding to a given threshold value from multiple sets of data at the same time. The essence of the algorithm remains the same for MDV: It examines all voxels of each volume data (one by one), and determines, from the arrangement of

vertex values above or below a threshold value, if and how an isosurface would pass through these elements. The algorithm thus processes one voxel at a time, and generates its isosurface geometry immediately before moving to the next voxel. Once all the voxels of one volume data are processed and the corresponding isosurface is extracted, the same algorithm is repeated for each other volume data in a given multiple set. We have visualized up to twenty-five sets of 256^3 data using Marching Cubes algorithm. Figure 1 shows MDV for the eight sets of the simulated charge density of MgO as a function of pressure.

4 MDV WITH 3D TEXTURE RENDERING

The texture mapping approach uses 2D or 3D textured data slices, combined with an appropriate blending factor (Cabral et al. 1994; Wilson et al, 1994). In the case of 2D textures, three stacks of slices, one for each major viewing axis, are stored and one most parallel to the current viewing direction is chosen. Hardware does bilinear interpolation in a 2D texture only and opacity changes with rotation. As such, image quality is best

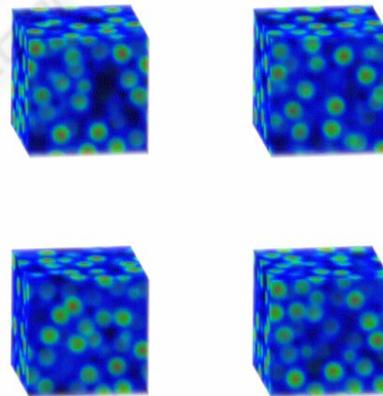


Figure 2: Texture-based MDV of four sets of electronic charge density distributions of MgO. The color and opacity values for each pixel are based on the density value associated with that pixel: A multiscale RGB color mapping is used: B represents values from 0 to 0.05, G is added to represent values up to 0.4 and then R is increased and both B and G are decreased for higher values.

only when the slices are parallel to the view plane. On the other hand, the 3D texture approach can sample the data in all directions freely so the slices can always be oriented perpendicular to the viewer's line of sight. Image quality is independent of the viewing direction. The intrinsic trilinear hardware

interpolation allows us to perform supersampling, i.e., to use an arbitrary number of slices with an appropriate resampling on the slices. Only one single 3D texture needs to be loaded thus requiring one third of the memory, compared to the case of 2D textures.

We apply the 3D texture-mapping hardware to support MDV. The first step is to load the volume data into a 3D texture; it involves simply reading a set of images or shading data points. All datasets are loaded one by one to generate multiple 3D textures. The second step involves choosing the number of slices perpendicular to the viewing direction for each texture. The number of slices is often chosen to be equal to the volume's dimensions, measured in texels. For instance, each dataset of 256^3 needs 256 slices. The third step is to use texture coordinate generation to texture the slice properly with respect to each 3D texture data. Finally, the textured slices are rendered from back to front, towards the viewing position, with appropriate blending performed at each slice. In this study, OpenGL supported "over" blending function is used. As the viewpoint and direction of view change, one needs to recompute the data slice positions and update the texture transformation matrix as necessary.

5 INTERACTIVE MDV APPROACH

We now adopt an approach by exploiting the texture-mapping hardware and general clipping to support a fast visualization of multiple sets of volumetric scalar data. Similar approaches were previously used to visualize a single dataset with

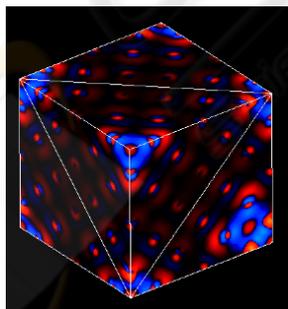


Figure 3: A 256^3 charge density data with the external surfaces of the volume rendered using texture mapping. Electrons are depleted from the bluish regions and deposited in the reddish regions due to a vacancy defect in MgO crystal.

interactive planar clipping and volume clipping via per-fragment operations supported by graphics hardware (van Gelder and Kim, 1996; Weiskopf et al. 2003, 2003; Khanduja and Karki, 2005). They involve rendering of all texels of the 3D textures passing a given clip test, for instance, on average the half of the total number of 256^3 texels are rendered. Thus, the texture-based volume rendering with/out clipping uses a large number of textured slices, which becomes critical as the number of datasets to be rendered concurrently increases.

5.1 External 3D Surface Rendering

Our texture-based MDV approach improves interactivity by reducing the amount of texture mapping. The basic idea is to restrict the rendering of data to the external (visible) surfaces of the volume instead of performing complete or nearly complete 3D volume texture mapping. One place where such surface rendering makes sense is the visualization of the volume data by clipping. In the case of clipping whether it uses a simple clip plane or a more complex 3D clip geometry, one is always interested to view the new surfaces that are exposed (and hence are visible) to the user. For instance, one can view scalar data on a cross-section of the volume with a cutting plane. One defines a regular grid on the clip plane and calculates data values on this grid by interpolation of the original data and

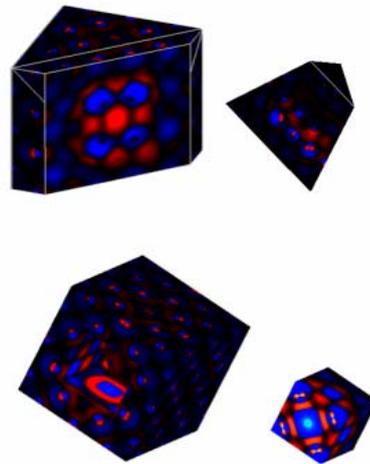


Figure 4: Planar (upper two) and box (bottom two) clipping. In the later case, inner (left) and outer (right) portions of the volume are removed.

uses an appropriate color-map to make the data visible. If this is the case and we are using 3D texture-based rendering, then there is no need to

have texture mapped on all slices to cover the complete volume.

Texture mapping is thus performed on only external surfaces of the volume at a given instant thereby restricting the rendering of the data only to those visible surfaces. For instance, the simulated charge density that considered here is confined to a cubic volume. The 3D surface rendering of the original volume can be done by simply extracting and mapping textures on the six surfaces of the cube (front and back, left and right, and top and bottom square faces), as shown in Figure 3. In effect, the problem of 3D volume texture mapping is reduced to the problem of 3D surface texture mapping, which renders textured data on only those six surfaces. Each square surface can be represented by two edge-sharing triangles so that a total of 12 triangles thus needed are used to implement the clipping operation,

which is described in the next Section. The 3D surface rendering approach works only with the 3D texture because it allows us to extract an arbitrary textured-slice without requiring re-sampling of the volume data. The polygon on which we want to map a texture can intersect the volume at any location and orientation. Texture mapping only requires the vertices of this polygon, which are passed as texture coordinates.

5.2 Clipping

Here we describe how clipping is combined with 3D surface texture mapping. The purpose of clipping is to find single or multiples surfaces cutting the volume and then bound the intersecting surfaces in

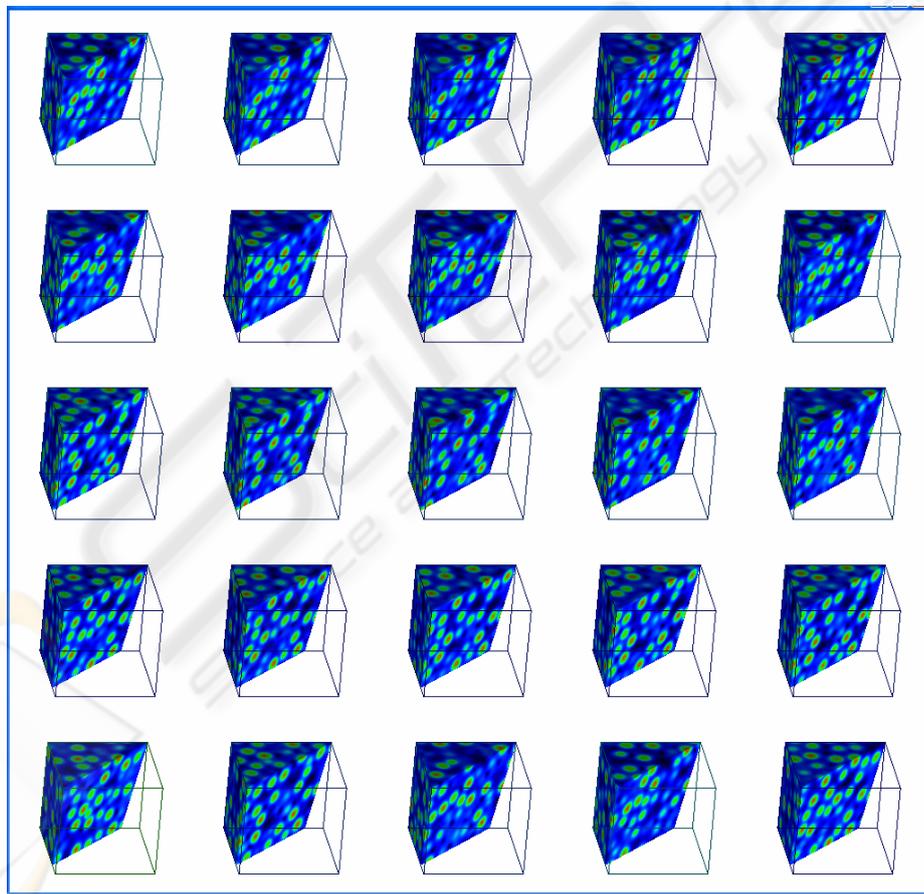


Figure 5: MDV of 25 sets of electronic charge density of liquid MgO (at different simulation times) using 3D surface texture mapping combined with a planar clipping. One can see, for instance, how the positions of high density regions (shown by green + red colors) change with time. A multiscale color map described in Figure 2 caption is used.

the form of simple polygons. These polygons determine the new set of externally visible surfaces of the volume and the textured data is mapped only on these polygons. Thus, only the surfaces defined by a set of visible clipping polygons (single or multiple) are rendered. Each clipping polygon is tessellated in terms of triangles. During initial rendering, the six planar surfaces of simulation box, each represented in terms of two adjacent triangles are rendered. During subsequent clipping process, intersections of these 12 triangles with a given object are calculated. If a triangle is intersected, it is divided into two polygons that lie on either side of the clip plane; and one of them is discarded. Intersection points are used to define new polygons to map textures. Every time the clip plane is adjusted in 3D space, intersections of the original 12 triangles are determined to define polygons (Stephenson and Christiansen, 1995), which bound new visible surfaces

A planner clipping is demonstrated in Figure 4. Every time a clip plane changes (rotates or translates in space), new surfaces for texture mapping are generated. We have also implemented a box-clipping object, which is represented as a set of six clipping planes. Visible surfaces are obtained by repeating the same process, which is used in the case of a single plane. The clip box can be rotated, translated and resized. Figure 4 also shows the outer and inner box clipping. Outer box clipping means removing portion of 3D object that lie outside the clipping box while the inner box clipping is just the reverse of outer box clipping where the portion outside the box is retained and portion inside the box is removed. Figure 5 illustrates the simultaneous visualization of 25 datasets.

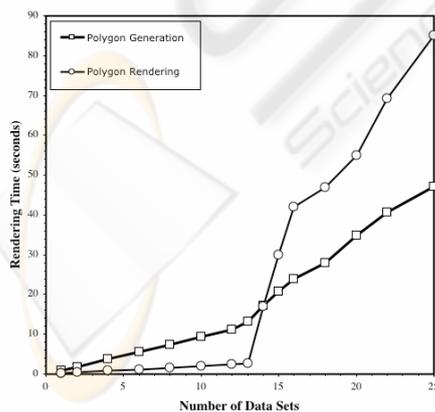


Figure 6: The calculated time as a function of the number of datasets used in MDV. Squares represent the time for generation of multiple lists for polygons representing isosurfaces and circles represent the time for subsequent rendering of polygons.

6 RESULTS AND DISCUSSION

We now present the performance measurements of three MDV techniques described in the Sections 3, 4 and 5. The results are based on the 3D charge density dataset, which was produced by parallel quantum mechanical simulations for different samples, conditions and time points. The size of each dataset used is 256^3 , which represents today's common moderate-sized scalar volume data. The rendering timings are calculated for single dataset visualization (SDV) using the viewport of size 512^2 and for multiple dataset visualization (MDV) using the viewport of size 1024^2 . A bigger viewport in MDV provides bigger space for simultaneous display of multiple datasets. Thus, the differences in rendering speeds between SDV and MDV should reflect the differences in the amounts of data to be processed as well as the number of the pixels to be displayed. The performance measurements have been conducted on a Windows XP PC with 3.2 GHz Pentium IV processor and 1 GB RAM. It uses an NVidia GeForce FX 5200 graphics board with 128 MB graphics memory and 110 MB texture memory. The implementation is based on C/C++, OpenGL and GLUT.

Our analysis in the case of isosurface extraction involves the calculation of the time for conversion of the data into a set of polygons representing isosurface and the time for subsequent rendering with polygon rendering hardware (Figure 6). For operations like rotation, translation and scaling, only the rendering time is relevant. The calculated rendering time is 0.16 seconds for SDV, and remains below 3 seconds for MDV with up to 13 datasets. A rapid increase starts when the number of datasets increases reaches 14. This can be associated with the

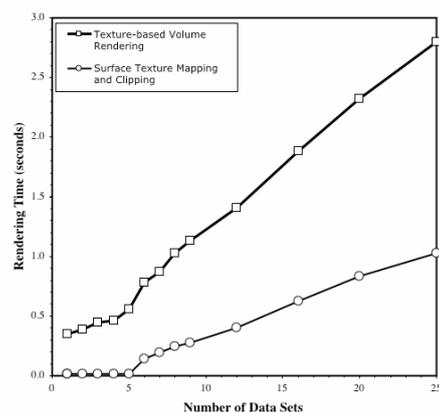


Figure 7: The calculated rendering time as a function of the number of datasets used in MDV. Squares represent the time for the texture-based volume rendering and circles represent the time for 3D surface texture mapping combined with clipping.

limited memory so that more than 14 sets of polygons representing isosurfaces cannot be stored in the memory concurrently thereby involving substantial memory swapping. The time for multiple execution of Marching Cubes' algorithm to produce multiple sets of polygons increases more rapidly with the increasing number of independent datasets after 14 (Figure 6).

For the texture-based MDV, the calculated time represents the time to map the textured data on a series of slices (polygons) with an appropriate blending enabled, i.e., to perform texture-based 3D rendering (Figure 7). All 3D textures are assumed to be already loaded/generated. The SDV rendering time is 0.013 seconds whereas the MDV time is 1.12 and 2.81 seconds, respectively, for 9 and 25 datasets. Note that the total number of slices to be rendered is 6400 for 25 datasets, compared to 256 slices for single dataset. The number of independent texture mappings becomes critical for texture-based MDV as the number of datasets increases. Moreover, when multiple sets of data are loaded as multiple textures, all or most of the textures needed for generating current view cannot be resident in the texture memory at same time due to its limited size. So swapping of the texture objects takes place between the main memory and texture memory and the bus bandwidth becomes a bottleneck. In our study, we notice that up to five 3D textures can be concurrent resident of the texture memory. This explains the presence of a small abrupt increase in the calculated time when the number of 3D textures (or equivalently, 3D datasets) increases from 5 to 6.

Based on our preliminary tests discussed above, the texture-based MDV shows a better performance than the isosurface-based MDV (Table I). However, the frame-rates are low for the both approaches in the context of interactivity. Even for the moderate datasize of 256^3 considered here, the frame-rate drops below 1 for six or higher number of datasets. In the case of isosurface, if one is interested to change the threshold isovalue to get a new set of isosurfaces during MDV process, the processing time becomes much longer.

We have also calculated the rendering time for the proposed MDV approach, which uses 3D surface texture mapping combined with a planar or box clipping. The MDV time is very small for datasets up to 5 and then it increases suddenly for 6 sets and thereafter increases gradually as the number of datasets increases (Figure 7). The rapid increase can again be associated with the limited memory as discussed earlier. The results show that the proposed MDV improves the frame-rate substantially (Table I). First of all, the frame-rate remains above one. Second, it is larger by a factor of 3 than that of the

3D volume texture rendering for MDV with 6 to 25 sets of data. This is consistent with the fact that the number of the slices or polygons rendered is dramatically reduced in the texture-based surface rendering, compared to that in the corresponding volume rendering. For simultaneous visualization of 25 datasets, each of size 256^3 , the 3D surface texture mapping needs a couple of hundreds of polygons, compared to 6,000 slices (or more polygons) required by the 3D volume texture mapping. Third, the differences with respect to the isosurface-based MDV are even bigger (Table I).

7 CONCLUSIONS

In this paper, we have presented a systematic analysis of the multiple dataset visualization (MDV). Many applications require datasets to be grouped and analyzed together based on certain criteria such as samples, conditions, and time-points. In particular, we have performed MDV using two well-known techniques, which are based on isosurface-extraction and hardware-assisted texture mapping. Our results have shown that the both techniques yield low frame-rates when six or more sets of moderate-sized (256^3) data are visualized concurrently. Besides the issues related to the larger memory requirements and limited display sizes, one important challenge is to make MDV interactive. We have proposed an interactive MDV approach in which the 3D surface texture mapping and clipping are exploited. The basic idea is to avoid the rendering of all the textured slices to cover complete or nearly complete volume data by restricting texture mapping onto the only externally visible surfaces of each volume data. The interior of the volume is then explored by exposing (and subsequently rendering) new surfaces with dynamic manipulation of some form of clipping such as a planar or box clipping enabled. For as many as 25 sets of 256^3 data visualized concurrently, our approach yields more than one frame per second, compared to much less than one frame per second with isosurfacing and 3D volume texture mapping. Our scheme is expected to be an effective MDV tool since it exploits the essence of general clipping to uncover important, otherwise hidden details of volume data sets to the extent which is often not feasible with other techniques. At the same time, it also benefits from the increasing processing power and flexibility of graphics processing unit.

Table 1: Comparison of the calculated frame-rates (number of frames per second, fps) between three different methods for single dataset visualization (SDV), and multiple dataset visualization (MDV) with different number of datasets.

Methods	SDV	MDV 4 datasets	MDV 9 datasets	MDV 16 datasets	MDV 25 datasets
Isosurface: Polygon rendering	5.02	1.221	0.556	0.024	0.012
Texture-based volume rendering	7.61	2.153	0.878	0.532	0.357
Clipping with surface texture mapping	>75	~75	3.597	1.611	1.002

We plan to implement more complex clip geometries and extend the performance analyses to multiple sets of 512^3 or larger data.

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