

# FUZZY PATTERN RECOGNITION BASED FAULT DIAGNOSIS

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**Abstract:** In order to avoid catastrophic situations when the dynamics of a physical system (entity in a M.A.S architecture) are evolving toward an undesirable operating mode, particular and quick safety actions have to be programmed in the control design. Classic control (PID and even state model based methods) becomes powerless for complex plants (nonlinear, MIMO and ill-defined systems). A more efficient diagnosis requires an artificial intelligence approach. We propose in this paper the design of a Fuzzy Pattern Recognition System (FPRS) that solves, in real time, the main following problems:

- Identification of an actual state,
- Identification of an eventual evolution towards a failure state,
- Diagnosis and decision-making.

## 1 INTRODUCTION

There is an increasing interest in the development of intelligent fault detection and diagnosis in industrial systems because of increasing requirements for reliable, safe and efficient operation of the plant and for maintaining quality of the products.

Many variables, unknown or not directly measured, have to be included in the state vector to better describe the plant behaviour: model accuracy, a very difficult task, is necessary for the effective processing of unpredictable and imprecise information. However, human expert can skilfully control plants, localise a fault and in many times make a good diagnosis: the human has the ability to learn, to manage imprecise data and he acts in terms of a complex combination of sensing signals instead of separate information sources. Because of complexity in modelling a real plant, we need to achieve this sophisticated level of information processing that the brain is capable of, to solve the difficult task of fault detection and diagnosis.

Pattern Recognition is a field concerned with machine recognition of meaningful regularities in noisy or complex environments. It is based upon the numerical representation of the  $k^{\text{th}}$  object observed in the process (physical entity such as a DC-motor, photograph, etc.) as a vector  $\mathbf{x}_k = [x_{k1}, \dots, x_{kq}]^T$ , called the *pattern vector* or *feature vector*, where  $x_{kj}$

the  $j^{\text{th}}$  characteristic (feature) associated with observation  $k$ : temperature, pressure, flow, sound noise frequency, etc. and  $q$  the pattern vector length. Fuzzy logic concept is included to better manage uncertainty and make useful quantification of hard attributes.

In this paper, a technique for membership function approximator design is presented. We discuss some classification approaches and apply CUSUM algorithm with additional criterions in fault detection problem. We propose a general diagnosis and decision making scheme and give simulation results for a fictive complex system.

## 2 FPRS DESCRIPTION

The pattern vector corresponds to a combination of sensing signals: temperature at point  $A$ , pressure level at  $B$ , incoming flow, etc. It is constructed in terms of the human expert point of view about the plant, and the effects listed in an FMEA (Failure Modes and Effects Analysis). Other mathematical techniques like PCA (Principal Component Analysis) help to design the pattern vector.

For each new incoming observation, we need to identify and quantify the actual plant status and any possible convergence toward an other state: in particular, a failure state. We have to estimate the

speed evolution and execute the necessary safety actions in acceptable delays. A general fault detection and diagnosis that meet these requirements is presented in figure 1.

### 3 MEMBERSHIP FUNCTION ESTIMATION

#### 3.1 Fuzzy Clustering

This first step of unsupervised learning is necessary to produce a logic initialisation of the fault detection and diagnosis system.

Given the training set  $\mathbf{X} = \{\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_n\}$ , where  $\mathbf{x}_k = [x_{k1}, \dots, x_{kd}]^T$  the pattern vector, the problem of fuzzy clustering in  $\mathbf{X}$  is to assign to the objects  $\{\mathbf{x}_k\}$  labels that identify 'natural subgroups' in  $\mathbf{X}$ . The *membership degrees*, are computed as  $\mathbf{U} = [u_{ik}]$  by the *Fuzzy c-Means* (FCM) algorithm with the following considerations:

- A class, set of observations that have similar properties, corresponds to one operating or failure mode, the number of clusters  $c$  is assumed to be known. It is also initialised in terms of the expert point of view,
- The training set is considered, as representative of the whole possible clusters, when its size is large enough. It is obtained by causing the plant to operate under different modes.

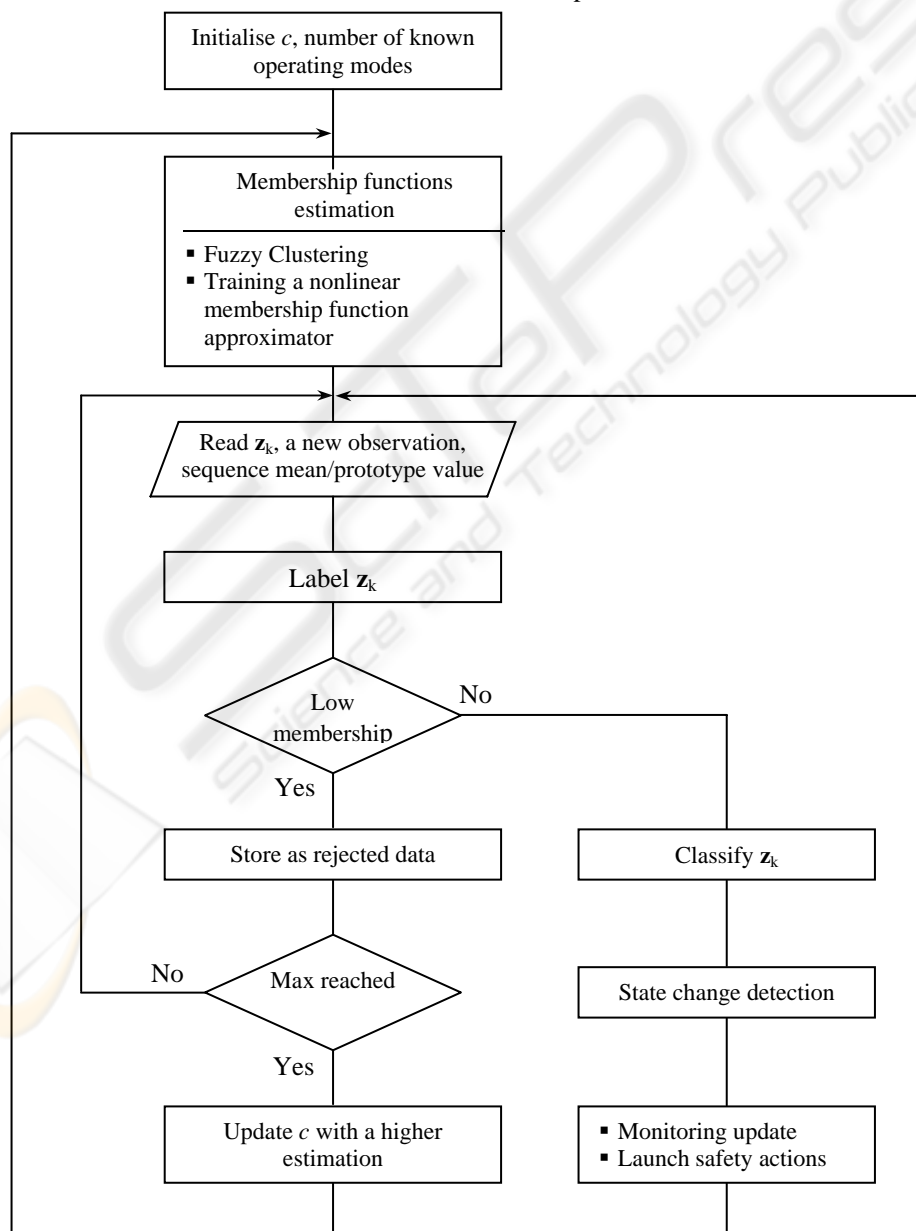


Figure 1: A general FPRS design strategy

The FCM algorithm converges from any initialisation to a local minimum. The prototypes and membership degrees are iteratively updated by [3]:

$$\mathbf{v}_i = \frac{\sum_{k=1}^q u_{ik}^m \mathbf{x}_k}{\sum_{k=1}^n u_{ik}^m} \text{ for } i = 1, 2, \dots, c \quad (1)$$

$$u_{ik} = f(\mathbf{x}_k, \mathbf{v}_i, \{\mathbf{v}_j\}, m)$$

where,

$u_{ik}$ : the membership degree of object  $\mathbf{x}_k$  to class  $i$ ,

$\mathbf{v}_i$ : prototype of class  $i$ ,

$m \in [1, \infty)$ : weight exponent on each fuzzy membership,

until an error threshold is reached.

Expression (1) is intuitively understood when we observe the similarity with the ‘centre of gravity’ concept.

### 3.2 Nonlinear Approximator Design

At this step,  $X = \{\mathbf{x}_k\}$  and  $U = [u_{ik}]$  feed the input of a nonlinear approximator optimisation algorithm. Let’s consider the structure of a Radial Basis Neural Network (RBNN) as shown in figure 2. The hidden layer is typically comprised of  $p$  radial basis activation functions with an associated Euclidean input mapping. The output is taken as a linear activation function with an inner product

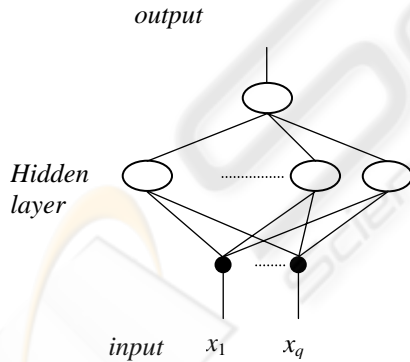


Figure 2: RBNN based nonlinear approximator.

The input-output relationship, with  $\mathbf{x} = [x_1, \dots, x_q]^T$ , is given by

$$F(\mathbf{x}, \boldsymbol{\theta}) = \sum_{j=1}^p w_j \exp(-|\mathbf{x} - \mathbf{c}_j|^2 / \gamma_j^2) \quad (2)$$

where,

$\boldsymbol{\theta} = [w_1, \dots, w_p]^T$ : the weight vector to be adjusted during learning,

$\mathbf{c}_j = [c_{j1}, \dots, c_{jn}]^T$ : the centres of Gaussian functions.

Now, it is desired to cause  $F_i(\mathbf{x}, \boldsymbol{\theta})$  to match a membership function of class  $i$  at the data points  $(\mathbf{x}_k, \{u_{ik}\})$  for  $i = 1, \dots, c$ , previously estimated by the FCM. The *Conjugate Gradient* method, chosen because of its good convergence properties, is applied for training the approximator. It is based upon the minimisation of:

$$J_i = \sum_{k=1}^n (e^k)^T e^k$$

where,

$$e^k = (u_{ik} - F_i(\mathbf{x}_k, \boldsymbol{\theta})), \text{ for } i = 1, \dots, c$$

The algorithm is given as follow [10,11]:

- 1) Calculate  $\zeta(k) = \frac{\partial J_i}{\partial \boldsymbol{\theta}} \bigg|_{\boldsymbol{\theta}=\boldsymbol{\theta}(k)}$ . Set the search direction equal to  $d(k) = -\zeta(k)$ .
- 2) Find  $\boldsymbol{\theta}(k+1)$  which minimises  $J_i(\boldsymbol{\theta})$  along  $d(k)$ , iteratively, by the Secant method:
  - a) Initialise  $\sigma < 1$ , set  $\boldsymbol{\theta} = \boldsymbol{\theta}(k)$
  - b) Set  $\alpha = -\sigma \frac{[\zeta(k)]^T d(k)}{[\zeta(k + \sigma \cdot d(k))]^T d(k) - [\zeta(k)]^T d(k)}$
  - c)  $\boldsymbol{\theta} = \boldsymbol{\theta} + \alpha d(k)$
  - d)  $\sigma = \alpha$
  - e) If  $|\alpha \cdot d(k)| < tol_\alpha$  then return  $\boldsymbol{\theta}(k+1) = \boldsymbol{\theta}$  else go to b
- 3) Calculate  $\zeta(k+1)$ .
- 4) If  $\left| \frac{\zeta(k)}{\zeta(0)} \right| < tol_\theta$  then return  $\boldsymbol{\theta}(k+1)$
- 5) Set the next search direction

$$d(k+1) = -\zeta(k+1) + \beta(k+1) d(k),$$

where,

$$\beta(k+1) = \frac{[\zeta(k+1)]^T \zeta(k+1)}{[\zeta(k)]^T \zeta(k)} \quad (\text{Fletcher-Reeves}$$

update), or

$$\beta(k+1) = \frac{[\zeta(k+1) - \zeta(k)]^T \zeta(k+1)}{[\zeta(k)]^T \zeta(k)} \quad (\text{Polak-Ribiere})$$

update)

6) Set  $k = k+1$  and goto 2.

$c$  RBNNs are trained to estimate a membership function for each corresponding class. Note that  $F_i(\mathbf{x}, \boldsymbol{\theta})$  may be outside  $[0,1]$  by a very small amount for the first training, because (2) doesn't include a saturation factor. The few false measures must be corrected (a value that is negative or greater than 1 is taken, respectively, as 0 or 1) to be processed correctly for fault detection. An other procedure, that adds a sigmoid stage to the structure of figure 2, can be tried in the future.

## 4 PROCESSING A NEW OBSERVATION

Once the membership approximator is well defined, a new observation  $\mathbf{z}$  is labelled and classified:

The membership value of  $\mathbf{z}$  to class  $i$  is

$$\mu_i(\mathbf{z}) = F_i(\mathbf{z}, \boldsymbol{\theta}) \quad (3)$$

We define a hard classifier on  $\mathbb{R}^q$  as a decision function  $\mathbf{D}$  imaged in the canonical (unit vector) basis of Euclidean  $c$ -space so that  $\mathbf{D}(\mathbf{z}) = \mathbf{e}_i$  means that  $\mathbf{z}$  belongs to class  $i$ . This hard attribution is quantified by (3) to explain how much  $\mathbf{z}$  is considered as  $i^{\text{th}}$  fault type and is useful to identify the actual operating/failure mode. There are many choices for classifier design:

Criterion 1:

$$\mathbf{z} \in i \Leftrightarrow \mu_i(\mathbf{z}) = \max \{ \mu_j(\mathbf{z}) \}_{j=1, \dots, c}. \quad (4)$$

Criterion 2: crisp nearest prototype rule (NP rule)

$$\mathbf{z} \in i \Leftrightarrow \mathbf{D}_{\text{NP},i}(\mathbf{z}) = \mathbf{e}_i \Leftrightarrow \|\mathbf{z} - \mathbf{v}_i\| \leq \|\mathbf{z} - \mathbf{v}_j\| \quad (5)$$

for  $j = 1, \dots, c$ .

Criterion 3: fuzzy  $k$ -nearest neighbor ( $k$ -NN) rule

Compute and rank the distances  $d(\mathbf{z}, \mathbf{x}_i)$  as  $\{d_1 \leq d_2 \leq \dots \leq d_k \leq d_{k+1} \leq \dots \leq d_n\}$ . Find the columns in  $\mathbf{U}$  corresponding to the  $k$  nearest neighbor indices  $\{1, 2, \dots, k\}$ . Calculate the vector  $\mathbf{u}^*(\mathbf{z}) = [u(1|\mathbf{z}) \ u(2|\mathbf{z}) \ \dots \ u(c|\mathbf{z})]^T$  with the NN labels:  $u(i|\mathbf{z}) = \sum_{j=1}^k \frac{u_{ij}}{k}$  for  $j = 1, \dots, c$ .

And finally decide

$$\mathbf{z} \in i \Leftrightarrow \mathbf{D}_{\text{NN},k}(\mathbf{z}) = \mathbf{e}_i \Leftrightarrow u(i|\mathbf{z}) = \max \{ u(j|\mathbf{z}) \}_{j=1, \dots, c}. \quad (6)$$

For a long training set and an efficient approximator, the first criterion is the most adequate. NP and  $k$ -NN may be used as a redundant alternative to solve ambiguous situations like the example illustrated in figure 3: it is easy to see that  $(\mathbf{z}_1 < \mathbf{z}^* \in \text{class 1})$  and  $(\mathbf{z}_2 > \mathbf{z}^* \in \text{class 1})$ , but we need an additional/other criterion to classify  $(\mathbf{z}_2 \approx \mathbf{z}^*)$

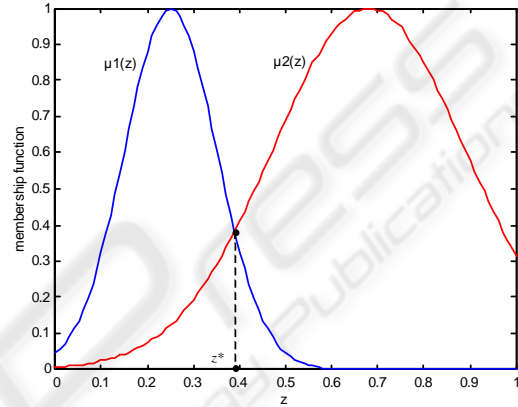


Figure 3: Example of an ambiguous classification problem.

We add the constraint

$$\sum_{i=1}^c \mu_i(\mathbf{z}) > u_{th} \quad (7)$$

to reject observations with low membership degrees,  $u_{th}$  is a small nonzero number taken lower than 0.5. When a sufficient number of similar (low variance for a Gaussian pdf approximation) observations are reached, a new cluster is created. Prototype and membership function parameters are computed individually (partial FCM with  $c=1$ ) or by restarting a global membership function estimation process.

## 5 FAULT DETECTION AND FORECASTS

This is a more ambitious and potentially useful task in maintenance monitoring. The detection of an actual or future operating/failure mode requires getting and processing, in real time, the signals  $\mathbf{z}(t)$  and  $\mu_i(\mathbf{z}, t)$ , and taking advantage of their stochastic properties. If the plant status is efficiently described by the pattern vector, we note by  $\mu_i(t)$  the membership degree of the plant state to class  $i$  at

time  $t$ , and we develop our approach through the following steps:

- 1) CUMulative SUM (CUSUM) algorithm is involved in change detection by processing a sequence of independent random variables with probability density function  $p_{\Theta}(\mathbf{z})$  depending upon one parameter  $\Theta$ . It relies on a fundamental concept: the log-likelihood ratio of an observation  $\mathbf{z}$ :

$$s(\mathbf{z}) = \ln \frac{p_{\Theta_1}(\mathbf{z})}{p_{\Theta_0}(\mathbf{z})} \quad (8)$$

before an unknown change time  $k_0$ ,  $\Theta$  is equal to  $\Theta_0$ . At time  $k_0$ , it changes to  $\Theta = \Theta_1 \neq \Theta_0$ . The problem is to detect the change time.

The cumulative sum

$$S(k) = \sum_{j=1}^k s(\mathbf{z}(j)) = \sum_{j=1}^k \ln \frac{p_{\Theta_1}(\mathbf{z}(j))}{p_{\Theta_0}(\mathbf{z}(j))} \quad (9)$$

(where,  $\{\mathbf{z}(j)\}_{j=1, \dots, k}$  a sequence of independent random variables) is expected to exhibit a negative drift before change, and a positive drift after change. CUSUM algorithm is derived under this idea and given as follow:

At each sample time,

- a) Acquire the new data  $\mathbf{z}(k)$ ,

- b) Compute the decision function

$$g(k) = \max\{0, g(k-1) + s(\mathbf{z}(k))\},$$

- c) Compute the number of successive observations for which the decision function remains strictly positive:

$$N(k) = N(k-1) \cdot 1_{\{g(k-1) > 0\}} + 1,$$

where  $1_{\{x\}} = 1$  when  $x$  is true and  $1_{\{x\}} = 0$  otherwise.

- d) If  $g(k) > h$ , issue an alarm, ( $h$  is a threshold chosen to meet either a specified mean time for detection or a specified mean time between false alarms)

Find the change occurrence time:  $k_0 = k_a - N(k_a)$ , where  $k_a$  is the alarm time,

Reinitialise the decision function to 0,

In many practical cases,  $\Theta$  is taken as the mean value of a Gaussian distribution  $p_{\Theta}(\mathbf{z})$ . In our problem, each typical value  $\Theta_i$  indicates a class prototype  $\mathbf{v}_i$ , and the problem of change detection between failure modes will require a prior knowledge about the class-statistical

properties. We only own a membership function database!

- 2) Because of the fact stated above, CUSUM will be applied with the following modification:

$$\ln \frac{\mu_i(\mathbf{z})}{\mu_j(\mathbf{z})} \text{ is considered instead of } \ln \frac{p_{\Theta_i}(\mathbf{z})}{p_{\Theta_j}(\mathbf{z})}$$

where  $i$  and  $j$  are class-indexes. A membership value doesn't have the same meaning as probability, but the ratios reflect the same information, so the ability to apply CUSUM with taking

$$s(\mathbf{z}) = \ln \frac{\mu_i(\mathbf{z})}{\mu_j(\mathbf{z})} \quad (10)$$

is intuitively concluded.

- 3) Change time detection between two states is presented. If the target class prototype remains far,  $k_0$  may be considered as an evolution detection occurrence and safety decisions are executed in acceptable delay. When the radius of target class membership function is very small, the safety task will be more difficult, so we need an other tool to better quantify the evolution between states and make an earlier alarm.

An evolution towards a fault is described by

$\frac{d\mu_i(t)}{dt}$ : A negative value means that the plant is leaving state  $i$ , a positive value means that it is evolving towards this state. The evolution speed attributes 'quick' or 'slow' are quantified by  $\frac{d^2\mu_i(t)}{dt^2}$ : the change in evolution speed is said to

be 'quick' for  $\frac{d^2\mu_i(t)}{dt^2} > 0$ , an observation may

leave quickly state  $i$  while converging slowly to state  $j$ . Information about the fault evolution direction are extracted from a  $3 \times c$  matrix defined by:

$$E = \begin{bmatrix} \mu_1 & \mu_2 & \dots & \mu_c \\ \frac{d\mu_1}{dt} & \frac{d\mu_2}{dt} & \dots & \frac{d\mu_c}{dt} \\ \frac{d^2\mu_1}{dt^2} & \frac{d^2\mu_2}{dt^2} & \dots & \frac{d^2\mu_c}{dt^2} \end{bmatrix} \quad (11)$$

The corresponding alarm time  $k_e$  is computed in terms of constraints on the elements of  $E$ . For example,  $k_e$  may be defined as the delay time for

which both  $\left(\frac{d\mu_i(t)}{dt}\right)$  and  $\left(\frac{d\mu_i(t)}{dt} \cdot \frac{d^2\mu_i(t)}{dt^2}\right)$



remain positive, and this corresponds to the alarm time  $k_a$  computed by CUSUM. Other conditions may be added to make an earlier alarm (optimisation problem).

Because of external disturbances, a noise is added to  $z$  when reading. We'll consider mean values instead of instantaneous values: the problem is solved by a digital FIR filter, the frequency bandwidth and sampling time are chosen in terms of the noise properties and the response time of all the mechanical/electrical plant parts considered in the diagnosis design.

## 6 DIAGNOSIS AND DECISION MAKING

We completely described a fault detection scheme. The  $i^{\text{th}}$  fault type effects (symptoms) may be caused by more than one physical entity, and this fact is described by conditional probabilities. Diagnosis is to decide that element  $e_j$  (a valve, transistor, heater, etc) is (or will be) the cause of the detected (or expected) fault. Previous fault events feed a statistical database with class-conditional pdf(s)  $\{p(i^{\text{th}} \text{ fault} | e_j\text{-fault})\}$ , used to compute  $p(e_j\text{-fault} | i^{\text{th}} \text{ fault})$  by Bayes' rule. The corresponding safety actions are made according to the diagnosis conclusion, the fault severity and the decision making scheme. One powerful solution is built upon an *Inference Engine*: this is a software or hardware system, which gives a *conclusion* (output) from a *fact* (input) and *knowledges* (production rules). If knowledges include fuzzy linguistic terms, it is referred to as *Fuzzy Inference Engine* (FIE). A conclusion may deal with:

- A new reference tracking (fuzzy control), the knowledge base includes rules of the form: if (mode2) and (low inflow), then (tank 3 temperature should be low)
- Diagnosis / binary logic instructions, a production rule may be:  
if (water outflow  $> 0.24\text{m}^3/\text{s}$ ) and (valve 21 closed), then (shut-off and repair/change element  $e_2$ ),  
if ( $d^2\mu_3/dt^2 > 0.12$ ) or (input control  $u_1$  not set), then ( $3^{\text{rd}}$  fault type in the next 3 minutes).

Beyond the construction/generation of production rules, one difficult task when implementing a fuzzy control algorithm is the accuracy of meaningful membership functions for all the fuzzy linguistic

terms considered in the knowledge base. We'll present later, through an example of temperature control, the different steps involved in fuzzy control implementation.

## 7 SIMULATION RESULTS

For the demonstration of the proposed diagnosis method, we consider a fictive complex process. We assumed that a human expert was supervising the plant state by observing three variables:  $v_1$  (pressure at point  $A_1$ ),  $v_2$  (temperature at point  $A_2$ ) and  $v_3$  (sound noise frequency). He makes detection and diagnosis upon two complex combinations:  $x_1=f_1(v_1, v_2, v_3)$  and  $x_2=f_2(v_1, v_2, v_3)$  (PCA). We want to apply the designed FPRS to act with a similar reasoning faculty.

Simulation is run, by causing the plant to operate during a sufficient time, under one normal (typical) operating mode and two failure modes (plant parameters randomly affected). PCA has reduced the pattern vector to  $[x_1, x_2]^T$ . The unsupervised learning step is applied with a training set of 100 data points. Samples are labelled; and the prototypes identified as shown in figure 4.

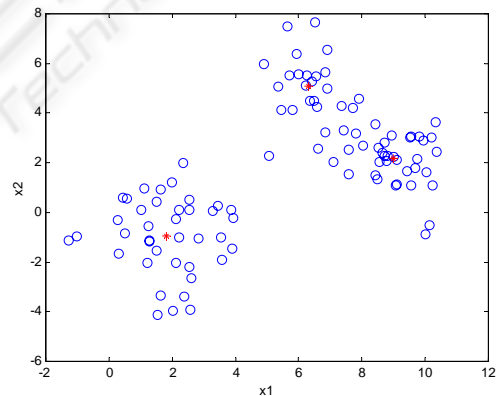


Figure 4: Fuzzy clustering with  $c=3$ ,  $q=2$ . The prototypes are marked as red stars:  $v_1=[1.823, -0.935]^T$ ,  $v_2=[9.006, 2.151]^T$ ,  $v_3=[6.297, 5.078]^T$

The method of Conjugate Gradients is successfully applied to train an RBNN based membership function approximator for each class (figure 5).

For classification and fault detection test, we caused the system to evolve towards mode 3 by generating a linear path sequence  $\{z_k=[z_{k1}, z_{k2}]^T\}$ , each observation is well labelled and classified (Figure9-a). CUSUM is applied with  $s(z)=\ln \frac{\mu_3(z)}{\mu_1(z)}$  (figure 6). Evolution towards fault 3 is detected

earlier when membership function derivatives are considered (figure 7-b).

Temperature control problem is presented to describe an example of a fuzzy inference engine (figure 8). A part of the knowledge base is given as follow:

**R1:** if (mode1) and (quick evolution toward mode3), then ( $T_5$  should be low)

**R2:** if ( $P_5 \approx 0.4$  bar) or (slow evolution toward mode3), then ( $T_5$  should be around  $15^\circ\text{C}$ )

**R3:** if (mode2) and (high sound noise frequency), then ( $T_5$  should be high)

.....

**Fact:**  $z=[7, 3.7]^T$ ,  $P_5 = 1.27$  bar,  $d\mu_3/dt = 0.2$  /sec,  $d^2\mu_3/dt^2 = -0.18$  /sec<sup>2</sup>,  $f_{sn} = 15$  kHz

**Conclusion:**  $T_5$  should be ?

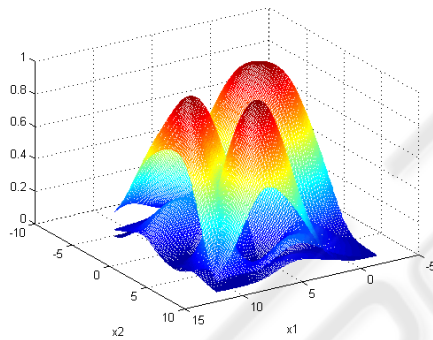
The fuzzy linguistic term ‘mode  $i$ ’ is described by the corresponding membership function  $F_i(\mathbf{x}, \boldsymbol{\theta})$ . The membership function for each other fuzzy linguistic term is initialised as shown but may be modified by learning to update the shape form and parameters.

The basic operators, involved in fuzzy control, are defined as follow:

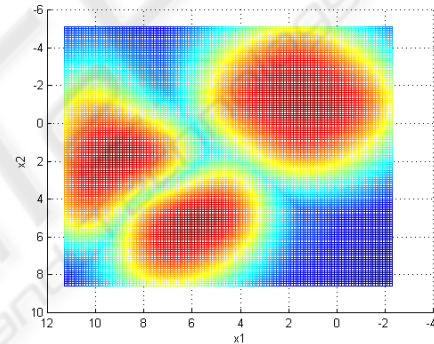
$$\text{AND: } \mu_{A \cap B} = \min(\mu_A, \mu_B) \quad (12)$$

$$\text{OR: } \mu_{A \cup B} = \max(\mu_A, \mu_B) \quad (13)$$

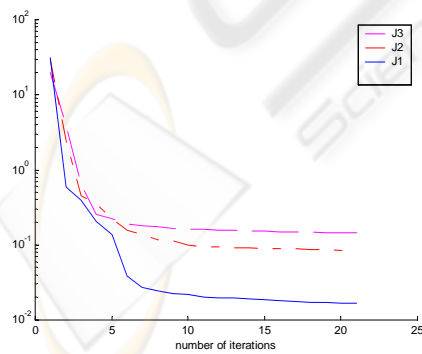
$$\text{NOT: } \mu_{\bar{A}} = 1 - \mu_A \quad (14)$$



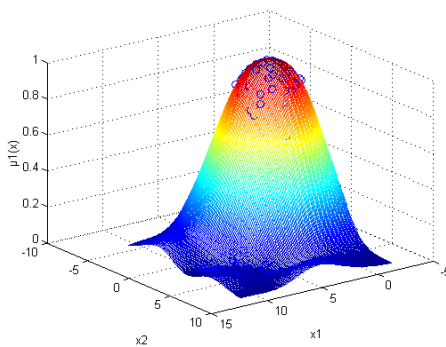
(a)



(b)



(c)



(d)

Figure 5: membership approximator,  $p=25$ ,  $\gamma = 2.5$ . (a) Plant status membership functions. (b) Projection of (a) on  $x_1$ - $x_2$  plane, the similarity with the plot of figure 4 is proved. (c) Cost function during learning. There is a trade-off between the learning time and accuracy requirements. (d)  $F_1(\mathbf{x}, \boldsymbol{\theta})$  matches the data pairs considered in training the RBNN.

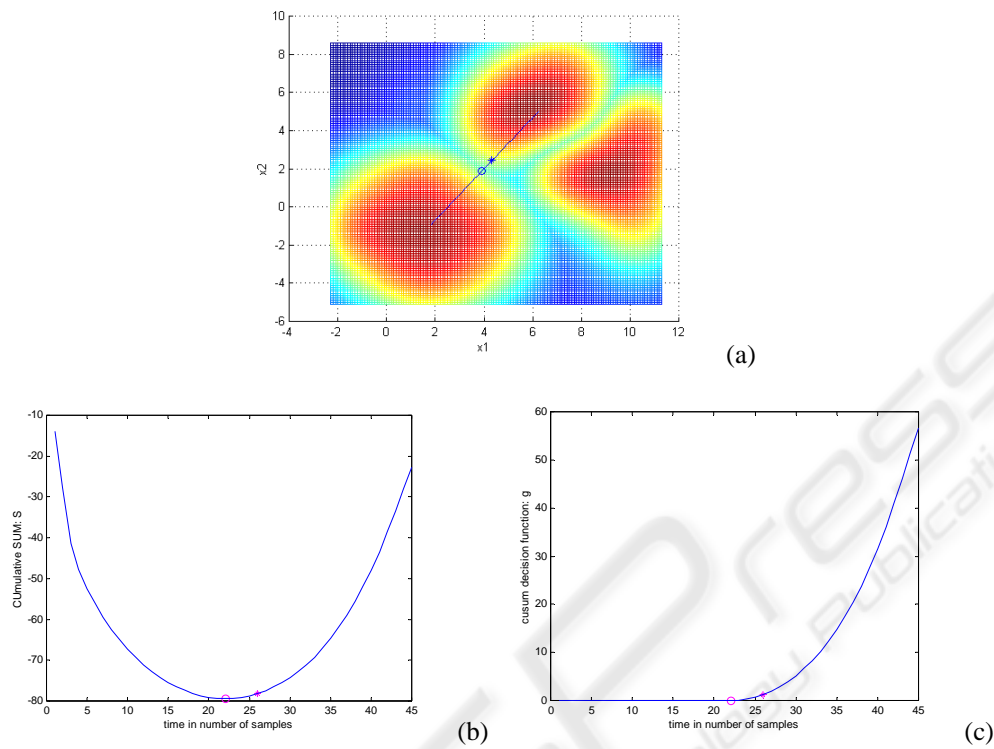


Figure 6: Fault change detection by CUSUM,  $h=1.2$ . The estimated change occurrence is marked as circle; the alarm time as star. (a) New observation-path, plant is leaving model1 towards mode3 (b) Cumulative Sum plot, (c) decision function plot.

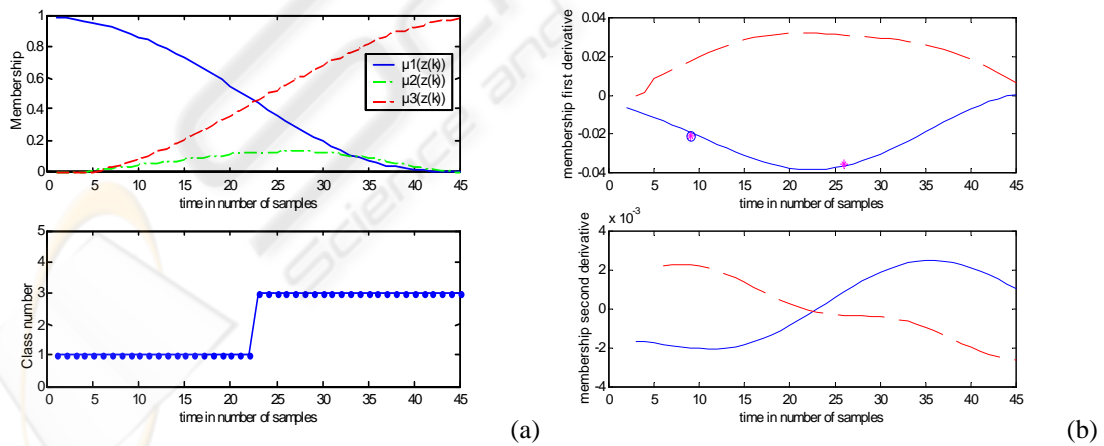


Figure 7: Future fault detection strategy with additional derivative based criteria. (a) Criterion 1-classification. (b) 1<sup>st</sup> and 2<sup>nd</sup> derivatives of  $\mu_1(t)$  and  $\mu_3(t)$ , the filled circle indicates an earlier change detection.



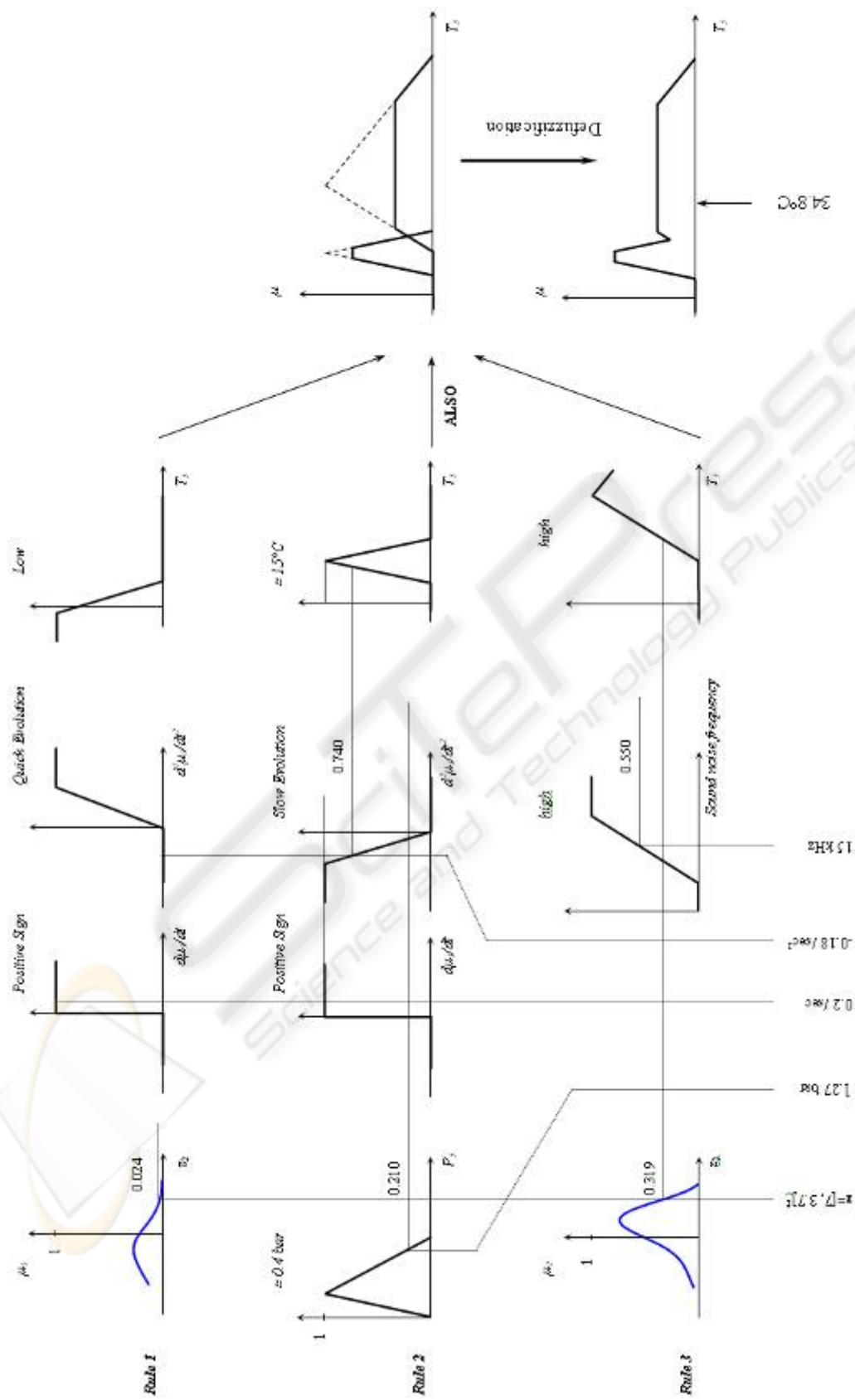


Figure 8. Example of a fuzzy inference engine based decision process

For each rule, the compatibility of the fact to the antecedent is obtained by projecting the fact to the corresponding membership function. The resulting membership degrees are combined by a conjunction 'AND' (rules 1, 3) or 'OR' (rule 2). An individual conclusion is obtained by truncating (minimising) the consequent membership function. All the rules are combined by conjunction 'ALSO' (maximisation of individual conclusions) to construct a relatively complicated membership function ' $\mu$ ' characterising the final conclusion. The final step is defuzzification: the new reference  $T_5^*$  that must be tracked, given the fact:  $(z=[7, 3.7]^T, P_5=1.27 \text{ bar}, d\mu_3/dt = 0.2 \text{ /sec}, d^2\mu_3/dt^2=-0.18 \text{ /sec}^2, f_{sn}=15 \text{ kHz})$ , is computed by the center-of-gravity method:

$$T_5^* = \frac{\int T_5 \mu(T_5) dT_5}{\int \mu(T_5) dT_5} = 34.8^\circ\text{C} \quad (15)$$

and  $T_5$  remains continuously under this control.

## 8 CONCLUSION

We have proposed a general FPRS design scheme for fault detection and diagnosis in industrial systems. This approach involves fuzzy clustering as a first partition of the training set into a number of classes initialised by the known operating/failure modes, and the conjugate gradient method as the learning tool for training membership function approximators. Incoming observations will be classified and new created classes are taken into account.

Fault detection efficiency is first tested by applying CUSUM with modified expression of the log-likelihood ratio: membership degrees are considered instead of probabilities. Then, an other proposed method that takes advantage of membership function derivatives is investigated, evolution towards a fault type target is quantified and safety actions will be executed in acceptable delays.

There are many ways to design the decision system, we proposed a knowledge based approach and presented a 'temperature fuzzy control' as an example of a safety action based on information

about fault change forecasts, extracted from the matrix E.

The designed FPRS is successfully tested for a fictive plant. Its proficiency will be more proven when tested in a real environnement, this involves additional hardware and software implementation and will be the subject of a future work.

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